Solutions of Optics & Modern Physics

Lesson 26th to 30th

By DC Pandey

26. Reflection of Light

Introductory Exercise 26.1

1. Since $c = \frac{1}{\sqrt{00}}$ where c is the speed of light in vacuum hence unit of $\frac{1}{\sqrt{00}}$ is m/s.

2. Hence

 B_y 2 10 ⁷ T sin [500x 1.5 10¹¹t] Comparing this equation with the standard wave equation B_y B_0 sin [kx t]

$$\frac{2}{k} = 500 \text{ m}^{-1} \quad k = \frac{2}{k}$$
$$\frac{2}{k} \text{ m}$$
$$\frac{2}{500} \text{ m} = \frac{2}{250} \text{ metre}$$

$$\begin{array}{rrrr} 1.5 & 10^{11} \ {\rm rad/s} \\ 2 & n & 1.5 & 10^{11} \\ & n & \frac{1.5}{2} & 10^{11} \ {\rm Hz} \end{array}$$
 Speed of the wave $v & \frac{1.5 & 10^{11}}{k} \\ & 3 & 10^8 \ {\rm m/s} \end{array}$ Let E_0 be the amplitude of electric field.

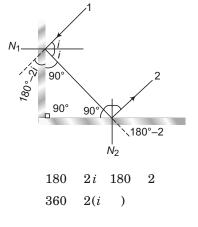
Then $E_0 \ cB_0 \ 3 \ 10^8 \ 2 \ 10^7 \ 60 \, \text{V/m}$

Since wave is propagating along *x*-axis and *B* along *y*-axis, hence *E* must be along *z*-axis

E 60 V/m sin [500x 1.5 $10^{11}t$]

Introductory Exercise 26.2

1. Total deviation produced



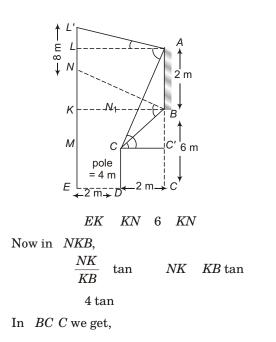
From figure

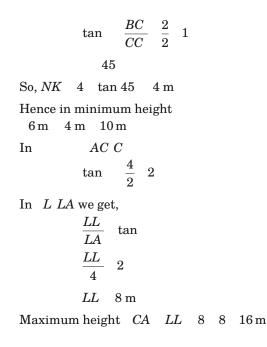
Hence rays 1 and 2 are parallel (antiparallel).

2. $v_0 = 2 \text{ m/s}$ for plane mirror $v_i = 2 \text{ m/s}$.

Velocity of approach $v_0 \quad v_i \quad 4 \text{ m/s}.$

3. In figure, *AB* is mirror, *G* is ground, *CD* is pole and *M* is the man. The minimum height to see the image of top of pole is *EN*





Introductory Exercise 26.3

1.	Here	f	10	cm	(concave	mirror)	
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(a) $u = 25 \,\mathrm{cm}$

Using mirror formula,

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f} \\ \frac{1}{v} \quad \frac{1}{f} \quad \frac{1}{u} \quad \frac{1}{10} \quad \frac{1}{25} \\ \frac{1}{v} \quad \frac{5}{50} \\ v \quad \frac{50}{3} \quad 16.7 \text{ cm}$$

Hence image is real, inverted and less height of the object.

(b) Since u = 10 cm,

Hence object is situated on focus of the image formed at $\ .$

(c)
$$u = 5, f = 10$$

 $\frac{1}{v} \cdot \frac{1}{f} \cdot \frac{1}{u} = \frac{1}{10} \cdot \frac{1}{5}$

$$\frac{1}{v} \quad \frac{1}{10} \frac{2}{10}$$
$$v \quad 10 \text{ cm}$$

Hence, image is virtual, erect and two time of the object.

2. Here
$$u = 3 \text{ m}, f = \frac{1}{2} \text{ m},$$

we have,
(a) $\frac{1}{v} = \frac{1}{f} = \frac{1}{u}$
 $\frac{1}{v} = 2 = \frac{1}{3}$
 $v = 0.6 \text{ m}$

As ball moves towards focus the image moves towards and image is real as the distance decreases by focal length image become virtual which moves from to zero.

(b) The image of the ball coincide with ball, when u = R = 1 m

Using
$$h$$
 ut $\frac{1}{2}gt^2$
t $\sqrt{\frac{2h}{g}}$ $\sqrt{\frac{2}{9.8}}$
0.639 s

Similarly again images match at t = 0.78 s.

- **3.** Since image is magnified, hence the mirror is concave.
 - Here,

$$m \quad \frac{v}{u} \quad \frac{v}{u} \quad 5$$
$$v \quad 5u \qquad \dots (i)$$

Let distance between mirror and object is *x*.

Since image is formed at a distance 5 m from mirror

From Eqs.(i) and (ii), we get

(5 x) 5x4x 5x 1.25

Hence mirror is placed at 1.25 m on right side of the object by mirror formula

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f},$$

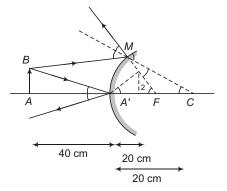
we have

$$\frac{1}{f} = \frac{1}{6.25} = \frac{1}{1.25}$$

$$f = \frac{6.25}{6},$$
Hence $R = 2f = R = \frac{6.25}{3} = 2.08 \text{ m}$

Thus mirror is concave mirror of radius of curvature 2.08 m.

- **4.** Since the incident rays and reflected rays are parallel to each other therefore mirror is plane mirror.
- **5.** Let us solve the first case :



By applying the geometry we can prove that,

$$PA \quad v \quad \frac{40}{3} \,\mathrm{cm}$$

Further, in triangles ABP and PA B we have,

$$\frac{AB}{40} \quad \frac{A \ B}{(40/3)}$$
$$A \ B \quad \frac{AB}{3} \quad \frac{2}{3} \ \text{cm}$$

Similary, we can solve other parts also.

6. Simply apply :

$$\frac{1}{v}$$
 $\frac{1}{u}$ $\frac{1}{f}$

and $m = \frac{I}{o} - \frac{v}{u}$ for lateral magnification. If

magnitication is positive, image will be virtual. If magnification is negative, image will be real.

AIEEE Corner

Subjective Questions (Level 1)

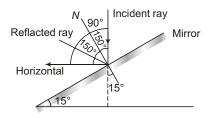
1. Here v 39.2 cm, hence v 39.2 cm

and magnification *m* 1

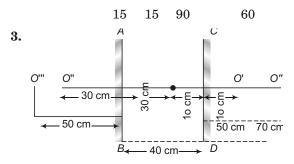
 $h_i \quad h_o \quad 4.85$

Hence image is formed at 39.2 cm behind the mirror and height of image is 4.85 cm.

2. From figure, angle of incident 15

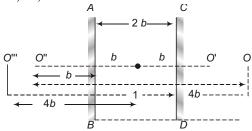


Let reflected ray makes an angle with the horizontal, then



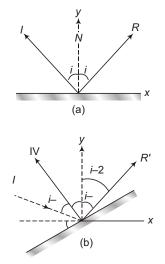
Since mirror are parallel to each other image are formed the distance of five closet to object are 20 cm, 60 cm, 80 cm, 100 cm and 140 cm.

