25. VOLUME AND SURFACE AREA

IMPORTANT FORMULAE

nel Le CUBOID a ni besaiq ed una tada eleg te-aner eda le dagast eda helli

Let length = I, breadth = b and height = h units. Then,

- 1. Volume = $(1 \times b \times h)$ cubic units.
- 2. Surface area = 2 (lb + bh + lh) sq. units.
- 3. Diagonal = $\sqrt{l^2 + b^2 + h^2}$ units.

II. CUBE

Let each edge of a cube be of length a. Then,

- Volume = a³ cubic units.
- Surface area = 6a² sq. units.
- Diagonal = √3 a units.

III. CYLINDER

Let radius of base = r and Height (or length) = h. Then,

- Volume = (πι²h) cubic units.
- Curved surface area = (2πrh) sq. units.
- 3. Total surface area = $(2\pi rh + 2\pi r^2)$ sq. units $= 2\pi r (h + r)$ sq. units.

IV. CONE

Let radius of base = r and Height = h. Then,

- 1. Slant height, $l = \sqrt{h^2 + r^2}$ units.
- 2. Volume = $\left(\frac{1}{3}\pi r^2 h\right)$ cubic units.
- 3. Curved surface area = (πrl) sq. units.
- 4. Total surface area = $(\pi rl + \pi r^2)$ sq. units.

V. SPHERE

Let the radius of the sphere be r. Then,

- 1. Volume = $\left(\frac{4}{3}\pi r^3\right)$ cubic units.
- 2. Surface area = $(4\pi r^2)$ sq. units.

VI. HEMISPHERE

Let the radius of a hemisphere be r. Then.

- 1. Volume = $\left(\frac{2}{3}\pi r^3\right)$ cubic units.
- 2. Curved surface area = $(2\pi r^2)$ sq. units.
- 3. Total surface area = $(3\pi r^2)$ sq. units.

Remember: 1 litre = 1000 cm3.

25. VOLUME AND SURFACE AREA

IMPORTANT FORMULAE

nel Le CUBOID a ni besaiq ed una tada eleg te-aner eda le dagast eda helli

Let length = I, breadth = b and height = h units. Then,

- 1. Volume = $(1 \times b \times h)$ cubic units.
- 2. Surface area = 2 (lb + bh + lh) sq. units.
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Let each edge of a cube be of length a. Then,

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Let radius of base = r and Height = h. Then,

- 1. Slant height, $l = \sqrt{h^2 + r^2}$ units.
- 2. Volume = $\left(\frac{1}{3}\pi r^2 h\right)$ cubic units.
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- 4. Total surface area = $(\pi rl + \pi r^2)$ sq. units.

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- 1. Volume = $\left(\frac{2}{3}\pi r^3\right)$ cubic units.
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- 3. Total surface area = $(3\pi r^2)$ sq. units.

Remember: 1 litre = 1000 cm3.

SOLVED EXAMPLES

- Ex. 1. Find the volume and surface area of a cuboid 16 m long, 14 m broad and 7 m high.
 - Sol. Volume = $(16 \times 14 \times 7)$ m³ = 1568 m³.

Surface area = $[2(16 \times 14 + 14 \times 7 + 16 \times 7)]$ cm² = (2×434) cm² = 868 cm².

- Ex. 2. Find the length of the longest pole that can be placed in a room 12 m long, 8 m broad and 9 m high.
 - Sol. Length of longest pole = Length of the diagonal of the room

$$=\sqrt{(12)^2+8^2+9^2}=\sqrt{289}=17 \text{ m}.$$

- Ex. 3. The volume of a wall, 5 times as high as it is broad and 8 times as long as it is high, is 12.8 cu. metres. Find the breadth of the wall.
 - Sol. Let the breadth of the wall be x metres.

Then, Height = 5x metres and Length = 40x metres.

$$\therefore x \times 5x \times 40x = 12.8 \iff x^3 = \frac{12.8}{200} = \frac{128}{2000} = \frac{64}{1000}.$$

So,
$$x = \frac{4}{10}$$
 m = $\left(\frac{4}{10} \times 100\right)$ cm = 40 cm.

- Ex. 4. Find the number of bricks, each measuring 24 cm x 12 cm x 8 cm, required to construct a wall 24 m long, 8m high and 60 cm thick, if 10% of the wall is filled with mortar?
 - Sol. Volume of the wall = (2400 × 800 × 60) cu. cm.

Volume of bricks = 90% of the volume of the wall

$$=$$
 $\left(\frac{90}{100} \times 2400 \times 800 \times 60\right)$ cu. cm.

Volume of 1 brick = (24 × 12 × 8) cu. cm.

: Number of bricks =
$$\left(\frac{90}{100} \times \frac{2400 \times 800 \times 60}{24 \times 12 \times 8}\right) = 45000$$
.

- Ex. 5. Water flows into a tank 200 m × 150 m through a rectangular pipe 1.5 m × 1.25 m @ 20 kmph. In what time (in minutes) will the water rise by 2 metres?
 - Sol. Volume required in the tank = $(200 \times 150 \times 2)$ m³ = 60000 m³.

Length of water column flown in 1 min. =
$$\left(\frac{20 \times 1000}{60}\right)$$
 m = $\frac{1000}{3}$ m.

Volume flown per minute =
$$\left(1.5 \times 1.25 \times \frac{1000}{3}\right)$$
 m³ = 625 m³.

- \therefore Required time = $\left(\frac{60000}{625}\right)$ min. = 96 min.
- Ex. 6. The dimensions of an open box are 50 cm, 40 cm and 23 cm. Its thickness is 3 cm. If 1 cubic cm of metal used in the box weighs 0.5 gms, find the weight of the box.
 - Sol. Volume of the metal used in the box External Volume Internal Volume

$$\therefore \text{ Weight of the metal } = \left(\frac{16080 \times 0.5}{1000}\right) \text{ kg = 8.04 kg}.$$

Ex. 7. The diagonal of a cube is 6\3 cm. Find its volume and surface area.

Sol. Let the edge of the cube be a.

$$\sqrt{3} \ a = 6\sqrt{3} \Rightarrow a = 6$$

Volume = $\mu^3 = (6 \times 6 \times 6) \text{ cm}^3 = 216 \text{ cm}^3$.

Surface area = $6a^2 = (6 \times 6 \times 6) \text{ cm}^2 - 216 \text{ cm}^2$.

Ex. 8. The surface area of a cube is 1734 sq. cm. Find its volume.

Sol. Let the edge of the cube be a Then,

$$6a^2 = 1734 \implies a^2 = 289 \implies a = 17 \text{ cm}.$$

Volume = $a^3 = (17)^3$ cm³ = 4913 cm³.

Ex. 9. A rectangular block 6 cm by 12 cm by 15 cm is cut up into an exact number of equal cubes. Find the least possible number of cubes. Sol. Volume of the block = $(6 \times 12 \times 15)$ cm³ = 1080 cm³. Side of the largest cube = H.C.F. of 6 cm, 10 cm, 15

Side of the largest cube = H.C.F. of 6 cm, 12 cm, 15 cm = 3 cm.

Volume of this cube = $(3 \times 3 \times 3)$ cm³ = 27 cm³.

Number of cubes =
$$\left(\frac{1080}{27}\right)$$
 = 40.

Ex. 10. A cube of edge 15 cm is immersed completely in a rectangular vessel containing water. If the dimensious of the base of vessel are 20 cm x 15 cm, find the rise in water (R.R.B. 2003) level.

Sol. Increase in volume = Volume of the cube = (15×15×15) cm3.

Rise in water level =
$$\left(\frac{\text{Volume}}{\text{Area}}\right) = \left(\frac{15 \times 15 \times 15}{20 \times 15}\right) \text{ cm} = 11.25 \text{ cm}.$$

Ex. 11. Three solid cubes of sides 1 cm, 6 cm and 8 cm are melted to form a new cube. Find the surface area of the cube so formed.

Volume of new cube = $(1^3 + 6^3 + 8^3)$ cm² = 729 cm³.

Edge of new cube = $\sqrt[3]{729}$ cm = 9 cm.

Surface area of the new cube = $(6 \times 9 \times 9)$ cm² = 486 cm².

Ex. 12. If each edge of a cube is increased by 50%, find the percentage increase in its surface area.

Sol. Let original length of each edge = a.

Then, original surface area = 6a2.

New edge =
$$(150\% \text{ of } a) = \left(\frac{150}{100} a\right) = \frac{3a}{2}$$
.

New surface area =
$$6 \times \left(\frac{3a}{2}\right)^2 = \frac{27}{2}a^2$$
.

Increase percent in surface area = $\left(\frac{15}{2}a^2 \times \frac{1}{6a^2} \times 100\right)\% = 125\%$.

Ex. 13. Two cubes have their volumes in the ratio 1: 27. Find the ratio of their surface areas.

Sol. Let their edges be a and b. Then.

$$\frac{a^3}{b^3} = \frac{1}{27} \text{ or } \left(\frac{a}{b}\right)^3 = \left(\frac{1}{3}\right)^3 \text{ or } \frac{a}{b} = \frac{1}{3}.$$

$$\therefore \quad \text{Ratio of their surface areas} = \frac{6a^2}{6b^2} = \frac{a^2}{b^2} = \left(\frac{a}{b}\right)^2 = \frac{1}{9}, i.e., 1:9.$$

Ex. 14. Find the volume, curved surface area and the total surface area of a cylinder with diameter of base 7 cm and height 40 cm.

Sol. Volume
$$= \pi r^2 h = \left(\frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 40\right) \text{ cm}^3 = 1540 \text{ cm}^3$$
.

Curved surface area =
$$2\pi rh = \left(2 \times \frac{22}{7} \times \frac{7}{2} \times 40\right) \text{ cm}^2 = 880 \text{ cm}^2$$
.

Total surface area =
$$2\pi rh + 2\pi r^2 = 2\pi r(h+r)$$

$$= \left[2 \times \frac{22}{7} \times \frac{7}{2} \times (40 + 3.5)\right] \text{ cm}^2 = 957 \text{ cm}^2.$$

Ex. 15. If the capacity of a cylindrical tank is 1848 m3 and the diameter of its base is 14 m, then find the depth of the tank.

Sol. Let the depth of the tank be h metres. Then,

$$\pi \times (7)^2 \times h = 1848 \Leftrightarrow h = \left(1848 \times \frac{7}{22} \times \frac{1}{7 \times 7}\right) = 12 \text{ m.}$$

Ex. 16. 2.2 cubic dm of lead is to be drawn into a cylindrical wire 0.50 cm in diameter. Find the length of the wire in metres.

Sol. Lct the length of the wire be h metres. Then,

$$n \times \left(\frac{0.50}{2 \times 100}\right)^2 \times h = \frac{22}{1000} \iff h = \left(\frac{2.2}{1000} \times \frac{100 \times 100}{0.25 \times 0.25} \times \frac{7}{22}\right) = 112 \text{ m}.$$

Ex. 17. How many iron rods, each of length 7 m and diameter 2 cm can be made out of 0.88 cubic metre of iron?

Sol. Volume of 1 rod =
$$\left(\frac{22}{7} \times \frac{1}{100} \times \frac{1}{100} \times 7\right)$$
 cu. m = $\frac{11}{5000}$ cu. m.

Volume of iron = 0.88 cu. m.

Number of rods =
$$\left(0.88 \times \frac{5000}{11}\right) = 400$$
.

Ex. 18. The radii of two cylinders are in the ratio 3: 5 and their heights are in the ratio of 2: 3. Find the ratio of their curved surface areas.

Let the radii of the cylinders be 3x, 5x and their heights be 2y, 3y respectively. Then,

Ratio of their curved surface areas =
$$\frac{2\pi \times 3x \times 2y}{2\pi \times 5x \times 3y} = \frac{2}{5} = 2:5$$
.

Ex. 19. If 1 cubic cm of cast iron weighs 21 gms, then find the weight of a cast iron pipe of length 1 metre with a bore of 3 cm and in which thickness of the metal is 1 cm.

Sol. Inner radius =
$$\left(\frac{3}{2}\right)$$
 cm = 1.5 cm, Outer radius = $(1.5+1)$ = 2.5 cm.

Volume of iron = $[\pi \times (2.5)^2 \times 100 - \pi \times (1.5)^2 \times 100]$ cm³

$$=\frac{22}{7}\times 100\times [(2.5)^2-(1.5)^2]$$
 cm³ = $\left(\frac{8800}{7}\right)$ cm³.

$$\therefore \text{ Weight of the pipe } = \left(\frac{8800}{7} \times \frac{21}{1000}\right) \text{ kg } = 26.4 \text{ kg}.$$

Ex. 20. Find the slant height, volume, curved surface area and the whole surface area of a cone of radius 21 cm and height 28 cm.

Sol. Here, r = 21 cm and h = 28 cm.

:. Slant height,
$$l = \sqrt{r^2 + h^2} = \sqrt{(21)^2 + (28)^2} = \sqrt{1225} = 35$$
 cm.

Volume =
$$\frac{1}{3}\pi r^2 h = \left(\frac{1}{3} \times \frac{22}{7} \times 21 \times 21 \times 28\right) \text{ cm}^3 = 12936 \text{ cm}^3$$
.

Curved surface area =
$$\pi rl = \left(\frac{22}{7} \times 21 \times 35\right) \text{ cm}^2 = 2310 \text{ cm}^2$$
.

Total surface area =
$$(\pi rl + \pi r^2) = \left(2310 + \frac{22}{7} \times 21 \times 21\right) \text{ cm}^2 = 3696 \text{ cm}^2$$
.

Ex. 21. Find the length of canvas 1.25 m wide required to build a conical tent of base radius 7 metres and height 24 metres.

Sol. Here,
$$r = 7m$$
 and $h = 24 m$.

So,
$$l = \sqrt{r^2 + h^2} = \sqrt{7^2 + (24)^2} = \sqrt{625} = 25 \text{ m}.$$

Area of canvas =
$$\pi rl = \left(\frac{22}{7} \times 7 \times 25\right) \text{ m}^2 = 550 \text{ m}^2$$
.

$$\therefore \quad \text{Length of canvas} = \left(\frac{\text{Area}}{\text{Width}}\right) = \left(\frac{550}{1.25}\right) \text{ m} = 440 \text{ m}.$$

Ex. 22. The heights of two right circular cones are in the ratio 1 : 2 and the perimeters of their bases are in the ratio 3: 4. Find the ratio of their volumes.

Sol. Let the radii of their bases be r and R and their heights be h and 2h respectively.

Then,
$$\frac{2\pi r}{2\pi R} = \frac{3}{4} \implies \frac{r}{R} = \frac{3}{4} \implies R = \frac{4}{3}r$$
.

:. Ratio of volumes =
$$\frac{\frac{1}{3}\pi r^2 h}{\frac{1}{3}\pi \left(\frac{4}{3}r\right)^2 (2h)} = \frac{9}{32} = 9:32$$

Ex. 23. The radii of the bases of a cylinder and a cone are in the ratio of 3: 4 and their heights are in the ratio 2: 3. Find the ratio of their volumes.

Sol. Let the radii of the cylinder and the cone be 3r and 4r and their heights be 2h and 3h respectively.

$$\therefore \frac{\text{Volume of cylinder}}{\text{Volume of cone}} = \frac{\pi \times (3r)^2 \times 2h}{\frac{1}{3}\pi \times (4r^2) \times 3h} = \frac{9}{8} = 9:8.$$

Ex. 24. A conical vessel, whose internal radius is 12 cm and height 50 cm, is full of liquid. The contents are emptied into a cylindrical vessel with internal radius 10 cm. Find the height to which the liquid rises in the cylindrical vessel.

