

Section B

21. Solve: $\frac{5}{6} + \left(\frac{-2}{5}\right) - \left(\frac{-2}{15}\right)$. [2]

22. Solve the equation and check your result: $4z + 3 = 6 + 2z$ [2]

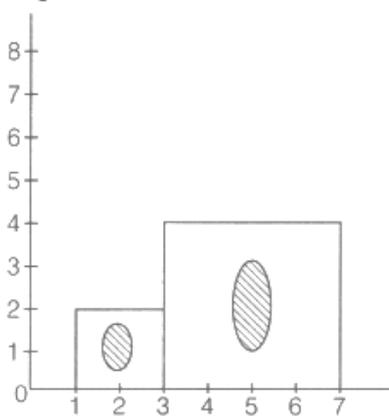
OR

Solve: $\frac{3t-2}{3} + \frac{2t+3}{2} = t + \frac{7}{6}$

23. What is the probability that a student chosen at random out of 3 girls and 4 boys is a boy? [2]

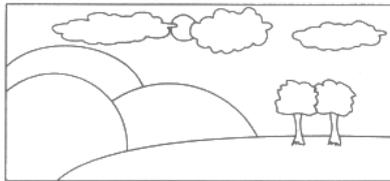
24. A decimal number is multiplied by itself. If the product is 51.84, then find the number. [2]

25. A photographer uses a computer program to enlarge a photograph. What is the scale according to which the width has enlarged in the given graph? [2]



OR

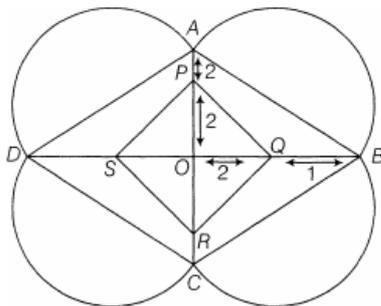
The actual length of a painting was 2m. What is the length in the photograph if the scale used is 1 mm : 20 cm.



26. Write 1625000000 in standard form. [2]

27. Solve: $\frac{2y-3}{4} - \frac{3y-5}{2} = y + \frac{3}{4}$ [3]

28. A rangoli has been drawn on the floor of a house. ABCD and PQRS both are in the shape of a rhombus. Find the radius of semi-circle drawn on each side of rhombus ABCD. [3]



OR

The adjacent angles of a parallelogram are $(2x - 4)^\circ$ and $(3x - 1)^\circ$. Find the measures of all angles of the parallelogram.

29. Using distributive law, find the square of 101. [3]

30. Find the cube root of 110592 by prime factorisation method. [3]

31. The price of a TV is ₹13000. The sales tax charged on it is at the rate of 12%. Find the amount that Vinod will have to pay if he buys it. [3]

OR

Find the difference between compound interest and simple interest on ₹45000 at 12% per annum for 5yr.

32. The sides of rectangle are $3a^2 + 2b$ and $5a^2 - 4b$. Find its perimeter. [3]
33. The ratio of the radius and height of a cylinder is 2 : 3. If its volume is 12936 cm^3 , find the total surface area of the cylinder. [3]
34. Work out the division: $9x^2y^2(3z - 24) \div 27xy(z - 8)$ [3]
35. The number of hours spent by a school student on various activities on a working day, is given below. Construct a pie chart using the angle measurement. [4]

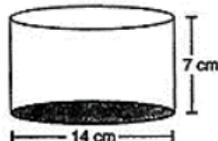
Activity	Sleep	School	Play	Homework	Others
Number of hours	8	6	3	3	4

36. What price should a shopkeeper mark on article that costs him ₹600 to gain 20%, after allowing a discount of 10%? [4]
37. The adjacent sides of a rectangle are $x^2 - 4xy + 7y^2$ and $x^3 - 5xy^2$. Find the area. [4]
38. Diameter of cylinder A is 7 cm, and the height is 14 cm. Diameter of cylinder B is 14 cm and height is 7 cm. Without doing any calculations can you suggest whose volume is greater? Verify it by finding the volume of both the cylinders. Check whether the cylinder with greater volume also has greater surface area? [4]

i.



ii.



39. Factorise: $25a^2 - 4b^2 + 28bc - 49c^2$ [4]

OR

Factorize $x^4 - y^4$

40. Draw a graph for the radius and circumference of circle using a suitable scale. Form the graph, [4]
- find the circumference of the circle when radius is 42 units.
 - at what radius will the circumference of the circle be 220 units?

