Class X Session 2024-25 Subject - Mathematics (Basic) Sample Question Paper - 1

Time Allowed: 3 hours

General Instructions:

- 1. This Question Paper has 5 Sections A, B, C, D and E.
- 2. Section A has 20 MCQs carrying 1 mark each
- 3. Section B has 5 questions carrying 02 marks each.
- 4. Section C has 6 questions carrying 03 marks each.
- 5. Section D has 4 questions carrying 05 marks each.
- 6. Section E has 3 case-based integrated units of assessment carrying 04 marks each.
- 7. All Questions are compulsory. However, an internal choice in 2 Qs of 5 marks, 2 Qs of 3 marks and 2 Questions of 2 marks has been provided. An internal choice has been provided in the 2 marks questions of Section E
- 8. Draw neat figures wherever required. Take $\pi = \frac{22}{7}$ wherever required if not stated.

	S	Section A	
1.	The HCF of 95 and 152, is		[1]
	a) 57	b) 19	
	c) 38	d) 1	
2.	Given that H.C.F. (306, 954, 1314) = 18, find L.C.M. (306, 954, 1314).		
	a) 1183234	b) 1123328	
	c) 1183914	d) 1123238	
3.	If $x = 3$ is a solution of the equation $3x^2 + (k - 1)x + 9 = 0$ then $k = ?$		
	a) 13	b) -11	
	c) 11	d) -13	
4.	The angles of a triangle are x ⁰ , y ⁰ and 40 ⁰ . The difference between the two angles x and y is 30 ⁰ , then		
	a) $x^{0} = 75^{0}$ and $y^{0} = 45^{0}$	b) $x^{o} = 85^{o}$ and $y^{o} = 55^{o}$	
	c) $x^{0} = 95^{0}$ and $y^{0} = 35^{0}$	d) $x^{o} = 65^{o}$ and $y^{o} = 95^{o}$	
5.	$x^2 - 6x + 6 = 0$ have		[1]
	a) Real and Equal roots	b) Real roots	
	c) No Real roots	d) Real and Distinct roots	
C	Two worthers of \wedge ADC are \wedge (1, 4) and D(F, 2) and	d its controld is $C(0, 2)$. Then the coordinates of C are	[1]

6. Two vertices of \triangle ABC are A (-1, 4) and B(5, 2) and its centroid is G(0, -3). Then, the coordinates of C are **[1]**

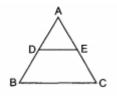
Maximum Marks: 80

	a) (4, 3)	b) (4, 15)	
	c) (-4, -15)	d) (-15, -4)	
7.	In triangles ABC and DEF, $\angle A = \angle E = 40^{\circ}$, AB : EE	D = AC : EF and \angle F = 65°, then \angle B =	[1]
	a) 75°	b) 85°	
	c) 35º	d) ₆₅ °	
8.	In the adjoining figure P and Q are points on the sides AB and AC respectively of ΔABC such that AP = 3.5 cm, PB = 7cm, AQ = 3 cm, QC = 6 cm and PQ = 4.5 cm. The measure of BC is equal to		
	a) 13.5 cm.	b) 12.5 cm.	
	c) 9 cm.	d) 15 cm	
9.	The distance between two parallel tangents of a circle	e of radius 3 cm is	[1]
	a) 6 cm	b) 3 cm	
	c) 4.5 cm	d) 12 cm	
10.	$(\ cosec heta-\cot heta)^2=?$		[1]
	a) $\frac{1+\sin\theta}{1-\sin\theta}$	b) $\frac{1-\cos\theta}{1+\cos\theta}$	
	c) $\frac{1-\sin\theta}{1+\sin\theta}$	d) $\frac{1+\cos\theta}{1-\cos\theta}$	
11.	An electric pole is $10\sqrt{3}$ m high and its shadow is 10	m in length, then the angle of elevation of the sun is	[1]
	a) 45°	b) 15°	
	c) 30°	d) 60°	
12.	$\frac{\sin\theta}{1+\cos\theta}$ is equal to		[1]
	a) $\frac{1-\sin\theta}{\cos\theta}$	b) $\frac{1-\cos\theta}{\cos\theta}$	
	c) $\frac{1-\cos\theta}{\sin\theta}$	d) $\frac{1+\cos\theta}{\sin\theta}$	
13.	If θ is the angle (in degrees) of a sector of a circle of	radius r, then area of the sector is	[1]
	a) $\frac{\pi r^2 \theta}{360}$	b) $\frac{2\pi r\theta}{360}$	
	$c) \frac{\pi r^2 \theta}{180}$	d) $\frac{2\pi r\theta}{180}$	
14.	A chord of a circle subtends an angle of 60 ^o at the ce	ntre. If the length of the chord is 100 cm, find the area of	[1]
	the major segment.		
	a) 30391.7 cm ²	b) 30720.5 cm ²	