Sol. Volume of the liquid in the cylindrical vessel

= Volume of the conical vessel

$$= \begin{array}{c} \text{Volume of the conical vessel} \\ = \left(\frac{1}{3} \times \frac{22}{7} \times 12 \times 12 \times 50\right) \text{ cm}^3 = \left(\frac{22 \times 4 \times 12 \times 50}{7}\right) \text{ cm}^3. \end{array}$$
Let the height of the liquid in the vessel be h

Let the height of the liquid in the vessel be h.

Then,
$$\frac{22}{7} \times 10 \times 10 \times h = \frac{22 \times 4 \times 12 \times 50}{7}$$
 or $h = \left(\frac{4 \times 12 \times 50}{10 \times 10}\right) = 24$ cm.

Ex. 25. Find the volume and surface area of a sphere of radius 10.5 cm.

Sol. Volume
$$=\frac{4}{3}\pi r^3 = \left(\frac{4}{3} \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} \times \frac{21}{2}\right) \text{ cm}^3 = 4851 \text{ cm}^3.$$

Surface area =
$$4\pi r^2 = \left(4 \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2}\right) \text{ cm}^2 = 1386 \text{ cm}^2$$
.

Ex. 26. If the radius of a sphere is increased by 50%, find the increase percent in volume and the increase percent in the surface area.

Sol. Let original radius = R. Then, new radius =
$$\frac{150}{100}$$
 R = $\frac{3R}{2}$.

Original volume =
$$\frac{4}{3}\pi R^3$$
, New volume = $\frac{4}{3}\pi \left(\frac{3R}{2}\right)^3 = \frac{9\pi R^3}{2}$.

Increase % in volume =
$$\left(\frac{19}{6} \pi R^3 \times \frac{3}{4\pi R^3} \times 100\right)$$
% = 237.5%.

Original surface area =
$$4\pi R^2$$
. New surface area = $4\pi \left(\frac{3R}{2}\right)^2 = 9\pi R^2$.

Increase % in surface area =
$$\left(\frac{5\pi R^2}{4\pi R^2} \times 100\right)$$
% = 125%.

Ex. 27. Find the number of lead balls, each 1 cm in diameter that can be made from a sphere of diameter 12 cm.

Sol. Volume of larger sphere =
$$\left(\frac{4}{3}\pi \times 6 \times 6 \times 6\right)$$
 cm³ = 288π cm³.

Volume of 1 small lead ball =
$$\left(\frac{4}{3}\pi \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}\right) \text{ cm}^3 = \frac{\pi}{6} \text{ cm}^3$$
.

.. Number of lead balls =
$$\left(288\pi \times \frac{6}{\pi}\right)$$
 = 1728.

Ex. 28. How many spherical bullets can be made out of a lead cylinder 28 cm high and with base radius 6 cm, each bullet being 1.5 cm in diameter? (R.R.B. 2003)

Sol. Volume of cylinder =
$$(\pi \times 6 \times 6 \times 28)$$
 cm³ = (36×28) π cm³.

Volume of each bullet =
$$\left(\frac{4}{3}\pi \times \frac{3}{4} \times \frac{3}{4} \times \frac{3}{4}\right)$$
 cm³ = $\frac{9\pi}{16}$ cm³.

Number of bullets =
$$\frac{\text{Volume of cylinder}}{\text{Volume of each bullet}} = \left[(36 \times 28) \pi \times \frac{16}{9\pi} \right] = 1792.$$

Ex. 29. A copper sphere of diameter 18 cm is drawn into a wire of diameter 4 mm. Find the length of the wire.

Sol. Volume of sphere =
$$\left(\frac{4}{3}\pi \times 9 \times 9 \times 9\right)$$
 cm³ = 972π cm³.

Volume of wire = $(\pi \times 0.2 \times 0.2 \times h)$ cm³. At dards at largest and hard one of

$$\therefore 972\pi = \pi \times \frac{2}{10} \times \frac{2}{10} \times h \implies h = (972 \times 5 \times 5) \text{ cm} = \left(\frac{972 \times 5 \times 5}{100}\right) \text{ m} = 243 \text{ m}.$$

Ex. 30. Two metallic right circular cones having their heights 4.1 cm and 4.3 cm and the radii of their bases 2.1 cm each, have been melted together and recast into a sphere. Find the diameter of the sphere.

Sol. Volume of sphere = Volume of 2 cones

$$= \left[\frac{1}{3} \pi \times (2.1)^2 \times 4.1 + \frac{1}{3} \pi \times (2.1)^2 \times 4.3 \right] \text{cm}^3 = \frac{1}{3} \pi \times (2.1)^2 (8.4) \text{ cm}^3.$$
we of the sphere by P.

Let the radius of the sphere be R.

$$\therefore \frac{4}{3} \pi R^3 = \frac{1}{3} \pi (2.1)^3 \times 4 \text{ or } R = 2.1 \text{ cm.}$$

Hence, diameter of the sphere = 4.2 cm.

Ex. 31. A cone and a sphere have equal radii and equal volumes. Find the ratio of the diameter of the sphere to the height of the cone.

Sol. Let radius of each be R and height of the cone be H.

Then,
$$\frac{4}{3} \pi R^3 = \frac{1}{3} \pi R^2 H$$
 or $\frac{R}{H} = \frac{1}{4}$ or $\frac{2R}{H} = \frac{2}{4} = \frac{1}{2}$.

.. Required ratio = 1 : 2.

Ex. 32. Find the volume, curved surface area and the total surface area of a hemisphere of radius 10.5 cm.

Sol. Volume =
$$\frac{2}{3}\pi r^3 = \left(\frac{2}{3} \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} \times \frac{21}{2}\right) \text{ cm}^3 = 2425.5 \text{ cm}^3$$
.

Curved surface area =
$$2\pi r^2 = \left(2 \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2}\right) \text{ cm}^2 = 693 \text{ cm}^2$$
.

Total surface area =
$$3\pi r^2 = \left(3 \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2}\right) \text{ cm}^2 = 1039.5 \text{ cm}^2$$
,

Ex. 33. A hemispherical bowl of internal radius 9 cm contains a liquid. This liquid is to be filled into cylindrical shaped small bottles of diameter 3 cm and height 4 cm. How many bottles will be needed to empty the bowl?

How many bottles will be needed to empty the bowl? (N.I.F.)

Sol. Volume of bowl =
$$\left(\frac{2}{3}\pi \times 9 \times 9 \times 9\right)$$
 cm³ = 486π cm³.

Volume of 1 battle =
$$\left(\pi \times \frac{3}{2} \times \frac{3}{2} \times 4\right)$$
 cm³ = 9π cm³.

Number of bottles =
$$\left(\frac{486\pi}{9\pi}\right)$$
 = 54.

Ex. 34. A cone, a hemisphere and a cylinder stand on equal bases and have the same height. Find the ratio of their volumes.

Sol. Let R be the radius of each.

Height of hemisphere = Its radius = R.

Height of each = R.

Ratio of volumes =
$$\frac{1}{3} \pi R^2 \times R : \frac{2}{3} \pi R^3 : \pi R^2 \times R = 1 : 2 : 3$$
.

EXERCISE 25A

(OBJECTIVE TYPE QUESTIONS)

Directions : Mark (✓) against the correct answer :

- 1. The capacity of a tank of dimensions (8 m × 6 m × 2.5 m) is :
- (a) 120 litres
- (b) 1200 litres
- (c) 12000 litres (d) 120000 litres
- Find the surface area of a 10 cm × 4 cm × 3 cm brick. (a) 84 sq. cm (b) 124 sq. cm (c) 164 sq. cm (d) 180 sq. cm
- 3. A cistern 6 m long and 4 m wide contains water up to a depth of 1 m 25 cm. The total area of the wet surface is : (S.S.C. 2004)
- (a) 49 m²
- (b) 50 m²
- (c) 53.5 m²
- (d) 55 m²
- 4. A boat having a length 3 m and breadth 2 m is floating on a lake. The boat sinks by 1 cm when a man gets on it. The mass of man is: (R.R.B. 2002)
 - (a) 12 kg
- (b) 60 kg
- (c) 72 kg
- (d) 96 kg

D.			depth of water in the ta			
-	(a) 3.5 m	(b) 4 m	(c) 5 m	(d) 6 m		
6.			gms, the weight of a manneth of the block is:	rble block 28 cm in		
	(a) 26.5 cm	(b) 32 cm	(c) 36 cm	(d) 37.5 cm		
7.		gold sheet is extend eness of the sheet is	ded by hammering so as	to cover an area of		
	(a) 0.0005 cm	(b) 0.005 cm	(c) 0.05 cm	(d) 0.5 cm		
8.	In a shower, 5 cm of is:	rain falls. The volum	e of water that falls on 1.5	hectares of ground		
	(a) 75 cu. m	(b) 750 cu. m	(c) 7500 cu. m	(d) 75000 cu. m		
9.			th and the length of the 28 cu. m, its width is :	(C.B.I. 1998)		
	(a) 4 m	(b) 4.5 m	(c) 5 m	(d) 6 m		
10.	The volume of a re- ratio of 3:2:1. If cost will be:	its entire surface is	one is 10368 dm ³ . Its din polished at 2 paise per o	im2, then the total		
	(a) Rs. 31.50	(b) Rs. 31.68		(d) Rs. 63.36		
11.	The edges of a cub volume of the cubo	d is:	1:2:3 and its surface a	(S.S.C. 1999)		
	(a) 24 cm ³	(b) 48 cm ³	(c) 64 cm ³	(d) 120 cm ³		
12.	8 cm × 6 cm × 2 cm	n, is :	n be kept in a rectangular	r box of dimensions		
	(a) 2√13 cm	(b) 2√14 cm	(c) 2√26 cm	(d) 10√2 cm		
13.	Find the length of t	he longest rod that c	an be placed in a room 16	m long, 12 m broad		
	and $10\frac{2}{3}$ m high.		ratio of their volumes, the riches of each	(S.S.C. 1999)		
	(a) $22\frac{1}{3}$ m	(b) $22\frac{2}{3}$ m	(c) 23 m	(d) 68 m		
14.	How many bricks, e a wall 8 m × 6 m		m × 11.25 cm × 6 cm, will	be needed to build (B.S.F. 2001)		
	(a) 5600	(b) 6000	(c) 6400	(d) 7200		
15.	i. The number of bricks, each measuring 25 cm × 12.5 cm × 7.5 cm, required to construe a wall 6 m long, 5 m high and 0.5 m thick, while the mortar occupies 5% of the volum of the wall, is: (M.B.A. 200)					
	(a) 3040	(b) 5740	(c) 6080	(d) 8120		
16.	50 men took a dip the average displac- in the tank will be	ement of water by a	m long and 20 m broad or man is 4 m ³ , then the ris	n a religious day. If e in the water level (N.I.F.T. 2000)		
	(a) 20 cm	(b) 25 cm	(e) 35 cm	(d) 50 cm		
17.	A tank 4 m long, 2 wide. If the earth of field is:	.5 m wide and 1.5 m ug out is evenly spr	n deep is dug in a field 3 ead out over the field, the	rise in level of the		
	(a) 3.1 cm	(b) 4.8 cm	(c) 5 cm	(d) 6.2 cm		
18.			ing at the rate of 3.5 km penute (in cubic metres) is:			
	(a) 3150	(b) 31500	(e) 6300	(d) 63000		

	 A rectangular water at the opening at a s tank in half an hour 	peed of 10 km/hr. By	how much, the water	rough a pipe 40 sq. cm er level will rise in the (M.B.A. 1997)
	(-) 3 cm	edup (4) peru multi	5	a In time soft. AE
	(a) 2 cm	(b) - cm	(c) = cm	(d) None of these
	A hall is 15 m long ar is equal to the sum (a) 720	nd 12 m broad. If the of areas of the four v (b) 900	sum of the areas of the walls, the volume of (c) 1200	ne floor and the ceiling the hall is: (d) 1800
21	The sum of the length	th broadth and dans		(L.I.C. A.A.O. 2003)
11111111111	The sum of the length 5√5 cm. It surface a	men in .	n of a cuboid is 19 c	m and its diagonal is
99	(a) 125 cm ²	(b) 236 cm ²	(c) 361 cm ²	(d) 486 cm ²
22.	A swimming pool 9 n deep on the deeper s (s) 208 m ³	ide. Its volume is :		(M.A.T. 1998)
0.0		(b) 270 m ³	(c) 360 m ³	(d) 408 m ³
23.	is 8 m, the volume of	s cut off so as to mal the box (in m ³) is :	ith dimensions 48 m ke an open box. If the	× 36 m. From each of e length of the square (M.A.T. 2003)
	(a) 4830	(b) 5120	(c) 6420	(d) 8960
24.	An open box is made o 8.3 dm. The cost of p is:	f wood 3 cm thick. Its ainting the inner sur	external dimensions a face of the box at 50	re 1.46 m, 1.16 m and paise per 100 sq. cm
	(a) Rs. 138.50	(b) Rs. 277	(e) Rs. 415. 50	(d) Rs. 554
25.	A cistern of capacity its walls are 5 cm th	8000 litres measures ick. The thickness of	externally 3.3 m by	2.6 m by 1.1 m and (S.S.C. 2003)
	(a) 90 cm	(b) 1 dm	(c) 1 m	(d) 1.1 m
26.	If a metallic cuboid we			uboid of metal weigh
	if all dimensions are	reduced to one-fourth	of the original?	(D.M.R.C. 2003)
	(a) 0.25 kg	(b) 0.50 kg	(c) 0.75 kg	(d) 1 kg
27.	The areas of the three known. The product of	these areas is equa	rectangular box which	n meet in a point are ion Officers', 2003)
	(a) the volume of the		(b) twice the volume	me of the box
	(c) the square of the v	clume of the box	(d) the cube root of	the volume of the box
28.	60 cm ² respectively, th	ree adjacent faces of sen find the volume	a cuboidal box are	120 cm ² , 72 cm ² and
	(a) 720 cm ³	(b) 864 cm ³	(e) 7200 cm ³	(d) (72)2 cm3
	and its volume is 900	djacent faces of a rec	tangular block are in	the ratio of 2 · 3 · 4
	(a) 10 cm	(b) 15 cm	(c) 20 cm	(d) 30 cm
30.	The perimeter of one (a) 125 cm ³	face a of cube is 20 of	m. Its volume must	he · (SSC 1999)
31.	Total surface area of :	mihe where side in	0.5 cm is	
				(I.M.T. 2002)
	(a) $\frac{1}{4}$ cm ²	(b) $\frac{1}{8}$ cm ²	(c) $\frac{3}{4}$ cm ²	$(d) \frac{3}{2} \text{ cm}^2$
32.	The cost of the paint i	s Rs. 36.50 per kg. If	1 kg of paint covers	16 square feet, how
	much will it cost to pa	aint outside of a cube (b) Rs. 76	having 8 feet each	side ?
	(d) Rs. 972	(e) None		(Bank P.O. 2002)

