

**Sample Question Paper**  
**Class – X Session -2021-22**

**TERM 1**

**Subject- Mathematics (Standard) 041**

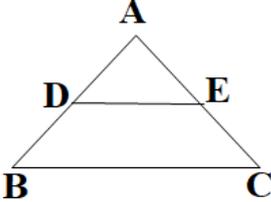
Time Allowed: 90 minutes

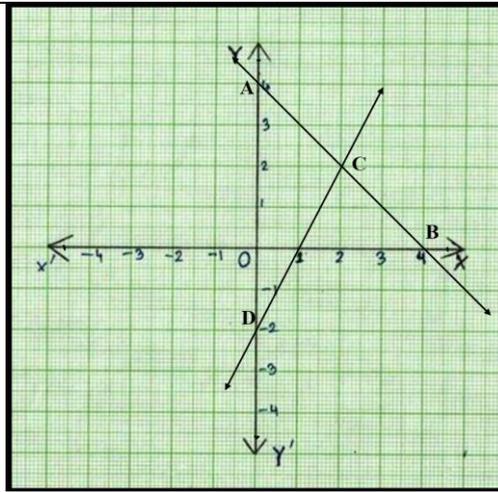
Maximum Marks: 40

**General Instructions:**

1. The question paper contains three parts A, B and C
2. Section A consists of 20 questions of 1 mark each. Any 16 questions are to be attempted
3. Section B consists of 20 questions of 1 mark each. Any 16 questions are to be attempted
- 4 Section C consists of 10 questions based on two Case Studies. Attempt any 8 questions.
5. There is no negative marking.

| SECTION A  |  |          |
|--|--|----------|
| <b>Section A consists of 20 questions of 1 mark each. Any 16 questions are to be attempted</b> |  |          |
| Q No   |  | Marks    |
| <b>1</b>   | The ratio of LCM and HCF of the least composite and the least prime numbers is<br>(a) 1:2                      (b) 2:1                      (c) 1:1                      (d) 1:3   | <b>1</b> |
| <b>2</b>   | The value of k for which the lines $5x+7y=3$ and $15x + 21y = k$ coincide is<br>(a) 9                      (b) 5                      (c) 7                      (d) 18  | <b>1</b> |
| <b>3</b>   | A girl walks 200m towards East and then 150m towards North. The distance of the girl from the starting point is<br>(a)350m                      (b) 250m                      (c) 300m                      (d) 225                                  | <b>1</b> |
| <b>4</b>   | The lengths of the diagonals of a rhombus are 24cm and 32cm, then the length of the altitude of the rhombus is<br>(a) 12cm                      (b) 12.8cm                      (c) 19 cm`                      (d) 19.2cm                           | <b>1</b> |
| <b>5</b>   | Two fair coins are tossed. What is the probability of getting at the most one head?<br>(a) $\frac{3}{4}$ (b) $\frac{1}{4}$ (c) $\frac{1}{2}$ (d) $\frac{3}{8}$   | <b>1</b> |
| <b>6</b>   | $\Delta ABC \sim \Delta PQR$ . If AM and PN are altitudes of $\Delta ABC$ and $\Delta PQR$ respectively and $AB^2 : PQ^2 = 4 : 9$ , then AM:PN =<br>(a) 16:81                      (b) 4:9                      (c) 3:2                      (d) 2:3 | <b>1</b> |
| <b>7</b>   | If $2\sin^2\beta - \cos^2\beta = 2$ , then $\beta$ is<br>(a) $0^\circ$ (b) $90^\circ$ (c) $45^\circ$ (d) $30^\circ$  | <b>1</b> |
| <b>8</b>   | Prime factors of the denominator of a rational number with the decimal expansion 44.123 are<br>(a) 2,3                      (b) 2,3,5                      (c) 2,5                      (d) 3,5  | <b>1</b> |
| <b>9</b>   | The lines $x = a$ and $y = b$ , are<br>(a) intersecting                      (b) parallel                      (c) overlapping                      (d) (None of these)  | <b>1</b> |
| <b>10</b>  | The distance of point A(-5, 6) from the origin is<br>(a) 11 units                      (b) 61 units                      (c) $\sqrt{11}$ units                      (d) $\sqrt{61}$ units  | <b>1</b> |
| <b>11</b>  | If $a^2 = 23/25$ , then a is<br>(a) rational                      (b) irrational                      (c) whole number                      (d) integer  | <b>1</b> |