c) 30520.61 cm² d) 31021.42 cm²

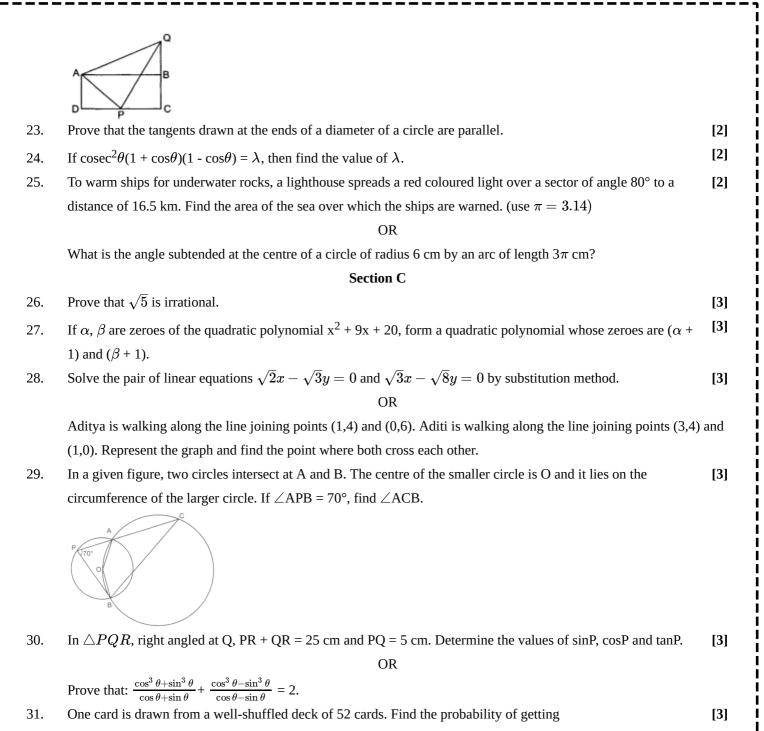
15.	Raju bought a fish from a shop for his aquarium. Th	e shop keeper takes out one fish from a tank containing 15	[1]	
	male fish and 18 female fish. The probability that th			
	a) $\frac{5}{11}$	b) $\frac{6}{11}$		
	c) $\frac{5}{12}$	d) $\frac{7}{11}$		
16.	If 35 is removed from the data: 30, 34, 35, 36, 37, 3	8, 39, 40, then the median increases by:	[1]	
	a) 0.5	b) 1.5		
	c) 2	d) 1		
17.		s full of water. A solid in the form of a right circular cone If the radius of the hemisphere is 3.5 cm and the height of he volume of water left in the tub. (Take $\pi = \frac{22}{7}$)	[1]	
	a) 716 cm ³	b) 616 cm ³		
	c) 600 cm ³	d) _{535 cm³}		
18.	If the mean of a frequency distribution is 8.1 and \sum) $f_i x_i = 132 + 5k$, $\sum f_i = 20$ then k =	[1]	
	a) 3	b) 4		
	c) 5	d) 6		
19.	Assertion (A): Distance between (5, 12) and origin	is 13 units.	[1]	
	Reason (R): D = $\sqrt{\left(x_1-x_2 ight)^2+\left(y_1-y_2 ight)^2}$			
	a) Both A and R are true and R is the correct	b) Both A and R are true but R is not the		
	explanation of A.	correct explanation of A.		
	c) A is true but R is false.	d) A is false but R is true.		
20.	Assertion (A): No two positive numbers can have 18 as their H.C.F and 380 as their L.C.M.			
	Reason (R): L.C.M. is always completely divisible by H.C.F.			
	a) Both A and R are true and R is the correct	b) Both A and R are true but R is not the		
	explanation of A.	correct explanation of A.		
	c) A is true but R is false.	d) A is false but R is true.		
	S	ection B		
21.	Is the pair of linear equation consistent/inconsistent' 0; $4x - 4y - 5 = 0$? If consistent, obtain the solution graphically: $2x - 2y - 2 =$	[2]	
22	-	ively such that DE BC If AD = $\frac{1}{2}$ BD AE = 4.5 cm find	[2]	

22. In figure, D and E are points on AB and AC respectively, such that DE || BC. If AD = $\frac{1}{3}$ BD, AE = 4.5 cm, find [2] AC.



OR

In the given figure, ABCD is a rectangle. P is mid-point of DC. If QB = 7 cm, AD = 9 cm and DC = 24 cm, then prove that $\angle APQ = 90^{\circ}$.



- i. a king of red colour
- ii. a face card
- iii. a red face card
- iv. the jack of hearts

v. a spade

vi. the queen of diamonds

Section D

OR

[5]

32. Solve for x:
$$\left(\frac{2x}{x-5}\right)^2 + 5\left(\frac{2x}{x-5}\right) - 24 = 0, x \neq 5$$

The sum of squares of two consecutive multiples of 7 is 637. Find the multiples.

- 33. Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and [5] median PM of another triangle PQR. Show that $\Delta ABC \sim \Delta PQR$.
- 34. A solid is in the shape of a hemisphere surmounted by a cone. If the radius of hemisphere and base radius of [5]

cone is 7 cm and height of cone is 3.5 cm, find the volume of the solid. (Take $\pi = \frac{22}{7}$)

OR

A solid toy is in the form of a hemisphere surmounted by a right circular cone. Height of the cone is 2 cm and the diameter of the base is 4 cm. If a right circular cylinder circumscribes the solid. Find how much more space it will cover.

35. The following data gives the distribution of total monthly household expenditure of 200 families of a village. [5]Find the modal monthly expenditure of the families. Also, find the mean monthly expenditure:

Expenditure (in ₹)	Frequency		
1000-1500	24		
1500-2000	40		
2000-2500	33		
2500-3000	28		
3000-3500	30		
3500-4000	22		
4000-4500	16		
4500-5000	7		

Section E

36. **Read the following text carefully and answer the questions that follow:**

Kamla and her husband were working in a factory in Seelampur, New Delhi. During the pandemic, they were asked to leave the job. As they have very limited resources to survive in a metro city, they decided to go back to their hometown in Himachal Pradesh. After a few months of struggle, they thought to grow roses in their fields and sell them to local vendors as roses have been always in demand. Their business started growing up and they hired many workers to manage their garden and do packaging of the flowers.



