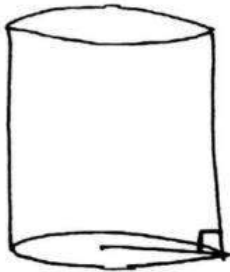


CLASS  
60

# 3D-MENSURATION

Prism

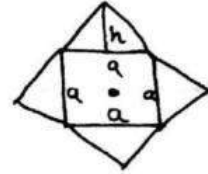
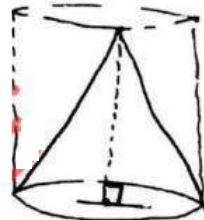


$$\text{Vol.} = \text{Base Area} \times \text{Height}$$

$$\text{L.S.A} = \text{Base Perimeter} \times H$$

$$\text{T.S.A} = \text{L.S.A} + 2 \cdot \text{Base Area}$$

Pyramid



$$\text{Vol.} = \frac{1}{3} \times \text{Base Area} \times \text{Height}$$

$$\text{L.S.A} = \frac{1}{2} \times \text{Base Perimeter} \times \text{slant Height}$$

$$\text{T.S.A} = \text{L.S.A} + \text{Base Area}$$

- ① Find the vol of a prism w/c is based on regular octagon of side 10 cm and height of the prism is 63 cm.

$$\text{Vol. of prism} = \text{Base Area} \times H.$$

$$2 \times 10 \times 10 (\sqrt{2} + 1) \times 63.$$

- ② The base of a right prism is a  $\Delta$  of side: 5, 12, 13 cm and its vol. is  $450 \text{ cm}^3$ . find its Total surface area.

$$450 = 30 \times H$$

$$H = 15 \text{ cm}$$

$$\text{T.S.A} = \frac{\text{L.S.A}}{30 \times 15} + \frac{2 \cdot \text{Base Area}}{2 \times 30}$$

$$= 510 \text{ cm}^2$$

- ③ The base of a right prism is a  $\Delta$  of perimeter 45 cm and its incircle radius is 9 cm. find its T.S.A if its

$$\text{Vol. is } 810 \text{ cm}^3.$$

$$r = \frac{A}{s}$$

$$9 = \frac{A}{\frac{45}{2}}$$

$$\text{Area of } \Delta = 9 \times \frac{45}{2}$$

Advance Maths (Volume-2)

$$\text{Vol.} = B.A \times H$$

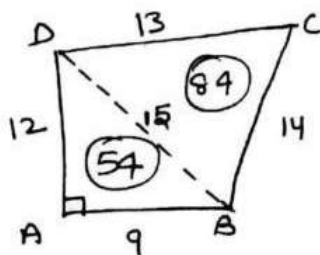
$$\frac{2 \times 90}{810} = 9 \times \frac{45}{2} \times H$$

$$H = 4$$

$$\begin{aligned} \text{T.S.A} &= 45 \times 4 = 180 \\ \text{T.S.A} &= \text{L.S.A} + 2 \left( 9 \times \frac{45}{2} \right) \\ &= 180 + 405 \\ &= 585 \text{ cm}^2 \end{aligned}$$

- ④ The base of a right prism is a quadrilateral ABCD. and the vol. of the prism is  $2070 \text{ cm}^3$ . find its L.S.A.

$$\begin{aligned} AB &= 9 \\ BC &= 14 \\ CD &= 13 \\ AD &= 12 \\ \angle A &= 90^\circ \end{aligned}$$



$$\text{Vol.} = B.A \times H.$$

$$B.A = 54 + 84 = 138$$

$$\Rightarrow 2070 = 138 \times H$$

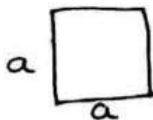
$$H = 15$$



$$\frac{1}{2} \times 9 \times 12 = 54$$

$$\begin{aligned} \text{L.S.A} &= \text{Base Perimeter} \times \text{Height} \\ &= 48 \times 15 = 720 \text{ cm}^2 \end{aligned}$$

- ⑤ The height of a right prism is  $15 \text{ cm}$  w/c is based on a square. If its total surface area is  $608 \text{ cm}^2$ . find its volume.



$$\text{T.S.A} = 608$$

$$4a \times 15 + 2a^2 = 608$$

$$30a + a^2 = 304$$

$$a(30+a) = 304$$

$$\begin{array}{cc} \downarrow & \downarrow \\ 8 & 8 \end{array} \quad \leftarrow \text{By unit digit concept}$$

$$a = 8$$

$$\text{Vol.} = 64 \times 15 = 960 \text{ cm}^3$$

- ⑥ find the vol. of a right prism w/c is based on a regular hexagon of height 10 cm. If its T.S.A is  $156\sqrt{3}$  cm.

$$6a \times 10 + 2 \times \frac{3\sqrt{3}}{2} a^2 = 156\sqrt{3}$$

$$20a + \sqrt{3}a^2 = 52\sqrt{3}$$

$$a(20 + \sqrt{3}a) = 52\sqrt{3}$$

$$2\sqrt{3}(20 + \sqrt{3} \times 2\sqrt{3}) = 52\sqrt{3}$$

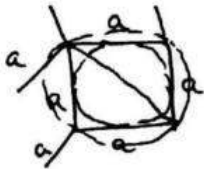
$$2\sqrt{3} \times 26 = 52\sqrt{3}$$

$$\text{so: } a = 2\sqrt{3}$$

$$\text{Vol.} = \frac{3\sqrt{3}}{2} \times (2\sqrt{3})^2 \times 10$$

put value of  $a = \sqrt{3}, 2\sqrt{3}, 3\sqrt{3}, 4\sqrt{3}$   
 $\therefore \sqrt{3}a$  का root खत्म करना है otherwise पौ 20 में add नहीं होगा

① **Cube**



$$\text{Vol.} = a^3$$

$$\text{L.S.A} = 4a^2$$

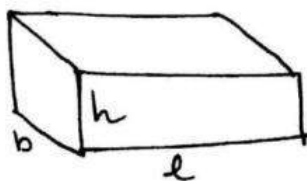
$$\text{T.S.A} = 6a^2$$

$$D = \sqrt{3}a$$

$$r = \frac{a}{2}$$

$$R = \frac{\sqrt{3}}{2}a$$

② **Cuboid**



$$V = lbh$$

$$\text{L.S.A} = 2(l+b)h$$

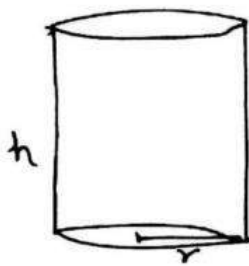
$$\text{T.S.A} = 2(lb + bh + hl)$$

$$\text{Diagonal (D)} = \sqrt{l^2 + b^2 + h^2}$$

- ⑥ A cubeid can be put in hemisphere.  
and the radius of hemisphere is =

$$R = \frac{1}{2} \sqrt{4h^2 + l^2 + b^2}$$

- ③ Cylinder.



$$V = \pi r^2 h$$

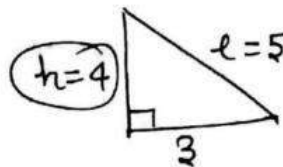
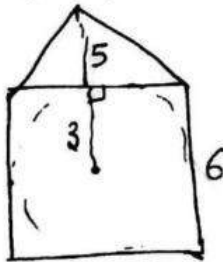
$$L.S.A = 2\pi r h$$

$$\begin{aligned} T.S.A &= L.S.A + 2\pi r^2 \\ &= 2\pi r (r + h) \end{aligned}$$

- ⑦ find the vol. of a pyramid w/c is based on a regular Hexagon of side  $2\sqrt{3}$  cm and Height of pyramid is 15 cm.

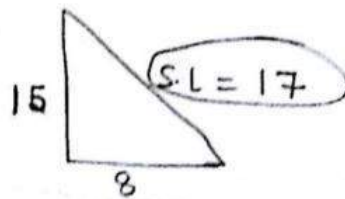
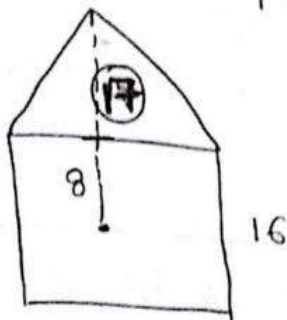
$$\text{vol.} = \frac{1}{3} \times \frac{3\sqrt{3}}{2} \times \frac{6}{12} \times 15 = 90\sqrt{3} \text{ Ans}$$

- ⑧ find the vol. of a pyramid w/c is based on a square of side 6 cm and its slant height is 5 cm.



$$\text{vol.} = \frac{1}{3} \times 36 \times 4 = 48 \text{ cm}^3$$

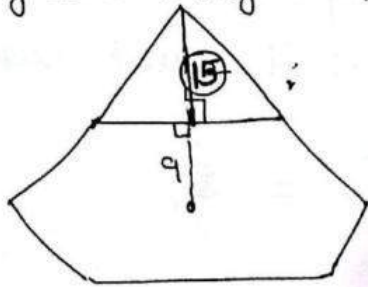
- ⑨ find the T.S.A of a pyramid of height 15 cm w/c is based on a square of side 16 cm.