33.	The dimensions of a	piece of iron in the shap	e of a cuboid are 270 c	m × 100 cm × 64 cm.
	If it is melted and	recast into a cube, then	the surface area of	the cube will be :
	(a) 14400 cm ²	(b) 44200 cm ²	(e) 57600 cm ²	(d) 86400 cm ²
34.		g the whole surface are		rate of 13 paise per
		3. Then the volume of t		(S.S.C. 2003)
		(b) 9000 cm ³		
		rube is 729 cm ³ , then the		
	(a) 456 cm ²	(b) 466 cm ²		(d) 486 cm ²
36.	The length of an ed length of the larges	ge of a hollow cube ope t pole that it can accor	en at one face is √3 nmodate ?	(M.A.T. 1997)
	(a) √3 metres	(b) 3 metres	(c) 3√3 metres	(d) $\sqrt{3}$ metres
37.	What is the volume	of a cube (in cubic cm) whose diagonal me	asures 4√3 cm ?
			(c) 27	(d) 64
				Management, 1999)
		a cube is 600 cm ² . The		
	10	10	to an Fi	(d) 10 fo
	(a) $\frac{10}{\sqrt{3}}$ cm	$\sqrt{2}$ cm	(c) 10√2 cm	(d) 10√3 cm
		resenting volume and sof the cube in terms of		
	(a) 3	(b) 4	(c) 5	(d) 6
40.	TO THE RESERVE THE PARTY OF THE	10 cm edge can be pu		
	(a) 10	(b) 100	(c) 1000	(d) 10000
			781 Ldm	(R.R.B. 2003)
41.	A rectangular box r number of cubical b	neasures internally 1.6 blocks each of edge 20 o	m long, 1 m broad a em that can be packe	and 50 cm deep. The ed inside the box is :
	(a) 30	(b) 53	(c) 60	(d) 120
		3 cm edge can be cut		
	(a) 36		(c) 218	
				(IGNOU, 2003)
	The least possible r	$6 \text{ cm} \times 9 \text{ cm} \times 12 \text{ cm}$ is consumber of cubes will be	: (Secti	ion Officers', 2003)
	(a) 6	(b) 9	(c) 24	(d) 30
44.	The size of a wooder	n block is 5 × 10 × 20 cr wooden cube of minim	n. How many such bl um size ?	ocks will be required
	(a) 6	(b) 8	(c) 12	(d) 16
45.		10 cm is hammered in sheet are in the ratio 1		
	(a) 10 cm, 50 cm	(b) 20 cm, 100 cm		(d) None of these
	Particological Control of the Contro		(Hotel]	Management, 1997)
46.		whose edges are 6 cm, single cube. The edge of		
		(b) 14 cm		
47.	Five equal cubes, es	ach of side 5 cm, are pla ed will be :	aced adjacent to each	other. The volume of
(10082.)	(a) 125 cm ³	(b) 625 cm ³	(c) 15525 cm ³	(d) None of these

48.			th of edge 1 cm. The ra the large cube is equ	
	(a) 1:5	(b) 1 : 25	(c) 1:125	(d) 1:625
		What is the ratio of	l obtained by melting the total surface area	
			(c) 25 : 18	(d) 27 ; 20
			: 5 are melted to form	
			cubes are :	
	(a) 3 cm, 4 cm, 5 c		(b) 6 cm, 8 cm, 1	10 cm
	(c) 9 cm, 12 cm, 1:	5 cm	(d) None of these	66, The radius
51.	If the volumes of t	wo cubes are in the	ratio 27 : 1, the ratio	of their edges is :
	(a) 1:3	(b) 1:27	(c) 3 : 1	(d) 27:1
				(S.S.C. 1999)
52.	The volumes of two	cubes are in the rat	io 8 : 27. The ratio of	their surface areas is :
	(a) 2:3	(b) 4:9	(c) 12:9	
				Management, 2003)
53.	Two cubes have vol	umes in the ratio 1 :	27. Then the ratio of	A CONTRACTOR OF THE PARTY OF TH
		that of the other is		Pind the rath
	(a) 1:3	(b) 1:6	(c) 1:9	(d) 1:12
54.	If each edge of a co	be is doubled, then	its volume :	
	(a) is doubled		(h) becomes 4 tir	
	(c) becomes 6 time	g woold (b)	(d) becomes 8 tir	
55.			, then the percentage	
	(a) 25%	(b) 48.75%	(c) 50%	(d) 56.25%
56.		a diameter of 2 met	res, is dug to a depth	of 14 metres. What is
			(c) 40 m ³	
57.		ylindrical tank is 246	6.4 litres. If the height	t is 4 metres, what is
			m (d) 28 m	(Bank P.O. 2003)
	The volume of a rig		whose curved surface	area is 2640 cm ² and
		(b) 7720 cm ³	(c) 13860 cm ³	(d) 55440 cm ³
59			der with its height e	ound to the radius is
	1 .	radius of the cylind		qual to the radius is
	(a) π cm	for all hose front i more		74. The section of
en		(b) 2 cm	(c) 3 cm	(d) 4 cm
ου.	Then its volume is	The second of the second of	14 cm and its curved	SHU I (B)
	(a) 1408 cm ³	(b) 2816 cm ³	(c) 5632 cm ³	(d) 9856 cm ³
61.			m high and its base r st of the material used	
	(a) Rs. 281.60	(b) Rs. 290	(c) Rs. 340.50	(d) Rs. 500
62.	The curved surface multiplying its volu		lar cylinder of base ra	dius r is obtained by
	The same of the sa			and any add 2
	(a) 2r	(b) 2	(c) 2r ²	(d) 2

63.		al surface area to tht 60 cm, is :		ice area of a	cylinder whose radius is
	(a) 2:1	(b) 3:2		c) 4:3	(d) 5:3
	A powder tin h	as a square base v	with side 8 cm	and height	14 cm. Another tin has a erence in their capacities
	is:			11	and the large er
	(a) 0	(b) 132 cm			(d) 192 cm ³
65.		en the radius of to			a cylinder is 2 : 3. If its ler is :
					(d) 38808 cm ²
66.	The radius of		half its hei many litres o	ght and are of milk can it	a of the inner part is contain?
	(a) 1.4	(b) 1.5	(c) 1.7	(d) 1.9	(e) 2.2
					(S.B.I.P.O. 2000)
67.	The sum of the	radius of the bas	e and the hei nder be 1628	ght of a solid sq. metres, i	cylinder is 37 metres. If ts volume is :
	(a) 3180 m ³	(b) 4620 r	n ³ (c) 5240 m³ 	(d) None of these
68.		face area of a cyl of its diameter to		is 264 m ² ar	id its volume is 924 m ³ . (S.S.C. 2002)
	(a) 3:7	(b) 7:3	(c) 6:7	(d) 7:6
69.	The height of a	closed cylinder o	f given volun	e and the mi	nimum surface area is :
	(a) equal to its			b) half of its	
	(c) double of it		(d) None of th	ese (R.R.B. 2002)
70.	If the radius of	the base of a right	circular cylin	der is halved,	keeping the height same, hat of the original one?
	(a) 1:2	(b) 1:4		c) 1:8	(d) 8:1
71.		o cylinders are in atio of their volum			heights are in the ratio
	(a) 4:9	(b) 9:4		c) 20 : 27	(d) 27:20
72.	Two right circu ratio of their r		ual volumes h	ave their heig	hts in the ratio 1 : 2. The (S.S.C. 1999)
	(a) 1:2	(b) 1:4	m 17	c) 2:1	(d) √2:1
73.	X and Y are tw	o cylinders of the	same height. he height of 2	The base of X X is doubled, t	has diameter that is half he volume of X becomes:
	(a) equal to th	e volume of Y		b) double the	
	(c) half the vo	lume of Y	(d) greater tha	an the volume of Y
					(C.B.I. 1997)
74.		wire is decreased now many times t			e remains the same. The
	(a) 1 time	(b) 3 time		(c) 6 times	(d) 9 times
75.	A cylindrical to	nk of diameter 35 in the tank will	cm is full of drop by :	water. If 11 lit	res of water is drawn off, (S.S.C. 1999)
	(a) $10\frac{1}{2}$ cm	(b) $11\frac{3}{7}$ c	m	(c) $12\frac{6}{7}$ cm	(d) 14 cm
76.	A well with 14	m inside diamete all around it to a	er is dug 10 n	n deep. Earth	taken out of it has been embankment. The height
	1	2		3	3
	(n) = m	(b) = m		(c) - m	(d) = m

77.			internal diameter 7 of is the volume of water	
		(b) 3850	(c) 4620	
78.			nd thickness 0.2 cm to	
m	right circular cyline	ler of height 8 cm an	d base radius 3 cm is	: (S.S,C. 2003)
mo			(c) 600	
79.	respectively are fill		and 10 cm and height s water is poured into vessel is :	
	(a) 17.5 cm	(b) 18 cm	(e) 20 cm	(d) 25 cm
80.	66 cubic centimetre the wire in metres		nto a wire 1 mm in di	ameter. The length of (C.B.I. 1998)
	(a) 84	(b) 90	(c) 168	(d) 336
81.			girth of 440 cm is ma	UUCUU 1600 17. 310 A
	The volume of the		4 > PRO04 3	Ch comes 3
no.	(a) 54982 cm ³	(b) 56372 cm ³	(e) 57636 cm ³	(d) 58752 cm ³
82.	tube is 11.2 cm and	its length is 21 cm.	nade of metal. The int The metal everywhere	e is 0.4 cm thick. The
		l is: 1000 talaono ida		(S.S.C. 2003)
AU.	(a) 280.52 cm ³	(b) 306.24 cm ³	(c) 310 cm ³	(d) 316 cm ³
83.			meter mush be taken cm thick and 15 cm	
	(a) 42.3215 cm	(b) 44.0123 cm	(c) 44.0625 cm	(d) 44.6023 cm
84.			external diameter is b cm ³ , then the weight	
	(a) 3.6 kg		(c) 36 kg	
	D.R.R. of the or	ner benom nelt le tuelt	at more more at the	(S.S.C. 2004)
85.			ter. If the height of the hickness of the materi	cylinder is 40 cm and
	(a) 0.2 mm	(b) 0.3 mm	(c) 1 mm	(d) 2 mm
86.			ne are 3 cm and 5 cm	The state of the s
		ase and height of a cy of cone to that of the	linder are 2 cm and 4 cylinder is :	cm respectively. The
	(a) 1:3	(b) 15:8	(c) 15 : 16	(d) 45 : 16
87.	The curved surface is:	of a right circular con	e of height 15 cm and	base diameter 16 cm (S.S.C. 1999)
	(a) 60π cm ²	(b) 68a cm ²	(e) 120π cm ²	
88.	What is the total su	rface area of a right ci	rcular cone of height 1 (Hotel	4 cm and base radius
		(b) 462 cm ²		(d) None of these
20				
00.	form a cone. The vo	olume of the cone so f	d 5 cm is rotated abo ormed is :	(S.S.C. 2000)
			(c) 16π cm ³	
90.		_	s 10 m and its height	
	(a) 30π m ²	(b) 40π m ²	(c) 60π m ²	(d) 80π m ²
	If a right circular coits curved surface it		nas a volume of 1232	cm ³ , then the area of (S.S.C. 2003)
	(a) 154 cm ²	(b) 550 cm ²	(e) 704 cm ²	(d) 1254 cm ²

4. When B runs 25 m, A runs 45 m.

When B runs 1000 m, A runs $\left(\frac{45}{2} \times \frac{1}{25} \times 1000\right)$ m = 900 m.

- ... B beats A by 100 m.
- To reach the winning post A will have to cover a distance of (500 140) m, i.e., 360 m.
 While A covers 3 m, B covers 4 m.

While A covers 360 m, B covers $\left(\frac{4}{3} \times 360\right)$ m = 480 m.

Thus, when A reaches the winning post, B covers 480 m and therefore remains 20 m behind.

- : A wins by 20 m.
- 6. Ratio of the speeds of A and B = $\frac{5}{3}$: 1 = 5: 3. Although 01. O area not B

Thus, in a race of 5 m, A gains 2 m over B.

2 m are gained by A in a race of 5 m.

80 m will be gained by A in a race of $\left(\frac{5}{2} \times 80\right)$ m = 200 m.

- .. Winning post is 200 m away from the starting point.
- 7. A : B = 100 : 75 and B : C = 100 : 96.

$$\therefore \quad A \, : \, C \, = \left(\frac{A}{B} \times \frac{B}{C} \right) = \left(\frac{100}{75} \times \frac{100}{96} \right) = \, \frac{100}{72} \, = \, 100 \, : \, 72.$$

- : A beats C by (100 72) m = 28 m.
- 8. A : B = 100 : 90 and A : C = 100 : 72.

B:
$$C = \frac{B}{A} \times \frac{A}{C} = \frac{90}{100} \times \frac{100}{72} = \frac{90}{72}$$
.

When B runs 90 m, C runs 72 m.

When B runs 100 m, C runs $\left(\frac{72}{90} \times 100\right)$ m = 80 m.

- : B can give C 20 m.
- 9. A : B = 100 : 90 and A : C = 100 : 87.

$$\frac{B}{C} = \frac{B}{A} \times \frac{A}{C} = \frac{90}{100} \times \frac{100}{87} = \frac{30}{29}$$

When B runs 30 m, C runs 29 m.

When B runs 180 m, C runs $\left(\frac{29}{30} \times 180\right)$ m = 174 m.

- .. B beats C by (180 174) m = 6 m.
- 10. A : B = 200 : 169 and A : C = 200 : 182.

$$\frac{C}{B} = \left(\frac{C}{A} \times \frac{A}{B}\right) = \left(\frac{182}{200} \times \frac{200}{169}\right) = 182 : 169.$$

When C covers 182 m, B covers 169 m.

When C covers 350 m, B covers $\left(\frac{169}{182} \times 350\right)$ m = 325 m.

11. A's speed = $\left(5 \times \frac{5}{18}\right)$ m/sec = $\frac{25}{18}$ m/sec.

92.		mountain is :		
	(a) 2.2 km	(b) 2.4 km		(d) 3.11 km
93.		base of a right circular		
		(b) 10010 cm ²		
94.		circular cone having b		
	(a) 823400 cm ³	(b) 824000 cm ³	(c) 840000 cm ³	(d) 862400 cm ³
95.	The radius and he 96π cm ³ , what is i	ight of a right circular ts slant height ?		(C.B.I. 1997
h rings	(a) 8 cm	(b) 9 cm	(e) 10 cm	(d) 12 cm
96.	The length of canv	as 1.1 m wide required 5 sq. m is :	to build a conical te	nt of height 14 m and
	(a) 490 m	(b) 525 m	(c) 665 m	(d) 860 m
97.		base and the height of		are doubled, then its
	(a) 2 times	(b) 3 times	(c) 4 times	(d) 8 times
98.	If both the radius a	and height of a right cir	cular cone are increas	
		(b) 40%		(d) 72.8%
99.		ight circular cone is in then the volume of th	-	the radius of the base (S.S.C. 2000
	(a) remains unalte	ered	(b) decreases by	25%
	(c) increases by 25	5%	(d) increases by	50%
100.		one be doubled and rad ne given cone to that o		
	(a) 1:2	(b) 2:1	(c) 1:8	(d) 8:1
101.	Two cones have the volumes is:	eir heights in the ration		
	(a) 1:1	(b) 1; 3	(c) 3:1	(d) 2:3
102.	The radii of two co	nes are in the ratio 2	: 1, their volumes are	equal. Find the ratio (C.B.I. 1998)
	(a) 1:8	(b) 1:4	(c) 2:1	(d) 4:1
103.	If the volumes of t ratio of 4:5, then	wo cones are in the ratio of their heigh	atio of 1 : 4 and their	diameters are in the
		(b) 5:4		
104.	The volume of the	largest right circular	cone that can be cut	out of a cube of edge
	(a) 13.6 cm ³	(b) 89.8 cm ³	(c) 121 cm ³	(d) 147.68 cm ³
105.	A cone of height 7 c	em and base radius 3 cr cm. The percentage of	n is carved from a rect	tangular block of wood
		(b) 46%		(d) 66%
106.	A right circular cor If the radius of the	ne and a right circular base and the height a of the cylinder to that	cylinder have equal t are in the ratio 5 : 12	ease and equal height then the ratio of the
	(a) 3 : 1	(b) 13:9	(c) 17:9	
	dead on the	THE RESERVE	Tak we have	2 mm 2 m 2 m 1 mm