In their garden bed, there are 23 rose plants in the first row, 21 are in the 2nd, 19 in 3rd row and so on. There are 5 plants in the last row.

- i. How many rows are there of rose plants? (1)
- ii. Also, find the total number of rose plants in the garden. (1)
- iii. How many plants are there in 6th row. (2)

OR

If total number of plants are 80 in the garden, then find number of rows? (2)

37. Read the following text carefully and answer the questions that follow:

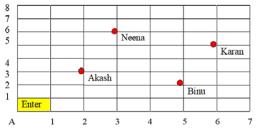
Karan went to the Lab near to his home for COVID 19 test along with his family members.

The seats in the waiting area were as per the norms of distancing during this pandemic (as shown in the figure).

[4]

[4]

His family member took their seats surrounded by red circular area.



i. What is the distance between Neena and Karan? (1)

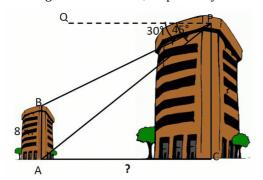
ii. What are the coordinates of seat of Akash? (1)

iii. What will be the coordinates of a point exactly between Akash and Binu where a person can be? (2)**OR**

Find distance between Binu and Karan. (2)

38. Basant and Vinod lives in a housing society in Dwarka, New Delhi. There are two building in their housing society. The first building is 8 meter tall. One day, both of them were just trying to guess the height of the other multi-storeyed building. Vinod said that it might be a 45 degree angle from the bottom of our building to the top of multi-storeyed building so the height of the building and distance from our building to this multi-storeyed building will be same. Then, both of them decided to estimate it using some trigonometric tools. Let's assume that the first angles of depression of the top and bottom of an 8 m tall building from top of a multi-storeyed building are 30° and 45°, respectively.

[4]



i. Now help Vinod and Basant to find the height of the multi-storeyed building.

ii. Also, find he distance between two buildings.

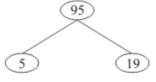
Solution

Section A

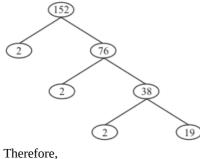
1.

(b) 19

Explanation: Using the factor tree for 95, we have:



Using the factor tree for 152, we have:



 $95 = 5 \times 19$ $152 = 2^3 \times 19$ HCF (95, 152) = 19

2.

(c) 1183914

$$\begin{split} & \textbf{Explanation: L.C.M. (306, 954, 1314)} \\ &= \frac{306 \times 954 \times 1314 \times \text{H.C.F. (306,954,1314)}}{\text{H.C.F. (306,954)} \times \text{H.C.F. (954,1314)} \times \text{H.C.F. (306,1314)}} \\ &= \frac{306 \times 954 \times 1314 \times 18}{18 \times 18 \times 18} = 1183914 \end{split}$$

3.

(b) -11

Explanation: $3x^2 + (k - 1)x + 9 = 0$ x = 3 is a solution of the equation means it satisfies the equation Put x = 3, we get $3(3)^2 + (k - 1) 3 + 9 = 0$ 27 + 3 k - 3 + 9 = 027 + 3 k + 6 = 03 k = -33k = -11

4.

(b) $x^{o} = 85^{o}$ and $y^{o} = 55^{o}$ **Explanation:** According to the question, $x^{o} + y^{o} + 40^{o} = 180^{o}$ $x^{o} + y^{o} = 140^{o}$... (i) and $x^{o} + y^{o} = 30^{o}$... (ii) and $y^{o} = 55^{o}$ On solving eq. (i) and eq. (ii), x + y + x - y = 140 + 302x = 170 $x = 85^{\circ}$ Putting the value of x in equation (i), we get $85^{\circ} + y = 140^{\circ}$ $y = 140^{\circ} - 85^{\circ}$ $y = 55^{\circ}$ we get $x^{\circ} = 85^{\circ}$ and $y^{\circ} = 55^{\circ}$

5.

(d) Real and Distinct roots

Explanation: Comparing the given equation to the below equation

 $ax^{2} + bx + c = 0$ a = 1, b = -6, c = 6 $D = b^{2} - 4ac$ $D = (-6)2 - 4 \times 1 \times 6$ D = 36 - 24 D = 12D > 0.

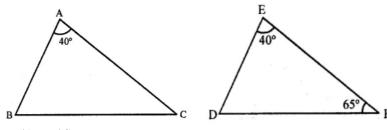
If $b^2 - 4ac > 0$, then the equation has real and distinct roots Hence Real and Distinct roots.

6.

(c) (-4, -15) Explanation: Let the vertex C be C (x,y). Then $\frac{-1+5+x}{1} = 0 \text{ and } \frac{4+2+y}{3} = -3 \Rightarrow x+4 = 0 \text{ and } 6+y = -9$ $\therefore \quad x = -4 \text{ and } y = -15$ so, the coordinates of C are (-4, -15).

7. **(a)** 75^o

Explanation: In \triangle ABC and \triangle DEF $\angle A = \angle E = 40^{\circ}$ $AB: ED = AC: EF, \angle F = 65^{\circ}$



 $\Rightarrow \frac{AB}{ED} = \frac{AC}{EF}$ $\therefore In \triangle ABC and \triangle EDF$ $\angle A = \angle E \quad (each = 40^{\circ})$ $\frac{AB}{ED} = \frac{AC}{EF}$ $\therefore \triangle ABC \sim \triangle EDF \text{ (SAS criterion)}$ $\therefore \angle C = \angle F = 65^{\circ}$ and $\angle B = \angle D$ But $\angle A + \angle B + \angle C = 180^{\circ} \quad (Sum \text{ of angles of a triangle})$ $\Rightarrow 40^{\circ} + 65^{\circ} + \angle C = 180^{\circ}$ $\Rightarrow 105^{\circ} + \angle C = 180^{\circ}$ $\therefore \angle C = 180^{\circ} - 105^{\circ} = 75^{\circ}$

8. **(a)** 13.5 cm.