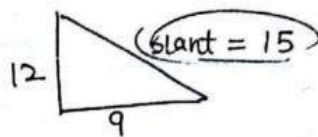
$$\begin{aligned} \text{T.S.A} &= \text{L.S.A} + \text{B.A} \\ &= \frac{1}{2} \times 16 \times 17 + 256 \\ &= 800 \text{ cm}^2 \end{aligned}$$

\* Radius of incircle in the square =  $\frac{a}{2}$

- ⑩ find the T.S.A of a pyramid w/c is based on a regular hexagon of side  $6\sqrt{3}$  cm and height 12 cm.



$$r = \frac{\sqrt{3}}{2} \times 6\sqrt{3} = 9$$

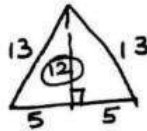
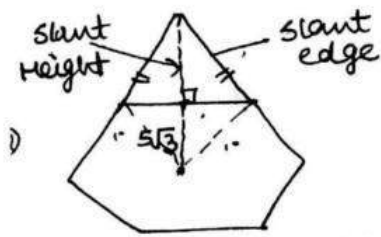


$$\text{Base Area} = \frac{\sqrt{3}}{4} \times (6\sqrt{3})^2 \times 6 = 162\sqrt{3}$$

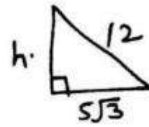
$$\text{C.S.A} = \frac{1}{2} \times 6 \times 6\sqrt{3} \times 15 = 270\sqrt{3}$$

$$\text{T.S.A} = 270\sqrt{3} + 162\sqrt{3} = 432\sqrt{3}$$

- ⑪ find the vol. of a pyramid w/c is based on regular hexagon of side 10 cm. and having slant edge 13 cm

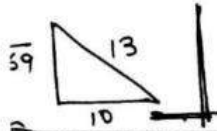


slant height = 12

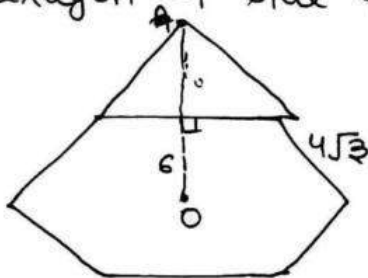


$$h = \sqrt{144 - 75} = \sqrt{69}$$

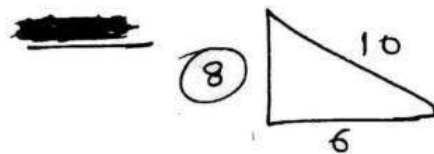
$$\text{vol.} = \frac{1}{3} \times \frac{3\sqrt{3}}{2} \times 5 \times 10 \times \sqrt{69} = 50\sqrt{207}$$



② find the vol. of a pyramid w/c is based on hexagon of side  $4\sqrt{3}$  and having slant ~~edge~~ height 10 cm.



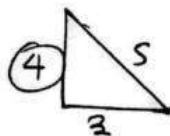
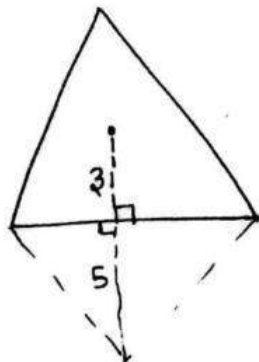
$$r = \frac{\sqrt{3}}{2} \times 4\sqrt{3} = 6$$



$$\text{vol.} = \frac{1}{3} \times \frac{3\sqrt{3}}{2} \times \frac{24}{48} \times 8 = 192\sqrt{3}$$

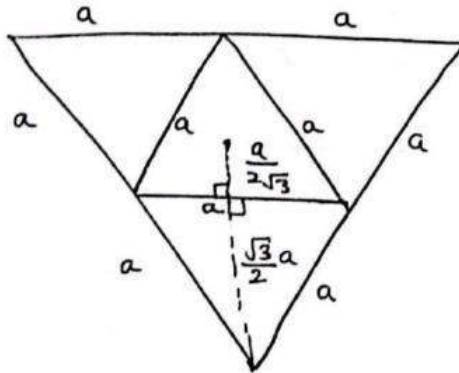
⑬ find the vol. of a pyramid w/c is based on an equilateral  $\Delta$  of side  $6\sqrt{3}$  cm if its slant height is 5 cm.

$$r = \frac{6\sqrt{3}}{2\sqrt{3}} = 3$$



$$\text{vol.} = \frac{1}{3} \times \frac{\sqrt{3}}{4} \times \frac{36}{108} \times 4 = 36\sqrt{3}$$

Tetrahedron



$$\text{Height} = \frac{\sqrt{2}}{3} a$$

$$\text{Vol.} = \frac{\sqrt{2}}{12} a^3$$

$$\text{L.S.A} = \frac{3\sqrt{3}}{4} a^2$$

$$\text{T.S.A} = \sqrt{3} a^2$$

$$\text{slant height} = \frac{\sqrt{3}}{2} a$$

$$\text{slant edge} = a$$

- 14) find the vol. of a tetrahedron whose height is  $2\sqrt{3}$

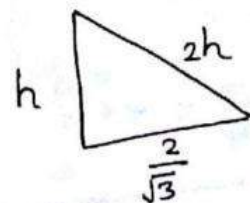
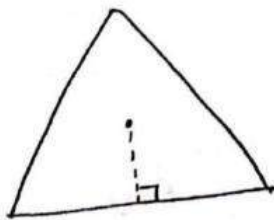
$$\frac{\sqrt{2}}{3} a = 2\sqrt{3}$$

$$a = \frac{6}{\sqrt{2}}$$

$$\text{vol.} = \frac{\sqrt{2}}{12} \times \frac{6 \times 6 \times 6}{\sqrt{2} \times \sqrt{2} \times \sqrt{2}} = \frac{18}{2} = 9 \text{ cm}^3$$

- 15) find the vol. of a pyramid w/c is based on an equilateral  $\Delta$  of side 4 cm. If its slant height is 2 times of its height

$$r = \frac{4}{2\sqrt{3}} = \frac{2}{\sqrt{3}} \text{ (Base length)}$$



$$h^2 + \frac{4}{3} = 4h^2$$

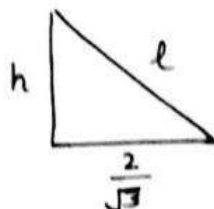
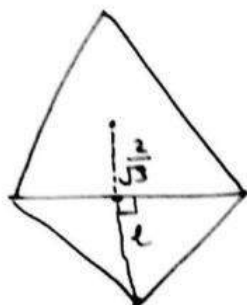
$$3h^2 = \frac{4}{3}$$

$$h^2 = \frac{4}{9}$$

$$h = \frac{2}{3}$$

$$\text{vol.} = \frac{1}{3} \times \frac{\sqrt{3}}{4} \times 4 \times 4 \times \frac{2}{3} = \frac{8}{9} \sqrt{3}$$

- ⑩ The base of a pyramid is equilateral  $\Delta$  of side 4 cm. if its total surface area is 3 times its volume. find the vol. of pyramid.



$$l^2 = h^2 + \frac{4}{3}$$

$$T.S.A = 3 \times V$$

$$\frac{1}{2} \times 4 \times 2\sqrt{3} \times l + \frac{\sqrt{3}}{4} \times 4 \times 4 = 3 \times \frac{1}{3} \times \frac{\sqrt{3}}{4} \times 4 \times 4 \times h$$

$$6l + 4\sqrt{3} = 4\sqrt{3}h$$

$$3l + 2\sqrt{3} = 2\sqrt{3}h$$

$$3l = 2\sqrt{3}(h-1)$$

square

$$9l^2 = 12(h^2 + 1 - 2h)$$

$$9\left(h^2 + \frac{4}{3}\right) = 12(h^2 + 1 - 2h)$$

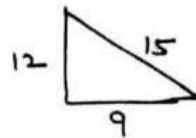
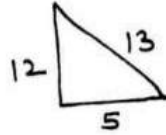
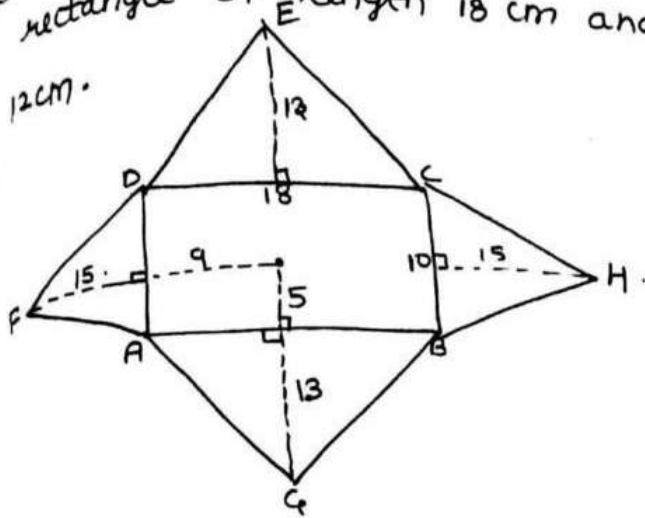
$$9h^2 + 12 = 12h^2 + 12 - 24h$$

$$3h^2 = 24h$$

$$\boxed{h = 8}$$

$$\text{Vol.} = \frac{1}{3} \times \frac{\sqrt{3}}{4} \times 4 \times 4 \times 8 = \frac{32\sqrt{3}}{3} \quad \underline{\underline{\text{Ans.}}}$$

② find the T.S.A of a pyramid w/c is based on rectangle of length 18 cm and breadth 10 cm. & height 12 cm.



$$2 \times \frac{1}{2} \times 18 \times 13 + 2 \times \frac{1}{2} \times 10 \times 15$$

Ar.  $\Delta DEC$  &  
Ar.  $\Delta ABG$

Ar.  $\Delta FGA$  &  
Ar.  $\Delta BCH$

$$\Rightarrow 234 + 150 = 384 = \text{L.S.A}$$

$$\begin{aligned} \text{T.S.A} &= \text{L.S.A} + 18 \times 10 \\ &= 384 + 180 = 564 \text{ cm}^2 \end{aligned}$$

③ The height of a conical tank is 9 m. A vertical pole of 6 m height is placed 4 m away from its centre such that it touches its surface. ~~a vertical~~ find the L.S.A of the tent.