4. The distance of the object from images are 2b, 4b, 6b.... etc.



Hence the images distance are 2nb, where n = 1, 2, ... Ans.

5. Suppose mirror is rotated at angle about its axis perpendicular to both the incident ray and normal as shown in figure



In figure (b) I remain unchanged N and R shift to N and R.

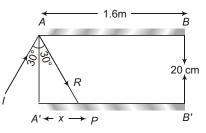
From figure (a) angle of rotation i,

From figure (b) it is i = 2

Thus, reflected ray has been rotated by angle 2.

r

6. I is incident ray i = 30



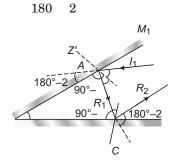
From *PA* A, we get

$$\frac{x}{20} \tan 30 \qquad x \quad 20 \tan 30$$
No. of reflection
$$\frac{AB}{x} \quad \frac{160 \text{ cm}}{20 \text{ cm} \tan 30}$$

$$8\sqrt{3} \quad 14$$

Hence the reflected ray reach other end after 14 reflections.

7. The deviation produced by mirror \boldsymbol{M}_1 is



and the deviation produced by mirror $M_{\rm 2}$ is 180 2

Hence total deviation

	180	2	180	2
	360	2()	
In	ABC we get,			
	90		90	180

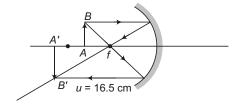
Hence deviation produces 180 2 .

8. Here
$$f = \frac{R}{2} = \frac{22}{2} = 11 \,\mathrm{cm}$$

Object height $h_0 = 6 \text{ mm}$

$16.5\,\mathrm{cm}$ и

(a) The ray diagram is shown in figure



Using mirror formula,
$$\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$$

 $\frac{1}{v} = \frac{1}{f} = \frac{1}{u}$
 $\frac{1}{v} = \frac{1}{11} = \frac{1}{16.5} = \frac{165 - 11}{16.5 - 11}$
 $v = \frac{16.5 - 11}{5.5} = 33 \text{ cm}$

Hence the image is formed at 33 cm from the pole (vertex) of mirror on the object side the image is real, inverted and magnified. The absolute magnification

$$|m| \quad \frac{v}{u} \quad \frac{33}{16.5} \quad 2$$

Hence size of image is $h_i = 2 - h_0$

1

12 cm, $f = \frac{R}{2}$ **9.** Here *u* $10\,\mathrm{cm}$

Using mirror formula

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$
we get

$$\frac{1}{v} \quad \frac{1}{f} \quad \frac{1}{u} \quad \frac{1}{10} \quad \frac{1}{12}$$

$$\frac{6}{60} \quad 5$$

we ge

÷

 $v = \frac{60}{11} \text{ cm} = 5.46 \text{ cm}$

The image is formed on right side of the vertex at a distance $\frac{60}{11}$ cm. the image is virtual and erect the absolute magnification $\frac{v}{u}$ is given by |m|

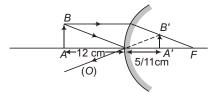
$$|m| = \frac{60}{11} (12) = \frac{5}{11}$$

Hence image is de-magnified. $\text{Height of image } h_i \quad |m| \quad h_0$

 $m \quad 1$

$$h_i = \frac{5}{11} \quad 9 = \frac{45}{11} \quad 4.09 \text{ mm}$$

The ray diagram is shown in figure



10. Here *f* 18 cm

> Let distance of object from vertex of concave mirror is *u*. Since image is real hence image and object lie left side of the vertex.

> > 1

Magnification
$$m$$
 $\frac{v}{u}$ $\frac{1}{9}$
 v $\frac{u}{9}$
By mirror formula, $\frac{1}{v}$ $\frac{1}{u}$ $\frac{1}{f}$, we have
 $\frac{1}{u/9}$ $\frac{1}{u}$ $\frac{1}{18}$ $\frac{10}{u}$ $\frac{1}{18}$

- и 180 cm (left side of the vertex).
- **11.** Here *u* 30 cm, since image is inverted.

Hence the mirror is concave.

$$m \quad \frac{1}{2} \quad \frac{v}{u} \quad v \quad \frac{u}{2}$$
Using mirror formula, $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$, we get
$$\frac{2}{u} \quad \frac{1}{u} \quad \frac{1}{f} \quad \frac{3}{u} \quad \frac{1}{f}$$

$$f \quad \frac{u}{3} \quad \frac{30}{3} \quad 10 \text{ cm}$$

Hence mirror is concave of focal length 10 cm.

 $\frac{24}{2}$ cm **12.** Here *f* $12\,\mathrm{cm}$

(a) Since image is virtual

$$m \frac{v}{u} v mu$$

 $v \quad 3 \quad u$

v 3u and v is +ve

By mirror formula,

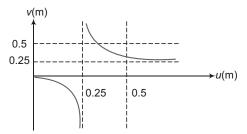
1	1	1	1	1	1
\overline{v}	u	\overline{f}	$\overline{3u}$	u	$\overline{12}$
1	3	1		.,	8 cm
3	u	$\overline{12}$		u	o cin

(b) Since image is real

$$m \quad \frac{v}{u} \quad 3 \quad v \quad 3u$$

By using $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$, we get
 $\frac{1}{e} \quad \frac{1}{u} \quad \frac{1}{12} \quad \frac{4}{3u} \quad \frac{1}{12}$
 $u \quad 16 \text{ cm}$
(c) Here $m \quad \frac{v}{m} \quad \frac{1}{3} \quad v \quad \frac{u}{3}$
 $\frac{1}{u/3} \quad \frac{1}{u} \quad \frac{1}{12}$
 $\frac{4}{u} \quad \frac{1}{12} \quad u \quad 48 \text{ cm}$
13. We have $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$
 $v \quad \frac{uf}{u} \quad atu \quad f, v$

The variation is shown in figure



Hence focal length if assymtote of the curve.

When u = f, Image is virtual. It means v is negative.

When 2fu 2fv 0, v 0 и

14. Here f = 21 cm R 2f = 42 cm

Since the object is placed on C. Hence its image by concave mirror is formed on C. This image acts as a virtual objet for plane mirror the distance between plane mirror and virtual object 21 cm.

Hence plane mirror forms its real image in front of plane mirror at 12 cm.

15. Let u is the object distance from vertex, v is the image distance for vertex and f is the focal length then distance between object and focus is u - f and distance between image and focus is v - f ie,

$$(u \ f)(v \ f) \ uv \ (u \ v)f \ f^2 \qquad \dots(i)$$

Using $\frac{1}{v} \ \frac{1}{u} \ \frac{1}{f}$, we get
 $uv \ (u \ v)f \qquad \dots(ii)$

Putting the value of uv in RHS of Eq. (i), we get

 $(u \ f)(u \ f) \ (v \ u)f \ (v \ u)f \ f^2$ $(u \ f)(v \ f) \ f^2$

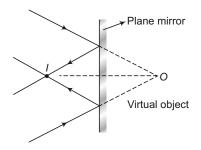
Hence proved.