107	. A cylinder with height 6 cm. The	base radius of 8 cm and radius of the cone will	i height of 2 cm is me	lted to form a cone of (R.R.B. 2003)
	(a) 4 cm	(b) 5 cm	(c) 6 cm	(A) 0
108	 A right cylindrica and height as th 	l vessel is full of water. I ose of the right cylinde	low many right cones h	pring the same as Jan-
	(a) 2	(b) 3	(c) 4	(d) 8
109	. A solid metallic c	ylinder of base radius 3	cm and beight 5 am is	multad to from a dis-
	each of height 1 (a) 450	cm and base radius 1 1 (b) 1350	mm. The number of co	nes 15 ;
		(D) 1330	(c) 4500	(d) 13500
110	is 40 cm and dep	he rate of 10 metres pe ng will it take to fill up hth 24 cm ?	a conical vessel whose	diameter at the base
	(a) 48 min. 15 se	c. (b) 51 min. 12 sec	c. (c) 52 min. 1 sec.	(d) 55 min
	block of radius 1 formed is :	2 cm and height 5 cm.	and height 18 cm is m The total lateral suri (Hotel	ounted with a conical face of the solid thus Management, 1998)
	(a) 528 cm ²	(b) $1357\frac{5}{7}$ cm ²	(c) 1848 cm ²	(d) None of these
112.	Consider the volu	mes of the following :	o Had show stress to ac-	ivil Services 2002)
	1 ansaran bahoor	a rengen o em, presqui	5 CIU And height 4 cm	n
2.	A cube of each sig	le 4 cm		
3.	A cylinder of radi	us 3 cm and length 3 c s 3 cm	m	
4.	A sphere of radiu	s 3 cm		
	The volumes of the (a) 1, 2, 3, 4	ese in the decreasing o	rder is :	
113	The volume of a c	(b) 1, 3, 2, 4 phere is 4851 cu. cm. I	(c) 4, 2, 3, 1	(d) 4, 3, 2, 1
	(a) 1386 cm ²	(b) 1625 cm ²	ts curved surface area (c) 1716 cm ²	(d) 3087 cm ²
114.	THE CHIVER SHIME	e area of a sphere is hi	544 sq. cm. Its volume	10.1
	(a) 22176 cm	(b) 33951 cm ³	(c) 38808 cm ³	(d) 42204 am3
115.	The volume of a s	phere of radius r is obt	ained by multiplying	its surface area by :
	(a) 3	$(b) \frac{r}{3}$	(c) 4r	(d) 3r
116.	If the volume of a s	phere is divided by its s	surface area, the result	is 27 cm. The radius
	(a) 9 cm	(b) 36 cm	CANADA STATE	(R.R.B. 2003)
117.	Spheres A and B ha	we their radii 40 cm and	(c) 54 cm	(d) 81 cm
	area of A to the st	iriace area of B is :		(C C C 0000)
110	(a) 1 : 4	(b) 1:16	(c) 4:1	(d) 16:1
110.	of the new anhance	phere is 2464 cm². If it	s radius be doubled, th	en the surface area
	(a) 4928 cm ²	(b) 9856 cm ²	(c) 19712 cm ²	(d) Data insufficient
119.	If the radius of a	sphere is doubled, how	many times does its v	volume become ?
	(a) 2 times	(b) 4 times	(c) 6 times	(d) 8 times
120.	If the radius of a 352 cm ² . The radiu	sphere is increased by as of the sphere before	2 cm, then its surfac	e area increases by
	(a) 3 cm	(b) 4 cm	(c) 5 cm	(C.B.I. 2003)
121.	ii the measured val	ue of the radius is 1.5%	larger, the percentage	error (correct to one
	(a) 2.1	e in calculating the vol	ume of a sphere is :	(C.B.I. 1997)
	1	(b) 3.2	(c) 4.6	(d) 5.4

	7.			
122.	The volumes of tw	o spheres are in the ra	tio of 64 : 27. The ratio	of their surface areas (R.R.B. 2002)
	(a) 1:2	(b) 2:3	(c) 9:16	(d) 16:9
123.		as of two spheres are	in the ratio of 4 : 25, t	hen the ratio of their
	(a) 4:25	(b) 25:4	(c) 125 : 8	(d) 8: 125
124.	If three metallic s sphere, the diame	eter of the new sphere	3 cms and 10 cms are m will be :	(D.M.R.C. 2003)
500	(a) 12 cms	(b) 24 cms	(c) 30 cms	(d) 36 cms
125.			s melted and recast int il balls, thus obtained,	is:
	(a) 16	(b) 48	(c) 64	(d) 82
126.		er of two of these are	ter is melted and recas 1.5 cm and 2 cm respo	
	(a) 2.5 cm	(b) 2.66 cm	(e) 3 cm	(d) 3.5 cm
127.	If a solid sphere of	f radius 10 cm is mould f each such ball is :	led into 8 spherical solid	l balls of equal radius,
	(a) 1.25 cm	(b) 2.5 cm	(c) 3.75 cm	(d) 5 cm
128.	A hollow spherica	d metallic ball has an	external diameter 6 cr	The second secon
	The volume of me	etal used in the ball is	1:	(S.S.C. 2004)
	(a) $37\frac{2}{3}$ cm ³	(b) $40\frac{2}{3}$ cm ³	(c) $41\frac{2}{3}$ cm ³	(d) $47\frac{2}{3}$ cm ³
129.	A solid piece of iro of the sphere is :	on of dimensions 49 × 33	3 × 24 cm is moulded int (Hotel	o a sphere. The radius Management, 1999)
	(a) 21 cm	(b) 28 cm	(c) 35 cm	(d) None of these
130.	How many bullets bullet being 2 cm		ube of lead whose edge	measures 22 cm, each
	(a) 1347	(b) 2541	(c) 2662	(d) 5324
131.	How many lead sh 9 cm × 11 cm × 1		eter can be made from	a cuboid of dimensions
	(a) 7200	(b) 8400	(c) 72000	(d) 84000
132.	A sphere and a cu	oe is :	areas. The ratio of the	
	(a) √π:√6	(b) √2:√π	(c) √π:√3	(d) √6:√π
133.	The ratio of the v	olume of a cube to that	of a sphere which will	fit inside the cube is:
		(b) 4:3π		(d) 2:π
134.	The surface area cylinder whose he	of a sphere is same a eight and diameter are	s the curved surface as 12 cm each. The radi	rea of a right circular us of the sphere is :
	(a) 3 cm	(b) 4 cm	(c) 6 cm	(d) 12 cm (S.S.C. 2002)
135.	The diameter of t	the iron ball used for t	he shot-put game is 14	cm. It is melted and
	because on the same and a second	der of height $2\frac{1}{3}$ cm is	made. What will be th	
	of the cylinder?		made in calculating the	(S.S.C. 2004)
	(a) 14 cm	(b) 14/3 cm	(c) 28 cm	(d) $\frac{28}{3}$ em

136.	The volume of to	he greatest sphere that I cm and height 5 cm	t can be cut off from a	cylindrical log of wood (C.B.I. 1997)
	(a) $\frac{4}{3}\pi$	(b) $\frac{10}{3}\pi$	(c) 5π	(d) $\frac{20}{3}$ π
137.	base radius 3 c	rical bullets can be ma m, each bullet being 5	mm in diameter ?	
		(b) 6480		
138.	A cylindrical roc spherical balls o is:	of iron whose height is each of half the radius	eight times its radius of the cylinder. The nu	is melted and cast into mber of spherical balls
	(a) 12	(b) 16	(c) 24	(d) 48
139		a sphere is 8 cm. It i		
	3 mm. The leng	th of the wine in .		
	(a) 36.9 m	(b) 37.9 m	(c) 38.9 m	(d) 39.9 m
140.	lowered into the	ssel of radius 4 cm con water until it is compl	tains water. A solid sp etely immersed. The w	here of radius 3 cm is
	(a) $\frac{2}{9}$ cm	(b) $\frac{4}{9}$ em	(c) 9/4 cm	(d) 9 cm
141.		e same size are made fr t. The diameter of each		
	(a) √3 cm	(b) 2 cm	(c) 3 cm	(d) 4 cm
142.	A cylindrical tul iron ball is drop radius of the ba	of radius 12 cm centa ped into the tub and the ill is:	ins water upto a depth as the level of water is	n of 20 cm. A spherical raised by 6.75 cm. The
	(a) 4.5 cm	(b) 6 cm	(c) 7.25 cm	(d) 9 cm
143.	diameter of the	spherical ball of diamet base as 12 cm. The he	ight of the cone is :	(C.B.I. 2003)
2021252	(a) 2 cm	(b) 3 cm	(c) 4 cm	(d) 6 cm
144.	solid sphere of r	9 cm with diameter of adius 9 cm. The percen	ntage of the wood was	ted is ? (S.S.C. 2000)
	(a) 25%	(b) 25π%	(c) 50%	(d) 75%
145.	of radius 2 cm e	of radius 12 cm and he each. How many sphere	s are there?	07 (6) 48.
12.2	(a) 108	107 120	10/ 199	(d) 180
	melted into a co	of internal and extern ne of base diameter 8 o	m. The height of the c	one is : (R.R.B. 2002)
		(b) 14 cm		
	diameter and th	e the volumes of a cylin- e same height?		
		(b) 2:3:1		
	(a) 308 cm ²	e area of a solid hemis (b) 462 cm ²	(c) 1232 cm ²	
149.	Volume of a her	(b) 17.5 cm	m. Its radius is :	
150.	The capacities o	f two hemispherical ve- surfaces of the vessels	ssels are 6.4 litres and	21.6 litres. The areas
	(a) √2 : √3	(b) 2;3	(e) 4:9	(d) 16:81

151.	A hemispherical bowl is filled to the brim with a beverage. The content	ts of the bowl
	are transferred into a cylindrical vessel whose radius is 50% more than	n its height. It
	the diameter is same for both the bowl and the cylinder, the volume of	the beverage
		(I.A.S. 1999)

(a)
$$66\frac{2}{3}$$

(b)
$$78\frac{1}{2}\%$$

(d) More than 100% (i.e., some liquid will be left in the bowl).

152. A metallic hemisphere is melted and recast in the shape of a cone with the same base radius (R) as that of the hemisphere. If H is the height of the cone, then:

(b)
$$H = 3R$$

(e)
$$H = \sqrt{3}R$$

(d)
$$H = \frac{2}{3}R$$

(S.S.C. 1999)

153. A hemisphere of lead of radius 6 cm is cast into a right circular cone of height 75 cm. The radius of the base of the cone is:

154. A hemisphere and a cone have equal bases. If their heights are also equal, then the ratio of their curved surfaces will be: (S.S.C. 2002)

155. A sphere of maximum volume is cut out from a solid hemisphere of radius r. The ratio of the volume of the hemisphere to that of the cut out sphere is:

153. (c) 154. (d) 155. (b)

ANSWERS

1. (d)	2. (c)	3. (a)	4. (b)	5. (b)	6. (b)	7. (b)	8. (b)	
9. (a)	10. (d)	11. (b)	12. (c)	13. (b)	14. (c)	15. (c)	16. (b)	
17. (c)	18. (a)	19. (c)	20. (c)	21. (b)	22. (b)	23. (b)	24. (b)	
25. (a)	26. (a)	27. (c)	28. (c)	29. (b)	30. (a)	31. (d)	32. (c)	
33. (d)	34. (d)	35. (d)	36. (b)	37. (d)	38. (d)	39. (d)	40. (c)	
41. (d)	42. (b)	43. (c)	44. (b)	45. (b)	46. (a)	47. (b)	48. (b)	
49. (c)	50. (b)	51. (c)	52. (b)	53. (c)	54. (d)	55. (d)	56. (d)	
57. (e)	58. (c)	59. (b)	60. (b)	61. (a)	62. (b)	63. (c)	64. (d)	
65. (b)	66. (b)	67. (b)	68. (b)	69. (a)	70. (b)	71. (c)	72. (d)	
73. (c)	74. (d)	75. (b)	76. (b)	77. (c)	78. (d)	79. (d)	80. (a)	
81. (d)	82. (b)	83. (c)	84. (b)	85. (c)	86. (c)	87. (d)	88. (c)	
89. (a)	90. (c)	91. (b)	92. (b)	93. (b)	94. (d)	95. (c)	96. (b)	
97. (d)	98. (d)	99. (b)	100. (a)	101. (c)	102. (b)	103. (d)	104. (b)	
105. (a)	106. (c)	107. (d)	108. (b)	109. (d)	110. (b)	111. (d)	112. (d)	
113. (a)	114. (c)	115. (b)	116. (d)	117. (d)	118. (b)	119. (d)	120. (d)	
121. (c)	122. (d)	123. (d)	124. (b)	125. (c)	126. (a)	127. (d)	128. (d)	
129. (a)	130. (b)	131. (d)	132. (d)	133. (c)	134. (a)	135. (c)	136. (a)	
137. (b)	138. (d)	139. (b)	140. (c)	141. (d)	142. (d)	143. (b)	144. (d)	
145. (a)	146. (b)	147. (c)	148. (b)	149. (c)	150. (c)	151. (c)	152. (a)	

solutions | Selection | Select

1. Capacity of the bank = Volume of the tank

$$= \left(\frac{8 \times 100 \times 6 \times 100 \times 2.5 \times 100}{1000}\right) \text{ litres} = 120000 \text{ litres}.$$

- Surface area = [2 (10 × 4 + 4 × 3 + 10 × 3)] cm² = (2 × 82) cm² = 164 cm².
- 3. Area of the wet surface = [2 (lb + bh + lh) lb] = 2 (bh + lh) + lb= $[2 (4 \times 1.25 + 6 \times 1.25) + 6 \times 4] m^2 = 49 m^2$
- 4. Volume of water displaced = (3 × 2 × 0.01) m3 = 0.06 m3.
 - Mass of man = Volume of water displaced × Density of water = (0.06 × 1000) kg = 60 kg.
- Volume = (2.6 × 100 × 100 × 100) eu. em.

$$Depth = \frac{Volume}{Area of the base} = \left(\frac{2.6 \times 100 \times 100 \times 100}{6500}\right) cm = 400 cm = 4 m.$$

- 6. Let length = x cm. Then, $x \times 28 \times 5 \times \frac{25}{1000} = 112$
 - $x = \left(112 \times \frac{1000}{25} \times \frac{1}{28} \times \frac{1}{5}\right) \text{ cm} = 32 \text{ cm}.$
- 7. Volume of gold = $\left(\frac{1}{2} \times 100 \times 100 \times 100\right) \text{cm}^3$.

Area of sheet = $10000 \text{ m}^2 = (10000 \times 100 \times 100) \text{ cm}^2$

- $\therefore \quad \text{Thickness of the sheet} = \left(\frac{1 \times 100 \times 100 \times 100}{2 \times 10000 \times 100 \times 100}\right) \text{cm} = 0.005 \text{ cm}.$
- 8. Area = $(1.5 \times 10000) \text{ m}^2 = 15000 \text{ m}^2$.

Depth =
$$\frac{5}{100}$$
 m = $\frac{1}{20}$ m.

- $\therefore \text{ Volume} = (\text{Area} \times \text{Depth}) = \left(15000 \times \frac{1}{20}\right) \text{m}^3 = 750 \text{ m}^3.$
- 9. Let the width of the wall be x metres.

Then, Height = (6x) metres and Length = (42x) metres.

$$42x \times x \times 6x = 16128 \iff x^3 = \left(\frac{16128}{42 \times 6}\right) = 64 \iff x = 4.$$

10. Let the dimensions be 3x, 2x and x respectively. Then,

$$3x \times 2x \times x = 10368 \iff x^3 = \left(\frac{10368}{6}\right) = 1728 \iff x = 12.$$

So, the dimensions of the block are 35 dm, 24 dm, and 12 dm.

Surface area =
$$[2 (36 \times 24 + 24 \times 12 + 36 \times 12)] \text{ dm}^2$$

= $[2 \times 144 (6 + 2 + 3)] \text{ dm}^2 = 3168 \text{ dm}^2$.