④ A cone is cut parallel to its base in such a way that height of the two parts is same. find the ratio of vol. of these two parts.

- (20) A cone is cut parallel to its base in such a way that the height of each part is same. find the ratio of vol. of these parts.
- (21) A cone is cut parallel to its base in such a way that the volume of the smaller cone is  $\frac{1}{729}$  times of bigger cone. find the height of the smaller cone if the cone is cut 40cm above the base.
- (22) The base radius and height of a cone are 5cm and 25cm. if the cone is cut parallel to its base at a height of  $h$  from the base. if the vol. of frustum is  $110 \text{ cm}^3$ . find the ~~vol~~ of the radius smaller cone.

~~(23) The side of a right angles is 15~~

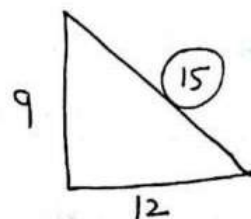
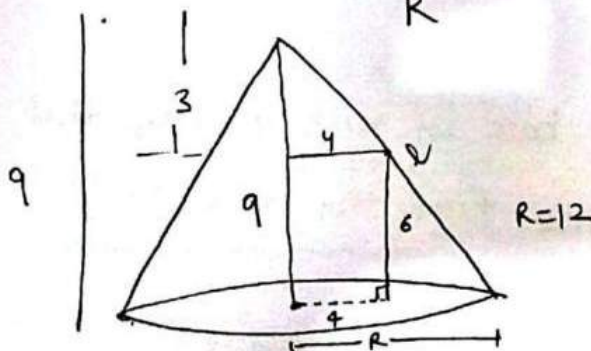
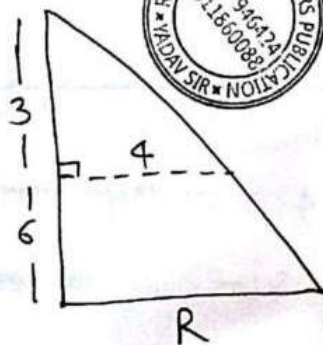
Soln

(18)



$$\frac{3}{9} = \frac{4}{R}$$

$$R = 12$$

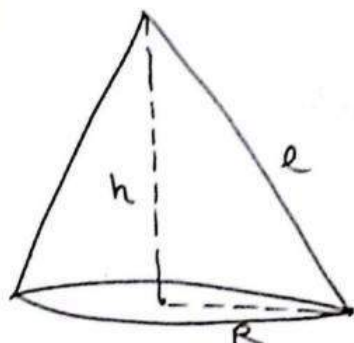


$$\text{vol} = \frac{1}{3} \times \frac{22}{7} \times 12 \times 12 \times 9 = 432\pi$$

$$\text{LSA} = \frac{22}{7} \times 12 \times 15 = 180\pi$$

#

CONE

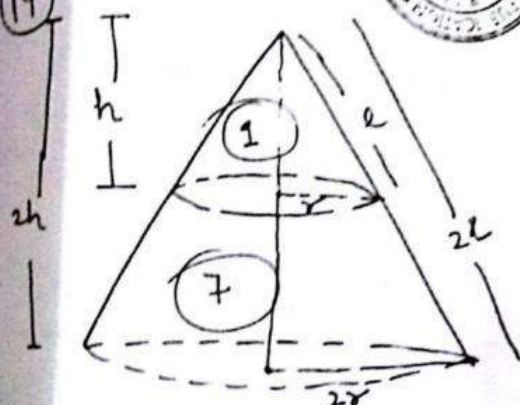


$$V = \frac{1}{3} \pi r^2 h$$

$$\text{LSA} = \pi r l$$

$$\text{T.S.A} = \pi r (r + l)$$

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small cone

larger cone

$$V = \frac{1}{3} \times \pi r^2 h$$

$$\frac{1}{3} \pi (2r)^2 \times 2h$$

$$1 : 8$$

$$\text{Ratio of vol. of two parts} = \frac{1}{7}$$

#

if a cone is cut parallel to its base then

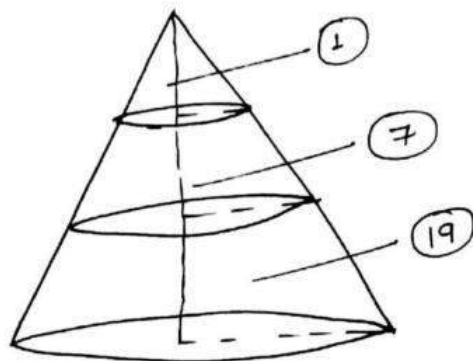
smaller cone

larger cone

height / slant height  $\rightarrow x : y$   
radius

volume  $\rightarrow x^3 : y^3$

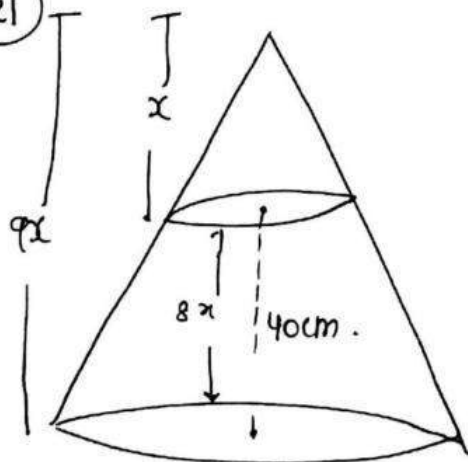
(20)



smaller medium larger  
 height  $\rightarrow$  1 : 2 : 3  
 vol.  $\rightarrow$  1 : 8 : 27

vol. of three parts = 1, 7, 19 Ans.

(21)



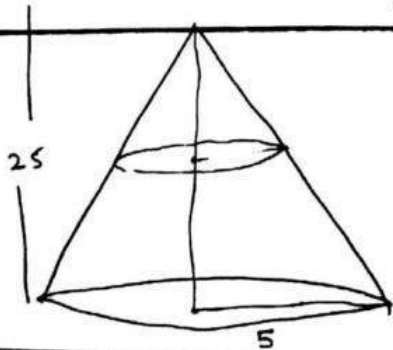
small larger  
 vol. 1 729  
 H/radius 1 : 9

$$8x = 40$$

$$x = 5$$

Height of smaller cone = 5 cm.

(22)



$$\frac{V_{\text{cone}}}{V_{\text{frustum}}} = \frac{\frac{1}{3} \times \frac{22}{7} \times 25 \times 25}{110}$$

$$\frac{V_{\text{cone}}}{V_{\text{frustum}}} = \frac{125}{21}$$

Rakesh Yadav

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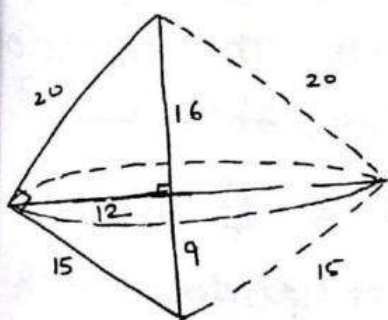
Advanced Maths (Volume 2)

Vol. larger cone  
125  
height/slant height/  
radius.  
5  
x1  
5

Vol. smaller cone  
104  
 $\sqrt[3]{104}$

$\therefore$  Radius of smaller  
cone =  $\sqrt[3]{104}$  Ans.

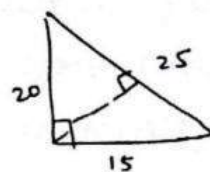
- 23) The side of a right angle  $\Delta$  are 15, 20 & 25 cm.  
if the  $\Delta$  is revolve around its hypotenuse, then  
find the vol. and T.S.A of the formed figure.



Vol. of such  
figure =  
 $\frac{1}{3} \pi \left[ \frac{P \times B}{H} \right]^2 \times H$

H  $\rightarrow$  Hypotenuse.

$$\frac{1}{3} \times \frac{22}{7} \times \frac{4}{1} \times 12 \times 25 = 1200\pi$$



$$\frac{20 \times 15}{25} = 12$$

$$T.S.A = \pi r l_1 + \pi r l_2 \Rightarrow \pi r (l_1 + l_2) \Rightarrow \pi \times 12 (20 + 15) = 420\pi$$

24)  $a = 12$

$$V = \frac{\sqrt{2}}{12} \times 12 \times 12 \times 12 = 144\sqrt{2}$$

$\rightarrow$  if the length of each side  
of regular tetrahedron is 12  
cm, find the vol.?