Solution

Section A

1.

(c) 1

$$\begin{aligned}\text{Explanation: } & \frac{-19}{21} \times \left(\frac{-21}{19}\right) \\ & = \frac{399}{399} \\ & = 1\end{aligned}$$

2.

(c) 1

$$\begin{aligned}\text{Explanation: } & \frac{-17}{18} \times \left(\frac{-18}{17}\right) \\ & = \frac{306}{306} \\ & = 1\end{aligned}$$

3.

(a) $\frac{b-a}{k-m}$

$$\begin{aligned}\text{Explanation: } & \text{Given equation } kx + a = mx + b \\ \Rightarrow & kx - mx = b - a \text{ [mx is transposed as } -mx, a \text{ is transposed as } -a] \\ \Rightarrow & x(k-m) = b - a \\ \Rightarrow & x = \frac{b-a}{k-m}\end{aligned}$$

4.

(d) 48

$$\begin{aligned}\text{Explanation: } & \text{let the number of boys and girls} = x \\ \text{ratio} & = 7 : 5 \\ \text{boys} & = 7x \\ \text{girls} & = 5x \\ \text{According to question,} \\ 7x & = 5x + 8 \\ \text{By transposing,} \\ 7x - 5x & = 8 \\ 2x & = 8 \\ x & = \frac{8}{2} \\ x & = 4 \\ \text{now the number of boys} & = 7x = 28 \\ \text{the number of girls} & = 5x = 20 \\ \text{total students} & = 28 + 20 = 48\end{aligned}$$

5.

(d) 144°

$$\begin{aligned}\text{Explanation: } & \text{Let the angles of quadrilateral be } x, 2x, 3x \text{ and } 4x. \\ \text{According to the question,} \\ \text{Sum of all angles of quadrilateral} & = 360^\circ \\ x + 2x + 3x + 4x & = 360^\circ \\ \Rightarrow 10x & = 360^\circ \\ \therefore x & = 36^\circ \\ \text{Hence, largest angle of quadrilateral} & = 4 \times 36^\circ \\ & = 144^\circ\end{aligned}$$

6.

(d) $10^\circ, 20^\circ$

$$\text{Explanation: In a parallelogram, adjacent angles are supplementary.}$$

$$\therefore 120^\circ + (5x + 10)^\circ = 180^\circ$$

$$\Rightarrow 5x + 10^\circ + 120^\circ = 180^\circ$$

$$\Rightarrow 5x = 180^\circ - 130^\circ$$

$$\Rightarrow 5x = 50^\circ$$

$$\Rightarrow x = 10^\circ$$

Also, opposite angles are equal in a parallelogram.

$$\text{Therefore, } 6y = 120^\circ \Rightarrow y = 20^\circ$$

7.

(c) $\frac{n(n-3)}{2}$

Explanation: We know that the number of diagonals in a polygon of n sides = $\frac{n(n-3)}{2}$

8.

(b) 1234

Explanation: From the prime factorization of $\sqrt{1522756}$ we get 1234.

9.

(c) 25

Explanation: Prime factors of 675,

3	675
3	225
3	75
5	25
5	5
	1

$$\therefore 675 = 3 \times 3 \times 3 \times 5 \times 5$$

Hence, quotient, on dividing of 675 by 25 = $3 \times 3 \times 3$, it is a perfect cube number.

10. (a) $\frac{5}{3}$

Explanation: $(5)^{3x} = 5^5 \Rightarrow 3x = 5$

$$\Rightarrow x = \frac{5}{3}$$

11.

(d) Rs 17,250

Explanation: Price of the Washing Machine = Rs.15,000

$$\text{Sale tax} = ₹ \frac{15000 \times 15}{100}$$

$$= \text{Rs } 2,250$$

$$\text{Amount Arjun will have to pay} = \text{Rs } (15,000 + 2,250)$$

$$= \text{Rs.17,250}$$

12.

