

• Cramer's Rule -

* * $\Delta = 0$ We can't Apply Cramer's.

(ex) $\begin{matrix} \Delta_1 & \Delta_2 & \Delta_3 \\ \swarrow & \searrow & \swarrow \\ x + 2y + 3z = 6 \\ 2x + 4y + z = 7 \\ 3x + 2y + 9z = 14 \end{matrix}$

$$\Rightarrow \Delta = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 4 & 1 \\ 3 & 2 & 9 \end{vmatrix} = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 4 & 1 \\ 0 & -4 & 0 \end{vmatrix} = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 0 & 1 \\ 0 & -4 & 0 \end{vmatrix}$$

$$= +4(1-6)$$

$$= -20$$

$$\Delta_1 = \begin{vmatrix} 6 & 2 & 3 \\ 7 & 4 & 1 \\ 14 & 2 & 9 \end{vmatrix} = \begin{vmatrix} 6 & 2 & 3 \\ 7 & 4 & 1 \\ 8 & 0 & 6 \end{vmatrix} = \begin{vmatrix} 6 & 2 & 3 \\ 6 & 4 & 1 \\ 2 & 0 & 6 \end{vmatrix}$$

$$= \begin{vmatrix} 6 & 2 & 3 \\ -5 & 0 & -5 \\ 8 & 0 & 6 \end{vmatrix}$$

$$= -10 + (-8)$$

$$= -18$$

$$= -2(-30 + 40)$$

$$= -20$$

$$\therefore x = \frac{\Delta_1}{\Delta} = \frac{-20}{-20} = 1$$

$$\Delta_2 = \begin{vmatrix} 1 & 6 & 3 \\ 2 & 7 & 1 \\ 3 & 14 & 9 \end{vmatrix}$$

$$= \begin{vmatrix} 1 & 0 & 0 \\ 2 & -5 & -5 \\ 3 & -4 & 0 \end{vmatrix}$$

$$= -20$$

$$\therefore y = \frac{\Delta_2}{\Delta} = \frac{-20}{-20} = 1$$

$$\Delta_3 = \begin{vmatrix} 1 & 2 & 6 \\ 2 & 4 & 7 \\ 3 & 2 & 14 \end{vmatrix}$$

$$= \begin{vmatrix} 1 & 0 & 0 \\ 2 & 0 & -5 \\ 3 & -4 & -4 \end{vmatrix} = 1(-20)$$

$$= -20$$

$$\therefore z = \frac{\Delta_3}{\Delta} = \frac{-20}{-20} = 1$$

So, ~~408~~ $x = y = z = 1$ ✓