|  |  |       |
|--|--|-------|
| 12   | If $\text{LCM}(x, 18) = 36$ and $\text{HCF}(x, 18) = 2$ , then $x$ is<br>(a) 2 (b) 3 (c) 4 (d) 5   | 1     |
| 13   | In $\Delta ABC$ right angled at B, if $\tan A = \sqrt{3}$ , then $\cos A \cos C - \sin A \sin C =$<br>(a) -1 (b) 0 (c) 1 (d) $\sqrt{3}/2$  | 1     |
| 14   | If the angles of $\Delta ABC$ are in ratio 1:1:2, respectively (the largest angle being angle C), then the value of $\frac{\sec A}{\operatorname{cosec} B} - \frac{\tan A}{\cot B}$ is<br>(a) 0 (b) $1/2$ (c) 1 (d) $\sqrt{3}/2$ | 1     |
| 15   | The number of revolutions made by a circular wheel of radius 0.7m in rolling a distance of 176m is<br>(a) 22 (b) 24 (c) 75 (d) 40  | 1     |
| 16   | $\Delta ABC$ is such that $AB=3$ cm, $BC= 2$ cm, $CA= 2.5$ cm. If $\Delta ABC \sim \Delta DEF$ and $EF = 4$ cm, then perimeter of $\Delta DEF$ is<br>(a) 7.5 cm (b) 15 cm (c) 22.5 cm (d) 30 cm                                  | 1     |
| 17   | In the figure, if $DE \parallel BC$ , $AD = 3$ cm, $BD = 4$ cm and $BC= 14$ cm, then $DE$ equals<br><br>(a) 7cm (b) 6cm (c) 4cm (d) 3cm        | 1     |
| 18   | If $4 \tan \beta = 3$ , then $\frac{4 \sin \beta - 3 \cos \beta}{4 \sin \beta + 3 \cos \beta} =$<br>(a) 0 (b) $1/3$ (c) $2/3$ (d) $3/4$  | 1     |
| 19   | One equation of a pair of dependent linear equations is $-5x + 7y = 2$ . The second equation can be<br>a) $10x+14y +4 = 0$ b) $-10x -14y+ 4 = 0$ c) $-10x+14y + 4 = 0$ (d) $10x - 14y = -4$                                      | 1     |
| 20   | A letter of English alphabets is chosen at random. What is the probability that it is a letter of the word 'MATHEMATICS'?<br>(a) $4/13$ (b) $9/26$ (c) $5/13$ (d) $11/26$  | 1     |
| <b>SECTION B</b>   |  |       |
| <b>Section B consists of 20 questions of 1 mark each. Any 16 questions are to be attempted</b> |  |       |
| QN   |  | MARKS |
| 21   | If sum of two numbers is 1215 and their HCF is 81, then the possible number of pairs of such numbers are<br>(a) 2 (b) 3 (c) 4 (d) 5  | 1     |
| 22   | Given below is the graph representing two linear equations by lines AB and CD respectively. What is the area of the triangle formed by these two lines and the line $x=0$ ?  | 1     |



- (a) 3sq. units      (b) 4sq. units      (c) 6sq. units      (d) 8sq. units

**23** If  $\tan \alpha + \cot \alpha = 2$ , then  $\tan^{20} \alpha + \cot^{20} \alpha =$   
 (a) 0      (b) 2      (c) 20      (d)  $2^{20}$       **1**

**24** If  $217x + 131y = 913$ ,  $131x + 217y = 827$ , then  $x + y$  is  
 (a) 5      (b) 6      (c) 7      (d) 8      **1**

**25** The LCM of two prime numbers  $p$  and  $q$  ( $p > q$ ) is 221. Find the value of  $3p - q$ .  
 (a) 4      (b) 28      (c) 38      (d) 48      **1**

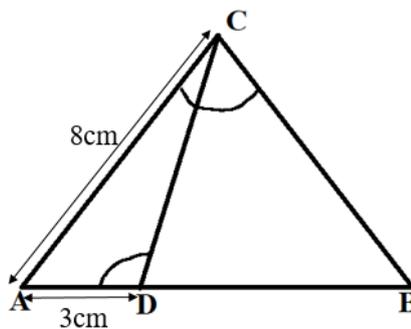
**26** A card is drawn from a well shuffled deck of cards. What is the probability that the card drawn is neither a king nor a queen?  
 (a)  $11/13$       (b)  $12/13$       (c)  $11/26$       (d)  $11/52$       **1**

**27** Two fair dice are rolled simultaneously. The probability that 5 will come up at least once is  
 (a)  $5/36$       (b)  $11/36$       (c)  $12/36$       (d)  $23/36$       **1**

**28** If  $1 + \sin^2 \alpha = 3 \sin \alpha \cos \alpha$ , then values of  $\cot \alpha$  are  
 (a) -1, 1      (b) 0, 1      (c) 1, 2      (d) -1, -1      **1**