- \therefore Cost of polishing = Rs. $\left(\frac{2 \times 3168}{100}\right)$ = Rs. 63.36.
- 11. Let the dimensions of the cuboid be x, 2x and 3x

Then, $2(x \times 2x + 2x \times 3x + x \times 3x) = 88$

$$\Rightarrow$$
 $2x^2 + 6x^2 + 3x^2 = 44 \Leftrightarrow 11x^2 = 44 \Leftrightarrow x^2 = 4 \Leftrightarrow x = 2.$

:. Volume of the cuboid = (2 × 4 × 6) cm³ = 48 cm³.

12. Required length =
$$\sqrt{8^2 + 6^2 + 2^2}$$
 cm = $\sqrt{104}$ cm = $2\sqrt{26}$ cm.

13. Required length =
$$\sqrt{(16)^2 + (12)^2 + \left(\frac{32}{3}\right)^2}$$
 m = $\sqrt{256 + 144 + \frac{1024}{9}}$ m = $\sqrt{\frac{4624}{9}}$ m = $\frac{68}{3}$ m = $22\frac{2}{3}$ m.

14. Number of bricks =
$$\frac{\text{Volume of the wall}}{\text{Volume of 1 brick}} = \left(\frac{800 \times 600 \times 22.5}{25 \times 11.25 \times 6}\right) = 6400.$$

15. Volume of the bricks = 95% of volume of wall =
$$\left(\frac{95}{100} \times 600 \times 500 \times 50\right) \text{cm}^3$$
.
Volume of 1 brick = $(25 \times 12.5 \times 7.5) \text{ cm}^3$.

:. Number of bricks =
$$\left(\frac{95}{100} \times \frac{600 \times 500 \times 50}{25 \times 125 \times 7.5}\right) = 6080$$
.

16. Total volume of water displaced =
$$(4 \times 50)$$
 m³ = 200 m³.

$$\therefore \text{ Rise in water level} = \left(\frac{200}{40 \times 20}\right) m = 0.25 \text{ m} = 25 \text{ cm}.$$

17. Volume of earth dug out =
$$\left(4 \times \frac{5}{2} \times \frac{3}{2}\right)$$
 m³ = 15 m³.

Area over which earth is spread =
$$\left(31 \times 10 - 4 \times \frac{5}{2}\right)$$
 m² = 300 m².

$$\therefore$$
 Rise in level = $\left(\frac{\text{Volume}}{\text{Area}}\right) = \left(\frac{15}{300} \times 100\right) \text{cm} = 5 \text{ cm}.$

18. Length of water column flown in 1 min. =
$$\left(\frac{3.5 \times 1000}{60}\right)$$
 m = $\frac{175}{3}$ m.

$$\therefore$$
 Volume flown per minute = $\left(\frac{175}{3} \times 36 \times \frac{3}{2}\right) \text{m}^3 = 3150 \text{ m}^3$.

19. Length of water column flown in 1 min. =
$$\left(\frac{10 \times 1000}{60}\right)$$
 m = $\frac{500}{3}$ m.

Volume flown per minute =
$$\left(\frac{500}{3} \times \frac{40}{100 \times 100}\right) \text{m}^3 = \frac{2}{3} \text{m}^3$$
.

Volume flown in half an hour =
$$\left(\frac{2}{3} \times 30\right)$$
 m³ = 20 m³.

$$\therefore \quad \text{Rise in water level} = \left(\frac{20}{40 \times 80}\right) m = \left(\frac{1}{160} \times 100\right) cm = \frac{5}{8} cm.$$

20.
$$2(15+12) \times h = 2(15 \times 12)$$
 or $h = \frac{180}{27}$ m = $\frac{20}{3}$ m.

.. Volume =
$$\left(15 \times 12 \times \frac{20}{3}\right)$$
 m³ = 1200 m³.

21.
$$(l+b+h) = 19$$
 and $\sqrt{l^2 + b^2 + h^2} = 5\sqrt{5}$ and so $(l^2 + b^2 + h^2) = 125$.
Now, $(l+b+h)^2 = 19^2 \implies (l^2 + b^2 + h^2) + 2(lb+bh+lh) = 361$
 $\implies 2(lb+bh+lh) = (361-125) = 236$.

22. Volume =
$$\left[12 \times 9 \times \left(\frac{1+4}{2}\right)\right]$$
 m³ = $(12 \times 9 \times 2.5)$ m³ = 270 m³.

24. Internal length =
$$(146 - 6)$$
 cm = 140 cm.

Internal breadth = (116 - 6) cm = 110 cm.

Internal depth = (83 - 3) cm = 80 cm.

Area of inner surface = $[2(I + b) \times h] + Ib$

$$\therefore \text{ Cost of painting} = \text{Rs.} \left(\frac{1}{2} \times \frac{1}{100} \times 55400 \right) = \text{Rs. 277.}$$

 $[(330 - 10) \times (260 - 10) \times (110 - x)] = 8000 \times 1000$

$$\Leftrightarrow$$
 320 × 250 × (110 - x) = 8000 × 1000 \Leftrightarrow (110 - x) = $\frac{8000 \times 1000}{320 \times 250}$ = 100

$$\Leftrightarrow$$
 $x = 10$ cm = 1 dm.

26. Let the dimensions of the bigger cuboid be x, y and z.

Then, Volume of the bigger cuboid = xyz.

Volume of the miniature cuboid =
$$\left(\frac{1}{4}x\right)\left(\frac{1}{4}y\right)\left(\frac{1}{4}z\right) = \frac{1}{64}xyz$$
.

... Weight of the miniature cuboid =
$$\left(\frac{1}{64} \times 16\right) \text{kg} = 0.25 \text{ kg}$$
.

Volume =
$$lbh = \sqrt{(lbh)^2} = \sqrt{lb \times bh \times lh} = \sqrt{120 \times 72 \times 60} = 720 \text{ cm}^3$$
.

Then, $24x^3 = (1bh)^2 = 9000 \times 9000 \implies x^3 = 375 \times 9000 \implies x = 150$.

So, lb = 300, bh = 450, lh = 600 and lbh = 9000.

$$h = \frac{9000}{300} = 30, I = \frac{9000}{450} = 20 \text{ and } b = \frac{9000}{600} = 15.$$

Hence, shortest side = 15 cm.

30. Edge of the cube =
$$\left(\frac{20}{4}\right)$$
 cm = 5 cm.

31. Surface area =
$$\left[6 \times \left(\frac{1}{2}\right)^2\right] \text{cm}^2 = \frac{3}{2} \text{cm}^2$$
.

32. Surface area of the cube =
$$(6 \times 8^2)$$
 sq. ft. = 384 sq. ft.

Quantity of paint required =
$$\left(\frac{384}{16}\right)$$
 kg = 24 kg.

33. Volume of the cube =
$$(270 \times 100 \times 64)$$
 cm³.

Edge of the cube =
$$\sqrt{270 \times 100 \times 64}$$
 cm = $(3 \times 10 \times 4)$ cm = 120 cm.

34. Surface area =
$$\left(\frac{34398}{13}\right)$$
 = 2646 cm².

∴
$$6a^2 = 2646$$
 $\Rightarrow a^2 = 441$ $\Rightarrow a = 21$.

So, Volume = $(21 \times 21 \times 21)$ cm³ = 9261 cm³.

35.
$$a^3 = 729 \implies a = 9$$
.

36. Required length = Diagonal =
$$\sqrt{3} \alpha = (\sqrt{3} \times \sqrt{3}) \text{ m} = 3 \text{ m}$$
.

37.
$$\sqrt{3} a = 4\sqrt{3} \implies a = 4$$
.

38.
$$6a^2 = 600 \implies a^2 = 100 \implies a = 10$$
.

39.
$$a^3 = 6a^2 \implies a = 6$$
.

40. Number of cubes =
$$\left(\frac{100 \times 100 \times 100}{10 \times 10 \times 10}\right) = 1000$$
.

41. Number of blocks =
$$\left(\frac{160 \times 100 \times 60}{20 \times 20 \times 20}\right)$$
 = 120.

42. Number of cubes =
$$\left(\frac{18 \times 18 \times 18}{3 \times 3 \times 3}\right)$$
 = 216.

43. Volume of block =
$$(6 \times 9 \times 12)$$
 cm³ = 648 cm³.
Side of largest cube = H.C.F. of 6 cm, 9 cm, 12 cm = 3 cm.
Volume of this cube = $(3 \times 3 \times 3) = 27$ cm³.

$$\therefore$$
 Number of cubes = $\left(\frac{648}{27}\right)$ = 24.

44. Side of smallest cube = L.C.M. of 5 cm, 10 cm, 20 cm = 20 cm. Volume of the cube = $(20 \times 20 \times 20)$ cm³ = 8000 cm³. Volume of the block = $(5 \times 10 \times 20)$ cm³ = 1000 cm³.

$$\therefore \text{ Number of blocks} = \left(\frac{8000}{1000}\right) = 8.$$

 Let the sides of the sheet be x and 5x. Then, Volume of the sheet = Volume of the cube

$$\Rightarrow x \times 5x \times \frac{1}{2} = 10 \times 10 \times 10 \Rightarrow 5x^2 = 2000 \Rightarrow x^2 = 400 \Rightarrow x = 20.$$

$$\therefore \text{ The sides are 20 cm and 100 cm.}$$

.. The sides are 20 cm and 100 cm.

46. Volume of the new cube = $(6^3 + 8^3 + 10^3)$ cm³ = 1728 cm³. Let the edge of the new cube be a cm.

$$a^3 = 1728 \implies a = 12.$$

47. The new solid formed is a cuboid of length 25 cm, breadth 5 cm and height 5 cm. : Volume = $(25 \times 5 \times 5)$ cm³ = 625 cm³.

48. Required ratio =
$$\frac{6 \times 1 \times 1}{6 \times 5 \times 5} = \frac{1}{25} = 1:25$$

49. Volume of the large cube = $(3^3 + 4^3 + 5^3)$ cm³ = 216 cm³. Let the edge of the large cube be a. So, $a^3 = 216 \Rightarrow a = 6$ cm.

:. Required ratio =
$$\frac{6 \times (3^2 + 4^2 + 5^2)}{6 \times 6^2} = \frac{50}{36} = 25:18$$
.

50. Let the sides of the three cubes be 3x, 4x and 5x. and 5x. Let the sides of the three cubes $3x^3 + (4x)^3 + (5x)^3 = 216x^3$. Then, Volume of the new cube $= [(3x)^3 + (4x)^3 + (5x)^3] = 216x^3$.

Diagonal of the new cube = $6\sqrt{3} x$.

$$\therefore 6\sqrt{3} \ x = 12\sqrt{3} \implies x = 2.$$

So, the sides of the cubes are 6 cm, 8 cm and 10 cm.

51. Let their edges be a and b. Then,

$$\frac{a^3}{b^3} = \frac{27}{1} \iff \left(\frac{a}{b}\right)^3 = \left(\frac{3}{1}\right)^3 \iff \frac{a}{b} = \frac{3}{1} \iff a:b=3:1.$$

52. Let their edges be a and b. Then,

$$\frac{a^3}{b^3} = \frac{8}{27} \iff \left(\frac{a}{b}\right)^3 = \left(\frac{2}{3}\right)^3 \iff \frac{a}{b} = \frac{2}{3} \iff \frac{a^2}{b^2} = \frac{4}{9} \iff \frac{6a^2}{6b^2} = \frac{4}{9}.$$

53. Let their edges be a and b. Then.

$$\frac{a^3}{b^3} = \frac{1}{27} \iff \left(\frac{a}{b}\right)^3 = \left(\frac{1}{3}\right)^3 \iff \frac{a}{b} = \frac{1}{3} \iff \frac{a^2}{b^2} = \frac{1}{9}.$$

Let original edge = a. Then, volume = a³.

New edge = 2a. So, new volume = $(2a)^3 = 8a^3$.

- .. Volume becomes 8 times.
- Let original edge = a. Then, surface area = 6a².

New edge =
$$\frac{125}{100} a = \frac{5a}{4}$$
.

New surface area = $6 \times \left(\frac{5\alpha}{4}\right)^2 = \frac{75\alpha^2}{8}$.

Increase in surface area = $\left(\frac{75a^2}{8} - 6a^2\right) = \frac{27a^2}{8}$.

- :. Increase % = $\left[\frac{27a^2}{8} \times \frac{1}{6a^2} \times 100\right]$ % = 56.25%.
- 56. Volume = $\pi r^2 h = \left(\frac{22}{7} \times 1 \times 1 \times 14\right) m^3 = 44 m^3$.
- Volume of the tank = 246.4 litres = 246400 cm³. Let the radius of the base be r cm. Then,

$$\left(\frac{22}{7} \times r^2 \times 400\right) = 246400 \iff r^2 = \left(\frac{246400 \times 7}{22 \times 400}\right) = 196 \iff r = 14.$$

- :. Diameter of the base = 2r = 28 cm.
- 58. $2\pi r = 66 \implies r = \left(66 \times \frac{1}{2} \times \frac{7}{22}\right) = \frac{21}{2}$ cm. 1 and the first the result of the second of the

$$\frac{2\pi rh}{2\pi r} = \left(\frac{2640}{66}\right) \implies h = 40 \text{ cm}.$$

:. Volume = $\left(\frac{22}{7} \times \frac{21}{2} \times \frac{21}{2} \times 40\right) \text{ cm}^3 = 13860 \text{ cm}^3$.

59. Let the radius and height be r cm each. I see the sent set to sold and to let the

Then,
$$\frac{22}{7} \times r^2 \times r = \frac{176}{7} \implies r^3 = \left(\frac{176}{7} \times \frac{7}{22}\right) = 8 \implies r = 2$$

60.
$$\frac{2\pi rh}{h} = \frac{704}{14} \implies 2\pi r = \frac{704}{14}$$
.

$$\therefore \quad r = \left(\frac{704}{14} \times \frac{1}{2} \times \frac{7}{22}\right) = 8 \text{ cm}.$$

:. Volume =
$$\left(\frac{22}{7} \times 8 \times 8 \times 14\right) \text{ cm}^3 = 2816 \text{ cm}^3$$
.

61. Total surface area =
$$2\pi r (h + r) = \left[2 \times \frac{22}{7} \times \frac{35}{100} \times (1.25 + 0.35)\right] \text{m}^2$$

= $\left(2 \times \frac{22}{7} \times \frac{35}{100} \times \frac{16}{10}\right) \text{m}^2 = 3.52 \text{ m}^2$.

.. Cost of the material = Rs. (3.52 × 80) = Rs. 281.60.

62. Curved surface area =
$$2\pi rh = (\pi r^2 h) \cdot \frac{2}{r} = \left(\text{Volume} \times \frac{2}{r}\right)$$
.

63.
$$\frac{\text{Total surface area}}{\text{Lateral surface area}} = \frac{2\pi rh + 2\pi r^2}{2\pi rh} = \frac{(h+r)}{h} = \frac{80}{60} = \frac{4}{3}.$$

64. Difference in capacities =
$$\left(8 \times 8 \times 14 - \frac{22}{7} \times 4 \times 4 \times 14\right) \text{cm}^3 = 192 \text{ cm}^3$$
.

$$\frac{22}{7} \times (2x)^2 \times 3x = 12936 \iff x^3 = \left(12936 \times \frac{7}{22} \times \frac{1}{12}\right) = 343 = 7^3$$

$$\therefore$$
 x = 7. So, radius = 14 cm and height = 21 cm.

.. Total surface area =
$$2 \times \frac{22}{7} \times 14 \times (21 + 14) = \left(2 \times \frac{22}{7} \times 14 \times 35\right) \text{cm}^2 = 3080 \text{ cm}^2$$
.