16. Let object is placed at a distance *x* from the convex mirror then for convex mirror

$$u \quad x \text{ and } f \qquad \frac{R}{2}$$

Objective Questions (Level 1)

1. When convergent beam incident on a plane mirror, then mirror forms real image



Let *v* be the distance of the image from pole (vertex) of convex mirror.

0

Using	$\frac{1}{v}$	$\frac{1}{u}$	$\frac{1}{f}$, w	e get	
	$\frac{1}{v}$	$\frac{1}{x}$	$\frac{2}{12}$	v	$\frac{xR}{2x R}$

For concave mirror

$$u \quad 2R \quad \frac{xR}{2x \quad R} \qquad \frac{2R^2 \quad 5xR}{2x \quad R}$$

$$v \quad (2R \quad x) \text{ and } f \qquad \frac{R}{2}$$
Using $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$, we get
$$\frac{1}{(2R \quad x)} \quad \frac{(2x \quad R)}{(2R^2 \quad 5xR)} \quad \frac{2}{R}$$

$$4R^3 \quad 2x^2R \quad 8xR^2$$

$$8R^3 \quad 16xR^2 \quad 10x^2R$$

$$4R^3 \quad 8xR^2 \quad 8x^2R \quad 0$$

$$4R[R^2 \quad 2xR \quad 2x^2] \quad 0$$

$$2x^2 \quad 2xR \quad R^2 \quad 0$$

$$\therefore \qquad R \quad 0$$

$$x \quad \frac{2R \quad 2\sqrt{3}R}{4} \quad \frac{[1 \quad \sqrt{3}]}{2}R$$

$$x \quad \frac{1 \quad \sqrt{3}}{2} R$$

2. When an object lies at the focus of a concave mirror u = f focal length of a concave mirror is negative.

v

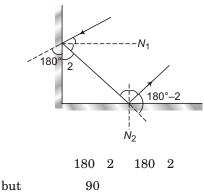
Using mirror formula

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$
we get,
$$\frac{1}{v} \quad \frac{1}{f}$$

also magnification $m = \frac{v}{u}$

Hence, correct option is (c) , .

3. Total deviation, 1



180 2 180 2(90) 180

2

Hence, option (a) is correct.

4. A concave mirror cannot from a virtual image of a virtual object.

Hence option (a) is correct.

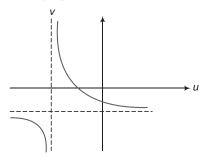
5. For a concave mirror for normal sign convention if u = f = v

,v

and at u

graph between *u* and *v* is

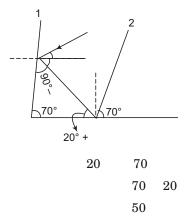
f



The dotted lines are the asymptotes (tangent at) of the curve.

Hence correct option is (b).

6. From figure



Here (1) and (2) are paralledl 11 to each other.

Hence the correct option is (a) 50.

7. The radius of curvature of convex mirror

R 60 cm. $\frac{R}{2}$ Its focal length f30 cm Magnification $m \quad \frac{v}{u} \quad \frac{1}{2}$ $\frac{u}{2}$ v Using mirror formula, $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$, $\frac{1}{30}$ $\frac{1}{u/2}$ $\frac{1}{u}$ we get, $\frac{1}{30}$ 3 и 90 cm и $45\,\mathrm{cm}$ v

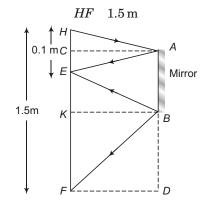
Hence distance between A and B is

90 45

$45\,\mathrm{cm}$

Hence the correct option is (c).

8



Length of mirror $AB = 0.75 \,\mathrm{m}$

The ray diagram is shown in above figure.

H is the Head of the boy and F is the feet. It also shows the paths of the rays that leaves the head of the man enter his eyes (E). After reflection from the mirror at point A, and the rays that leave his feet and enter his eyes after reflected at point B.

From figure
$$CE = \frac{1}{2}HE = 0.05 \text{ m}$$

 $CF = HF = HC = HF = CE$
 $1.50 = 0.05 = 1.45 \text{ m}$

The distance of the bottom edge of mirror above the floor is

But according to question BD = 0.8 m (given) which is greater than 0.7 m, the height required to see full image. Hence the boy cannot see his feet.

Option (c) is correct

9. Since the image is magnified hence mirror is concave mirror.

Here
$$m \quad \frac{v}{u} \quad 3 \quad v \quad 3u$$

 $|v| \quad | \quad 3u| \quad 3u$
but $|v \quad u| \quad 80$
 $|3u \quad u| \quad 80 \quad u \quad 40 \text{ cm}'$

Using mirror formula, we get

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$

$$\frac{1}{3u} \quad \frac{1}{u} \quad \frac{1}{f}$$

$$f \quad \frac{3u}{4}$$

$$f \quad \frac{3}{2} \quad 30 \text{ cm}$$

Mirror is concave and focal length is 30 cm.

Correct option is (a).

10. Here
$$m = \frac{1}{n} = \frac{v}{u}$$

 $v = \frac{u}{n}$

From mirror formula $\frac{1}{f} = \frac{1}{v} = \frac{1}{u}$,

we get,

$$\frac{1}{f} \quad \frac{1}{(u/n)} \quad \frac{1}{u}$$
$$u \quad (n \quad 1)f$$

Hence the correct option is (d).

11. Differentiating mirror formula, we get

$$\frac{dv}{dt} = \frac{v^2}{u^2} \frac{du}{dt}$$
 [: here $\frac{du}{dt}$ is -ve]

Using mirror formula

 $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f},$ we get $\frac{1}{v} \quad \frac{1}{f} \quad \frac{1}{u}$ Here $u \quad 60 \text{ cm}, f \quad 24 \text{ cm}$ Putting these we get, $v \quad 40 \text{ cm}$ Hence, $\frac{dv}{dt} \quad \frac{40^2}{60^2} \quad 9 \quad 4 \text{ cm/s}$

Hence the speed of the image is 4 cm/s away from the mirror.

Hence correct option is (c).

12. The wrong statement is (d)

13. Let $v_{\rm m}$ is the speed of mirror, $v_{\rm p}$ is the speed of particle and v_p is the speed of the observer, then speed of the image measured by observer is given by

Assertion and Reason

1. Assertion is wrong since when a virtual object is placed at a distance less than the focal length its real image is formed.

Hence answer is (d).

2. Using mirror formula $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$ we get $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ v 10 cm

ie image is virtual exect and since $m = \frac{v}{u} = \frac{1}{2}$. Hence image is diminished, thus assertion is true.

If u 20 cm for virtual object vhence reason is true but reason is not correct explanation of assertion. Hence answer is (b).