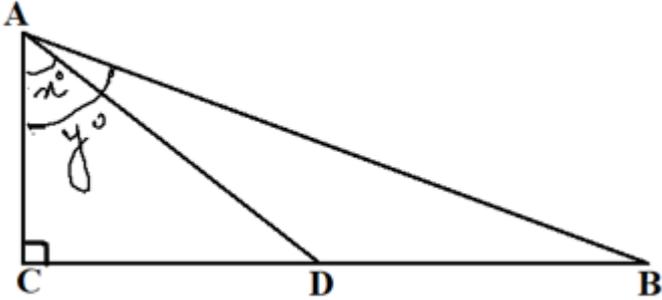
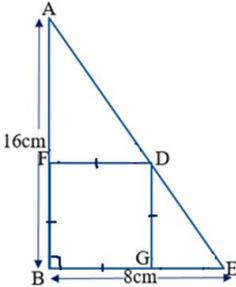
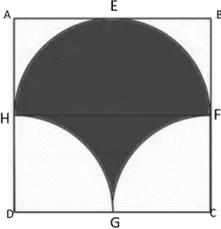
**29** The vertices of a parallelogram in order are A(1,2), B(4, y), C(x, 6) and D(3,5). Then (x, y) is  
 (a) (6, 3)      (b) (3, 6)      (c) (5, 6)      (d) (1, 4)      **1**

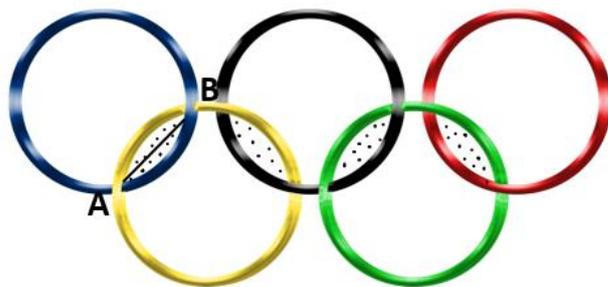
**30** In the given figure,  $\angle ACB = \angle CDA$ ,  $AC = 8\text{cm}$ ,  $AD = 3\text{cm}$ , then  $BD$  is      **1**



- (a)  $22/3$  cm      (b)  $26/3$  cm      (c)  $55/3$  cm      (d)  $64/3$  cm

**31** The equation of the perpendicular bisector of line segment joining points A(4,5) and B(-2,3) is  
 (a)  $2x - y + 7 = 0$       (b)  $3x + 2y - 7 = 0$       (c)  $3x - y - 7 = 0$       (d)  $3x + y - 7 = 0$       **1**

|           |   |          |
|-----------|---|----------|
| <p>32</p> | <p>In the given figure, D is the mid-point of BC, then the value of <math>\frac{\cot y^\circ}{\cot x^\circ}</math> is</p>  <p>(a) 2                      (b) 1/2                      (c) 1/3                      (d) 1/4</p>  | <p>1</p> |
| <p>33</p> | <p>The smallest number by which <math>\frac{1}{13}</math> should be multiplied so that its decimal expansion terminates after two decimal places is</p> <p>(a) <math>\frac{13}{100}</math>                      (b) <math>\frac{13}{10}</math>                      (c) <math>\frac{10}{13}</math>                      (d) <math>\frac{100}{13}</math></p>   | <p>1</p> |
| <p>34</p> | <p>Sides AB and BE of a right triangle, right angled at B are of lengths 16 cm and 8 cm respectively. The length of the side of largest square FDGB that can be inscribed in the triangle ABE is</p>  <p>(a) <math>\frac{32}{3}</math>cm                      (b) <math>\frac{16}{3}</math>cm                      (c) <math>\frac{8}{3}</math>cm                      (d) <math>\frac{4}{3}</math>cm</p> | <p>1</p> |
| <p>35</p> | <p>Point P divides the line segment joining R(-1, 3) and S(9,8) in ratio k:1. If P lies on the line <math>x - y + 2 = 0</math>, then value of k is</p> <p>(a) <math>\frac{2}{3}</math>                      (b) <math>\frac{1}{2}</math>                      (c) <math>\frac{1}{3}</math>                      (d) <math>\frac{1}{4}</math></p>  | <p>1</p> |
| <p>36</p> | <p>In the figure given below, ABCD is a square of side 14 cm with E, F, G and H as the mid points of sides AB, BC, CD and DA respectively. The area of the shaded portion is</p>  <p>(a) <math>44\text{cm}^2</math>                      (b) <math>49\text{ cm}^2</math>                      (c) <math>98\text{ cm}^2</math>                      (d) <math>49\pi/2\text{ cm}^2</math></p>              | <p>1</p> |
| <p>37</p> | <p>Given below is the picture of the Olympic rings made by taking five congruent circles of radius 1cm each, intersecting in such a way that the chord formed by joining the point of intersection of two circles is also of length 1cm. Total area of all the dotted regions assuming the thickness of the rings to be negligible is</p>   | <p>1</p> |



- (a)  $4(\pi/12 - \sqrt{3}/4) \text{ cm}^2$    (b)  $(\pi/6 - \sqrt{3}/4) \text{ cm}^2$    (c)  $4(\pi/6 - \sqrt{3}/4) \text{ cm}^2$    (d)  $8(\pi/6 - \sqrt{3}/4) \text{ cm}^2$

**38** If 2 and  $\frac{1}{2}$  are the zeros of  $px^2+5x+r$ , then  
 (a)  $p = r = 2$    (b)  $p = r = -2$    (c)  $p = 2, r = -2$    (d)  $p = -2, r = 2$    **1**