66. It is given that
$$r = \frac{1}{2}h$$
 and $2\pi rh + \pi r^2 = 616 \text{ m}^2$

$$\therefore 2\pi \times \frac{1}{2}h \times h + \pi \times \frac{1}{4}h^2 = 616$$

$$\Rightarrow \quad \frac{5}{4} \times \frac{22}{7} \times h^2 = 616 \quad \Rightarrow \quad h^2 = \left(616 \times \frac{28}{110}\right) = \frac{28 \times 28}{5}.$$

$$\begin{array}{ll} \therefore & \text{Volume} = \pi r^2 h = \frac{22}{7} \times \frac{1}{4} \, h^2 \times h = \frac{22}{7} \times \frac{1}{4} \times \frac{28 \times 28}{5} \times \frac{28}{\sqrt{5}} \, \, \text{cm}^3 \\ & = \left(\frac{22 \times 28 \times 28}{25} \times \sqrt{5} \right) \, \text{cm}^3 = \left(\frac{22 \times 28 \times 28 \times 223}{25 \times 1000} \right) \, \text{litres} = 1.53 \, \, \text{litre}. \end{array}$$

67. (h + r) = 37 and $2\pi r (h + r) = 1628$.

$$\therefore 2\pi r \times 37 = 1628 \text{ or } r = \left(\frac{1628}{2 \times 37} \times \frac{7}{22}\right) = 7.$$

So, r = 7 m and h = 30 m.

: Volume =
$$\left(\frac{22}{7} \times 7 \times 7 \times 30\right)$$
 m³ = 4620 m³.

68.
$$\frac{\pi r^2 h}{2\pi r h} = \frac{924}{264}$$
 $\Rightarrow r = \left(\frac{924}{264} \times 2\right) = 7 \text{ m.}$

And,
$$2\pi rh = 264 \implies h = \left(264 \times \frac{7}{22} \times \frac{1}{2} \times \frac{1}{7}\right) = 6 \text{ m}.$$

$$\therefore \text{ Required ratio} = \frac{2r}{h} = \frac{14}{6} = 7:3.$$

69.
$$V = \pi r^2 h$$
 and $S = 2\pi r h + 2\pi r^2$

$$\Rightarrow$$
 S = $2\pi r (h + r)$, where $h = \frac{V}{\pi r^2}$

$$\Rightarrow S = 2\pi r \left(\frac{V}{\pi r^2} + r \right) = \frac{2V}{r} + 2\pi r^2 \Rightarrow \frac{dS}{dr} = \frac{-2V}{r^2} + 4\pi r \text{ and } \frac{d^2S}{dr^2} = \left(\frac{4V}{r^3} + 4\pi \right) > 0$$

$$\therefore S \text{ is minimum when } \frac{dS}{dr} = 0$$

$$\Leftrightarrow \frac{-2V}{r^2} + 4\pi r = 0 \Leftrightarrow V = 2\pi r^3 \Leftrightarrow \pi r^2 h = 2\pi r^3 \Leftrightarrow h = 2r$$
.

70. Let original radius = R. Then, new radius = $\frac{R}{2}$.

$$\frac{\text{Volume of reduced cylinder}}{\text{Volume of original cylinder}} = \frac{\pi \times \left(\frac{R}{2}\right)^2 \times h}{\pi \times R^2 \times h} = \frac{1}{4}.$$

71. Let their radii be 2x, 3x and heights be 5y, 3y.

Ratio of their volumes =
$$\frac{\pi \times (2x)^2 \times 5y}{\pi \times (3x)^2 \times 3y} = \frac{20}{27}.$$

72. Let their heights be h and 2h and radii be r and R respectively. Then,

$$\pi r^2 h = \pi R^2 (2h) \implies \frac{r^2}{R^2} = \frac{2h}{h} = \frac{2}{1} \implies \frac{r}{R} - \frac{\sqrt{2}}{1} i.e. \sqrt{2}:1.$$

73. Let the height of X and Y be h, and their radii be r and 2r respectively. Then, Volume of X = πr²h and Volume of Y = π (2r)² h = 4πr²h.
New height of X = 2h.

So, new volume of
$$X = \pi r^2 (2h) = 2\pi r^2 h = \frac{1}{2} (4\pi r^2 h) = \frac{1}{2} \times (Volume of Y).$$

74. Let original radius = r and original length = h.

New radius = $\frac{r}{3}$ and let new length = H.

Then,
$$\pi r^2 h = \pi \left(\frac{r}{3}\right)^2 \times H$$
 or $H = 9h$.

75. Let the drop in the water level be h cm. Then,

$$\frac{22}{7} \times \frac{35}{2} \times \frac{35}{2} \times h = 11000 \iff h = \left(\frac{11000 \times 7 \times 4}{22 \times 35 \times 35}\right) \text{cm} = \frac{80}{7} \text{ cm} = 11\frac{3}{7} \text{ cm}.$$

76. Volume of earth dug out =
$$\left(\frac{22}{7} \times 7 \times 7 \times 10\right)$$
 m³ = 1540 m³.

Area of embankment = $\frac{22}{7} \times \left[(28)^2 - (7)^2\right] = \left(\frac{22}{7} \times 35 \times 21\right)$ m² = 2310 m².

Height of embankment = $\left(\frac{\text{Volume}}{\text{Area}}\right) = \left(\frac{1540}{2310}\right)$ m = $\frac{2}{3}$ m.

77. Volume of water flown in 1 sec. = $\left(\frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 200\right)$ cm³ = 7700 cm³. Volume of water flown in 10 min. = $(7700 \times 60 \times 10)$ cm³ = $\left(\frac{7700 \times 60 \times 10}{1000}\right)$ litres = 4620 litres.

78. Volume of one coin =
$$\left(\frac{22}{7} \times \frac{75}{100} \times \frac{75}{100} \times \frac{2}{10}\right) \text{ cm}^3 = \frac{99}{280} \text{ cm}^3$$
.
Volume of larger cylinder = $\left(\frac{22}{7} \times 3 \times 3 \times 8\right) \text{cm}^3$.

$$\therefore \quad \text{Number of coins} = \left(\frac{22 \times 9 \times 8}{7} \times \frac{280}{99}\right) = 640.$$

79. Let the radius of the vessel be R. Then, $\pi R^2 \times 15 = \pi \times (15)^2 \times 35 + \pi \times (10)^2 \times 15$ $\Leftrightarrow \pi R^2 \times 15 = 9375\pi \iff R^2 = 625 \iff R = 25 \text{ cm.}$

80. Let the length of the wire be h. Radius = $\frac{1}{2}$ mm = $\frac{1}{20}$ cm. Then,

$$\frac{22}{7} \times \frac{1}{20} \times \frac{1}{20} \times h = 66 \iff h = \left(\frac{66 \times 20 \times 20 \times 7}{22}\right) = 8400 \text{ cm} = 84 \text{ m}.$$

81. Circumference of the girth = 440 cm.

$$\therefore 2\pi R = 440 \implies R = \left(440 \times \frac{1}{2} \times \frac{7}{22}\right) = 70 \text{ cm}.$$

So, Outer radius = 70 cm. Inner radius = (70 - 4) cm = 66 cm.

Volume of iron = $\pi \left[(70)^2 - (66)^2 \right] \times 63 = \left(\frac{22}{7} \times 136 \times 4 \times 63 \right) \text{cm}^3 = 58752 \text{ cm}^3$

82. Internal radius = $\left(\frac{11.2}{2}\right)$ cm = 5.6 cm, External radius = (5.6 + 0.4) cm = 6 cm. Volume of metal = $\left\{\frac{22}{7} \times [(6)^2 - (5.6)^2] \times 21\right\}$ cm³ = (66 × 11.6 × 0.4) cm³ = 306.24 cm³.

External radius = 6 cm, Internal radius = (6 - 0.25) cm = 5.75 cm.
 Volume of material in hollow cylinder

$$= \left\{ \frac{22}{7} \times [(6)^2 - (5.75)^2] \times 15 \right\} \text{ cm}^3 = \left(\frac{22}{7} \times 11.75 \times 0.25 \times 15 \right) \text{ cm}^3$$

$$= \left(\frac{22}{7} \times \frac{1175}{100} \times \frac{25}{100} \times 15 \right) \text{ cm}^3 = \left(\frac{11 \times 705}{56} \right) \text{ cm}^3.$$

Let the length of solid cylinder be h. Then,

$$\frac{22}{7} \times 1 \times 1 \times h = \left(\frac{11 \times 705}{56}\right) \iff h = \left(\frac{11 \times 705}{56} \times \frac{7}{22}\right) \text{cm} = 44.0625 \text{ cm}.$$

84. External radius = 4 cm, Internal radius = 3 cm.

Volume of iron =
$$\left\{ \frac{22}{7} \times [(4)^2 - (3)^2] \times 21 \right\} \text{ cm}^3 = \left(\frac{22}{7} \times 7 \times 1 \times 21 \right) \text{ cm}^3 = 462 \text{ cm}^3.$$

.. Weight of iron = (462 × 8) gm = 3696 gm = 3.696 kg.

85. Let the internal radius of the cylinder be x. Then,

$$\frac{22}{7} \times r^2 \times 40 = \frac{616}{10} \iff r^2 = \left(\frac{616 \times 7}{10 \times 22 \times 40}\right) = 0.49 \iff r = 0.7.$$

So, internal radius = 0.7 cm = 7 mm.

: Thickness = (8 - 7) mm = 1 mm.

86. Volume of cone Volume of cylinder =
$$\frac{\frac{1}{3} \times \pi \times (3)^2 \times 5}{\pi \times (2)^2 \times 4} = \frac{45}{48} = \frac{15}{16}$$
.

87.
$$h = 15$$
 cm, $r = 8$ cm. So, $l = \sqrt{r^2 + h^2} = \sqrt{8^2 + (15)^2} = 17$ cm.

.. Curved surface area = $\pi rI = (\pi \times 8 \times 17)$ cm² = 136 π cm².

88.
$$h = 14$$
 cm, $r = 7$ cm. So, $l = \sqrt{(7)^2 + (14)^2} = \sqrt{245} = 7\sqrt{5}$ cm.

$$\therefore \text{ Total surface area} = \pi r l + \pi r^2 = \left(\frac{22}{7} \times 7 \times 7\sqrt{5} + \frac{22}{7} \times 7 \times 7\right) \text{cm}^2$$

=
$$[154 (\sqrt{5} + 1)]$$
 cm² = (164×3.236) cm² = 498.35 cm².

89. Clearly, we have r = 3 cm and h = 4 cm.

$$\therefore \text{ Volume} = \frac{1}{3}\pi r^2 h = \left(\frac{1}{3} \times \pi \times 3^2 \times 4\right) \text{cm}^3 = 12\pi \text{ cm}^3.$$

90.
$$l = 10$$
 m, $h = 8$ m. So, $r = \sqrt{l^2 - h^2} = \sqrt{(10)^2 - 8^2} = 6$ m.

∴ Curved surface area = πrl = (π × 6 × 10) m² = 60π m².

91.
$$\frac{1}{3} \times \frac{22}{7} \times r^2 \times 24 = 1232 \iff r^2 = \left(\frac{1232 \times 7 \times 3}{22 \times 24}\right) = 49 \iff r = 7.$$

Now, r = 7 cm, h = 24 cm. So, $l = \sqrt{(7)^2 + (24)^2} = 25$ cm.

$$\therefore \text{ Curved surface area} = \left(\frac{22}{7} \times 7 \times 25\right) \text{cm}^2 - 550 \text{ cm}^2.$$

92. Let the radius of the base be r km. Then,

$$\pi r^2 = 1.54 \implies r^2 = \left(\frac{1.54 \times 7}{22}\right) = 0.49 \implies r = 0.7 \text{ km}.$$

Now, l = 2.5 km, r = 0.7 km.

$$h = \sqrt{(2.5)^2 - (0.7)^2} \text{ km} = \sqrt{6.25 - 0.49} \text{ km} = \sqrt{5.76} \text{ km} = 2.4 \text{ km}.$$

So, height of the mountain = 2.4 km.

93.
$$\pi r^2 = 3850 \implies r^2 = \left(\frac{3850 \times 7}{22}\right) = 1225 \implies r = 35.$$

Now, r = 35 cm, h = 84 cm.

So,
$$l = \sqrt{(35)^2 + (84)^2} = \sqrt{1225 + 7056} = \sqrt{8281} = 91 \text{ cm}$$
.

$$\therefore \quad \text{Curved surface area} = \left(\frac{22}{7} \times 35 \times 91\right) \text{ cm}^2 = 10010 \text{ cm}^2.$$

94.
$$\frac{22}{7} \times 70 \times l = 40040 \implies l = \left(\frac{40040 \times 7}{22 \times 70}\right) = 182.$$

Now, l = 182 cm, r = 70 cm.

So,
$$h = \sqrt{(182)^2 - (70)^2} = \sqrt{252 \times 112} = 168 \text{ cm.}$$

$$\therefore$$
 Volume = $\left(\frac{1}{3} \times \frac{22}{7} \times 70 \times 70 \times 168\right)$ cm³ = 862400 cm³.

95. Let the radius and the height of the cone be 3x and 4x respectively. Then,

$$\frac{1}{3}\times\pi\times(3x)^2\times4x=96\pi\iff 36x^3=(96\times3)\iff x^3=\left(\frac{96\times3}{36}\right)=8\iff x=2.$$

:. Radius - 6 cm, Height = 8 cm.

Slant height = $\sqrt{6^2 + 8^2}$ cm = $\sqrt{100}$ cm = 10 cm.

96.
$$w^2 = 346.5 \implies r^2 = \left(346.5 \times \frac{7}{22}\right) = \frac{441}{4} \implies r = \frac{21}{2}$$
.

$$I = \sqrt{r^2 + h^2} = \sqrt{\frac{441}{4} + (14)^2} = \sqrt{\frac{1225}{4}} = \frac{35}{2}.$$

So, area of canvas needed =
$$\pi rl = \left(\frac{22}{7} \times \frac{21}{2} \times \frac{35}{2}\right) m^2 = \left(\frac{33 \times 35}{2}\right) m^2$$
.

: Length of canvas =
$$\left(\frac{33 \times 35}{2 \times 1.1}\right)$$
 m = 525 m.

97. Let the original radius and height of the cone be r and h respectively. Then, new radius = 2r. New height = 2h.

$$\therefore \frac{\text{New Volume}}{\text{Original Volume}} = \frac{\frac{1}{3} \times \pi \times (2r)^2 \times 2h}{\frac{1}{3} \times \pi \times r^2 \times h} = \frac{8}{1}.$$

98. Let the original radius and height of the cone be r and h respectively.

Then, Original volume = $\frac{1}{3}\pi r^2 h$.

New radius =
$$\frac{120}{100}r = \frac{6}{5}r$$
, New height = $\frac{6}{5}h$.

New volume =
$$\frac{1}{3} \pi \times \left(\frac{6}{5}r\right)^2 \times \left(\frac{6}{5}h\right) = \frac{216}{125} \times \frac{1}{3}\pi r^2 h$$
.

Increase in volume = $\frac{91}{125} \times \frac{1}{3} \pi r^2 h$.

$$\therefore \text{ Increase \%} = \left(\frac{\frac{91}{125} \times \frac{1}{3} \pi v^2 h}{\frac{1}{3} \pi v^2 h} \times 100\right) \% = 72.8\%.$$

99. Let the original radius and height of the cone be r and h respectively.

Then, original volume =
$$\frac{1}{3}\pi r^2 h$$
.

New radius = $\frac{r}{2}$ and new height = 3h.