- **3.** Using mirror formula $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$ we get $\frac{1}{v}$ $\frac{1}{f}$ $\frac{1}{u}$

If u is front of mirror u is negative and f is negative for concave mirror.

$$\frac{1}{v} \quad \frac{1}{f} \quad \frac{1}{u} \qquad v \quad \frac{uf}{f \quad u}$$
$$u \quad f \quad v$$

Hence assertion is true also in refractive image and object moves in opposite direction. Hence both assertion and reason are true and reason correctly explain the assertion Correct answer is (a).

4. Real view mirror of vehicles is convex mirror, hence assertion is true.

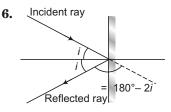
 $v_{\rm op} \quad 2[v_{\rm m} \quad v_{\rm p}] \quad v_{\rm o}$ v_{op} 2[10 4] 2 28 2 26 cm/s

Hence correct option is (d).

It never makes real image of real object reason is also true but convex mirror is used because since its field of view is greatest. Hence both assertion and reason are true but reason is not correct explanation of assertion. Correct answer is (b).

2 hence it is definitely a concave **5.** Since *m* mirror since only concave mirror form magnified image. Since concave mirror form only real image of real object hence reason is also true. Hence it may true but when object is placed between C and F, m = 1.

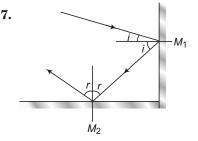
Hence correct answer be (a) or (b).



Hence assertion is true.

For normal incidence *i* 0 hence 180.

hence assertion is true but reason is false. hence correct option is (c).



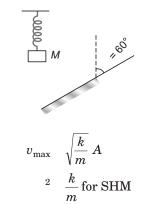
Deviation produced by M_1	180	2i	
Deviation produced by $M_{\rm 2}$	180	2r	
Total deviation produced	360	2(i	r)
But from figure $i r 90$,	hence	devia	tion

Objective Questions (Level 2)

180 for any value of *i*.

 \boldsymbol{A}





Maximum speed of insect relative to its image

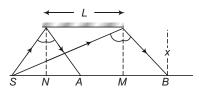


Hence correct option is (c).

2. au^n g

÷

Height x



Let after time t paperndicular distance between mirror and source is x we have from figure

Hence assertion is true but reason is false. Correct option is (c).

- **8.** The correct option is (b).
- **9.** The correct option is (a, b).
- **10.** The correct option is (b).

$$AB 2MB SA 2x \tan SA$$
$$2x \tan 2x \tan SA$$
$$AB 2x \tan 2x \tan I$$
$$AB 2x [\tan \tan I]$$
$$2x \frac{SM}{x} \frac{SN}{x} 2[SM SN]$$
$$AB 2 L,$$

where
$$SM = SN = L$$
 Length of mirror
 $\frac{d}{dt}[AB] = \frac{d}{dt}(2L) = 0$

 \therefore Length of mirror is constant.

Hence the correct option is (d).

3. Here $u = 10 \operatorname{cm} \operatorname{and} v = 20 \operatorname{cm}$

Using mirror formula

$$\frac{1}{u} \quad \frac{1}{v} \quad \frac{1}{f} \text{ we get } \frac{dv}{v^2} \quad \frac{du}{u^2} \quad 0$$

$$\frac{dv}{du} \quad \frac{v^2}{u^2} \quad \frac{20^2}{10^2} \quad 4$$

$$dv \quad 4du$$

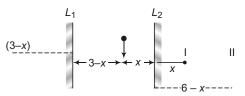
$$dv \quad 4 \quad (0.1), \text{ here } du \quad 0.1$$

$$dv \quad 0.4 \text{ cm},$$

ie, 0.4 cm away from the mirror.

Hence the correct option is (a).

4. The first and second images are shown in figure but according to question

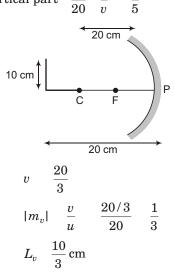


1

v

Hence the correct option is (c).

1 **5.** For vertical part $\overline{20}$



For horizontal part first end is at C hence its image is also at C *ie* at v 10 cm, for other end

The ratio $L_V: L_H = 1:1.$

Hence correct option is (c) 1:1.

6. Here *u* 15 cm, f 10 cm $\frac{1}{v}$ Using We get, $30\,\mathrm{cm}$ v We have $m \quad \frac{v}{m} \quad \frac{(v_2 \quad v_1)}{u_2 \quad u_2}$

$$\frac{dv}{du} = 2$$

$$dv = 2 du,$$

$$A = B$$

$$2 mm = 2 mm$$

$$AB = du = 4 mm$$

$$dv = 2 = 4 mm$$

$$dv = 8 mm$$

Hence the correct option is (c).

7. If the mirror is rotated by an angle in anticlock, wise direction about an axis to the plane mirror, the new angle of incidence becomes *i* and angle of reflection also $i \ 2 \ .$

According to problem

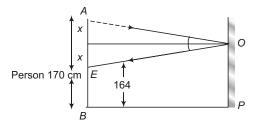
i i $\mathbf{2}$ 45 $\mathbf{2}$ 452 20 2i 45 85

But angle of incidence angle of reflection.

Hence the angle between origial incident and reflected ray was 85. Similarly is the mirror is rotated clockwise the angle became 5.

Hence correct option is (c) 85 or 5.

8. The person see his hair if the incident ray statics from point A after reflected by mirror reach his eyes. Let O is point at minimum at a distance *x* below the point *A*.

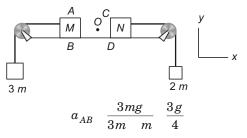


We have 2x = 60 cmx 3 cm The distance of O from P is

> 170 3 167 cm

Hence correct option is (a).

9. Acceleration of block



Acceleration of block CD :

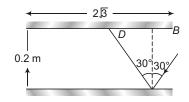
$$a_{CD} = \frac{2mg}{2m m} = \frac{2g}{3}$$

Since the accelerations are in opposite directions relative acceleration of one image with respect to other is given by

$$a_{AB} = a_{CD} = \frac{3g}{4} = \frac{2g}{13} = \frac{17g}{12}$$

Hence the correct option is (c).

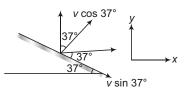
10. Here
$$\frac{BD}{0.2}$$
 tan 30



$$BD \quad 0.2 \quad \frac{1}{\sqrt{3}}$$
 No. of reflections $\frac{2\sqrt{3}}{0.2/\sqrt{3}} \quad 30$

Hence, the correct option is (b).

11. Resolving velocity along parallel to mirror and perpendicular to mirror, we get

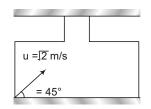


Hence velocity of image is given by

$$\mathbf{v} \quad v_x \,\hat{\mathbf{i}} \quad v_y \,\hat{\mathbf{j}}$$
$$\mathbf{v} \quad 4.8 \,\hat{\mathbf{i}} \quad 1.4 \,\hat{\mathbf{j}}$$

Hence the correct option is (c).

12. Since elevator start falling freely, the relative acceleration of the particle in elevator frame g = g = 0



Hence, in elevator frame path of the particle is a straight line.