**39** The circumference of a circle is 100 cm. The side of a square inscribed in the circle is  
 (a)  $50\sqrt{2} \text{ cm}$    (b)  $100/\pi \text{ cm}$    (c)  $50\sqrt{2}/\pi \text{ cm}$    (d)  $100\sqrt{2}/\pi \text{ cm}$    **1**

**40** The number of solutions of  $3^{x+y} = 243$  and  $243^{x-y} = 3$  is  
 (a) 0   (b) 1   (c) 2   (d) infinite   **1**

**SECTION C**

**Case study based questions:**  
**Section C consists of 10 questions of 1 mark each. Any 8 questions are to be attempted.**

**Q41-Q45 are based on Case Study -1**

**Case Study -1**



The figure given alongside shows the path of a diver, when she takes a jump from the diving board. Clearly it is a parabola.

Annie was standing on a diving board, 48 feet above the water level. She took a dive into the pool. Her height (in feet) above the water level at any time 't' in seconds is given by the polynomial h(t) such that

$$h(t) = -16t^2 + 8t + k.$$

**41** What is the value of k?  
 (a) 0  
 (b) - 48  
 (c) 48  
 (d)  $48/-16$    **1**

**42** At what time will she touch the water in the pool?  
 (a) 30 seconds  
 (b) 2 seconds  
 (c) 1.5 seconds  
 (d) 0.5 seconds   **1**

|    |  |   |
|----|--|---|
| 43 | Rita's height (in feet) above the water level is given by another polynomial $p(t)$ with zeroes $-1$ and $2$ . Then $p(t)$ is given by-<br>(a) $t^2 + t - 2$ .<br>(b) $t^2 + 2t - 1$<br>(c) $24t^2 - 24t + 48$ .<br>(d) $-24t^2 + 24t + 48$ .                            | 1 |
| 44 | A polynomial $q(t)$ with sum of zeroes as $1$ and the product as $-6$ is modelling Anu's height in feet above the water at any time $t$ (in seconds). Then $q(t)$ is given by<br>(a) $t^2 + t + 6$<br>(b) $t^2 + t - 6$<br>(c) $-8t^2 + 8t + 48$<br>(d) $8t^2 - 8t + 48$ | 1 |
| 45 | The zeroes of the polynomial $r(t) = -12t^2 + (k-3)t + 48$ are negative of each other. Then $k$ is<br>(a) $3$<br>(b) $0$<br>(c) $-1.5$<br>(d) $-3$   | 1 |

**Q46-Q50 are based on Case Study -2**

**Case Study -2**

A **hockey field** is the playing surface for the game of hockey. Historically, the game was played on natural turf (grass) but nowadays it is predominantly played on an artificial turf.

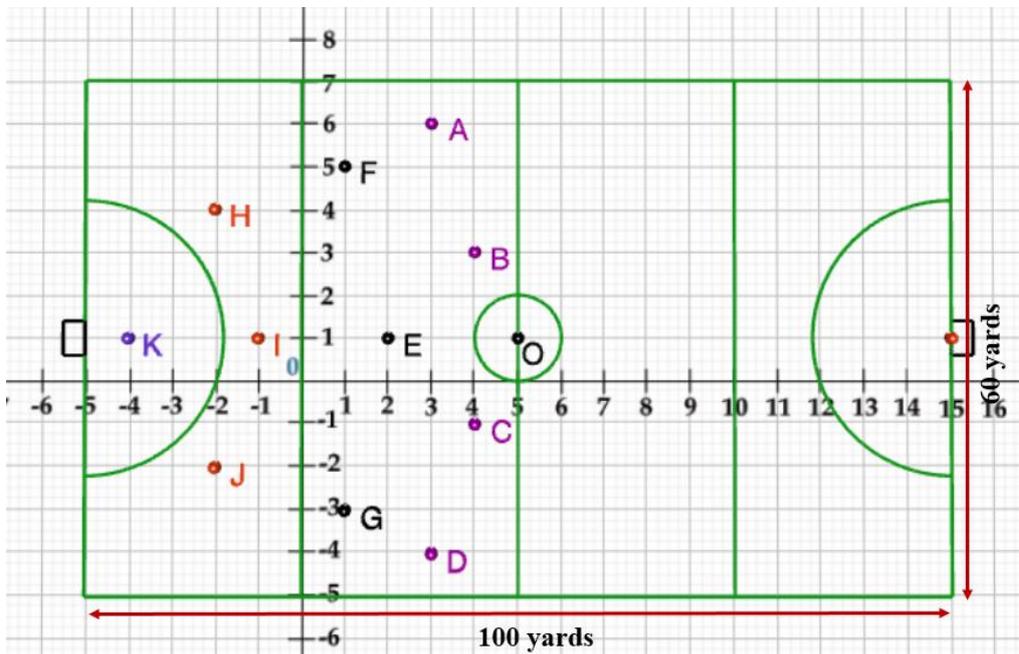
It is rectangular in shape - 100 yards by 60 yards. Goals consist of two upright posts placed equidistant from the centre of the backline, joined at the top by a horizontal crossbar. The inner edges of the posts must be 3.66 metres (4 yards) apart, and the lower edge of the crossbar must be 2.14 metres (7 feet) above the ground.