New volume =
$$\frac{1}{3} \times \pi \times \left(\frac{r}{2}\right)^2 \times 3h = \frac{3}{4} \times \frac{1}{3} \pi r^2 h$$

$$\therefore \quad \text{Decrease } \% = \left(\frac{\frac{1}{4} \times \frac{1}{3} \, \varpi^2 h}{\frac{1}{3} \, \varpi^2 h} \times 100\right) \% = 25\%.$$

100. Required ratio =
$$\frac{\frac{1}{3}\pi r^2 h}{\frac{1}{3}\pi r^2 \times (2h)} = \frac{1}{2}$$

101. Let their heights be x, 3x and their radii be 3y, y.

Then, Ratio of volumes
$$= \frac{\frac{1}{3} \times \pi \times (3y)^2 \times x}{\frac{1}{3} \times \pi \times y^2 \times (3x)} = \frac{9}{3} = 3:1.$$

102. Let their radii be 2x, x and their heights be h and H respectively. Then,

$$\frac{1}{3} \times \pi \times (2x)^2 \times h = \frac{1}{3} \times \pi \times x^2 \times H \text{ or } \frac{h}{H} = \frac{1}{4}.$$

103. Let their radii be 4x and 5x, and their heights be h and H respectively. Then,

$$\frac{\frac{1}{3} \times \pi \times (4x)^2 \times h}{\frac{1}{3} \times \pi \times (5x)^2 \times H} = \frac{1}{4} \text{ or } \frac{h}{H} = \frac{1}{4} \times \frac{25}{16} = \frac{25}{64}.$$

104. Volume of the largest cone = Volume of the cone with diameter of base 7 cm and height 7 cm =
$$\left(\frac{1}{3} \times \frac{22}{7} \times 3.5 \times 3.5 \times 7\right)$$
 cm³ = $\left(\frac{269.5}{3}\right)$ cm³ = 89.8 cm³.

106. Volume of the block = $(10 \times 5 \times 2)$ cm³ = 100 cm³.

Volume of the cone carved out =
$$\left(\frac{1}{3} \times \frac{22}{7} \times 3 \times 3 \times 7\right)$$
 cm³ = 66 cm³.

106. Let their radius and height be 5x and 12x respectively.

Slant height of the cone, $l = \sqrt{(5x)^2 + (12x)^2} = 13x$.

$$\frac{\text{Total surface area of cylinder}}{\text{Total surface area of cone}} = \frac{2\pi r \left(h+r\right)}{\pi r \left(l+r\right)} = \frac{2\left(h+r\right)}{\left(l+r\right)} = \frac{2\times \left(12x+5x\right)}{\left(13x+5x\right)} = \frac{34x}{18x} = \frac{17}{9},$$

107. Let the radius of the cone be r cm.

Then,
$$\frac{1}{3}\pi \times r^2 \times 6 = \pi \times 8 \times 8 \times 2 \iff r^2 = \left(\frac{8 \times 8 \times 2 \times 3}{6}\right) = 64 \iff r = 8 \text{ cm}.$$

108. Let radius of each be r and height of each be h.

Then, number of cones needed =
$$\frac{\text{Volume of cylinder}}{\text{Volume of 1 cone}} = \frac{\pi r^2 h}{\frac{1}{3} \pi r^2 h} = 3.$$

109. Volume of cylinder = $(\pi \times 3 \times 3 \times 5)$ cm³ = 45π cm³.

Volume of cylinder =
$$(\pi \times 3 \times 3 \times 5)$$
 cm³ = 45π cm³.
Volume of 1 cone = $\left(\frac{1}{3}\pi \times \frac{1}{10} \times \frac{1}{10} \times 1\right)$ cm³ = $\frac{\pi}{300}$ cm³.

$$\therefore \text{ Number of cones} = \left(45\pi \times \frac{300}{\pi}\right) = 13500.$$

110. Volume flown in conical vessel = $\frac{1}{3}\pi \times (20)^2 \times 24 = 3200\pi$.

Volume flown in 1 min. = $\left(\pi \times \frac{2.5}{10} \times \frac{2.5}{10} \times 1000\right) = 62.5\pi$.

- : Time taken = $\left(\frac{3200\pi}{62.5\pi}\right)$ = 51 min. 12 sec.
- 111. Slant height of the cone, l = √(12)² + (5)² = 13 cm.
 Lateral surface of the solid = Curved surface of cone + Curved surface of cylinder

+ Surface area of bottom = $\pi rl + 2\pi rh + \pi r^2$, where h is the height of the cylinder

$$= \pi r (l + h + r) = \left[\frac{22}{7} \times 12 \times (13 + 18 + 12) \right] \text{cm}^2$$

$$= \left(\frac{22}{7} \times 12 \times 43 \right) \text{cm}^2 = \left(\frac{11352}{7} \right) \text{cm}^2 = 1621 \frac{5}{7} \text{cm}^2.$$
Allelopined = $(5 \times 3 \times 4) \text{ cm}^3 = 60 = 3$

112. Volume of parallelopiped = (5 × 3 × 4) cm³ = 60 cm³.
Volume of cube = (4)³ cm³ = 64 cm³.

Volume of cylinder = $\left(\frac{22}{7} \times 3 \times 3 \times 3\right)$ cm³ = 84.86 cm³.

Volume of sphere = $\left(\frac{4}{3} \times \frac{22}{7} \times 3 \times 3 \times 3\right) = 113.14 \text{ cm}^3$.

- 113. $\frac{4}{3} \times \frac{22}{7} \times R^3 = 4851 \implies R^3 = \left(4851 \times \frac{3}{4} \times \frac{7}{22}\right) = \left(\frac{21}{2}\right)^3 \implies R = \frac{21}{2}$
 - \therefore Curved surface area = $\left(4 \times \frac{22}{7} \times \frac{21}{2} \times \frac{21}{2}\right) \text{cm}^2 = 1386 \text{ cm}^2$.
- 114. $4\pi R^2 = 5544 \implies R^2 = \left(5544 \times \frac{1}{4} \times \frac{7}{22}\right) = 441 \implies R = 21.$

115. Volume = $\frac{4}{3} \pi r^3 = \frac{r}{3} (4\pi r^2) = \frac{r}{3} \times \text{Surface area.}$

116. $\frac{\frac{4}{3}\pi R^3}{4\pi R^2} = 27 \implies R = 81 \text{ cm}.$

117. Let the radii of A and B be r and R respectively.

:. Required ratio = $\frac{4\pi r^2}{4\pi R^2} = \frac{r^2}{R^2} = \left(\frac{r}{R}\right)^2 = \left(\frac{40}{10}\right)^2 = 16:1.$

118. Let the original radius be r.

Then, original surface area = $4\pi r^2$ = 2464 cm² (given).

New radius = 2r.

- .. New surface area = $4\pi (2r)^2 = 4 \times 4\pi r^2 = (4 \times 2464) \text{ cm}^2 = 9856 \text{ cm}^2$.
- 119. Let the original radius be r. Then, original volume = $\frac{4}{3} \pi r^3$. New radius = 2r.
 - ∴ New volume = $\frac{4}{3}\pi(2r)^3 = 8 \times \frac{4}{3}\pi r^3 = 8 \times \text{original volume}$.

120.
$$4\pi (r + 2)^2 - 4\pi r^2 = 352 \Leftrightarrow (r + 2)^2 - r^2 = \left(352 \times \frac{7}{22} \times \frac{1}{4}\right) = 28.$$

 $\Leftrightarrow (r + 2 + r) (r + 2 - r) = 28 \Leftrightarrow 2r + 2 = 14 \Rightarrow r = \left(\frac{14}{2} - 1\right) = 6 \text{ cm}.$

121. Let the correct radius be 100 cm, Then, measured radius = 101.5 cm.

$$\therefore \quad \text{Error in volume} = \frac{4}{3} \pi \left[(101.5)^3 - (160)^3 \right] \text{em}^3$$

$$= \frac{4}{3} \pi \left(1045678.375 - 10000000 \right) \text{cm}^3 = \left(\frac{4}{3} \times \pi \times 45678.375 \right) \text{cm}^3.$$

$$\therefore \quad \text{Error \%} = \left\{ \frac{\frac{4}{3} \pi (45678.375)}{\frac{4}{3} \pi (100 \times 100 \times 100)} \times 100 \right\} \% = 4.56\% = 4.6\% \text{ (app.)}.$$

122. Let their radii be R and r. Then,

$$\frac{\frac{4}{3}\pi R^3}{\frac{4}{3}\pi r^3} = \frac{64}{27} \implies \left(\frac{R}{r}\right)^3 = \frac{64}{27} = \left(\frac{4}{3}\right)^3 \implies \frac{R}{r} = \frac{4}{3}.$$

Ratio of surface areas = $\frac{4\pi R^2}{4\pi r^2} = \left(\frac{R}{r}\right)^2 = \left(\frac{4}{3}\right)^2 = \frac{16}{9}$.

123. Let their radii be R and r. Then,

$$\frac{4\pi R^2}{4\pi r^2} = \frac{4}{25} \implies \left(\frac{R}{r}\right)^2 = \left(\frac{2}{5}\right)^2 \implies \frac{R}{r} = \frac{2}{5}, \quad \text{and } r$$

$$\therefore \text{ Ratio of volumes} = \frac{\frac{4}{3} \pi R^3}{\frac{4}{3} \pi r^3} = \left(\frac{R}{r}\right)^3 = \left(\frac{2}{5}\right)^3 = \frac{8}{125}.$$

124. Volume of new sphere =
$$\left[\frac{4}{3}\pi \times (6)^3 + \frac{4}{3}\pi \times (8)^3 + \frac{4}{3}\pi \times (10)^3\right] \text{cm}^3$$

= $\left\{\frac{4}{3}\pi \left[(6)^3 + (8)^3 + (10)^3\right]\right\} \text{cm}^3$
= $\left(\frac{4}{3}\pi \times 1728\right) \text{cm}^3 = \left[\frac{4}{3}\pi \times (12)^3\right] \text{cm}^3$.

Let the radius of the new sphere be R. Then,

$$\frac{4}{3} \pi R^3 = \frac{4}{3} \pi \times (12)^3 \implies R = 12 \text{ cm}.$$

.. Diameter = 2R = 24 cm.

125. Volume of bigger sphere =
$$\left[\frac{4}{3}\pi \times (8)^3\right] \text{cm}^3 = \left(\frac{4}{3}\pi \times 512\right) \text{cm}^3$$
.
Volume of 1 ball = $\left[\frac{4}{3}\pi \times (2)^3\right] \text{cm}^3 = \left(\frac{4}{3}\pi \times 8\right) \text{cm}^3$.

$$\therefore \text{ Number of balls} = \left(\frac{\frac{4}{3}\pi \times 512}{\frac{4}{3}\pi \times 8}\right) = \frac{512}{8} = 64.$$

126. Let the radius of the third ball be R cm. Then,

Let the radius of the third ball be R cm. Then,
$$\frac{4}{3} \pi \times \left(\frac{3}{4}\right)^3 + \frac{4}{3} \pi \times (1)^3 + \frac{4}{3} \pi \times \mathbb{R}^3 = \frac{4}{3} \pi \times \left(\frac{3}{2}\right)^3 \\ \Rightarrow \frac{27}{64} + 1 + \mathbb{R}^3 = \frac{27}{8} \Rightarrow \mathbb{R}^3 = \frac{125}{64} = \left(\frac{5}{4}\right)^3 \Rightarrow \mathbb{R} = \frac{5}{4}.$$

∴ Diameter of the third ball = $2R = \frac{5}{2}$ cm = 2.5 cm.

127. Volume of each ball =
$$\frac{1}{8} \times \left(\frac{4}{3} \pi \times 10 \times 10 \times 10\right) \text{ cm}^3$$
.

$$\therefore \quad \frac{4}{3} \pi R^3 = \frac{1}{8} \times \frac{4}{3} \pi \times 10 \times 10 \times 10 \quad \Rightarrow \quad R^3 = \left(\frac{10}{2}\right)^3 = 5^3 \quad \Rightarrow \quad R = 5.$$

128. External radius = 3 cm, Internal radius = (3 - 0.5) cm = 2.5 cm.

Volume of the metal =
$$\left[\frac{4}{3} \times \frac{22}{7} \times \{(3)^3 - (2.5)^3\}\right] \text{cm}^3$$

= $\left(\frac{4}{3} \times \frac{22}{7} \times \frac{91}{8}\right) \text{cm}^3 = \left(\frac{143}{3}\right) \text{cm}^3 = 47\frac{2}{3} \text{cm}^3$.

129. Volume of the solid = (49 × 33 × 24) cm³. Let the radius of the sphere be r.

Then,
$$\frac{4}{3}\pi r^3 = (49 \times 33 \times 24) \iff r^3 = \left(\frac{49 \times 33 \times 24 \times 3 \times 7}{4 \times 22}\right) = (21)^3 \iff r = 21.$$

130. Number of bullets =
$$\frac{\text{Volume of the cube}}{\text{Volume of 1 bullet}} = \left(\frac{22 \times 22 \times 22}{\frac{4}{3} \times \frac{22}{7} \times 1 \times 1 \times 1}\right) = 2541.$$

131. Volume of each lead shot =
$$\left[\frac{4}{3}\pi \times \left(\frac{0.3}{2}\right)^3\right] \text{ cm}^3 = \left(\frac{4}{3} \times \frac{22}{7} \times \frac{27}{8000}\right) \text{ cm}^3 = \frac{99}{7000} \text{ cm}^3$$
.

$$\therefore \text{ Number of lead shots} = \left(9 \times 11 \times 12 \times \frac{7000}{99}\right) = 84000.$$

132.
$$4\pi R^2 = 6a^2 \implies \frac{R^2}{a^2} - \frac{3}{2\pi} \implies \frac{R}{a} = \frac{\sqrt{3}}{\sqrt{2\pi}}$$

$$\frac{\text{Volume of sphere}}{\text{Volume of cube}} = \frac{\frac{4}{3}\pi R^3}{a^3} = \frac{4}{3}\pi \cdot \left(\frac{R}{a}\right)^3 = \frac{4}{3}\pi \cdot \frac{3\sqrt{3}}{2\pi\sqrt{2\pi}} = \frac{2\sqrt{3}}{\sqrt{2\pi}} = \frac{\sqrt{12}}{\sqrt{2\pi}} = \frac{\sqrt{6}}{\sqrt{\pi}}.$$

133. Let the edge of the cube be a. Then, volume of the cube = a³. Radius of the sphere = (a/2).

Volume of the sphere = $\frac{4}{3}\pi \left(\frac{a}{2}\right)^3 = \frac{\pi a^3}{6}$.

$$\therefore \text{ Required ratio} = a^3 : \frac{\pi a^3}{6} = 6 : \pi. \quad \text{ and } \frac{1}{6} = 1 \text{ and } 1 \text{ be somethally}$$

134.
$$4\pi R^2 = 2\pi \times 6 \times 12 \implies R^2 = \left(\frac{6 \times 12}{2}\right) = 36 \implies R = 6 \text{ cm}.$$

135. Let the radius of the cylinder be R.

Then,
$$\pi \times \mathbb{R}^2 \times \frac{7}{3} = \frac{4}{3} \pi \times 7 \times 7 \times 7$$

$$\rightarrow R^2 = \left(\frac{4 \times 7 \times 7 \times 7}{3} \times \frac{3}{7}\right) = 196 = (14)^2 \rightarrow R = 14 \text{ cm}.$$

Diameter = 2R = 28 cm.

136. Required volume - Volume of a sphere of radius 1 cm

$$= \left(\frac{4}{3}\pi \times 1 \times 1 \times 1\right) \text{cm}^3 = \frac{4}{3}\pi \text{ cm}^3.$$

137. Volume of cylinder = $\pi \times (3)^2 \times 15 = 135\pi$ cm³.

Radius of 1 bullet =
$$\frac{5}{2}$$
 mm = $\frac{5}{20}$ cm = $\frac{1}{4}$ cm.