Ans

- 25) The length of diagonal of a cube with volume  
729  $\text{cm}^3$  is  $\rightarrow$

$$a^3 = 729$$

$$a = 9$$

$$D = \sqrt{3} a = 9\sqrt{3}$$

Ans

102 Advance Maths (Volume-2)

- 6) The ratio of radii of two right circular cylinders is 2:3 and their heights are in the ratio 5:4. Then ratio of their curved surface area is  $\rightarrow$

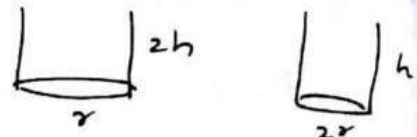
$$\cancel{2\pi} (2) \times 5 : \cancel{2\pi} (3) \times 4$$

$$5 : 6$$

- 7) If the radius of right circular cylinder is doubled and the height is halved, then the ratio b/w the new volume and the previous volume of the cylinder is  $\rightarrow$

$$\pi r^2 \times 2h : \pi 4r^2 \times h$$

$$1 : 2$$



- 8) A solid cylinder has total surface area of 462 sq. cm. curved surface area is  $\frac{1}{3}$ rd of its T.S.A. The volume of the cylinder is -

$$\cancel{2\pi} r h \times 3 = \cancel{2\pi} r (r+h)$$

$$3h = r+h$$

$$2h = r$$

$$2\pi r (h+r) = 462$$

$$2\pi r \times 2h (h+2h) = 462$$



$$4 \times \frac{22}{7} \times 3h^2 = 462$$

$$h^2 = \frac{49}{4} \Rightarrow h = \frac{7}{2}$$

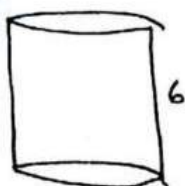
$$\text{Vol. of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 4h^2 \times h$$

$$= \frac{22}{7} \times 4 \times \frac{49}{4} \times \frac{7}{2}$$

$$= 539 \text{ cm}^3 \text{ Ans}$$

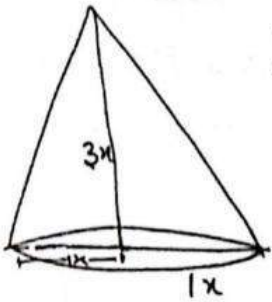
- 9) The height of a right circular cylinder is 6 m and three times the sum of the areas of its two end faces is equal to twice the area of its curved surface. The radius of its base, in metre is ?



$$2\pi r^2 \times 3 = (2\pi r \times 6) 2$$

$$r = 4$$

- 30) The ratio of height and diameter of a right circular cone is 3:2 and its vol. is 1078 cc, then its height is



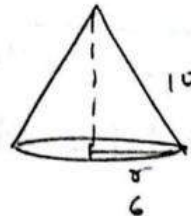
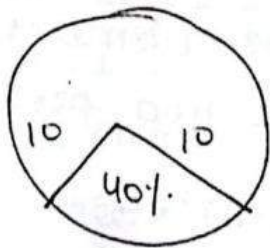
$$\frac{1}{3} \times \frac{22}{7} \times 2x \times 3x = 1078$$

$$x^3 = 49 \times 7$$

$$x = 7$$

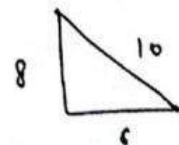
$$\text{Height} = 3x \Rightarrow 3 \times 7 = 21 \text{ cm} \quad \underline{\text{Ans.}}$$

- 31) In a circular sheet of paper of radius 10 cm, a sector of 40% area is removed and the remaining part is used to make a conical surface. find the volume of the conical surface.



$$\frac{60}{100} \times \pi \times 10^2 \times \frac{10}{100} = \pi r^2 \times \frac{1}{6}$$

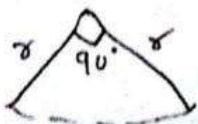
$$r = 6$$



$$\text{Height} = 8$$

$$\text{Vol.} = \frac{1}{3} \times \frac{22}{7} \times 6^2 \times 8 = 96\pi$$

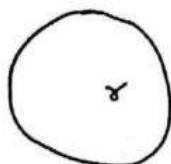
- 32) A right angled sector of radius  $r$  cm is rolled up into a cone in a way that two bounding radii are joined together. find the C.S.A of the cone  $\rightarrow$



$$\text{C.S.A} = \frac{90}{360} \times \pi r^2 = \frac{\pi}{4} r^2$$

⑧

sphere



$$\begin{aligned}V &= \frac{4}{3} \pi r^3 \\L.S.A &= 4 \pi r^2 \\T.S.A &= 4 \pi r^2\end{aligned}$$

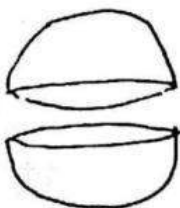
⑧

Hemisphere



$$\begin{aligned}V &= \frac{2}{3} \pi r^3 \\L.S.A &= 2 \pi r^2 \\T.S.A &= 3 \pi r^2\end{aligned}$$

- ③③ A sphere is cut in two parts along its diameter. find the total surface area of these two parts



$$4\pi r^2 + \pi r^2 + \pi r^2 = 6\pi r^2$$

if sphere is cut into  $n$  parts, then  
T.S.A of  $n$  parts =  $4\pi r^2 + n\pi r^2$

③④

The T.S.A of a solid hemisphere is  $1848 \text{ sq. cm.}$   
then the diameter of the same is —

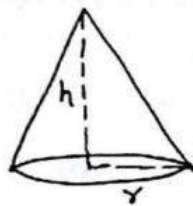
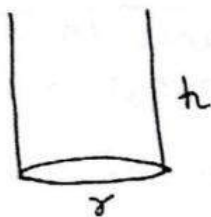
$$3 \times \frac{22}{7} \times 12 = \frac{84}{1} \times 28$$

$$r^2 = 7 \times 7 \times 4$$

$$r = 14$$

$$D = 28 \text{ cm.}$$

- 35) A cylinder and a cone have equal radii of their bases and equal heights. If their curved surface area are in the ratio 8:5, the ratio of their radius & height is →

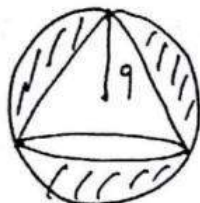
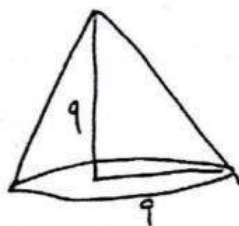


$$\frac{2\pi r h}{\pi r \sqrt{h^2 + r^2}} = \frac{8}{5}$$

$$\frac{4h^2}{h^2 + r^2} = \frac{64}{25}$$

$$\frac{h}{r} = \frac{8}{5} = \frac{4}{3}$$

- 36) A solid cone of height 9 cm with diameter of its base 18 cm is cut from a wooden solid sphere of radius 9 cm. The percentage of wood wasted is :

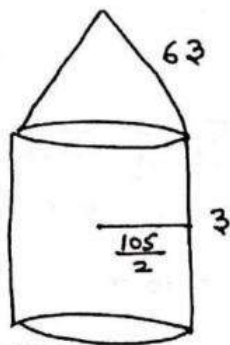


$$\frac{\frac{1}{3} \pi (9)^2 \times 9}{\frac{4}{3} \pi (9)^3}$$

$$= \frac{1}{4} \begin{matrix} \text{cone volume} \\ \text{sphere vol.} \end{matrix}$$

$$\therefore \frac{3}{4} \times 100 = 75\% \text{ wasted.}$$

- 37) From a solid cylinder of height 10 cm and radius of the base 6 cm, a cone of same height and same base is removed. Volume of the remaining solid is :-

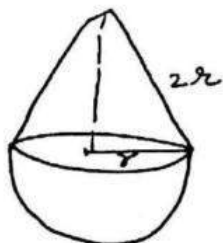


$$2\pi \left(\frac{105}{2}\right) \times 3 + \pi \left(\frac{105}{2}\right) \times 63$$

$$\frac{22}{7} \left(\frac{105}{2}\right) [6 + 63]$$

$$\text{|| } \frac{22}{7} \times \frac{15}{2} \times 69 = 11385 \text{ वर्ग मी.}$$

- 41) A solid is hemispherical at the bottom and conical above if the surface areas of the two parts are equal then the ratio of radius and height of its conical part is :-



$$\pi r l = 2\pi r^2$$

$$l = 2r$$

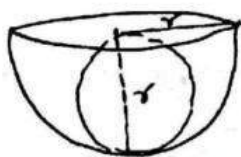
$$h = \sqrt{(2r)^2 - r^2} = \sqrt{3}r$$

$$r : \sqrt{3}r$$

$$1 : \sqrt{3}$$



- 42) A maximum size sphere is cut from a hemisphere of radius  $r$ . Find the ratio of volumes of hemisphere to sphere :-