(b) $3x^2 + 2xy - 5y^2$

Explanation: $(x - y)(3x + 5y)$

solving brackets we get,

$$x(3x + 5y) - y(3x + 5y)$$

$$3x^2 + 5xy - 3xy - 5y^2$$

$$3x^2 + 2xy - 5y^2$$

13. (a) 1 : 100

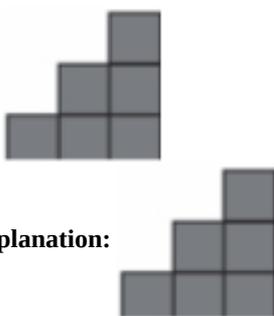
Explanation: Scale of map = $\frac{\text{Size drawn}}{\text{Actual size}}$

$$= \frac{9 \text{ cm}}{900 \text{ cm}} \text{ (because 9 m = 900 cm)}$$

$$= \frac{1}{100}$$

Thus, scale is 1 : 100.

14. (a)



Explanation:

15. (a) 162 cm^3

Explanation: Let edges of a cuboid be x , $2x$ and $3x$, respectively.

$$\therefore l = x, b = 2x, h = 3x$$

Total surface area of cuboid = $2(lb + bh + hn)$

$$\Rightarrow 198 = 2(x \cdot 2x + 2x \cdot 3x + 3x \cdot x)$$

$$\Rightarrow 99 = 2x^2 + 6x^2 + 3x^2$$

$$\Rightarrow 11x^2 = 99$$

$$\Rightarrow x^2 = \frac{99}{11} \Rightarrow x^2 = 9$$

$$\therefore x = 3$$

\therefore Volume of cuboid = $x \times 2x \times 3x$

$$= 6x^3 = 6(3)^3$$

$$= 6 \times 27 = 162 \text{ cm}^3$$

16.

(d) 10^6

Explanation: 10^6

17.

(d) -1

Explanation:
$$\frac{\left(-\frac{1}{2}\right)^5}{\left(-\frac{1}{2}\right)^4} \div \frac{\left(-\frac{1}{8}\right)}{\left(-\frac{1}{4}\right)} = \left(-\frac{1}{2}\right)^{5-4} \div \left[\left(\frac{1}{2}\right)^3 \times \left(\frac{1}{2}\right)^{-2}\right]$$

$$= \left(-\frac{1}{2}\right)^1 \div \left(\frac{1}{2}\right)^1 = -1$$

18. (a) 512

Explanation: 512

19.

(c) 12.5 days

Explanation: This is a case of inverse proportion as with a decrease in the number of men more days will be needed to complete the work

In inverse proportion, the value of constant is given by $x \times y$

$$10 \times 6 \times 5 = 8 \times a \times 3 \text{ (where } a \text{ is the number of days)}$$

$$\frac{300}{24} = a$$

$$12.5 \text{ days} = a$$

20.

(d) $60x$

Explanation: No. of shirts Time

$$x \frac{3}{4} \text{ min}$$

$$s \frac{3}{4} \times 60 = 45 \text{ min}$$

\therefore It is direct variation

$$x : \frac{3}{4} :: s : 45$$

$$s = \frac{45x}{3/4} = 60x$$

Section B

21. LCM of 6,5 and 15 is 30

$$= \frac{[25+(-12)-(-4)]}{30}$$

$$= \frac{[25-12+4]}{30}$$

$$= \frac{[29-12]}{30}$$

$$= \frac{17}{30}$$

22. $4z + 3 = 6 + 2z$

$4z - 2z = 6 - 3$... [Transposing $2z$ to L.H.S. and 3 to R.H.S]

$$\therefore 2z = 3$$

$$\therefore z = \frac{3}{2}$$
 ... [Dividing both sides by 2]

This is the required solution.

Verification,

$$\text{L.H.S} = 4 \left(\frac{3}{2} \right) + 3 = 6 + 3 = 9$$

$$\text{R.H.S} = 6 + 2z = 6 + 2 \left(\frac{3}{2} \right) = 6 + 3 = 9$$

Therefore, L.H.S = R.H.S

OR

$$\text{Given, } \frac{3t-2}{3} + \frac{2t+3}{2} = t + \frac{7}{6}$$

$$\Rightarrow \frac{2(3t-2)+3(2t+3)}{6} = \frac{6t+7}{6}$$

$$\Rightarrow 6t - 4 + 6t + 9 = 6t + 7$$

$$\Rightarrow 12t + 5 = 6t + 7$$

$$\Rightarrow 12t - 6t = 7 - 5$$
 [transposing $6t$ to LHS and 5 to RHS]

$$\Rightarrow 6t = 2$$

$$\Rightarrow \frac{6t}{6} = \frac{2}{6}$$
 [dividing both sides by 6]