Each team plays with 11 players on the field during the game including the goalie.

Positions you might play include-

- **Forward:** As shown by players A, B, C and D.
- **Midfielders:** As shown by players E, F and G.
- **Fullbacks:** As shown by players H, I and J.
- **Goalie:** As shown by player K

Using the picture of a hockey field below, answer the questions that follow:

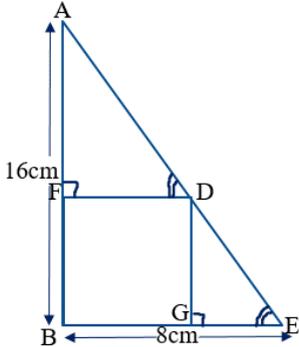
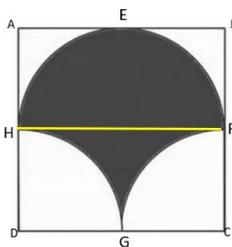


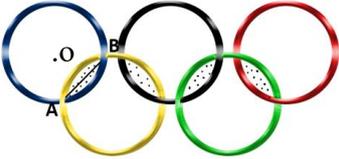
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| 46 | <p>The coordinates of the centroid of <math>\Delta E H J</math> are</p> <p>(a) <math>(-2/3, 1)</math><br/> (b) <math>(1, -2/3)</math><br/> (c) <math>(2/3, 1)</math><br/> (d) <math>(-2/3, -1)</math></p>  | 1 |
| 47 | <p>If a player P needs to be at equal distances from A and G, such that A, P and G are in straight line, then position of P will be given by</p> <p>(a) <math>(-3/2, 2)</math><br/> (b) <math>(2, -3/2)</math><br/> (c) <math>(2, 3/2)</math><br/> (d) <math>(-2, -3)</math></p> | 1 |
| 48 | <p>The point on x axis equidistant from I and E is</p> <p>(a) <math>(1/2, 0)</math><br/> (b) <math>(0, -1/2)</math><br/> (c) <math>(-1/2, 0)</math><br/> (d) <math>(0, 1/2)</math></p>   | 1 |
| 49 | <p>What are the coordinates of the position of a player Q such that his distance from K is twice his distance from E and K, Q and E are collinear?</p> <p>(a) <math>(1, 0)</math><br/> (b) <math>(0, 1)</math><br/> (c) <math>(-2, 1)</math><br/> (d) <math>(-1, 0)</math></p>   | 1 |
| 50 | <p>The point on y axis equidistant from B and C is</p> <p>(a) <math>(-1, 0)</math><br/> (b) <math>(0, -1)</math><br/> (c) <math>(1, 0)</math><br/> (d) <math>(0, 1)</math></p>   | 1 |