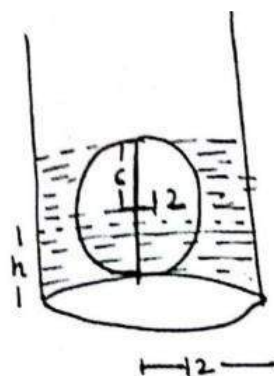


$$\frac{2}{3} \pi r^3 : \frac{4}{3} \pi \left(\frac{r}{2}\right)^3$$

$$1 : \frac{1}{4}$$

$$4 : 1$$

- 43) In a cylindrical vessel of diameter 24 m filled up with sufficient quantity of water, a solid spherical ball of radius 6 cm is completely immersed. Then the increases in height of water level is :-



$$\pi (12)^2 \times 12 - \frac{4}{3} \pi (6)^3 = \pi (12)^2 \times h$$

$$12^2 \times 12 - \frac{4}{3} \times 6 \times 6 \times 6 = (12)^2 \times h$$

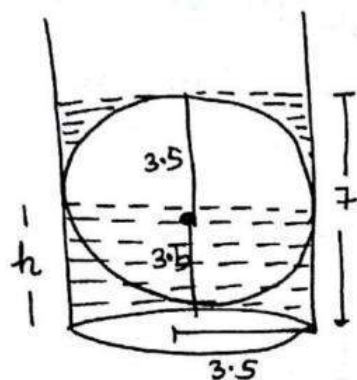
$$12 - 2 = h$$

$$h = 10 \text{ cm}$$

$$\therefore \uparrow \text{ in water level} = 12 - 10 = 2 \text{ cm.}$$

44) ~~A cone, a hemisphere~~

A cylindrical can whose base is horizontal is of internal radius 3.5 cm contain sufficient water so that when a solid sphere <sup>of max. size</sup> is placed, water just immersed it. Calculate the depth of water in the can before the sphere was put.



$$\pi (3.5)^2 \times 7 - \frac{4}{3} \pi (3.5)^3 = \pi (3.5)^2 \times h$$

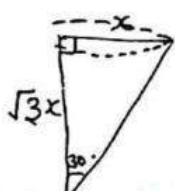
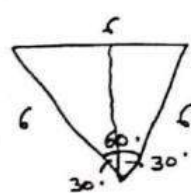
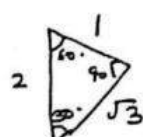
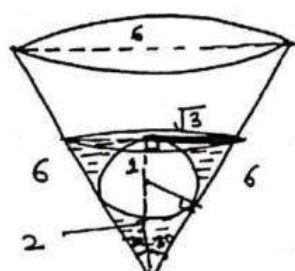
$$7 - \frac{4}{3} \times \frac{7}{4} = h$$

$$7 - \frac{14}{3} = h$$

$$h = \frac{7}{3} \quad \underline{\text{Ans.}}$$

45) The base radius and slant height of a conical vessel is 3 cm and 6 cm respectively. Find the volume of sufficient water in the vessel such that when a sphere of radius 1 cm is placed into it, water just immersed it.

3



$$\sqrt{3}x \rightarrow 3$$

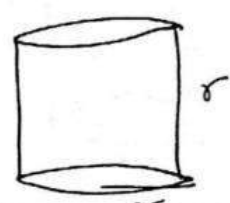
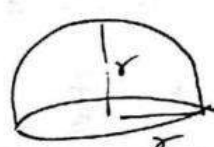
$$x \rightarrow \frac{3}{\sqrt{3}} = \sqrt{3}$$

$$\frac{1}{3} \pi (\sqrt{3})^2 \times \sqrt{3} - \frac{4}{3} \pi (1)^3$$

$$3\pi - \frac{4}{3} \pi$$

$$\frac{5}{3} \pi \quad \underline{\text{Ans.}}$$

46) A cone, a hemisphere and a cylinder stand on equal base and have the same height. Their vol. are in the ratio -

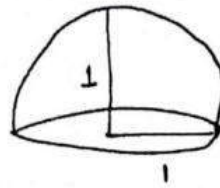
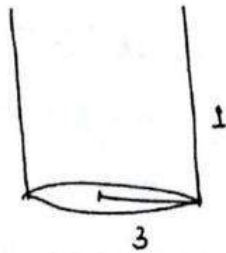
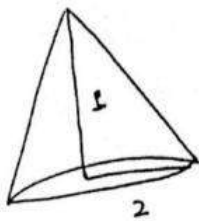


$$\frac{1}{3} \pi r^2 \cdot r : \frac{2}{3} \pi r^3 : \pi r^2 \cdot r$$

$$\frac{1}{3} : \frac{2}{3} : 1$$

$$1 : 2 : 3 \quad \underline{\text{Ans.}}$$

47) The height of a cone, cylinder and hemisphere are equal. If their radii are in the ratio 2:3:1, then the ratio of their volumes is :-

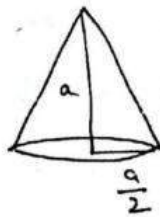
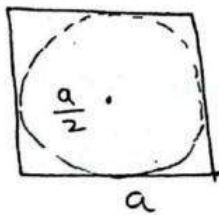


$$\frac{1}{3} \times \pi \times 2^2 \times 1 \quad : \quad \pi (3)^2 \times 1 \quad : \quad \frac{2}{3} \pi (1)^2 \times 1$$

$$\frac{4}{3} \quad : \quad 9 \quad : \quad \frac{2}{3}$$

$$4 \quad : \quad 27 \quad : \quad 2 \quad \underline{\text{Ans.}}$$

48) A cylinder is kept inside the cube in such a way that it touches all side of the cube and a cone is further placed inside the cylinder and the base & height of all the three are same. find the ratio of their volumes.



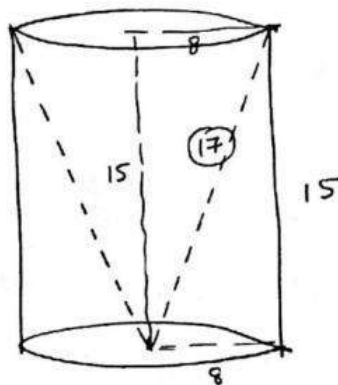
$$a^3 \quad : \quad \pi \left(\frac{a}{2}\right)^2 \times a \quad : \quad \frac{1}{3} \pi \left(\frac{a}{2}\right)^2 \times a$$

$$12 \quad : \quad 3\pi \quad : \quad \pi$$

$$6 \times 12 \quad : \quad 3 \times \frac{22}{7} \times 11 \quad : \quad \frac{22}{7} \times 11$$

$$42 \quad : \quad 33 \quad : \quad 11 \quad \underline{\text{Ans.}}$$

- (49) if a conical cavity is drilled out into a circular cylinder of height 15 cm and base radius 8 cm. the height and base radius of conical cavity is same. find the volume and T.S.A of the remaining solid.



vol. of remaining solid =

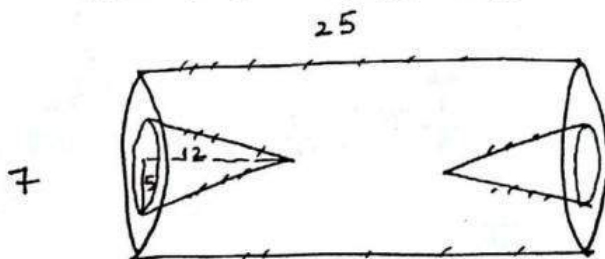
$$\frac{2}{3} \times \frac{22}{7} \times 8 \times 8 \times 15$$

$$640 \pi \text{ cm}^3$$



$$\begin{aligned} \text{T.S.A of remaining solid} &= 2\pi(8) \times 15 + \pi(8)^2 + \pi(8) \times 15 \\ &= 440\pi \end{aligned}$$

- (50) The base radius and height of a cylinder are 7 cm & 25 cm. 2 conical cavity of radius 5 cm and height 12 cm are drilled out on the both ends of the cylinder find the volume and T.S.A of the remaining solid



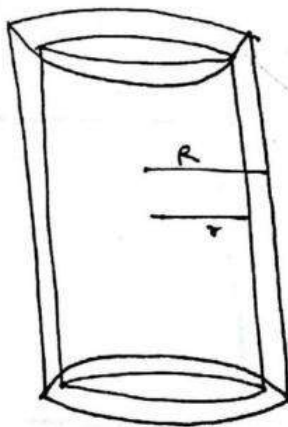
$$\begin{aligned} \text{vol. of remaining solid} &= \pi(7)^2 \times 25 - 2 \times \frac{1}{3} \pi(5)^2 \times 12 \\ &= \pi(1225 - 200) = 1025\pi \end{aligned}$$

$$\begin{aligned} \text{T.S.A} &= \underbrace{2\pi(7) \times 25}_{\text{cylinder}} + \underbrace{2\pi(5) \times 12}_{2 \text{ cavity}} + \left[ 2\pi(7^2 - 5^2) \right] \\ &= 528\pi \text{ Ans} \end{aligned}$$

↓ दोनों ends पर बचा हुआ area.

The height of a metallic hollow cylinder is 14 cm and the diff b/w its inner curved surface area & outer C.S.A is  $44 \text{ cm}^2$ . if the cylinder is made up of volume  $99 \text{ cm}^3$  metal. find its inner & outer radius.