Explanation: In $\triangle ABC$, $\Rightarrow \frac{AQ}{QC} = \frac{AP}{PB} \Rightarrow \frac{3}{6} = \frac{3.5}{7} \Rightarrow \frac{1}{2}$ Since $\frac{AQ}{QC} = \frac{AP}{PB}$, therefore, QP || BC $\therefore \frac{AQ}{AC} = \frac{QP}{BC}$ $\Rightarrow \frac{1}{3} = \frac{4.5}{BC}$ $\Rightarrow BC = 13.5 cm$

9. **(a)** 6 cm

Explanation: Since the distance between two parallel tangents of a circle is equal to the diameter of the circle. Given: Radius (OP) = 3 cm

: Diameter = $2 \times \text{Radius} = 2 \times 3 = 6 \text{ cm}$

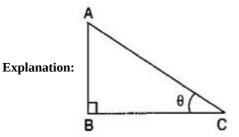
10.

(b) $\frac{1-\cos\theta}{1+\cos\theta}$

Explanation: $(\csc\theta - \cot\theta)^2 = \left(\frac{1}{\sin\theta} - \frac{\cos\theta}{\sin\theta}\right)^2 = \frac{(1-\cos\theta)^2}{\sin^2\theta} = \frac{(1-\cos\theta)^2}{(1-\cos^2\theta)} = \frac{(1-\cos\theta)}{(1+\cos\theta)}$

11.

(d) 60°



Let AB be the electric pole of height $10\sqrt{3}$ m and its shadow be BC of length 10 m. And the angle of elevation of the sun be θ .

 $\therefore \tan \theta = \frac{AB}{BC}$ $\Rightarrow \tan \theta = \frac{10\sqrt{3}}{10}$ $\Rightarrow \tan \theta = \sqrt{3}$ $\Rightarrow \tan \theta = \tan 60^{\circ}$ $\Rightarrow \theta = 60^{\circ}$

12.

(c)
$$\frac{1-\cos\theta}{\sin\theta}$$

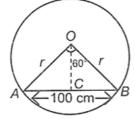
Explanation: We have, $\frac{\sin\theta}{1+\cos\theta} = \frac{\sin\theta(1-\cos\theta)}{(1+\cos\theta)(1-\cos\theta)}$ $= \frac{\sin\theta(1-\cos\theta)}{1-\cos^2\theta} = \frac{\sin\theta(1-\cos\theta)}{\sin^2\theta}$ $= \frac{1-\cos\theta}{\sin\theta}$ (a) $\frac{\pi r^2\theta}{360}$ Explanation: $\frac{\pi r^2\theta}{360}$

14.

13.

(c) 30520.61 cm²

Explanation: In \triangle OAB, by angle sum property



 $60^{\circ} + \angle OAB + \angle OBA = 180^{\circ}$ $\Rightarrow 2\angle OAB = 120^{\circ} \Rightarrow \angle OAB = 60^{\circ}$ $\Rightarrow \triangle OAB$ is an equilateral triangle. $\Rightarrow r = 100 \text{ cm}$ Area of major segment = Area of major sector + Area of $\triangle OAB$

$$= \frac{(360^{\circ} - 60^{\circ})}{360^{\circ}} \times \pi r^{2} + \frac{\sqrt{3}}{4}r^{2}$$

= $\frac{300}{360} \times \frac{22}{7} \times (100)^{2} + \frac{\sqrt{3}}{4} \times 100^{2}$
= $\frac{5}{6} \times \frac{22}{7} \times (100)^{2} + \sqrt{3} \times 2500$
= 26190.48 + 4330.13 = 30520.61 cm²

15. (a) $\frac{5}{11}$

Explanation: Total number of fish = 15 + 18 = 33Male fish = 15Number of possible outcomes = 15Number of total outcomes = 15 + 18 = 33Required Probability = $\frac{15}{33} = \frac{5}{11}$

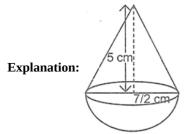
16. **(a)** 0.5

Explanation: Given data = 30, 34, 35, 36, 37, 38, 39, 40 Here n = 8 which is even ∴ Median = $\frac{1}{2} \left[\frac{n}{2} \text{th} + \left(\frac{n}{2} + 1 \right) \text{th} \right]$ term = $\frac{1}{2} (4\text{th} + 5\text{th} \text{ term})$ = $\frac{1}{2} (36 + 37) = \frac{73}{2} = 36.5$ After removing 35, then n = 7 ∴ New median = $\frac{7+1}{2}$ th term = 4th term = 37

$$\therefore$$
 Increase in median = 37 - 36.5 = 0.5

17.

(b) 616 cm³



Volume of water in the cylindrical tub = Volume of the tub

$$=\pi r^2 h=\left(rac{22}{7} imes 5 imes 5 imes 9.8
ight) ext{cm}^3$$
 = 770 cm³

Volume of the solid immersed in the tub = Volume of the hemisphere + Volume of the cone

$$= \left[\left(\frac{2}{3} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times \frac{7}{2} \right) + \left(\frac{1}{3} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 5 \right) \right] \text{cm}^{3}$$
$$= \left(\frac{539}{6} + \frac{385}{6} \right) \text{cm}^{3} = \left(\frac{924}{6} \right) \text{cm}^{3} = 154 \text{ cm}^{3}$$

Volume of water left in the tub = Volume of the tub - Volume of solid immersed

 $= (770 - 154) \text{ cm}^3 = 616 \text{ cm}^3$

18.