The vertical component of velocity is

$$u \sin 45 \quad \sqrt{2} \quad \frac{1}{\sqrt{2}} \quad 1 \text{ m/s}$$

The separation between mirror and particle in 0.5 s is

$$y v_y t = 1 \quad 0.5 \quad 0.5 \text{ m}$$

The separation between image of particle and particle at this moment

2y 2 0.5 m 1 m

Hence the correct option is (b).

13. Here velocity of mirror

$$\mathbf{v}_m$$
 4 $\hat{\mathbf{i}}$ 4 $\hat{\mathbf{j}}$ 8 $\hat{\mathbf{k}}$

and velocity of object

$$\mathbf{v}_o$$
 3 $\hat{\mathbf{i}}$ 4 $\hat{\mathbf{j}}$ 5 $\hat{\mathbf{k}}$

Since $\hat{\mathbf{k}}$ is normal to the mirror hence $\hat{\mathbf{i}}$ and $\hat{\mathbf{j}}$ components of image velocity remain unchanged *ie*, velocity of image can be written as

$$\mathbf{v}_i$$
 3 î 4 ĵ v_{iz} k

but v_{iz} $2u_{mz}$ v_{oz} 2 8 5 11 Hence, we get

$$\mathbf{v}_i$$
 3 $\hat{\mathbf{i}}$ 4 $\hat{\mathbf{j}}$ 11 $\hat{\mathbf{k}}$ (*wrt* ground)

Hence, the correct option is (b).

$3\hat{\mathbf{i}}$ $4\hat{\mathbf{j}}$ $11\hat{\mathbf{k}}$

14. Only option (b) satisfy the given condition.

Here
$$X_0$$
 2, X_i 10
Using $\frac{1}{X_0}$ $\frac{1}{X_i}$ $\frac{1}{f}$

we get

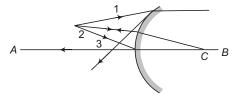
$$\frac{1}{10} \quad \frac{1}{2} \quad \frac{1}{f}$$
$$f \qquad 2.5 \, \mathrm{cm}$$

Hence, the mirror is concave.

We know that
$$y_i = \frac{fy_0}{f = x_0}$$
$$\frac{2.5 \quad 1}{2.5 \quad 2} \quad 5 \text{ cm}$$

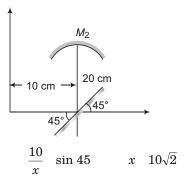
Hence, the correct option is (b).

16. There are two mistakes one in ray (1) and other in ray (3).

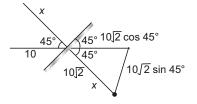


Hence correct option is (b).

17. The image formation by plane mirror is shown as



The x-coordinate is $10\sqrt{2}\cos 45$ 10 and y-coordinate is $10\sqrt{2}\sin 45$ 10



Hence, the convert option if (c), (10, 10).

18.
$$x_i = \frac{fx_0}{x_0 - f} = \frac{10 - 10}{10 - 10} = 5 \text{ cm}$$

For concave mirror
$$f$$
 10 cm.
 $y_i = \frac{fy_0}{f x_0} = \frac{10 \quad 20}{10 \quad 10}$ cm
10 cm

Hence the coordinates of image are (5, 10). Therefore, the correct option is (d). **19.** For convex mirror f 10 cm

$$\begin{array}{cccc} x_i & \frac{fx_0}{x_0 & f} & \frac{10 & 10}{10 & 10} \\ y_i & \frac{fy_0}{f & y_0} & \frac{10 & 20}{10 & 10} \end{array}$$

More than one options are correct

1. Here f = 20 cm

Case 1. (if image is real) u, v and f all are –ve.

Here $m \ 2 \ v \ 2u$

using mirror formula

we get, $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$ $\frac{1}{2u} \quad \frac{1}{u} \quad \frac{1}{20}$ $\frac{3}{2u} \quad \frac{1}{20} \quad u \qquad 30 \text{ cm}$

Case 2. (if image is virtual)

u and f are ve, while v is +ve

$$\frac{1}{2u} \quad \frac{1}{u} \quad \frac{1}{20}$$
$$u \quad 10 \,\mathrm{cm}$$

Hence possible values of u are 10 cm, 30 cm.

The correct options are (a) and (b).

2. Magnitude of focal length spherical mirror is *f* and linear magnification is $\frac{1}{2}$

Since concave mirror fro inverted real image and magnification is less than unity, therefore u = 2f.

Hence option (a) is correct.'

If image is erect than it is a convex mirror.

Let mirror is concave hence focal length

f.

Here $m \quad \frac{1}{2} \quad \frac{v}{u}$

20. It concave mirror is replaced by plane mirror the coordinates are (0, 40).Hence the correct option is (d).

 $v \quad \frac{u}{2}$ Using mirror formula $\frac{1}{u} \quad \frac{1}{v} \quad \frac{1}{f}$, we get $\frac{1}{u/2} \quad \frac{1}{u} \quad \frac{1}{f}$ $\frac{3}{u} \quad \frac{1}{f}$ $u \quad 3f$

Hence, if the mirror is concave the object distance will be 3f.

Let mirror is convex, then

$$m \quad \frac{v}{u} \quad \frac{1}{2} \quad u \quad \frac{v}{2}$$

Using mirror formula, we get

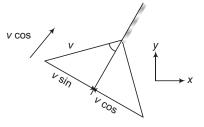
$$\frac{1}{u/2}$$
 $\frac{1}{u}$ $\frac{1}{f}$ u f

Hence, if mirror is convex the object distance will be f.

Hence correct options are (a), (b), (c) and (d).

3. Since by a plane mirror

speed of image speed of object



Hence speed of image also v.

Horizontal component (along mirror)

 $v\cos$

Vertical component (to mirror)

 $v \sin$

Hence image velocity also make an angle with the mirror.

Resolving velocity along (*y*-axis *ie*, parallel to mirror) and (*x*-axis *ie* perpendicular to mirror).

$$\mathbf{v}_0 \quad v \sin \hat{\mathbf{i}} \quad v \cos \hat{\mathbf{j}}$$

 $\mathbf{v}_i \quad v \sin \hat{\mathbf{i}} \quad v \cos \hat{\mathbf{j}}$

Relative velocity of object w.r.t. image is

$$\mathbf{v}_{0i}$$
 \mathbf{v}_0 \mathbf{v}_i $2v\sin$ i

Hence, correct options are (a), (b) and (d).

4.

•

As image is on opposite side of the principle axis (inverter image) hence the mirror is concave because convex mirror always form erect image.

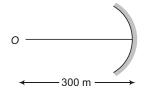
The mirror is lying to the right of *O* and the *O* lies between *C* and *F*.

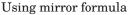
If centre of curvature lies to the right hand side of O then v = u.

Hence, this option is incorrect.

Hence, the correct options are (a), (b) and (d).