Q Outer diameter of a 20 cm long pipe is 25 cm. if the thickness of the metal in the pipe is 1 cm. find the T.S.A of the pipe.



$$\Rightarrow 2\pi R \times 14 - 2\pi r \times 14 = 44$$

$$2 \times \frac{22}{7} \times 14 [R - r] = 44$$

$$[R - r] = \frac{1}{2}$$

$$\Rightarrow \pi R^2 \times 14 - \pi r^2 \times 14 = 99$$

$$\frac{22}{7} \times 14 (R^2 - r^2) = 99$$

$$44(R - r)(R + r) = 99$$

$$2 \times \frac{1}{2} (R + r) = 9$$

$$(R + r) = \frac{9}{2}$$



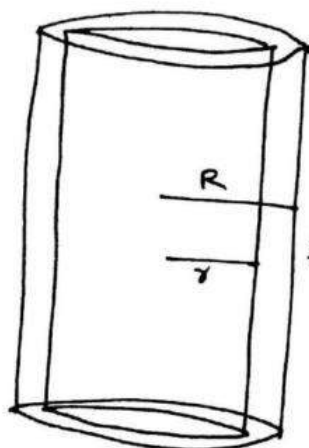
$$\Rightarrow \begin{array}{l} R - r = \frac{1}{2} \\ R + r = \frac{9}{2} \end{array}$$

$$2R = 5$$

$$R = \frac{5}{2}$$

$$r = 2$$

52



$$2\pi Rh + 2\pi rh + 2\pi [R^2 - r^2]$$

$$2\pi h [R + r] + 2\pi [(R + t)(R - t)]$$

$$2\pi [R + r] [h + R - t]$$

$$2\pi (R + r) (h + t)$$

$$2 \times \frac{22}{7} (12.5 + 11.5) (20 + 1)$$

$$2 \times \frac{22}{7} \times 24 \times 21 = 44 \times 72 = 3168$$

53

$$\text{T.S.A of the Hollow cylinder} = 2\pi (R + r) (h + t)$$

CLASS

63

53) A room 8m long, 6m broad and 3m high have 2 windows of  $1\frac{1}{2} \text{m} \times 1 \text{m}$  and a door of  $2 \text{m} \times 1\frac{1}{2} \text{m}$ . find the cost of papering the 4 walls with paper 50cm wide at the rate of 25 paise per metre.

54) find the length of wire of radius 0.25 cm w/c can completely cover the surface of a cylinder whose height is 1.2 m and base radius 14 cm.

Rakesh Yadav

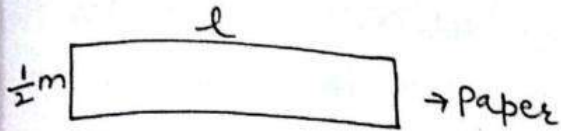
194

Advance Maths (Volume-2)

Rol

Area of 4 walls =  $2(l+b)h$   
 to be papered =  $2 \times 14 \times 3 = 84$   
 $84 - 6 = 78 \text{ m}^2$

$2 \times \left[ \frac{3}{2} \times 1 \right] - 2 \times \frac{3}{2}$   
 $\uparrow$  windows Area  $\uparrow$  door Area.

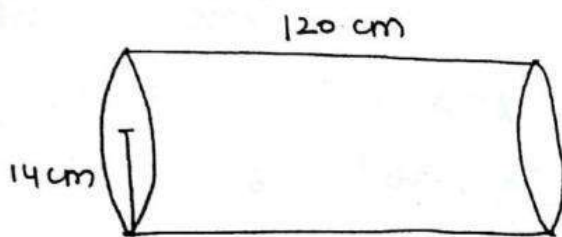


$$78 \text{ m}^2 = l \times \frac{1}{2}$$

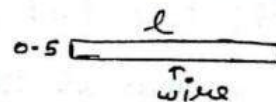
length of paper = 156 metre

cost of papering the wall =  $156 \times \frac{25}{100} = 39 \text{ Rs.}$

54



$$\frac{2 \times \frac{22}{7} \times 14 \times 120}{\uparrow \text{ surface area of cylinder}} = \frac{l \times \frac{0.5}{10}}{\uparrow \text{ area of wire}}$$



(\*) wire radius = 0.25  
 $\therefore$  width of wire = diameter of wire =  $0.25 \times 2 = 0.5$

$$\Rightarrow 88 \times 120 \times 2 = l$$

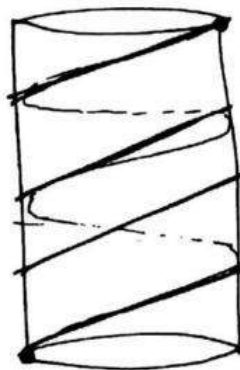
$$l = 21120 \text{ cm.} \quad \underline{\text{Ans.}}$$

OR

$$\frac{120}{0.5} = 240 \text{ rounds of wire}$$

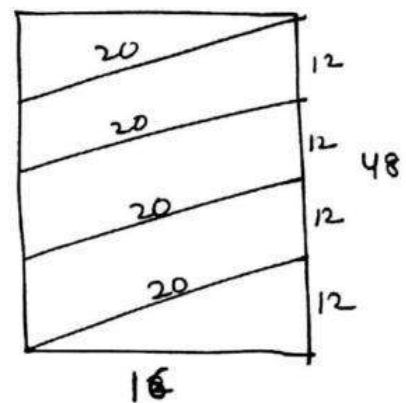
$$\Rightarrow \frac{2 \times \frac{22}{7} \times 14 \times 240}{\uparrow} = 21120 \text{ cm.}$$

- (55) find the length of the string wound on a cylindrical tank whose base diameter and height are  $5\frac{1}{11}$  cm and 48 cm. The string makes exactly 4 complete turns around the cylinder while its two ends touch the top and bottom of the tank.



48 cm

$$d = \frac{56}{11}$$

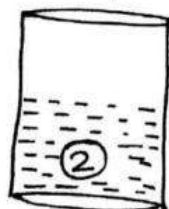


$2\pi r$

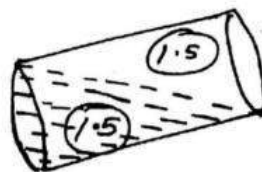
$$8 \times \frac{56}{11} \times \frac{22^2}{7} = 16$$

length of string =  $20 + 20 + 20 + 20 = 80$ . (approx.)

- (56) Two-third part of an aquarium is full of water. when we tilt the aquarium in such a way that the water becomes diagonal shape, in this process 93.5 L of water is flown out. find the capacity of the aquarium?



let capacity = 3 L  
filled =  $\frac{2}{3} \times 3 = 2$  L



$$2 - 0.5 = 0.5 \rightarrow 93.5$$

$$1 \rightarrow \frac{93.5}{0.5} = 187$$

Capacity =  $3 \times 187$  L

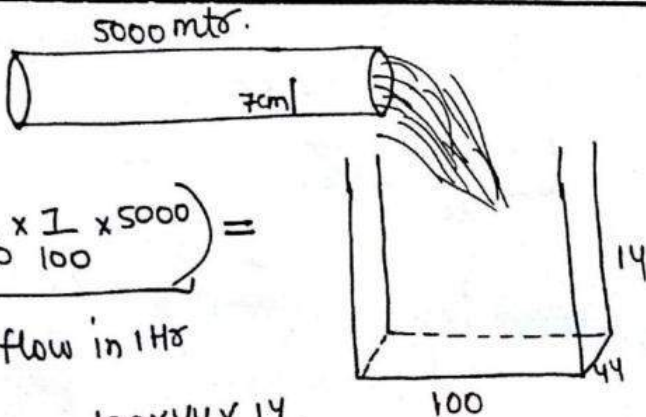
57) water flowing at the rate of  $5 \text{ km/hr}$  through a pipe of radius  $7 \text{ cm}$  into a rectangular tank w/c is  $100 \text{ m}$  long and  $44 \text{ m}$  wide. In what time the water level will rise by  $14 \text{ cm}$ .

58) The water in a rectangular reservoir having  $80 \text{ m} \times 60 \text{ m} \times 6.5 \text{ m}$  dimension. In what time can the water be emptied by a pipe of w/c the cross-section is a square of side  $20 \text{ cm}$ . If the water run through the pipe at the rate of  $15 \text{ km/hr}$ .

59) A rectangular tank of dimension  $225 \text{ m} \times 162 \text{ m}$  at the base, with what speed must water flow into it through a rectangular pipe of base  $40 \text{ m} \times 60 \text{ m}$  so that the water level may be  $\uparrow$  by  $20 \text{ cm}$  in  $5$  hours

60) If the length of a rectangular pipe is 3 times of its breadth and 5 times of its height. If its vol. is  $14400 \text{ cm}^3$ , find its T.S.A ?

