

CBSE Class 11 Mathematics

Important Questions

Chapter 9

Sequences and Series

4 Marks Questions

22 23

$$S_n = \frac{a(1-r^n)}{1-r}$$

24 25

$$= \frac{1 \left[1 - \left(\frac{2}{3} \right)^n \right]}{1 - \frac{2}{3}}$$

26 27

$$= 3 \left[1 - \left(\frac{2}{3} \right)^n \right]$$

28 29

$$S_5 = 3 \left[1 - \left(\frac{2}{3} \right)^5 \right] = \frac{211}{81}$$

30 31

32

3. Find the sum to n terms of the series $1^2 + (1^2 + 2^2) + (1^2 + 2^2 + 3^2) + \dots$

33 34

Ans. $a_n = 1^2 + 2^2 + 3^2 + \dots + n^2$

35 36

$$a_n = \frac{n(n+1)(2n+1)}{6}$$

37 38

$$S_n = \frac{1}{6} \left[2 \sum_{k=1}^n k^3 + 3 \sum_{k=1}^n k^2 + \sum k \right]$$

39 40

$$= \frac{1}{6} \left[2 \cdot \frac{n^2(n+1)^2}{4} + \frac{3 \cdot n(n+1)(2n+1)}{6} + \frac{n(n+1)}{2} \right]$$

41 42

$$= \frac{n(n+1)}{12} [n(n+1) + (2n+1) + 1]$$

43 44

$$= \frac{n(n+1)}{12} (n^2 + n + 2n + 1 + 1)$$

45 46

$$= \frac{n(n+1)(n^2 + 3n + 2)}{12}$$

47 48

$$= \frac{n(n+1)^2(n+2)}{12}$$

49 50

51

4. Show that the sum of $(m+n)^{\text{th}}$ and $(m-n)^{\text{th}}$ terms of an A. P. is equal to twice the m^{th} term.

52 53

Ans. $a_{m+n} = a + (m+n-1)d$

54

CBSE Class 12 Mathematics

Important Questions

Chapter 9

Sequences and Series

6 Marks Questions

1. 150 workers were engaged to finish a job in a certain no. of days 4 workers dropped out on the second day, 4 more workers dropped out on the third day and so on. It took 8 more days to finish the work find the no. of days in which the work was completed

Ans. $a = 150$, $d = -4$

$$S_n = \frac{n}{2} [2 \times 150 + (n-1)(-4)]$$

If total works who would have worked all n days $150(n-8)$

$$\text{A T Q } \frac{n}{2} [300 + (n-1)(-4)] = 150(n-8)$$

$$n = 25$$

2. Prove that the sum to n terms of the series

$$11 + 103 + 1005 + \dots \text{ is } \frac{10}{9}(10^n - 1) + n^2$$

Ans. $S_n = 11 + 103 + 1005 + \dots + n \text{ terms}$

$$S_n = (10+1) + (102 + 3) + (103 + 5) + \dots + [10n + (2n-1)]$$

$$S_n = \frac{10(10^n - 1)}{10 - 1} + \frac{n}{2}(1 + 2n - 1)$$

$$= \frac{10}{9}(10^n - 1) + n^2$$

3. The ratio of A.M and G.M of two positive no. a and b is m : n show that

$$a : b = \left(m + \sqrt{m^2 - n^2} \right) : \left(m - \sqrt{m^2 - n^2} \right)$$

Ans. $\frac{a+b}{2\sqrt{ab}} = \frac{m}{n}$

$$\frac{a+b}{2\sqrt{ab}} = \frac{m}{n}$$

by C and D

$$\frac{a+b+2\sqrt{ab}}{a+b-2\sqrt{ab}} = \frac{m+n}{m-n}$$

$$\frac{(\sqrt{a} + \sqrt{b})^2}{(\sqrt{a} - \sqrt{b})^2} = \frac{m+n}{m-n}$$

$$\frac{\sqrt{a} + \sqrt{b}}{\sqrt{a} - \sqrt{b}} = \frac{\sqrt{m+n}}{\sqrt{m-n}}$$

by C and D

$$\frac{\sqrt{a}}{\sqrt{b}} = \frac{\sqrt{m+n} + \sqrt{m-n}}{\sqrt{m+n} - \sqrt{m-n}}$$

Sq both side

$$\frac{a}{b} = \frac{m + \cancel{\sqrt{m+n}} + m - \cancel{\sqrt{m-n}} + 2\sqrt{m^2 - n^2}}{m + \cancel{\sqrt{m+n}} + m - \cancel{\sqrt{m-n}} - 2\sqrt{m^2 - n^2}}$$

$$\frac{a}{b} = \frac{m + \sqrt{m^2 - n^2}}{m - \sqrt{m^2 - n^2}}$$

4. Between 1 and 31, m number have been inserted in such a way that the resulting sequence is an A.P. and the ratio of 7th and (m-1)th no. is 5:9 find the value of m.

Ans. 1, $A_1, A_2, A_3, \dots, A_m, 31$ are in AP

$$a = 1$$

$$a_n = 31$$

$$a_{m+2} = 31$$

$$a_n = a + (n-1)d$$

$$31 = a + (m+2-1)d$$

$$d = \frac{30}{m+1}$$

$$\frac{A_7}{A_{m-1}} = \frac{5}{9} \quad (\text{Given})$$

$$\frac{1 + 7\left(\frac{30}{m+1}\right)}{1 + (m-1)\left(\frac{30}{m+1}\right)} = \frac{5}{9}$$

$$m = 1$$

5. The Sum of two no. is 6 times their geometric mean, show that no. are in the ratio $(3 + 3\sqrt{2}) : (3 - 2\sqrt{2})$

Ans. $a + b = 6\sqrt{ab}$

$$\frac{a+b}{2\sqrt{ab}} = \frac{3}{1}$$

by C and D

$$\frac{a+b+2\sqrt{ab}}{a+b-2\sqrt{ab}} = \frac{3+1}{3-1}$$

$$\frac{(\sqrt{a}+\sqrt{b})^2}{(\sqrt{a}-\sqrt{b})^2} = \frac{2}{1}$$

$$\frac{\sqrt{a}+\sqrt{b}}{\sqrt{a}-\sqrt{b}} = \frac{\sqrt{2}}{1}$$

again by C and D

$$\frac{\sqrt{a}+\sqrt{b}+\sqrt{a}-\sqrt{b}}{\sqrt{a}+\sqrt{b}-\sqrt{a}-\sqrt{b}} = \frac{\sqrt{2}+1}{\sqrt{2}-1}$$

$$\frac{2\sqrt{a}}{2\sqrt{b}} = \frac{\sqrt{2}+1}{\sqrt{2}-1}$$

$$\frac{a}{b} = \frac{(\sqrt{2}+1)^2}{(\sqrt{2}-1)^2} \text{ (on squaring both side)}$$

$$\frac{a}{b} = \frac{2+1+2\sqrt{2}}{2+1-2\sqrt{2}}$$

$$\frac{a}{b} = \frac{3+2\sqrt{2}}{3-2\sqrt{2}}$$

$$a:b = (3+2\sqrt{2}):(3-2\sqrt{2})$$