**Marking Scheme**  
**Class- X Session- 2021-22**  
**TERM 1**  
**Subject- Mathematics (Standard)**

| SECTION A |                |  |       |
|-----------|----------------|--|-------|
| QN        | Correct Option | HINTS/SOLUTION   | MARKS |
| 1         | (b)            | Least composite number is 4 and the least prime number is 2. LCM(4,2) :<br>HCF(4,2) = 4:2 = 2:1  | 1     |
| 2         | (a)            | For lines to coincide: $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$<br>so, $\frac{5}{15} = \frac{7}{21} = \frac{-3}{-k}$<br>i.e. k=9  | 1     |
| 3         | (b)            | By Pythagoras theorem<br>The required distance = $\sqrt{(200^2 + 150^2)}$<br>= $\sqrt{(40000 + 22500)} = \sqrt{(62500)} = 250\text{m}$ .<br>So the distance of the girl from the starting point is 250m.   | 1     |
| 4         | (d)            | Area of the Rhombus = $\frac{1}{2} d_1 d_2 = \frac{1}{2} \times 24 \times 32 = 384 \text{ cm}^2$ .<br>Using Pythagoras theorem<br>side <sup>2</sup> = $(\frac{1}{2}d_1)^2 + (\frac{1}{2}d_2)^2 = 12^2 + 16^2 = 144 + 256 = 400$<br>Side = 20cm<br>Area of the Rhombus = base x altitude<br>384 = 20 x altitude<br>So altitude = $384/20 = 19.2\text{cm}$ | 1     |
| 5         | (a)            | Possible outcomes are (HH), (HT), (TH), (TT)<br>Favorable outcomes(at the most one head) are (HT), (TH), (TT)<br>So probability of getting at the most one head = 3/4  | 1     |
| 6         | (d)            | Ratio of altitudes = Ratio of sides for similar triangles<br>So AM:PN = AB:PQ = 2:3  | 1     |
| 7         | (b)            | $2\sin^2\beta - \cos^2\beta = 2$<br>Then $2\sin^2\beta - (1 - \sin^2\beta) = 2$<br>$3\sin^2\beta = 3$ or $\sin^2\beta = 1$<br>$\beta$ is $90^\circ$  | 1     |
| 8         | (c)            | Since it has a terminating decimal expansion,<br>so prime factors of the denominator will be 2,5   | 1     |
| 9         | (a)            | Lines x=a is a line parallel to y axis and y=b is a line parallel to x axis. So they will intersect.   | 1     |
| 10        | (d)            | Distance of point A(-5,6) from the origin(0,0) is<br>$\sqrt{(0 + 5)^2 + (0 - 6)^2} = \sqrt{25 + 36} = \sqrt{61}$ units   | 1     |
| 11        | (b)            | $a^2 = 23/25$ , then $a = \sqrt{23}/5$ , which is irrational   | 1     |
| 12        | (c)            | LCM X HCF = Product of two numbers<br>$36 \times 2 = 18 \times x$<br>$x = 4$   | 1     |
| 13        | (b)            | $\tan A = \sqrt{3} = \tan 60^\circ$ so $\angle A = 60^\circ$ , Hence $\angle C = 30^\circ$ .<br>So $\cos A \cos C - \sin A \sin C = (1/2) \times (\sqrt{3}/2) - (\sqrt{3}/2) \times (1/2) = 0$   | 1     |
| 14        | (a)            | $1x + 1x + 2x = 180^\circ$ , $x = 45^\circ$ .<br>$\angle A$ , $\angle B$ and $\angle C$ are $45^\circ$ , $45^\circ$ and $90^\circ$ resp.<br>$\frac{\sec A}{\csc B} - \frac{\tan A}{\cot B} = \frac{\sec 45}{\csc 45} - \frac{\tan 45}{\cot 45} = \frac{\sqrt{2}}{\sqrt{2}} - \frac{1}{1} = 1 - 1 = 0$  | 1     |

|                  |     |  |   |
|------------------|-----|--|---|
| 15               | (d) | Number of revolutions = $\frac{\text{total distance}}{\text{circumference}} = \frac{176}{2 \times \frac{22}{7} \times 0.7}$<br>= 40  | 1 |
| 16               | (b) | $\frac{\text{perimeter of } \triangle ABC}{\text{perimeter of } \triangle DEF} = \frac{BC}{EF}$<br>$\frac{7.5}{\text{perimeter of } \triangle DEF} = \frac{2}{4}$ . So perimeter of $\triangle DEF = 15\text{cm}$  | 1 |
| 17               | (b) | Since $DE \parallel BC$ , $\triangle ABC \sim \triangle ADE$ ( By AA rule of similarity)<br>So $\frac{AD}{AB} = \frac{DE}{BC}$ i.e. $\frac{3}{7} = \frac{DE}{14}$ . So $DE = 6\text{cm}$   | 1 |
| 18               | (a) | Dividing both numerator and denominator by $\cos \beta$ ,<br>$\frac{4 \sin \beta - 3 \cos \beta}{4 \sin \beta + 3 \cos \beta} = \frac{4 \tan \beta - 3}{4 \tan \beta + 3} = \frac{3-3}{3+3} = 0$   | 1 |
| 19               | (d) | $-2(-5x + 7y = 2)$ gives $10x - 14y = -4$ . Now $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} = -2$   | 1 |
| 20               | (a) | Number of Possible outcomes are 26<br>Favorable outcomes are M, A, T, H, E, I, C, S<br>probability = $8/26 = 4/13$   | 1 |
| <b>SECTION B</b> |     |  |   |
| 21               | (c) | Since HCF = 81, two numbers can be taken as $81x$ and $81y$ ,<br>ATQ $81x + 81y = 1215$<br>Or $x + y = 15$<br>which gives four co prime pairs-<br>1,14<br>2,13<br>4,11<br>7, 8   | 1 |
| 22               | (c) | Required Area is area of triangle $ACD = \frac{1}{2}(6)2$<br>= 6 sq units  | 1 |
| 23               | (b) | $\tan \alpha + \cot \alpha = 2$ gives $\alpha = 45^\circ$ . So $\tan \alpha = \cot \alpha = 1$<br>$\tan^{20} \alpha + \cot^{20} \alpha = 1^{20} + 1^{20} = 1 + 1 = 2$  | 1 |
| 24               | (a) | Adding the two given equations we get: $348x + 348y = 1740$ .<br>So $x + y = 5$  | 1 |
| 25               | (c) | LCM of two prime numbers = product of the numbers<br>$221 = 13 \times 17$ .<br>So $p = 17$ & $q = 13$<br>$\therefore 3p - q = 51 - 13 = 38$  | 1 |
| 26               | (a) | Probability that the card drawn is neither a king nor a queen<br>$= \frac{52-8}{52}$<br>$= 44/52 = 11/13$  | 1 |
| 27               | (b) | Outcomes when 5 will come up at least once are-<br>(1,5), (2,5), (3,5), (4,5), (5,5), (6,5), (5,1), (5,2), (5,3), (5,4) and (5,6)<br>Probability that 5 will come up at least once = $11/36$   | 1 |
| 28               | (c) | $1 + \sin^2 \alpha = 3 \sin \alpha \cos \alpha$<br>$\sin^2 \alpha + \cos^2 \alpha + \sin^2 \alpha = 3 \sin \alpha \cos \alpha$<br>$2 \sin^2 \alpha - 3 \sin \alpha \cos \alpha + \cos^2 \alpha = 0$<br>$(2 \sin \alpha - \cos \alpha)(\sin \alpha - \cos \alpha) = 0$<br>$\therefore \cot \alpha = 2$ or $\cot \alpha = 1$ | 1 |
| 29               | (a) | Since ABCD is a parallelogram, diagonals AC and BD bisect each other, $\therefore$ mid point of AC = mid point of BD   | 1 |