57



$$\uparrow \left( \frac{22}{7} \times \frac{1}{100} \times \frac{1}{100} \times 5000 \right) =$$

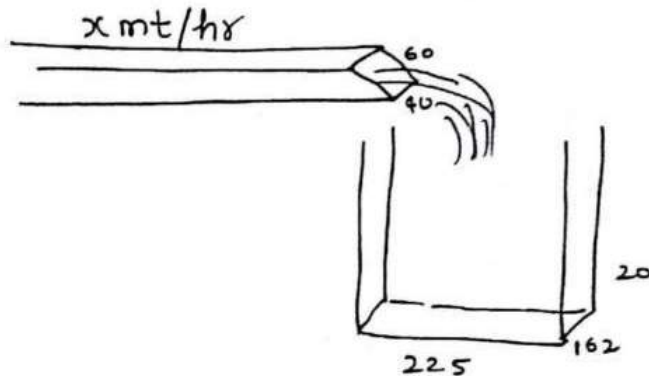
water flow in 1 Hr

$$\downarrow \frac{100 \times 44 \times \frac{14}{100}}{\text{vol. of pipe}}$$

$$n \left( \frac{22}{7} \times \frac{7}{100} \times \frac{7}{100} \times 5000 \right) = \frac{100 \times 44 \times 44}{100}$$

$$n = 8 \text{ Hours.}$$

(59)

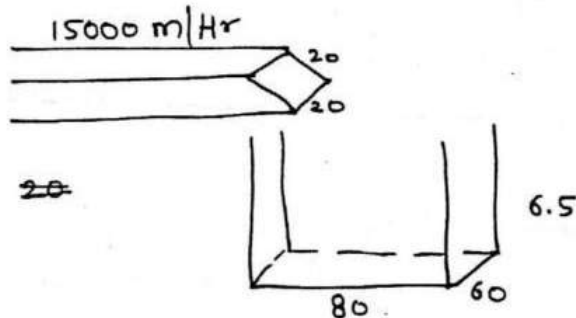


$$\frac{1}{2} \times \left[ \frac{60 \times 40}{100 \times 100} \times x \right] = \frac{9 \times 45 \times 27}{225 \times 162 \times 100} \times 20$$

↑  
1 Hr vol.

$$x = 25 \times 9 \times 27 = 6075 \text{ m.}$$

(58)



$$\left[ \frac{20}{100} \times \frac{20}{100} \times 15000 \right] \times n = \frac{4}{80 \times 60 \times 100} \times \frac{13}{65}$$

$$n = 52 \text{ Hours.}$$

60

$$\begin{aligned} L &= 15x \\ B &= 5x \\ H &= 3x \end{aligned}$$

$$15x \times 5x \times 3x = 14400$$

$$4800$$

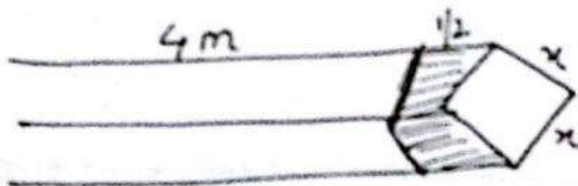
$$x = 4$$

$$\text{Surface Area} = 2(L+B) \times h.$$

$$2(60+20) \times 12 = 1920$$

61) The weight of a cubic metre metal is 480 kg

It is melted and cast into a square rod of 4m length. A solid cube of maximum size is taken out from one end. find the weight of the solid cube?



$$x \times x \times x \times 4 = 1$$

$$x^2 = \frac{1}{4}$$

$$x = \frac{1}{2}$$

( vol. of square rod =  
vol. of metal )

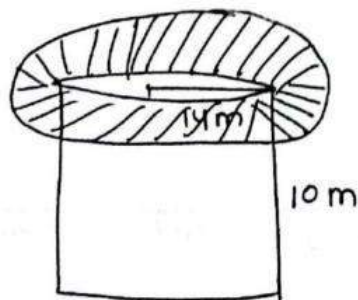
$$\text{Vol. of cube} = \left(\frac{1}{2}\right)^3 = \frac{1}{8} \text{ m}^3$$

$$\text{weight} = \frac{1}{8} \times 480 = 60 \text{ kg}$$

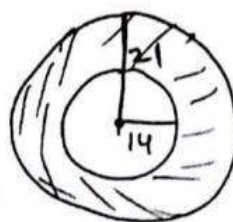
62) A well of 14 m base radius is digged upto a depth of 10 m & A 7 m wide platform was made around the well. find the height of platform?

63) In the middle of a rectangular field of length 35 m and breadth 15.4 m, a bit of length 5.5 m, breadth 4 m and depth 2.5 m was dug. and the earth taken out was spread over rest of the ground. How much the level of the ground will be increased?

62



$$\text{Vol. of earth} = \frac{22}{7} \times 14 \times 14 \times 10.$$



→ it would be prism like

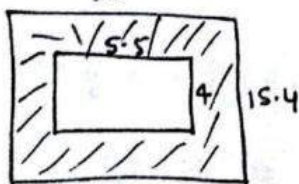
$$\frac{22}{7} \times 14 \times 14 \times 10 = \frac{22}{7} [21^2 - 14^2] \times h$$

$$14 \times 14 \times 10 = (21 + 14)(21 - 14) \times h$$

$$2 \cancel{14} \times \cancel{14} \times 10 = 5 \cancel{35} \times \cancel{7} \times h$$

$$h = 8$$

63



↑  
would be prism

$$\text{Vol. of earth} = 5.5 \times 4 \times 2.5$$

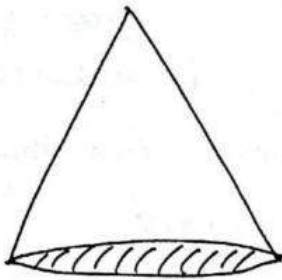
$$(35 \times 15.4 - 5.5 \times 4) \times h = 5.5 \times 4 \times 2.5$$

$$(539 - 22) \times h = 55$$

$$517h = 55$$

$$h = 9.4 \text{ m}$$

- 64) A conical tent is required to accommodate 5 people and each person needs  $16\text{ m}^2$  square of space on the ground and  $100\text{ m}^3$  air to breathe. find the height of the conical tent?



$$\text{Base Area} = \pi r^2 = 5 \times 16$$

$$\frac{1}{3} \pi r^2 h = 5 \times 100$$

$$\frac{1}{3} \times 5 \times 16 \times h = 500$$

$$\frac{1}{3} \times \frac{4}{1} \times 16 \times h = \frac{25}{1}$$

$$h = \frac{75}{4}$$

- 65) What is the semi-vertical angle of the cone whose L.S.A is double of the base area.

- 66) Find the no. of cones of semi-vertical angle  $\alpha$  and having  $r$  as the radius of the mid section w/c can be made out of the cylinder of base radius  $R$  and height  $2R \cot \alpha$ .

- 67) Find the radius of maximum size sphere w/c can be inscribed in a cone whose base radius and height are 6 cm and 8 cm.

- 68) The base ~~area~~<sup>radius</sup> and height of a rod roller are 0.7 cm and 10 cm respectively. When it revolves 1200 times then it levels only 88% area. Find the cost of leveling the whole ground at the rate of 6.75 Rs per  $\text{cm}^2$ .

- (69) The height of a cylinder is 2 cm, find its base radius if 6 cm is added either in radius or height gives same change in the volume. (चरकर  $\frac{1}{4}$  हो गया)
- (70) A cylinder whose area of the base is reduced to  $\frac{1}{9}$  and its height is increased to 6 times. find the increase or decrease in the c.s.A of the cylinder.
- (71) The radius of a cylinder is 10 cm and its height is 4 cm. How much cm does we add either in radius or in height to get the same change in the vol.
- (72) Rs 1000 is spent on the maintenance of a rectangular ground. When the cost per metre is 25 paise. The width of the ground is 50 m. if the length of the ground is increased by 20 m, then find the new cost of the maintenance.
- (73) 2 cm of rain has fallen on a square km of length 50% of the water was stored in a tank of dimensi 100 m x 10 m. Find the  $\uparrow$  in the water level in tank
- (74) if P is the height of a tetrahedron and length of each side is ~~2A~~ 2A. find the value of  $3P^2$
- (75) A prism based on a trapezium with parallel sides of length 8 cm and 14 cm have a distance of 14 cm between its two parallel lines. find the height

- ⑦⑥ if  $h$ ,  $c$  and  $v$  are the height, c.s.A, and vol respectively of a cone. find

$$3\pi v h^3 - c^2 h^2 + 9v^2$$

- ⑦⑦ A person requires  $4 \text{ m}^2$  of space on the ground and  $20 \text{ m}^3$  vol. to breath. What is the height of a conical tent if 11 person has to be accomodated in the tent.

- ⑦⑧ How many smaller cylinder of height & radius  $3.5 \text{ cm}$  can be made from a larger cylinder of height  $14 \text{ cm}$  and radius  $7 \text{ cm}$

- ⑦⑨ The length of a rectangular metallic sheet is  $20 \text{ m}$  and width is  $14 \text{ cm}$ . A water tank of maximum vol. possible is made from the sheet of height  $2 \text{ cm}$ . find the vol. of the tank.

- ⑧⑩ Few people dive in a swimming pool of dimension  $20 \text{ m} \times 10 \text{ m}$ . Due to this the water level rises by  $2 \text{ m}$ . If one person displace  $1 \text{ cubic m}$  of water find the no. of people who are diving.

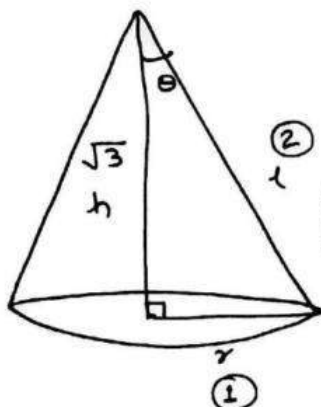
- ⑧⑪ A rectangular sheet of length  $44 \text{ cm}$  and breadth  $18 \text{ cm}$  was rolled along its length <sup>(length को मोला है)</sup> to form a cylinder. find the vol. of the formed cylinder.

- ⑧⑫ The capacity of two hemispherical bowls is  $6.4 \text{ l}$  and  $21.6 \text{ l}$ . find the ratio of their c.s.A.

- 83) The length of a swimming pool is 20 m and width 10 m. Its depth in starting is 4.5 m w/c reaches upto 7.5 m in the other end. find the vol. of the pool.