5. Here f = 20 cm, u = 30 cm





$$\frac{1}{v}$$
 $\frac{1}{u}$ $\frac{1}{f}$

we get,

Different this w.r.t. time, we get

 $\frac{1}{v^2}\frac{dv}{dt} \quad \frac{1}{u^2}\frac{du}{dt} \quad 0$ $\frac{dv}{dt} \quad \frac{v^2}{u^2} \quad \frac{du}{dt}$

Hence in event (1),

$$\begin{array}{ll} \displaystyle \frac{du}{dt} & v \\ \\ \displaystyle \frac{dv}{dt} & \displaystyle \frac{60^2}{30^2} & v & 4v \end{array}$$

Hence, speed of image in event (1) is 4v. after time *y* coordinate of object $y_0 = v t$

but
$$x_0$$
 30
then $y_i = \frac{fy_0}{f x_0} = \frac{20 \quad v \, t}{20 \quad 30}$
 $y_i = 2vt = 2vt$
 $\frac{dy_i}{dt} = 2v$

Hence, option (b) and (c) are correct.

6. For plane mirror

For concave mirror

u = 3f

Using mirror formula

 $\frac{1}{v} \quad \frac{1}{3f} \quad \frac{1}{f} \quad \frac{2}{3f}$ $v \quad 1.5f$ $|v| \quad 1.5f$

For convex mirror,

$$\frac{1}{v} \quad \frac{1}{3f} \quad \frac{1}{f} \quad \frac{4}{3f}$$
$$v \quad 0.75f$$

Hence maximum distance in event (1) if image is from plane mirror and minimum distance from convex mirror

When v = 1.5f, then v = 1.5f

by plane mirror

For concave mirror

1	1	1	2	1
u	$\overline{1.5 f}$	\overline{f}	$\overline{3f}$	\overline{f}

Match the Columns

1. (a) m 2, since |m| 2 1.

Therefore mirror is concave and :: m is ve.

Hence image is real [for concave mirror m is ve]

Therefore,

(a) q, r

(b) Since
$$m \qquad \frac{1}{2}, \because m$$
 is ve

Hence mirror is concave and image is real.

(b) q, r

(c) $m = 2, \because m = 1$

Hence mirror is concave and :: m is + ve

Hence image is virtual.

(c) q, s
(d)::1m
$$\frac{1}{2}$$
 1 and + ve

Hence the mirror is convex and image is virtual.

(d) p, s

2. Plane mirror (for virtual object) only real image

(a) p

$$\frac{2}{3f} = \frac{3}{3f}$$

$$v = 3f$$

$$|v| = 3f$$

For convex mirror

1	2	1	5
\overline{v}	$\overline{3f}$	\overline{f}	$\overline{3f}$
v	0.6f		

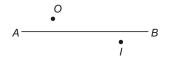
Hence, in event (2) maximum distance of image from the concave mirror.

Hence, correct options are (a), (b) and (c).

(b) r

(c) p

3. (a) Since object and its image are on opposite side of principle axis.



Hence mirror is concave

(a) r.

- (b) Similarly as for option (a).
- (b) r

(c) Since image and object are of same height from AB.

Hence mirror is plane mirror.

(c) p

(d) Since image is magnified.



Hence mirror is concave [D is. distance between O and mirror is less than the focal length].

Hence

(d) r.

- 4. (a) For concave mirror M_1 focal length 20 cmWhen x = 20 cm, Mirror is M_1 v and magnified (a) p, s
 - (b) For convex mirror M_2 of focal length 20 cm if X (distance of object from pole)
 - 20 Using mirror formula $\frac{1}{v} = \frac{1}{v} = \frac{1}{f}$

we get

 $\frac{1}{v} \quad \frac{1}{20} \quad \frac{1}{20} \quad \frac{1}{10} \\ v \quad 10 \text{ cm}$

Hence image is virtual.

(b) r

(c) u = 30 cm, f = 20 cm $\frac{1}{v} = \frac{1}{30} = \frac{1}{20} = \frac{2}{60} = \frac{3}{60}$ v = 60 cm

Hence image is real.

 $m = \frac{60}{30} = 2$

Hence image is magnified (2 times).

(d) for mirror M_2 (convex) at $X \qquad 30~{\rm cm}$ image again virtual.

(d) r

5. (a) For concave mirror f = 20 cm

Case I. Image is real.

 $m 2 \frac{v}{u}$ v 2u $\frac{1}{u} \quad \frac{1}{u} \quad \frac{1}{f}$ Using $\frac{1}{2u} \quad \frac{1}{u}$ 1 we get, $\overline{20}$ 3 1 $\overline{20}$ $\overline{2u}$ $u \quad 30 \,\mathrm{cm}$ If image is virtual v = 2v $\frac{1}{2u}$ 1 20*u* 10 cm Hence correct option are as (a) p, q (b) Here $m = \frac{1}{2} = 1$ Hence image is real. $\frac{1}{2}$ $\frac{v}{u}$ v $\frac{u}{2}$ Using $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$, we get $\frac{1}{u/2} \quad \frac{1}{u} \qquad \frac{1}{20}$ $\frac{3}{4} \quad \frac{1}{20} \quad u \quad 60 \, \mathrm{cm}$ Hence correct option is none of these. (b) \mathbf{s} (c) if m = 1, than u = 2f $40\,\mathrm{cm}$ и

Hence correct option is none of these.

(c) (s)

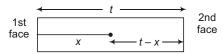
(d) Similarly as in part (b) we see that answer is none of these.

(d) (s)

27 Refraction of Light

Introductory Exercise 27.1

1. Let real depth of dust particle is x and thickness of slab is t



From Ist surface

$$\frac{\text{Real depth}}{\text{App. depth}}$$
1.5 $\frac{x}{6 \text{ cm}}$ x 9 cm ...(i)

From other face

$$\frac{t \ x}{4} \ t \ x \ 4 \ 1.5$$

$$t \ x \ 6 \ 9 \ 6 \ 16 \ cm$$
2. $_{1 \ 2} \ \frac{4}{3} \ \frac{-2}{1} \ \frac{4}{3} \ \dots (i)$
 $_{2 \ 3} \ \frac{3}{2} \ \frac{-3}{2} \ \frac{3}{2} \ \dots \dots (i)$

Introductory Exercise 27.2

 $2. \frac{2}{v} \frac{1}{u} \frac{2}{R}$ 1. Since light rays are coming from glass to air applying $\frac{2}{v}$ $\frac{1}{u}$ $\frac{2}{R}$ R $1 \ 1.5 \ 1 \ 1.5$ v 10 1.5 $\frac{1}{v}$ $\frac{1}{30} \quad \frac{1.5}{10} \quad \frac{1}{30} \quad \frac{4.5}{30}$ $\frac{30}{3.5}$ 8.57 cm v

$$-\frac{3}{1}$$
 $\frac{4}{3}$ $\frac{3}{2}$ 2

3. Frequency remain same.

Let v_1 is velocity in medium (1) and v_2 in Medium (2)

We have

$$\begin{array}{cccc} _{1} & \frac{c}{v_{1}} \text{ and } _{2} & \frac{c}{v_{2}} \\ \\ \frac{-1}{2} & \frac{v_{2}}{v_{1}} & v_{2} & \frac{-1}{2} v_{1} \end{array}$$