$$\therefore t = \frac{1}{3}$$

23. Probability = $\frac{\text{Number of favourable outcomes}}{\text{Total number of possible outcomes}}$

Number of favourable chance to get boys = 4

$$\text{Total} = 4+3 = 7$$

$$\text{Probability} = \frac{4}{7}$$

24. Let the number be x . Then, product = $x \times x = x^2$

But product = 51.84 [given]

$$\text{therefore, } x^2 = 51.84$$

$$\Rightarrow x = \sqrt{51.84}$$

Now, place the bar over the numbers, then square root is given below,

$$\therefore x = \sqrt{51.84} = 7.2$$

	7.2
7	51.84
	49
142	284
	284
	0

Hence, the required number is 7.2

25. By the given graph, we have width before editing = 2 units

Width after editing = 4 units

$$\text{We know that, Scale} = \frac{\text{Size before editing}}{\text{Size after editing}}$$

$$\therefore \text{Scale} = \frac{2}{4} = \frac{1}{2} = 1:2$$

Hence, scale used to enlarge the photograph is 1 : 2.

OR

The actual length of the painting was 2 m or $2 \times 100 = 200$ cm [∵ 1 m = 100 cm]

Scale used in the painting = 1 mm : 20 cm

Hence, length of painting in photograph = Scale \times Actual Size $\left[\because \text{scale} = \frac{\text{size drawn}}{\text{actual size}} \right]$
 $= \frac{1}{20} \times 200 = 10 \text{ mm}$

26. $16250000000 = 1625 \times 10000000 = 1.625 \times 1000 \times 10000000 = 1.625 \times 10^3 \times 10^7 = 1.625 \times 10^{10}$

27. Given, $\frac{2y-3}{4} - \frac{3y-5}{2} = y + \frac{3}{4}$

$$\Rightarrow \frac{2y-3-2(3y-5)}{4} = \frac{4y+3}{4}$$

$$\Rightarrow 2y - 3 - 6y + 10 = 4y + 3$$

$$\Rightarrow -4y + 7 = 4y + 3$$

$$\Rightarrow -4y - 4y = 3 - 7 \text{ [transposing } 4y \text{ to LHS and } 7 \text{ to RHS]}$$

$$\Rightarrow -8y = -4$$

$$\Rightarrow \frac{-8y}{-8} = \frac{-4}{-8} \text{ [dividing both sides by } -8]$$

$$\therefore y = \frac{1}{2}$$

28. In rhombus ABCD,

$$AO = OP + PA = 2 + 2 = 4 \text{ units and } OB = OQ + QB = 2 + 1 = 3 \text{ units}$$

We know that, diagonals of rhombus bisect each other at 90° .

Now,

$$\text{In } \triangle OAB, (AB)^2 = (OA)^2 + (OB)^2 \text{ [by Pythagoras theorem]}$$

$$\Rightarrow (AB)^2 = (4)^2 + (3)^2 = 25$$

$$\Rightarrow AB = \sqrt{25} \Rightarrow AB = 5 \text{ units'}$$

Since, AS is diameter of semi-circle.

$$\therefore \text{radius} = \frac{\text{Diameter}}{2} = \frac{AB}{2} = \frac{5}{2} = 2.5 \text{ units}$$

Hence, radius of the semi-circle is 2.5 units.

OR

Since, the adjacent angles of a parallelogram are supplementary.

$$\therefore (2x - 4)^\circ + (3x - 1)^\circ = 180^\circ$$

$$\Rightarrow 5x - 5^\circ = 180^\circ$$

$$\Rightarrow 5x = 185^\circ$$

$$\Rightarrow x = \frac{185^\circ}{5} \Rightarrow x = 37^\circ$$

Thus, the adjacent angles are

$$x = 37^\circ$$

$$2x - 4 = 2 \times 37^\circ - 4 = 74 - 4 = 70^\circ$$

$$\text{and } 3x - 1 = 3 \times 37^\circ - 1 = 111 - 1 = 110^\circ$$

Hence, the angles are $70^\circ, 110^\circ, 70^\circ, 110^\circ$

[\because opposite angles in a parallelogram are equal]