(d) 6 Explanation: Mean = 8.1 $\Sigma f_{i}x_{i} = 132 + 5k$

$$\sum_{i=1}^{1} f_i = 20$$

$$\therefore \text{ Mean} = \frac{\sum f_i x_i}{\sum f_i} \Rightarrow 8.1 = \frac{132 + 5k}{20}$$

$$\Rightarrow 132 + 5k = 8.1 \times 20 = 162$$

$$\Rightarrow 5k = 162 - 132 = 30$$

$$\Rightarrow k = \frac{30}{5} = 6$$

19. **(a)** Both A and R are true and R is the correct explanation of A. **Explanation:** Distance of point (5, 12) from 8 origin is given, $d = \sqrt{(5-0)^2 + (12-0)^2}$ $= \sqrt{25 + 144} = \sqrt{169} = 13$

20. (a) Both A and R are true and R is the correct explanation of A. Explanation: 380 is not divisible by 18.

Section B

21. 2 x - 2 y - 2 = 0.....(1) 4 x - 4 y - 5 = 0.....(2) Here, $a_1 = 2$, b = -2, $c_1 = -2$ $a_2 = 4$, $b_2 = -4$, $c_2 = -5$ We see that $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

Hence, the lines represented by the equations(1) and (2) are parallel.

Therefore, equations (1) and (2) have no solution, i.e., the given pair of a linear equation is inconsistent.

22. According to question it is given that D and E are the points on sides AB and AC respectively

Also $AD = \frac{1}{3}BD$, $AE = 4.5 \text{ cm}, DE \parallel BC$ $\therefore \frac{AD}{BD} = \frac{AE}{EC}$ $\Rightarrow \frac{\frac{1}{3}BD}{BD} = \frac{4.5}{EC}$ $\Rightarrow \frac{1}{3} = \frac{4.5}{EC}$ $\Rightarrow EC = 4.5 \times 3 \text{ cm}$ $\Rightarrow EC = 13.5 \text{ cm}$ Now, AC = AE + EC = 4.5 + 13.5 = 18 cm

OR

According to question it is given that ABCD is a rectangle and p is the midpoint of DC.

 \therefore AD = BC = 9 cm QC = BQ + BC = 7 + 9 = 16 cm $PC = \frac{1}{2}CD \Rightarrow PC = 12 cm$ In right riangle PCQ using Pythagoras theorem $PQ^2 = QC^2 + PC^2$ $PQ^2 = 16^2 + 12^2 = 400 \Rightarrow PQ = 20 \text{ cm}$ In right \triangle ABQ using Pythagoras theorem $AQ^2 = AB^2 + BQ^2 \Rightarrow AQ^2 = 24^2 + 7^2 = 625$ \Rightarrow AQ = 25 cm In right \triangle ADP using Pythagoras theorem $AP^2 = AD^2 + DP^2 \Rightarrow AP^2 = 9^2 + 12^2$ $\Rightarrow AP^2 = 81 + 144$ $\Rightarrow AP^2 = 255$ AP = 15 cmIn $\triangle APQ$, $AP^2 = 15^2 = 225$ $PQ^2 = 20^2 = 400 \Rightarrow AP^2 + PQ^2 = 625$ Also, $AQ^2 = 25^2 = 625 \Rightarrow AQ^2 = AP^2 + PQ^2$ $\therefore \triangle$ APQ is a right angled \triangle (using converse of BPT) $\therefore \angle APQ = 90^{\circ}$ 23. 0

Given: PQ is a diameter of a circle with centre O.

The lines AB and CD are the tangents at P and Q respectively.

To Prove: AB || CD

Proof: Since AB is a tangent to the circle at P and OP is the radius through the point of contact.

∴∠OPA = 90[°] (i)

[The tangent at any point of a circle is \perp to the radius through the point of contact]

 \because CD is a tangent to the circle at Q and OQ is the radius through the point of contact.

 $\therefore \angle OQD = 90^{\circ}$ (ii)

[The tangent at any point of a circle is \perp to the radius through the point of contact]

From eq. (i) and (ii), $\angle OPA = \angle OQD$

But these form a pair of equal alternate angles also,

 \therefore AB \parallel CD

24. Given: $cosec^{2}\theta(1 + \cos\theta)(1 - \cos\theta) = \lambda$ $\Rightarrow cosec^{2}\theta\{(1 + \cos\theta)(1 - \cos\theta)\} = \lambda$ $\Rightarrow cosec^{2}\theta(1 - \cos^{2}\theta) = \lambda$ $\Rightarrow cosec^{2}\theta\sin^{2}\theta = \lambda$ $\Rightarrow \frac{1}{\sin^{2}\theta} \times \sin^{2}\theta = \lambda$ $\Rightarrow 1 = \lambda$ $\Rightarrow \lambda = 1$

Thus, the value of λ is 1.

25. We have, r = 16.5 km and θ = 80°.

Let A be the area of the sea over which the ships are warmed. Then,

$$A = rac{ heta}{360} imes \pi r^2$$
 = $rac{80}{360} imes 3.14 imes 16.5 imes 16.5 imes m^2$ = 189.97 km² OR

We have

R = 6 cm Length of the arc = 3π cm as we know that arc length = $\frac{\theta}{360} \times 2\pi r$ Substituting the values we get, $3\pi = \frac{\theta}{360} \times 2\pi \times 6$...(1) Now we will simplify the equation (1) as below, $3\pi = \frac{\theta}{360} \times 12\pi$ $3\pi = \frac{\theta}{30} \times \pi$ $3 = \frac{\theta}{30}$ $\theta = 90^{\circ}$

Therefore, the angle subtended at the centre of the circle is 90° .