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|    |     | $\left(\frac{x+1}{2}, \frac{6+2}{2}\right) = \left(\frac{3+4}{2}, \frac{5+y}{2}\right)$ <p>Comparing the co-ordinates, we get,<br/> <math>\frac{x+1}{2} = \frac{3+4}{2}</math>. So, <math>x=6</math><br/> Similarly, <math>\frac{6+2}{2} = \frac{5+y}{2}</math>. So, <math>y=3</math><br/> <math>\therefore (x, y) = (6,3)</math></p>  |   |
| 30 | (c) | $\triangle ACD \sim \triangle ABC$ (AA)<br>$\therefore \frac{AC}{AB} = \frac{AD}{AC}$ (CPST)<br>$8/AB = 3/8$<br>This gives $AB = 64/3$ cm.<br>So $BD = AB - AD = 64/3 - 3 = 55/3$ cm.  | 1 |
| 31 | (d) | Any point $(x, y)$ of perpendicular bisector will be equidistant from A & B.<br>$\therefore \sqrt{(x-4)^2 + (y-5)^2} = \sqrt{(x+2)^2 + (y-3)^2}$<br>Solving we get $-12x - 4y + 28 = 0$ or $3x + y - 7 = 0$  | 1 |
| 32 | (b) | $\frac{\cot y^\circ}{\cot x^\circ} = \frac{AC/BC}{AC/CD} = CD/BC = CD/2CD = 1/2$   | 1 |
| 33 | (a) | The smallest number by which $1/13$ should be multiplied so that its decimal expansion terminates after two decimal points is $13/100$ as $\frac{1}{13} \times \frac{13}{100} = \frac{1}{100} = 0.01$<br>Ans: $13/100$   | 1 |
| 34 | (b) |  <p><math>\triangle ABE</math> is a right triangle &amp; <math>FDGB</math> is a square of side <math>x</math> cm<br/> <math>\triangle AFD \sim \triangle DGE</math> (AA)<br/> <math display="block">\therefore \frac{AF}{DG} = \frac{FD}{GE}</math> (CPST)<br/> <math display="block">\frac{16-x}{x} = \frac{x}{8-x}</math> (CPST)<br/> <math>128 = 24x</math> or <math>x = 16/3</math>cm</p> | 1 |
| 35 | (a) | Since P divides the line segment joining $R(-1, 3)$ and $S(9,8)$ in ratio $k:1$ $\therefore$ coordinates of P are $\left(\frac{9k-1}{k+1}, \frac{8k+3}{k+1}\right)$<br>Since P lies on the line $x - y + 2 = 0$ , then $\frac{9k-1}{k+1} - \frac{8k+3}{k+1} + 2 = 0$<br>$9k - 1 - 8k - 3 + 2k + 2 = 0$<br>which gives $k = 2/3$  | 1 |
| 36 | (c) | <p>Shaded area = Area of semicircle + (Area of half square – Area of two quadrants)<br/> = Area of semicircle + (Area of half square – Area of semicircle)<br/> = Area of half square<br/> = <math>\frac{1}{2} \times 14 \times 14 = 98\text{cm}^2</math></p>    | 1 |