29. By using distributive law,

$$\text{We have, } 101 = 100 + 1$$

$$\text{So, } 101^2 = (100 + 1)^2$$

$$= (100 + 1)(100 + 1)$$

$$= 100(100 + 1) + 1(100 + 1)$$

$$= ((100 \times 100) + (100 \times 1)) + ((1 \times 100) + (1 \times 1))$$

$$= 10000 + 100 + 100 + 1$$

$$= 10201$$

\therefore The square of the given number i.e. $101^2 = 10201$

32. Perimeter of a rectangle = 2(Sum of the sides)

$$= 2 [(3a^2 + 2b) + (5a^2 - 4b)]$$

$$= 2 [3a^2 + 2b + 5a^2 - 4b]$$

$$= 2 [8a^2 - 2b]$$

$$= 16a^2 - 4b$$

33. The ratio of the radius and height of a cylinder = 2 : 3

Let the radius of the cylinder be $2x$ and the height of the cylinder be $3x$.

$$\text{Volume of the cylinder} = 12936 \text{ cm}^3$$

$$\text{Volume of a cylinder} = \pi r^2 h$$

$$\therefore 12936 = \frac{22}{7} \times (2x)^2 \times 3x$$

$$\Rightarrow 12936 = \frac{22}{7} \times 4x^2 \times 3x$$

$$\Rightarrow 12936 = \frac{264}{7} x^3$$

$$\Rightarrow x^3 = \frac{12936 \times 7}{264} = 49 \times 7$$

$$\Rightarrow x^3 = 7 \times 7 \times 7 = (7)^3$$

$$\Rightarrow x^3 = (7)^3$$

$$\therefore x = 7$$

So, radius = $2x = 2 \times 7 = 14$ cm and height = $3x = 3 \times 7 = 21$ cm

The total surface area of the cylinder = $2\pi r(r + h)$

$$= 2 \times \frac{22}{7} \times 14(14 + 21)$$

$$= \frac{44 \times 14}{7} \times 35 = 44 \times 14 \times 5 = 3080 \text{ cm}^2$$

34. $9x^2y^2(3z - 24) \div 27xy(z - 8)$

$$= \frac{9x^2y^2(3z - 24)}{27xy(z - 8)}$$

$$= \frac{9x^2y^2 \cdot 3(z - 8)}{27xy(z - 8)}$$

$$= xy$$

35. Total enrolment $8 + 6 + 3 + 3 + 4 = 24$

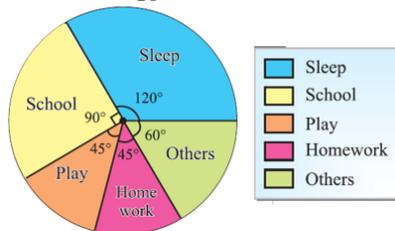
$$\therefore \text{Sleep} = \frac{8}{24} \times 360 = 120^\circ$$

$$\therefore \text{School} = \frac{6}{24} \times 360 = 90^\circ$$

$$\therefore \text{Play} = \frac{3}{24} \times 360 = 45^\circ$$

$$\therefore \text{Homework} = \frac{3}{24} \times 360 = 45^\circ$$

$$\therefore \text{Others} = \frac{4}{24} \times 360 = 60^\circ$$



36. We have given that,

The cost price of the article = ₹ 600

Gain% = 20%

$$\therefore \text{Total Gain} = \frac{600 \times 20}{100} = ₹ 120$$

$$\therefore \text{SP} = \text{Gain} + \text{CP} = ₹ 600 + ₹ 120 = ₹ 720$$

Let marked price be ₹ x .

Now shopkeeper allows a discount of 10%

According to the question, $x - 10\%$ of $x = ₹ 720$

$$\Rightarrow x - \frac{10 \times x}{100} = 720$$

$$\Rightarrow \frac{100x - 10x}{100} = 720$$

$$\Rightarrow \frac{90x}{100} = 720$$

$$\Rightarrow x = \frac{720 \times 100}{90}$$

$$x = ₹ 800$$

Hence, the required marked price is ₹ 800.

$$37. \text{Length} = x^2 - 4xy + 7y^2 \text{ and Breadth} = x^3 - 5xy^2$$

Area of rectangle = Length \times Breadth

$$\begin{aligned} &= (x^2 - 4xy + 7y^2) \times (x^3 - 5xy^2) \\ &= x^3(x^2 - 4xy + 7y^2) - 5xy^2(x^2 - 4xy + 7y^2) \\ &= x^5 - 4x^4y + 7x^3y^2 - 5x^3y^2 + 20x^2y^3 - 35xy^4 \\ &= [x^5 - 4x^4y + 2x^3y^2 + 20x^2y^3 - 35xy^4] \text{ sq. unit} \end{aligned}$$