Section C

26. Let us prove $\sqrt{5}$ irrational by contradiction.

Let us suppose that $\sqrt{5}$ is rational. It means that we have co-prime integers a and b ($b \neq 0$) Such that $\sqrt{5} = \frac{a}{b}$ $\Rightarrow b \sqrt{5}=a$ Squaring both sides, we get $\Rightarrow 5b^2 = a^2 \dots (1)$ It means that 5 is factor of a^2 Hence, 5 is also factor of a by Theorem. ... (2) If, 5 is factor of a, it means that we can write a = 5c for some integer c. Substituting value of a in (1), $5b^2 = 25c^2$

 $\Rightarrow b^2 = 5c^2$

It means that 5 is factor of b^2 .

Hence, 5 is also factor of *b* by Theorem. ... (3)

From (2) and (3) , we can say that 5 is factor of both a and b .

But, *a* and *b* are co-prime .

Therefore, our assumption was wrong. $\sqrt{5}$ cannot be rational. Hence, it is irrational.

27. : α and β are zeroes of given polynomial

So, $x^2 + 9x + 20 = 0$

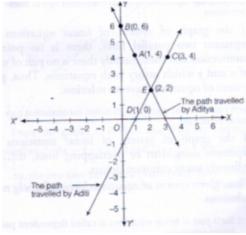
 $x^2 + 4x + 5x + 20 = 0$ x(x + 4) + 5(x + 4) = 0(x + 5)(x + 4) = 0x = -5 and x = -4 $\therefore \alpha = -5 \text{ and } \beta = -4$ Now, $\alpha + 1 = -4$ and $\beta + 1 = -3$ So, product of zeroes= $(-4) \times (-3) = 12$ Sum of zeroes = -7Now polynomial = x^2 - (sum of zeroes)x + (product of zeroes) $Polynomial = x^2 + 7x + 12$ 28. The given equations are $\sqrt{2}x - \sqrt{3}y = 0$ (i) $\sqrt{3}x - \sqrt{8}y = 0$ (ii) From equation (i), we obtain: $x = rac{\sqrt{3}y}{\sqrt{2}}$...(iii) Substituting this value in equation (ii), we obtain: $\sqrt{3}\left(\frac{\sqrt{3}y}{\sqrt{2}}\right) - \sqrt{8}y = 0$ $\frac{3y}{\sqrt{2}} - 2\sqrt{2}y = 0$ $y\left(\frac{3}{\sqrt{2}} - 2\sqrt{2}\right) = 0$ y = 0Substituting the value of y in equation (iii), we obtain: x = 0 $\therefore x = 0, y = 0$

Hence the solution of given equation is (0,0).

OR

Let the given points be A(1,4), B(0,6), C(3,4) and D(1,0).

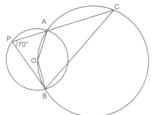
On plotting points A and B and joining them, we get the path travelled by Aditya. Similarly, on plotting points C and D and joining them, we get path travelled by Aditi.



It is clear from the graph that both of them cross each other at point E(2,2).

29. Consider the smaller circle whose centre is given as O.

The angle subtended by an arc at the centre of the circle is double the angle subtended by the arc in the remaining part of the circle.



Therefore, we have,

∠AOB = 2∠APB

 $= 2(70^{\circ})$

 $\angle AOB = 140^{\circ}$

Now consider the larger circle and the points A,C, B and O along its circumference. AOBC from a cycle quadrilateral.

In a cyclic quadrilateral, the opposite angles are supplementary, meaning that the opposite angles add up to 180°.

 $\angle AOB + \angle ACB = 180^{\circ}$

 $\angle ACB = 180^{\circ} - \angle AOB$

 $= 180^{\circ} - 140^{\circ}$

 $\angle ACB = 40^{\circ}$

Therefore, the measure of angle ACB is 40°.

30. $\begin{array}{c}
30.\\
P & 5 \text{ cm} & 0\\
In \triangle PQR, \text{ by Pythagoras theorem}\\
PR^2 = PQ^2 + QR^2\\
\Rightarrow (25 - QR)^2 = 5^2 + QR^2[\because PR + QR = 25 \text{ cm} \Rightarrow PR = 25 - QR]\\
625 - 50QR + QR^2 = 25 + QR^2\\
\Rightarrow 600 - 50QR = 0\\
\Rightarrow QR = \frac{600}{50} = 12 \text{ cm}\\
Now, PR + QR = 25 \text{ cm}\\
\Rightarrow PR = 25 - QR = 25 - 12 = 13 \text{ cm}\\
\text{Hence, sin } P = \frac{QR}{PR} = \frac{12}{13}, \cos P = \frac{PQ}{PR} = \frac{5}{13} \text{ and, tan } P = \frac{QR}{PQ} = \frac{12}{5} \\
OR\\
\text{LHS} = \frac{\cos^3 \theta + \sin^3 \theta}{\cos \theta + \sin \theta} + \frac{\cos^3 \theta - \sin^3 \theta}{\cos \theta - \sin \theta} \\
= \frac{(\cos \theta + \sin \theta)(\cos^2 \theta + \sin^2 \theta - \sin \theta \cos \theta)}{(\cos \theta + \sin \theta)} + \frac{(\cos \theta - \sin \theta)(\cos^2 \theta + \sin^2 \theta + \sin \theta \cos \theta)}{(\cos \theta - \sin \theta)}
\end{array}$