Volume of 1 bullet =
$$\left(\frac{4}{3}\pi \times \frac{1}{4} \times \frac{1}{4} \times \frac{1}{4}\right) \text{ cm}^3 = \frac{\pi}{48} \text{ cm}^3$$
.

$$\therefore \text{ Number of bullets} = \left(135\pi \times \frac{48}{\pi}\right) = 6480.$$

138. Let the radius of the cylindrical rod be r.

Then, height of the rod = 8r and radius of one ball = $\frac{r}{2}$.

.. Number of balls =
$$\frac{\pi \times r^2 \times 8r}{\frac{4}{3} \pi \times \left(\frac{r}{2}\right)^3} = \left(\frac{8 \times 8 \times 3}{4}\right) = 48.$$

139. Let the length of the wire be h

Then,
$$\pi \times \frac{3}{20} \times \frac{3}{20} \times h = \frac{4}{3} \pi \times 4 \times 4 \times 4$$

$$\Leftrightarrow h = \left(\frac{4 \times 4 \times 4 \times 4 \times 20 \times 20}{3 \times 3 \times 3}\right) \text{ cm} = \left(\frac{102400}{27}\right) \text{ cm} = 3792.5 \text{ cm} = 37.9 \text{ m}.$$

140. Let the rise in the water level be h cm.

Let the rise in the water level be
$$h$$
 cm. Then, $\pi \times 4 \times 4 \times h = \frac{4}{3} \pi \times 3 \times 3 \times 3 \implies h = \left(\frac{3 \times 3}{4}\right) = \frac{9}{4}$ cm.

141. Let the radius of each sphere be r cm.

Then, Volume of 12 spheres = Volume of cylinder

$$\Rightarrow 12 \times \frac{4}{3} \pi \times r^3 = \pi \times 8 \times 8 \times 2 \Rightarrow r^3 = \left(\frac{8 \times 8 \times 2 \times 3}{12 \times 4}\right) = 8 \Rightarrow r = 2 \text{ cm}.$$

Diameter of each sphere = 2r = 4 cm.

142. Let the radius of the ball be r cm.

Volume of ball = Volume of water displaced by it

$$\therefore \frac{4}{3}\pi r^3 = \pi \times 12 \times 12 \times 6.75 \implies r^3 = 9 \times 9 \times 9 \implies r = 9 \text{ cm}.$$

143. Let the height of the cone be h cm. Then,

$$\frac{1}{3}\pi \times 6 \times 6 \times h = \frac{4}{3}\pi \times 3 \times 3 \times 3 \implies h = \left(\frac{36 \times 3}{36}\right) = 3 \text{ cm}.$$

144. Volume of sphere =
$$\left(\frac{4}{3}\pi \times 9 \times 9 \times 9\right)$$
 cm³.

Volume of cone =
$$\left(\frac{1}{3}\pi \times 9 \times 9 \times 9\right)$$
 em³.

Volume of wood wasted =
$$\left[\left(\frac{4}{3} \pi \times 9 \times 9 \times 9 \right) - \left(\frac{1}{3} \pi \times 9 \times 9 \times 9 \right) \right] \text{cm}^3$$
= $(\pi \times 9 \times 9 \times 9) \text{ cm}^3$.

$$\therefore \text{ Required percentage} = \left(\frac{\pi \times 9 \times 9 \times 9}{\frac{4}{3}\pi \times 9 \times 9 \times 9} \times 100\right)\% = \left(\frac{3}{4} \times 100\right)\% = 75\%.$$

145. Number of spheres =
$$\frac{\text{Volume of cone}}{\text{Volume of 1 sphere}} = \frac{\frac{1}{3}\pi \times 12 \times 12 \times 24}{\frac{4}{3}\pi \times 2 \times 2 \times 2} = 108.$$

146. Volume of material in the sphere =
$$\left[\frac{4}{3}\pi \times ((4)^3 - (2)^3)\right] \text{cm}^3 = \left(\frac{4}{3}\pi \times 56\right) \text{cm}^3$$
.
Let the height of the cone be h cm.

Let the height of the cone be
$$h$$
 cm.

Then, $\frac{1}{3} \pi \times 4 \times 4 \times h = \left(\frac{4}{3} \pi \times 56\right) \iff h = \left(\frac{4 \times 56}{4 \times 4}\right) = 14 \text{ cm.}$

148. Total surface area =
$$3\pi R^2 = \left(3 \times \frac{22}{7} \times 7 \times 7\right) \text{ cm}^2 = 462 \text{ cm}^2$$
.

$$\frac{2}{3} \times \frac{22}{7} \times R^3 \ = \ 19404 \quad \Leftrightarrow \quad R^3 \ = \left(19404 \times \frac{21}{44}\right) = \ (21)^3 \quad \Leftrightarrow \quad R \ = \ 21 \ \text{cm}.$$

150. Let their radii be R and r. Then,

$$\frac{\frac{2}{3}\pi R^3}{\frac{2}{3}\pi r^3} = \frac{6.4}{21.6} \iff \left(\frac{R}{r}\right)^3 = \frac{8}{27} = \left(\frac{2}{3}\right)^3 \iff \frac{R}{r} = \frac{2}{3}.$$

∴ Ratio of curved surface areas =
$$\frac{2\pi R^2}{2\pi r^2} = \left(\frac{R}{r}\right)^2 = \frac{4}{9}$$
.

151. Let the height of the vessel be x. Then, radius of the bowl = radius of the vessel = $\frac{x}{2}$.

Volume of the bowl,
$$V_1 = \frac{2}{3} \pi \left(\frac{x}{2}\right)^3 = \frac{1}{12} \pi x^3$$
.

Volume of the vessel,
$$V_2 = \pi \left(\frac{x}{2}\right)^2 x = \frac{1}{4}\pi x^3$$
.

Since V2 > V1, so the vessel can contain 100% of the beverage filled in the bowl.

152.
$$\frac{2}{3}\pi R^3 = \frac{1}{3}\pi R^2 H \implies H = 2R$$
.

153. Let the radius of the cone be R cm. Then,

153. Let the radius of the cone be K cm. Then,
$$\frac{1}{3}\pi \times R^2 \times 75 = \frac{2}{3}\pi \times 6 \times 6 \times 6$$

154. Let the radius of each be R. Height of hemisphere, H = R. So, height of cone = height of hemisphere = R.

Slant beight of cone =
$$\sqrt{R^2 + R^2}$$
 = $\sqrt{2}$ R.

$$\frac{\text{Curved surface area of hemisphere}}{\text{Curved surface area of cone}} = \frac{2\pi R^2}{\pi R \times \sqrt{2} R} = \sqrt{2} : 1.$$

155. Volume of hemisphere = $\frac{2}{3}\pi r^3$.

Volume of biggest sphere = Volume of sphere with diameter $r = \frac{4}{3} \pi \left[\frac{r}{2} \right]^2 = \frac{1}{6} \pi r^3$

$$\therefore \text{ Required ratio} = \frac{\frac{2}{3}\pi r^3}{\frac{1}{6}\pi r^3} = \frac{4}{1}i.c. 4:1.$$

EXERCISE 25B

(DATA SUFFICIENCY TYPE QUESTIONS)

Directions (Questions 1 to 10): Each of the questions given below consists of a statement and or a question and two statements numbered I and II given below it. You have to decide whether the data provided in the statement(s) is/are sufficient to answer the given question. Read both the statements and

Give answer (a) if the data in Statement I alone are sufficient to answer the question, while the data in Statement II alone are not sufficient to answer the question;

Give answer (b) if the data in Statement II alone are sufficient to answer the question, while the data in Statement I alone are not sufficient to answer the question;

Give answer (c) if the data either in Statement I or in Statement II alone are sufficient to answer the question;

Give answer (d) if the data even in both Statements I and II together are not sufficient to answer the question;

Give answer (e) if the data in both Statements I and II together are necessary to answer the question.

- What is the weight of the iron beam?
 - I. The beam is 9 m long, 40 cm wide and 20 cm high.
 - II. Iron weighs 50 kg per cubic metre.
- What is the volume of 32 metre high cylindrical tank? (Bank P.O. 2003)

- I. The area of its base is 154 m².
- II. The diameter of the base is 14 m.
- What is the volume of a cube?

(Bank P.O. 2003)

- I. The area of each face of the cube is 64 square metres.
- II. The length of one side of the cube is 8 metres.

(e) None of these

	Quantitative Aptitude
I. The box is made of	wood 3 cm thick.
II. The external dimens	ions of the box are 50 cm, 40 cm and 23 cm.
What is the capacity of	
I. Radius of the base i	s half of its height which is 28 metres. (I.B.P.S. 2002)
II. Area of the base is	516 sq. metres and its height is 28 metres.
What is the volume of the	
I. Height is equal to the	(Bank P.O. 2003)
II. Perimeter of the bas	is 352 cm
7. What will be the total co per square metre?	st of whitewashing the conical tomb at the rate of 80 paise
II The height of the	slant height of the tomb are 28 m and 50 m.
and the neight of the tor	no is 48 m and the area of its base is 616 as
and the same mengant on a C	reular cone ?
II The area of that cone	is equal to the area of a rectangle whose length is 33 cm.
aren of the pase	of that cone is 154 so cm
9. Is a given rectangular blo	ck, a cube ? (M.A.T. 1999)
II. The volume of the ble	rectangular block are squares.
10. A spherical ball of given as	ck is 64.
The state of the s	dius x cm is melted and made into a right circular cylinder. cylinder? (S.B.I.P.O. 2003)
 The volume of the cyl 	inder is equal to the volume of the ball
ii. The area of the base	of the cylinder is given
questions (Questions 11-13 question followed by three statem and decide which of the statem	ents. You have to study the question and the statements
and emperercy of the	CVIIII TITE TO THE TOTAL
I. The area of the base	s 61,600 sq. cm.
ii. The neight of the tank	is 1.5 times the radius
in the circumference of h	ase is 880 cm
The state of the s	(D) Univ II and III
and and of rife filles	(c) Only II and either I or III
sphere ?	ited and recast into a sphere. What is the radius of the
I. The radius of the base	of the cone is 2.1 cm.
11. The height of the cone	is four times the radius of its bace
	is 8.4 cm.
(a) Only I and II	(In Col. II and seems and it is because with
(d) Any two of the three	(c) All I. II and III
What is the total surface a	ea of the cone?
a. Asse area of the base of	the cone is 154 cm ²
in the curved surface area	of the cone is 550 cm ²
Air. The volume of the cone	is 1232 cm ³ .
(a) I, and either II or III	(b) II, and either 1 or III
(c) III, and either I or II	(d) Any two of the three

(d) Any two of the three

ANSWERS

1. (e) 2. (c) 3. (c) 4. (e) 5. (c) 6. (e) 7. (c) 8. (d)

9. (d) 10. (b) 11. (e) 12. (d) 13. (a)

SOLUTIONS

1. I gives, l = 9 m, $b = \frac{40}{100} \text{ m} = \frac{2}{5} \text{ m}$ and $h = \frac{20}{100} \text{ m} = \frac{1}{5} \text{ m}$.

This gives, volume = $(l \times b \times h) = \left(9 \times \frac{2}{5} \times \frac{1}{5}\right) m^3 = \frac{18}{25} m^3$.

II gives, weight of iron is 50 kg/m3.

 \therefore Weight = $\left(\frac{18}{25} \times 50\right)$ kg = 36 kg.

Thus, both I and II are needed to get the answer.

: Correct answer is (e).

2. Given, height = 32 m.

I gives, area of the base = 154 m².

 \therefore Volume = (area of the base \times height) = (154 \times 32) m³ = 4928 m³.

Thus, I alone gives the answer. II gives, radius of the base = 7 m.

:. Volume = $\pi r^2 h = \left(\frac{22}{7} \times 7 \times 7 \times 32\right) m^3 = 4928 m^3$.

Thus, II alone gives the answer.

.. Correct answer is (c).

Let each edge be a metres. Then,

I. $a^2 = 64 \implies a = 8 \text{ m} \implies \text{Volume} = (8 \times 8 \times 8) \text{ m}^3 = 512 \text{ m}^3$. Thus, I alone gives the answer.

II. $a = 8 \text{ m} \implies \text{Volume} = (8 \times 8 \times 8) \text{ m}^3 = 512 \text{ m}^3$.

Thus, II alone gives the answer.

:. Correct answer is (c).

4. I gives, thickness of the wall of the box = 3 cm.

II gives, Internal length = (50-6) cm = 44 cm, Internal breadth = (40-6) = 34 cm, Internal height = (23-3) cm = 20 cm.

Area to be painted = (area of 4 walls + area of floor) = $[2 (l + b) \times h + (l \times b)]$ = $[2 (44 + 34) \times 20 + (44 \times 34)] \text{ cm}^2 = 4616 \text{ cm}^2$.

Cost of painting = Rs. $\left(\frac{1}{2 \times 100} \times 4616\right)$ = Rs. 23.08.

Thus, both I and II are needed to get the answer.

.. Correct answer is (e).

I gives, h = 28 m and r = 14 cm.

∴ Capacity = πr²h, which can be obtained.

Thus, I alone gives the answer.

II gives, $\pi r^2 = 616 \text{ m}^2$ and h = 28 m.

∴ Capacity = (πr² × h) = (616 × 28) m³.

Thus, II alone gives the answer.

- :. Correct answer is (c).
- I gives, h = 2r.

II gives,
$$2\pi r = 352 \implies r = \left(\frac{352}{2} \times \frac{7}{22}\right) \text{ cm} = 56 \text{ cm}.$$

From I and II, we have r = 56 cm, $h = (2 \times 56)$ cm = 112 cm.

Thus, we can find the volume.

- .: Correct answer is (e).
- 7. I gives, r = 14 m, l = 50 m.

$$\therefore \text{ Curved surface} = \pi r l = \left(\frac{22}{7} \times 14 \times 50\right) \text{m}^2 = 2200 \text{ m}^2.$$

Cost of whitewashing = Rs. $\left(2200 \times \frac{80}{100}\right)$ = Rs. 1760.

Thus, I alone gives the answer.

II gives, h = 48 m, $\pi r^2 = 616 \text{ m}^2$.

These results give r and h and so I can be found out.

∴ Curved surface = πrl.

Thus, II alone gives the answer.

- .: Correct answer is (c).
- 8. II gives the value of r.

But, in I, the breadth of rectangle is not given.

So, we cannot find the surface area of the cone.

Hence, the height of the cone cannot be determined.

- .. Correct answer is (d).
- I gives, any two of l, b, h are equal. 9.

II gives, lbh = 64.

From I and II, the values of l, b, h may be (1, 1, 64), (2, 2, 16), (4, 4, 4), Thus, the block may be a cube or cuboid.

Volume - target fit the base

- Correct answer is (d).
- 10. Clearly, I is not needed, since it is evident from the given question. From II, we get radius of the base of the cylinder.

Now, $\frac{4}{3}\pi x^3 = \pi r^2 h$ in which x and r are known.

- .. h can be determined.
- : Correct answer is (b).
- 11.

Capacity = $\pi r^2 h$. 80 so see a super $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ I gives, $\pi r^2 = 61600$. This gives r.

II gives, h = 1.5 r.

Thurs, both I and II are needed to get the answers. Thus, I and II give the answer.

Again, III gives $2\pi r = 880$. This gives r.

So, II and III also give the answer.

Correct answer is (e).

12. $\frac{4}{3} \pi R^3 = \frac{1}{3} \pi r^2 h$ 3 MAD QMA 3 HOAF 3 S

Now r and h can be determined from any two of I, II and III. Thus, R can be calculated.

- .. Correct answer is (d).
- Total surface area of the cone = $(\pi rI + \pi r^2)$ cm². I gives, $\pi r^2 = 154$. Thus, we can find r. II gives, $\pi rI = 550$.

From I and II we get the answer.

III gives, $\frac{1}{3} \pi r^2 h = 1232$.

From I and III, we can find h and therefore, L. Hence the surface area can be determined.

.. Correct answer is (a).