38. The volume of cylinder B is greater.

i. For Cylinder A

$$r = \frac{7}{2} \text{ cm}$$

$$h = 14 \text{ cm}$$

$$\therefore \text{Volume} = \pi r^2 h$$

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 14$$

$$= 539 \text{ cm}^3$$

ii. For Cylinder B

$$r = \frac{14}{2} \text{ cm} = 7 \text{ cm}$$

$$h = 7 \text{ cm}$$

$$\therefore \text{Volume} = \pi r^2 h$$

$$= \frac{22}{7} \times 7 \times 7 \times 7$$

$$= 1078 \text{ cm}^3.$$

By actual calculation of volumes of both, it is verified that the volume of cylinder B is greater.

i. For Cylinder A

$$\text{Surface area} = 2\pi r(r + h)$$

$$= 2 \times \frac{22}{7} \times \frac{7}{2} \times \left(\frac{7}{2} + 14\right)$$

$$= 2 \times \frac{22}{7} \times \frac{7}{2} \times \frac{35}{2}$$

$$= 385 \text{ cm}^2$$

ii. For Cylinder B

$$\text{Surface area} = 2\pi r(r + h)$$

$$= 2 \times \frac{22}{7} \times 7 \times (7 + 7)$$

$$= 2 \times \frac{22}{7} \times 7 \times 14$$

$$= 616 \text{ cm}^2.$$

By actual calculation of surface area of both, we observe that the cylinder with greater volume has greater surface area.

$$39. 25a^2 - 4b^2 + 28bc - 49c^2$$

$$= 25a^2 - (4b^2 - 28bc + 49c^2)$$

$$= 25a^2 - \{(2b)^2 - 2(2b)(7c) + (7c)^2\}$$

$$= (5a)^2 - (2b - 7c)^2 \dots \text{ [Using Identity II]}$$

$$= \{5a - (2b - 7c)\} \{5a + (2b - 7c)\}$$

$$= (5a - 2b + 7c)(5a + 2b - 7c)$$

OR

$$x^4 - y^4 = (x^2)^2 - (y^2)^2$$

$$= (x^2 - y^2)(x^2 + y^2) \text{ Using } a^2 - b^2 = (a + b)(a - b)$$

$$= (x - y)(x + y)(x^2 + y^2) \text{ Using } a^2 - b^2 = (a + b)(a - b)$$

40. If the radius is 7 units, then the circumference of the circle = $2 \times \pi \times 7$

$$= 2 \times \frac{22}{7} \times 7 = 2 \times 22 = 44 \text{ units [}\therefore \text{ circumference of a circle} = 2\pi r]$$

$$\text{If radius is 14 units, then circumference} = 2 \times \pi \times 14 = 28 \times \frac{22}{7} = 88 \text{ units units}$$

$$\text{If radius is 21 units, then circumference} = 2 \times \pi \times 21 = 42 \times \frac{22}{7} = 132 \text{ units}$$

If the radius is 28 units, then circumference = $2 \times \pi \times 28 = 56 \times \frac{22}{7} = 176$ units

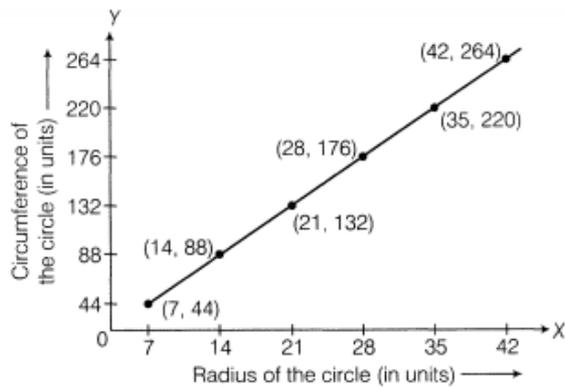
If the radius is 35 units, then circumference = $2 \times \pi \times 35 = 70 \times \frac{22}{7} = 220$ units

If the radius is 42 units, then circumference = $2 \times \pi \times 42 = 84 \times \frac{22}{7} = 264$ units

Now put these values in the table for the graph,

The radius of the circle	7	14	21	28	35	42
Circumference of the circle	44	88	132	176	220	264

Graph from the above data



From the graph, it is clear that:

- The circumference of the circle will be 264 units when the radius is 42 units.
- The radius of the circle will be 35 units when the circumference of the circle equals 220 units.