Similarly, wavelength $_2 - \frac{1}{1}$

4. From v_a n_a

$$a \frac{v_a}{n_a} \frac{3 10^8}{6 10^{-14}} 5 10^7 m$$

50 nm

$$\frac{a}{m} = \frac{300}{300} = \frac{3}{3} = 1.67$$

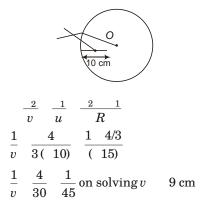
(a)
$$\frac{1.5}{v} = \frac{1}{(20)} = \frac{0.5}{6}$$

On solving $v = 45$ cm
(b) $\frac{1.5}{v} = \frac{1}{(10)} = \frac{0.5}{6}$
On solving we get $v = 90$ cm

(c)
$$\frac{1.5}{v}$$
 $\frac{1}{(3)}$ $\frac{0.5}{6}$

On solving v 6.0 cm

3. Light rays are coming from glass to air



4. Applying
$$\frac{u_2}{v} = \frac{1}{u} = \frac{2}{R}$$

 $\frac{1.44}{v} = \frac{1}{L} = \frac{0.44}{1.25}$
On solving $v = 0.795 \text{ cm}$
5. $\frac{2}{v} = \frac{1}{u} = \frac{2}{R}$
 $\frac{1.635}{v} = \frac{1}{(9)} = \frac{0.635}{(2.50)}$
on solving $v = 6.993 \text{ cm}$
Lateral magnification $m = \frac{v}{u}$
 $\frac{6.993}{9} = 0.777$

Introductory Exercise 27.3

1. We have

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f} \quad (1) \quad \frac{1}{R_1} \quad \frac{1}{R_2}$$

$$\frac{1}{20} \quad \frac{1}{60} \quad (1.65 \quad 1) \quad \frac{1}{R} \quad \frac{1}{R}$$

$$\frac{3}{60} \quad 0.65 \quad \frac{2}{R}$$

$$R \quad 60 \quad 0.65 \quad 39 \text{ cm}$$
2. Using $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$, we get
$$\frac{1}{50} \quad \frac{1}{x} \quad \frac{1}{30} \quad \frac{1}{x} \quad \frac{1}{30} \quad \frac{1}{50}$$
On solving $x \quad 18.75 \text{ cm}$

$$m \quad \frac{v}{u} \quad \frac{50}{18.75}$$
Height of filament image $2 \quad \frac{50}{18.75}$
Height of filament image $2 \quad \frac{50}{18.75}$

$$5.3 \text{ cm}$$
3. $\frac{1}{f} \quad (1) \quad \frac{1}{R} \quad \frac{1}{R}$

If lens faces becomes opposite three is no change in radius of curvature hence focal length does not change.

4. Using formula $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$ when $u = 0_1 v = 0$ when u = f, v hence image moves from surface to .

5.
$$\frac{1}{f}$$
 (1) $\frac{1}{R_1}$ $\frac{1}{R_2}$
 $\frac{1}{f}$ (1.3 1) $\frac{1}{R}$ $\frac{1}{R}$ 0.3 $\frac{2}{20}$
 f $\frac{100}{3}$ cm

(a) When immersed in a liquid of 1.8 refractive index

$$\frac{1}{f_1}$$
 $\frac{1.3}{1.8}$ 1 $\frac{2}{R}$ $\frac{0.5}{1.8}$ $\frac{2}{20}$

f 36 cm

(b) The minimum distance is equal to the focal length 36 cm

6. Using $\frac{1}{v} \cdot \frac{1}{u} \cdot \frac{1}{f}$ $\frac{1}{v} \cdot \frac{1}{(20)} \cdot \frac{12}{10}$

On solving v = 20 cm

Magnification $\frac{v}{u} = 1$

Hence the image of same size and inverted. Let the distance between second lens is xSince magnification is unity image distance also x using again

$$\frac{1}{v}$$
 $\frac{1}{u}$ $\frac{1}{f}$

we get

$$\frac{1}{x} = \frac{1}{(x)} = \frac{1}{f} = \frac{1}{10} = x = 20 \,\mathrm{cm}$$

Hence the distance between two lenses

$$20 \text{ cm } 20 \text{ cm } 40 \text{ cm}$$
7. $\frac{1}{v}$ $\frac{1}{f}$ $\frac{1}{u}$...(i)
 $\frac{1}{v_1}$ $\frac{1}{f}$ $\frac{1}{u}$ du ...(ii)
 $\frac{1}{v}$ $\frac{1}{v}$ $\frac{(u \ du \ u)}{(u \ du)u}$ on solving, we get
 $\frac{v \ v}{v}$ $\frac{du}{u(u \ du)}$ thickness dv $\frac{v^2}{u^2} du$
10. Size of image $\sqrt{6 \ \frac{2}{3}} \ 2 \text{ cm}.$
11. Let image distance is u

$$|m| \ 3 \ v \ 3u$$

$$\frac{1}{3u} \quad \frac{1}{u} \quad \frac{1}{12} \quad v \quad 16 \, \mathrm{cm}$$

12. Since image is upright and diminished hence lens is concave. Now

$$u \quad v \quad 20 \qquad \dots(i)$$

$$m \quad \frac{v}{u} \quad \frac{1}{2}$$

$$\frac{1}{2} \quad \frac{u \quad 20}{u}$$

$$u \quad 40 \text{ cm and } v \quad 20 \text{ cm}$$
Using
$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$

$$\frac{1}{20} \quad \frac{1}{40} \quad \frac{1}{f} \quad f \quad 40 \text{ cm}$$

13. The image coincide itself if light falls normally on plane mirror hence object must be on focus *i.e.* 10 cm.

8.
$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{2(2)}{R_2} \quad \frac{2(2)}{R_1} \quad \frac{1}{R_1}$$

 $\frac{1}{v} \quad \frac{1}{0.2} \quad \frac{2(4/3)}{0.4} \quad \frac{2(4/3-1)}{0.4}$

On solving $v = 12 \,\mathrm{cm}$

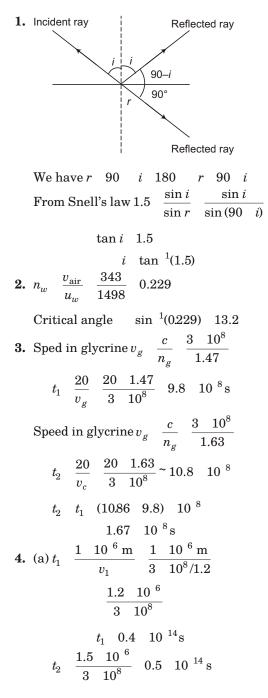
9. Since shift in position t = 0.1 m

Hence real depth $(0.1 \quad 0.2)$ m

 $0.3 \mathrm{m}$

and apparent depth 0.2 mreal depth apparent depth $\frac{0.3}{0.2}$ 1.5

AIEEE Corner



t_3	$\frac{1}{3}$	$\frac{10^{-6}}{10^8/1.8}$	$\frac{1.8}{3}$	$\frac{10}{10^8}$	6 — 0	.6	10 14
Hence t	t_1 is	least an	d t_1	0.4	10^{-1}	4 s	
(b) Tota	al nu	umber o	f wav	eleng	gths		
		1 m	1.5	m	1 m	ı	
		$/n_1$	//	\imath_2	$/n_{3}$	-	
		1000	$1.2 \mathrm{r}$	nm	1.5	10	0 nm
		60	0 nm		60	00 r	ım
				1	1.8	10	000 nm
					60	0 m	m
		$\frac{4500}{600}$	7.5				