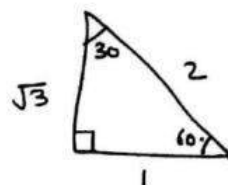
Solutions

65



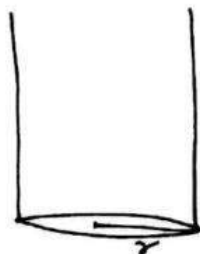
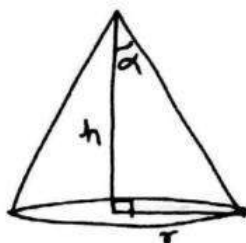
$$\pi r l = 2 \pi r^2$$

$$\frac{l}{r} = \frac{2}{1}$$



$$\therefore \theta = 30^\circ \quad \underline{\text{Ans.}}$$

66



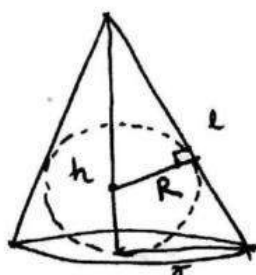
$$\frac{h}{r} = \cot \alpha$$

$$h = r \cot \alpha$$

$$\pi r^2 \times 2r \cot \alpha = n \times \frac{1}{3} \pi r^2 \times h$$

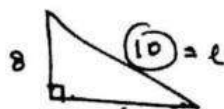
$$n = 6 \quad \underline{\text{Ans.}}$$

67

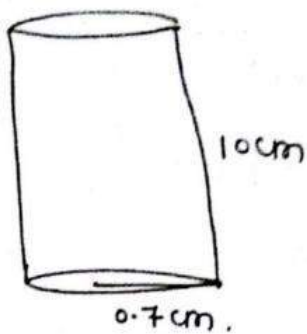


$$\text{Radius of sphere} = \frac{h \times r}{h + r}$$

$$= \frac{8 \times 6}{10 + 6} = \frac{48}{16} = 3 \text{ cm. } \underline{\underline{\text{Ans}}}$$



(68)



एक बार में मल्लह.  
धुमेगा तो वो अपने  
surface Area जितना  
area cover करेगा।

$$2 \times \frac{22}{7} \times 0.7 \times 10 \times 1200 = A \times \frac{88}{100}$$

$$A = 60,000 \text{ cm}^2$$

$$\text{cost} = 60,000 \times 6.75 = 405,000 \text{ Rs.}$$

(70)

$$\pi R^2 = 9$$

(R=3)

$$\pi r^2 = 1$$

(r=1)

Surface Area

$$2\pi R H = 3 \times 1 = 3$$

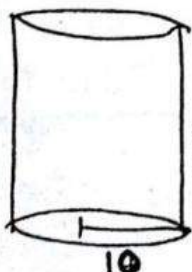
height

$$2\pi r h = 1 \times 6 = 6$$

height

S.A. becomes 2 times.

(71)



$$\begin{aligned} \text{Vol.} &= \pi (10)^2 \times 4 \\ &= 400\pi \end{aligned}$$

if Add 5 in radius then.

$$\text{Vol} = \pi \times 15^2 \times 4 = 900\pi$$

if Add 5 in height then

$$\text{Vol} = \pi \times 10^2 \times 9 = 900\pi$$

$\therefore$  The no. is 5. Ans

options are -

A) 5

B) 16

C) 25

D) 36.

OR

$$\pi(10+x)^2 \times 4 = \pi(10)^2(4+x)$$

$$(100+x^2+20x)4 = 100(4+x)$$

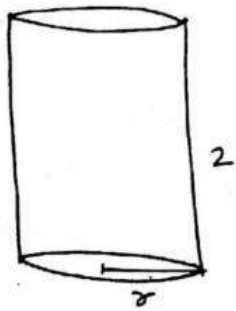
$$400+4x^2+80x = 400+100x$$

$$4x^2 = 20x$$

$$4x = 20$$

$$x = 5 \quad \underline{\text{Ans.}}$$

(69)



$$\pi(r+6)^2 \times 2 = \pi r^2(6+2)$$

$$(r+6)^2 \times 2 = r^2(8)$$

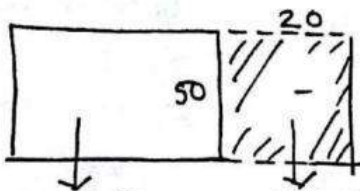
squaring

$$\sqrt{(r+6)^2 \times 2} = \sqrt{r^2(8)}$$

$$r+6 = 2r$$

$$r = 6$$

(72)



1000 Rs

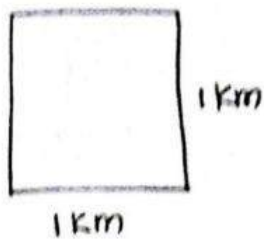
250 Rs

$50 \times 20 = 1000 \text{ m}^2$  (Area increase due to  $\uparrow$  in length)

$$\text{increase in cost} = 1000 \times \frac{25}{100} = 250 \text{ Rs}$$

$$\text{Now cost} = 1000 + 250 = 1250 \text{ Rs.}$$

73



$$\text{Area} = 1000 \times 1000$$

$$\underbrace{1000 \times 1000 \times \frac{2}{100}}_{\text{इतना पानी गिरा है}} \times \underbrace{\frac{5\%}{100}}_{\substack{\downarrow \\ \text{कितना stone किया है}}} = \underbrace{100 \times 10 \times h}_{\text{tank area}}$$

$$\boxed{h = 10 \text{ m}} \quad \underline{\text{Ans.}}$$

74

$$\frac{\sqrt{2}}{\sqrt{3}} \times 2A = P$$

$$\therefore \text{Height of tetrahedron} = \frac{\sqrt{2}}{\sqrt{3}} a$$

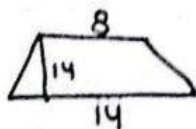
$$\frac{2}{3} \times 4 \times A^2 = P^2$$

$$8A^2 = 3P^2$$

Ans.



75



$$\frac{1}{2} \times (8+14) \times 14 \times h = 1056$$

$$\text{Base Area} \times h = \text{Vol.}$$

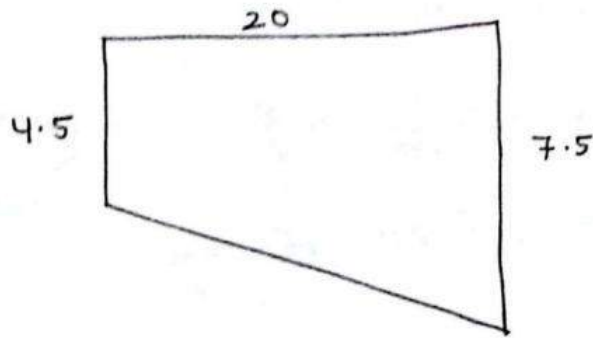
$$\Rightarrow \frac{1}{2} \times 22 \times 14 \times h = 1056$$

$$\boxed{h = \frac{48}{7}} \quad \underline{\text{Ans.}}$$

76

$$\text{Vol. of swimming pool} = \frac{1}{2} [\text{sum of depth of both end}] \times \text{length} \times \text{breadth}$$

(83)

Trapezium like

$$\begin{aligned} \text{Vol.} &= \frac{1}{2} (4.5 + 7.5) \times 20 \times 10 \\ &= \frac{1}{2} \times \frac{6}{2} \times 20 \times 10 = 1200 \text{ m}^3. \end{aligned}$$

(76)

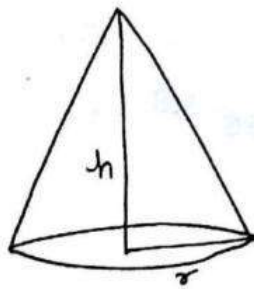
$$v = \frac{1}{3} \pi r^2 h, \quad c = \pi r l, \quad l^2 = r^2 + h^2$$

$$3\pi v h^3 - c^2 h^2 + 9v^2$$

$$\Rightarrow 3\pi \times \frac{1}{3} \pi r^2 h \times h^3 - \pi^2 r^2 (r^2 + h^2) h^2 + 9 \times \frac{1}{9} \pi^2 r^4 h^2$$

$$\Rightarrow \pi^2 r^2 h^4 - \pi^2 r^4 h^2 - \pi^2 r^2 h^4 + \pi^2 r^4 h^2 = 0 \quad \underline{\text{Ans.}}$$

(77)



$$\pi r^2 = 4 \times 11 \quad (\text{Area})$$

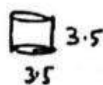
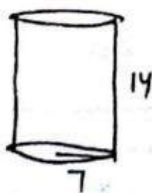
$$\frac{1}{3} \pi r^2 h = 20 \times 11 \quad (\text{Vol.})$$

$$\frac{1}{3} (4 \times 11) h = \frac{5}{3} \times 11$$

$$\boxed{h = 15}$$

Ans.

(78)



$$\pi (7^2) \times 14 = n \times \pi (3.5)^2 \times 3.5$$

$$\boxed{n = 16}$$

Ans

⊕ Frustum of a cone

$$\text{Vol.} = \frac{1}{3} \pi [R^2 + r^2 + Rr] h$$

$$\text{Surface Area} = \pi (R+r) l$$

$$\text{T.S.A} = \pi [R+r] l + \pi r^2 + \pi R^2$$

$$l = \sqrt{h^2 + (R-r)^2}$$