 $= (1 - \sin\theta \cos\theta) + (1 + \sin\theta \cos\theta)$

 $= 1 + 1 - sin\theta cos\theta + sin\theta cos\theta$

= 2 = RHS

31. Total number of cards in one deck of cards is 52.

 \therefore Total number of outcomes n = 52

i. Let E₁= Event of getting a king of red color. So number of outcomes favourable to E₁ m = 2 So P(E₁)= $\frac{m}{n} = \frac{2}{52} = \frac{1}{26}$

ii. Let E₂= Event of getting a face card

 \therefore Numbers of outcomes favourable to E₂, m= 12. Hence P(E₂) = $\frac{m}{n} = \frac{12}{52} = \frac{3}{13}$

iii. Let E₃= Event of getting a red face card

 \therefore Numbers of outcomes favourable to E₃ = 6 [\therefore there are 6 red face cards in a deck] Hence P(E₃) = $\frac{m}{n} = \frac{6}{52} = \frac{3}{26}$

iv. Let E_4 = Event of getting a jack of heart

: Numbers of outcomes favourable to $E_4 = 1$ [: there is only one jack of heart in deck of cards.]

Hence P(E₄)= $\frac{m}{n} = \frac{1}{52}$

v. Let E₅= Event of getting a spade

 \therefore Numbers of outcomes favourable to $E_5 = 13$ [\because there are 13 spade in a deck]

Hence P(E₅) = $\frac{m}{n} = \frac{13}{52}$

vi. Let E_6 = Event of getting the queen of diamond

: Numbers of outcomes favourable to $E_6 = 1$ [: there is only one queen of diamond in a deck]

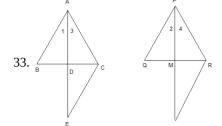
Hence, $P(E_6) = \frac{m}{n} = \frac{1}{52}$

Section D

 $\left(rac{2x}{x-5}
ight)^2+5\left(rac{2x}{x-5}
ight)-24=0$ Let $rac{2x}{(x-5)}$ be y $\therefore y^2 + 5y - 24 = 0$ Now factorise, $y^2 + 8y - 3y - 24 = 0$ y(y+8) - 3(y+8) = 0(y+8)(y-3) = 0y = 3, -8Putting y=3 $\frac{2x}{x-5} = 3$ 2x = 3x - 15x = 15 Putting y = -8 $\frac{2x}{x-5} = -8$ 2x = -8x + 4010x = 40x = 4Hence, x is 15, 4

OR

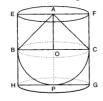
According to the question, let the consecutive multiples of 7 be 7x and 7x +7 $(7x)^2 + (7x + 7)^2 = 637$ or, $49x^2 + 49x^2 + 49 + 98x = 637$ or, $98x^2 + 98x - 588 = 0$ or, $x^2 + x - 6 = 0$ or, (x + 3)(x - 2) = 0or, x = -3, 2 Rejecting the value, x=2Thus, the required multiples are, 14 and 21.



Given : In $\triangle ABC$ and $\triangle PQR$ The AD and PM are their medians, such that $\frac{AB}{PQ} = \frac{AD}{PM} = \frac{AC}{PR}$ To prove : $\triangle ABC \sim \triangle PQR$ Construction : Produce AD to E such that AD = DE and produce PM to N such that PM = MN. Join CE and RN. Proof : In $\triangle ABD$ and $\triangle EDC$ AD = DE $\angle ADB = \angle EDC$ (vertically opposite angles) BD = DC(as AD is a median) $\therefore \quad \triangle ABD \equiv \triangle EDC$ (By SAS congruency) or, AB = CE (By CPCT) Similarly, PQ = RN $\frac{AB}{PQ} = \frac{AD}{PM} = \frac{AC}{PR} \text{ (Given)}$ or, $\frac{CE}{RN} = \frac{2AD}{2PM} = \frac{AC}{PR}$ or $\frac{CE}{RN} = \frac{AE}{PN} = \frac{AC}{PR}$ So $\Delta ACE \sim \Delta PRN$ $\angle 3 = \angle 4$ Similarly $\angle 1 = \angle 2$ $\angle 1 + \angle 3 = \angle 2 + \angle 4$ So $\angle A = \angle P$ and $\frac{AB}{PQ} = \frac{AC}{PR} \text{ (given)}$ Hence $\Delta ABC \sim \Delta PQR$ 34. Volume of solid = $\frac{1}{3} \times \frac{22}{7} \times (7)^2 \times 3.5 + \frac{2}{3} \times \frac{22}{7} \times (7)^3$ $= \frac{22}{7} \times (7)^2 \times \left[\frac{3.5}{3} + \frac{2}{3} \times 7\right]$ $= 898\frac{1}{3}$ or 898.33 cm³

OR

Let BPC be the hemisphere and ABC be the cone mounted on the base of the hemisphere. Let EFGH be the right circular cylinder circumscribing the given toy.



We have,

Given radius of cone, cylinder and hemisphere (r) = $\frac{4}{2}$ = 2 cm

Height of cone (l) = 2 cmHeight of cylinder (h) = 4 cm

Now, Volume of the right circular cylinder = $\pi r^2 h = \pi \times 2^2 \times 4 cm^3 = 16\pi cm^3$ Volume of the solid toy = $\left\{\frac{2}{3}\pi \times 2^3 + \frac{1}{3}\pi \times 2^2 \times 2\right\} cm^3 = 8\pi cm^3$

. Required space = Volume of the right circular cylinder - Volume of the toy

 $= 16\pi \text{cm}^3 - 8\pi \text{cm}^3 = 8\pi \text{cm}^3.$

Hence, the right circular cylinder covers 8π cm³ more space than the solid toy.