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| 37               | (d) |  <p>Let O be the center of the circle. <math>OA = OB = AB = 1\text{cm}</math>.<br/> So <math>\Delta OAB</math> is an equilateral triangle and <math>\therefore \angle AOB = 60^\circ</math><br/> Required Area = <math>8 \times</math> Area of one segment with <math>r=1\text{cm}</math>, <math>\theta = 60^\circ</math><br/> <math>= 8 \times \left( \frac{60}{360} \times \pi \times 1^2 - \frac{\sqrt{3}}{4} \times 1^2 \right)</math><br/> <math>= 8(\pi/6 - \sqrt{3}/4)\text{cm}^2</math></p> | 1 |
| 38               | (b) | Sum of zeroes = $2 + \frac{1}{2} = -5/p$<br>i.e. $5/2 = -5/p$ . So $p = -2$<br>Product of zeroes = $2 \times \frac{1}{2} = r/p$<br>i.e. $r/p = 1$ or $r = p = -2$  | 1 |
| 39               | (c) | $2\pi r = 100$ . So Diameter = $2r = 100/\pi =$ diagonal of the square.<br>side $\sqrt{2} =$ diagonal of square = $100/\pi$<br>$\therefore$ side = $100/\sqrt{2}\pi = 50\sqrt{2}/\pi$  | 1 |
| 40               | (b) | $3^{x+y} = 243 = 3^5$<br>So $x+y = 5$ -----(1)<br>$243^{x-y} = 3$<br>$(3^5)^{x-y} = 3^1$<br>So $5x - 5y = 1$ -----(2)<br>Since $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ , so unique solution   | 1 |
| <b>SECTION C</b> |     |  |   |
| 41               | (c) | Initially, at $t=0$ , Annie's height is 48ft<br>So, at $t=0$ , $h$ should be equal to 48<br>$h(0) = -16(0)^2 + 8(0) + k = 48$<br>So $k = 48$   | 1 |
| 42               | (b) | When Annie touches the pool, her height = 0 feet<br>i.e. $-16t^2 + 8t + 48 = 0$ above water level<br>$2t^2 - t - 6 = 0$<br>$2t^2 - 4t + 3t - 6 = 0$<br>$2t(t-2) + 3(t-2) = 0$<br>$(2t+3)(t-2) = 0$<br>i.e. $t = 2$ or $t = -3/2$<br>Since time cannot be negative, so $t = 2$ seconds  | 1 |
| 43               | (d) | $t = -1$ & $t = 2$ are the two zeroes of the polynomial $p(t)$<br>Then $p(t) = k(t - (-1))(t - 2)$<br>$= k(t + 1)(t - 2)$<br>When $t = 0$ (initially) $h_1 = 48\text{ft}$<br>$p(0) = k(0^2 - 0 - 2) = 48$<br>i.e. $-2k = 48$<br>So the polynomial is $-24(t^2 - t - 2) = -24t^2 + 24t + 48$ .  | 1 |
| 44               | (c) | A polynomial $q(t)$ with sum of zeroes as 1 and the product as -6 is given by<br>$q(t) = k(t^2 - (\text{sum of zeroes})t + \text{product of zeroes})$<br>$= k(t^2 - 1t + -6)$ .....(1)<br>When $t=0$ (initially) $q(0) = 48\text{ft}$  | 1 |

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|    |     | $q(0)=k(0^2- 1(0) -6)= 48$<br>i.e. $-6k = 48$ or $k= -8$<br>Putting $k = -8$ in equation (1), reqd. polynomial is $-8(t^2 -1t + -6)$<br>$= -8t^2 + 8t + 48$  |   |
| 45 | (a) | When the zeroes are negative of each other,<br>sum of the zeroes = 0<br>So, $-b/a = 0$<br>$-\frac{(k-3)}{-12} = 0$<br>$+\frac{k-3}{12} = 0$<br>$k-3 = 0,$<br>i.e. $k = 3.$   | 1 |
| 46 | (a) | Centroid of $\Delta E H J$ with $E(2,1), H(-2,4)$ & $J(-2,-2)$ is<br>$(\frac{2+-2+-2}{3}, \frac{1+4+-2}{3}) = (-2/3, 1)$   | 1 |
| 47 | (c) | If P needs to be at equal distance from $A(3,6)$ and $G(1,-3)$ , such that A,P and G are collinear, then P will be the mid-point of AG.<br>So coordinates of P will be $(\frac{3+1}{2}, \frac{6+-3}{2}) = (2, 3/2)$  | 1 |
| 48 | (a) | Let the point on x axis equidistant from $I(-1,1)$ and $E(2,1)$ be $(x,0)$<br>then $\sqrt{(x+1)^2 + (0-1)^2} = \sqrt{(x-2)^2 + (0-1)^2}$<br>$x^2 + 1 + 2x + 1 = x^2 + 4 - 4x + 1$<br>$6x = 3$<br>So $x = 1/2.$<br>$\therefore$ the required point is $(1/2, 0)$        | 1 |
| 49 | (b) | Let the coordinates of the position of a player Q such that his distance from $K(-4,1)$ is twice his distance from $E(2,1)$ be $Q(x, y)$<br>Then $KQ : QE = 2 : 1$<br>$Q(x, y) = (\frac{2 \times 2 + 1 \times -4}{3}, \frac{2 \times 1 + 1 \times 1}{3})$<br>$= (0,1)$ | 1 |
| 50 | (d) | Let the point on y axis equidistant from $B(4,3)$ and $C(4,-1)$ be $(0,y)$<br>then $\sqrt{(4-0)^2 + (3-y)^2} = \sqrt{(4-0)^2 + (y+1)^2}$<br>$16 + y^2 + 9 - 6y = 16 + y^2 + 1 + 2y$<br>$-8y = -8$<br>So $y = 1.$<br>$\therefore$ the required point is $(0, 1)$        | 1 |