So, remaining volume of cylinder when toy is inserted in it = 8π cm³

35. We may observe from the given data that maximum class frequency is 40 belonging to 1500 - 2000 interval.

Class size (h) = 500 Mode = $1 + \frac{f - f_1}{2f - f_1 - f_2} \times h$ Lower limit (*l*) of modal class = 1500 Frequency (f) of modal class = 40 Frequency (f_1) of class preceding modal class = 24 Frequency (f_2) of class succeeding modal class = 33 mode = $1500 + \frac{40 - 24}{2 \times 40 - 24 - 33} \times 500$ = $1500 + \frac{16}{80 - 57} \times 500$ = 1500 + 347.826= $1847.826 \approx 1847.83$

Expenditure (in ₹.)	Number of families f _i	x _i	d _i = x _i - 2750	u _i	u _i f _i
1000-1500	24	1250	-1500	-3	-72
1500-2000	40	1750	-1000	-2	-80
2000-2500	33	2250	-500	-1	-33
2500-3000	28	2750=a	0	0	0
3000-3500	30	3250	500	1	30
3500-4000	22	3750	1000	2	44
4000-4500	16	4250	1500	3	48
4500-5000	7	4750	2000	4	28
	Σf_i = 200				$\Sigma f_i d_i$ = - 35

Mean $\overline{x} = a + \frac{\Sigma f_i d_i}{\Sigma f_i} \times h$ $\overline{x} = 2750 + \frac{-35}{200} \times 500$ $\overline{x} = 2750 - 87.5$ $\bar{x} = 2662.5$

Section E

36. i. The number of rose plants in the 1st, 2nd, are 23, 21, 19, ... 5 a = 23, d = 21 - 23 = - 2, a_n = 5 $\therefore a_n = a + (n - 1)d$ or, 5 = 23 + (n - 1)(-2)

or, 5 = 23 - 2n + 2

or, 5 = 25 - 2n

or, 2n = 20

or, n = 10

ii. Total number of rose plants in the flower bed, nr

$$S_{n} = \frac{n}{2} [2a + (n - 1)d]$$

$$S_{10} = \frac{10}{2} [2(23) + (10 - 1)(-2)]$$

$$S_{10} = 5[46 - 20 + 2]$$

$$S_{10} = 5(46 - 18)$$

$$S_{10} = 5(28)$$

$$S_{10} = 140$$
iii. $a_{n} = a + (n - 1)d$

$$\Rightarrow a_{6} = 23 + 5 \times (-2)$$

$$\Rightarrow a_{6} = 13$$
OR

$$S_{n} = \frac{n}{2} [2a + (n - 1)d]$$

$$\Rightarrow 80 = \frac{n}{2} [2 \times 23 + (n - 1) \times -2]$$

$$\Rightarrow 80 = 23n - n^{2} + n$$

$$\Rightarrow n^{2} - 24n + 80 = 0$$

$$\Rightarrow (n - 4)(n - 20) = 0$$

$$\Rightarrow n = 4 \text{ or } n = 20$$

$$n = 20 \text{ not possible}$$

$$a_{20} = 23 + 19 \times (-2) = -15$$
Number of plants cannot be negative.

n = 4

37. i. Position of Neena = (3, 6) Position of Karan = (6, 5) Distance between Neena and Karan = $\sqrt{(6-3)^2 + (5-6)^2}$ = $\sqrt{9 + (-1)^2}$ = $\sqrt{10}$ ii. Co-ordinate of seat of Akash = 2, 3 iii. Akash Middle point Binu (2,3) (5.2) Co-ordinate of middle point = $\left(\frac{2+5}{2}, \frac{3+2}{2}\right)$ = 3.5, 2.5 OR Discontinue of point (6, 5)

Binu = (5, 5); Karan = (6, 5)
Distance =
$$\sqrt{(6-5)^2 + (5-2)^2}$$

= $\sqrt{1+9}$
= $\sqrt{10}$

38. Let h is height of big building, here as per the diagram.

AE = CD = 8 m (Given) BE = AB-AE = (h - 8) mLet AC = DE = xAlso, $\angle FBD = \angle BDE = 30^{\circ}$ $\angle FBC = \angle BCA = 45^{\circ}$ в 30 (h – 8 m 300 Е D h m 8 cm 8 cm 45° xm In \triangle ACB, $\angle A = 90^{\circ}$ $an 45^\circ = rac{AB}{AC}$ \Rightarrow x = h, ...(i) In \triangle BDE, $\angle E = 90^{\circ}$ $an 30^\circ = rac{BE}{ED}$ \Rightarrow $x = \sqrt{3}(h-8)$.(ii) From (i) and (ii), we get $h = \sqrt{3}h - 8\sqrt{3}$ $h(\sqrt{3} - 1) = 8\sqrt{3}$ $h(\sqrt{3} - \frac{1}{2}) = 0.02$ $h = \frac{8\sqrt{3}}{\sqrt{3} - 1} = \frac{8\sqrt{3}}{\sqrt{3} - 1} \times \frac{\sqrt{3} + 1}{\sqrt{3} + 1}$ $= \frac{1}{2} \times (24 + 8\sqrt{3}) = \frac{1}{2} \times (24 + 13.84) = 18.92m$

Hence height of the multistory building is 18.92 m and the distance between two buildings is 18.92 m.