5. The given wave equation is

$$E_x(y,t) \quad E_{ax} \sin \frac{2 y}{5 \cdot 10^{-7}} \quad 3 \quad 10^{14} \quad 2 t$$

Comparing with standard equation

$$E_{x}(y,t) = E_{0} \sin [ky = t]$$

$$k = \frac{2}{5 - 10^{-7}} = 2 = 3 - 10^{14}$$

$$v = \frac{2}{k} = \frac{3 - 10^{14}}{2 - 5 - 10^{-7}} = 1.5 - 10^{8} \text{ m/s}$$
Refractive index $n = \frac{c}{v} = \frac{3 - 10^{8}}{1.5 - 10^{8}} = 2$
Wavelength in this way $n = \frac{2}{k}$

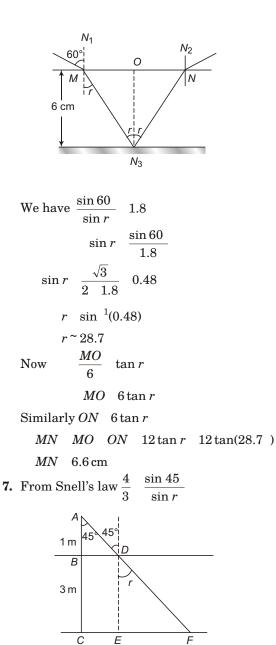
$$n = \frac{2}{25/5 - 10^{-7}} = 5 - 10^{-7} \text{ m}$$

$$n = 500 \text{ nm}$$
If vacuum, wavelength is then

 $n \frac{n}{n}$

n _{*n*} 2 500 1000 nm

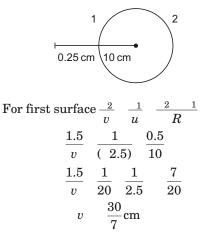
6. Refraction from plane and spherical surfaces



- Solving we get r = 32
 - EF $DE \tan r$ $3 \tan 32$

1.88 m

Total length of shadow 1 1.88 2.88 m **8.** The situation is shown in figure

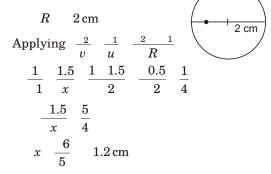


This image acts as a virtual object for 2nd surface

	u	2	20	$\frac{30}{7}$	-	$\frac{170}{7}$ cm
and		R	10	cm		
	2	1	2	1		
	υı	ı	r			
1	1.5		0.5	ó		
\overline{v}	170/	$\overline{7}$	10	_		
		1	1	10.5		
		v	$\overline{20}$	170		
		v	85	cm		

Hence final image will produced at 65 cm from Ist surface.

9. Here v = 1 cm



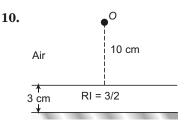


Image formed by refection acts the virtual object for the mirror.

Here shift $t \ 1 \ \frac{1}{-}$

$$3\ 1\ \frac{1}{3/2}$$
 1 cm

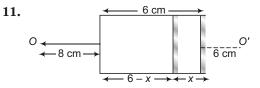
Hence object appear to the mirror

(10 1) cm

 $11\,\mathrm{cm}$

The image formed by mirror 11 cm

Hence image formed by the mirror at 11 cm behind the mirror.



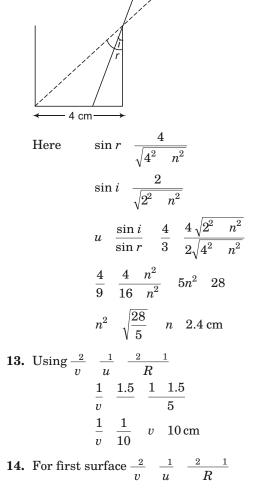
Step. Let shift in mirror is *x* then the distance of object.

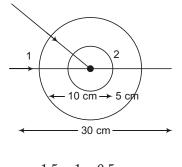
From the mirror is 8 (6 *x*).

Step II. Plane mirror form image behind the mirror at same distance as the distance object from mirror hence

$$8 \quad (6 \quad x) \quad x \quad 6 \quad x \quad 4 \text{ cm}$$
Step III.
$$\frac{\text{real depth}}{\text{app. depth}} \quad \frac{6}{4} \quad 1.5$$

hence real position of the bubble inside sphere is 1.2 cm from the surface.





 $\frac{1.5}{v} = \frac{1}{v} = \frac{0.5}{10} = v = 30 \,\mathrm{cm}$

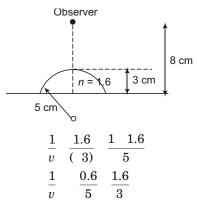
12.

For 2nd surface

$$\frac{1}{v} \quad \frac{1.5}{(15)} \quad \frac{0.5}{5} \\ \frac{1}{v} \quad \frac{1}{10} \quad \frac{1}{10} \quad v \qquad 5 \text{ cm}$$

Hence the distance from first face is

15. Since rays goes from paper weight (n 1.6) to air hence



On solving we get v = 0.58 |v| = 0.58 cm Hence the distance between observer and table top is (8 = 0.58) cm = 7.42 cm.

16. Let real velocity of bird $v_B \text{ cm/s}$

Velocity of bird w.r.t. fish 16 cm/s

Velocity of bird w.r.t. water v_B

But
$$v_B = v_f = 16 \,\mathrm{cm/s}$$

Here
$$v_f = 4 \text{ cm/s}$$

$$\frac{4}{3}v_B \quad 4 \quad 16$$
$$\frac{4}{3}v_B \quad 12 \text{ cm/s}$$

$$v_B \quad 9 \text{ cm/s}$$

17. Let the distance between the object and screen is d and let distance between object and lens is x

Using lens formula $\frac{1}{v}$ $\frac{1}{u}$ $\frac{1}{f}$ we get $\frac{1}{d x} \frac{1}{(x)} \frac{1}{16}$ $x^{2} xd \quad 16d \quad 0$ $x \quad \frac{d \sqrt{d^{2} \quad 64d}}{2}$ Let $x_{1} \quad \frac{d \quad \sqrt{d^{2} \quad 64d}}{2}$ and $x_{2} \quad \frac{d \quad \sqrt{d^{2} \quad 64d}}{2}$ $x_{1} \quad x_{2} \quad \sqrt{d^{2} \quad 64d}$ But $x_{1} \quad x_{2} \quad 60 \quad d^{2} \quad 64d \quad 3600 \quad 0$ $(d \quad 100) (d \quad 36) \quad 0$ $d \quad 100 \because d \quad 36$

Hence the distance between object and screen is 100 cm.

18.
$$:: \frac{1}{f}$$
 (*n* 1) $\frac{1}{R_1}$ $\frac{1}{R_2}$

For identical double convex lens $|R_1| |R_2| R$

but
$$R_1 R \text{ and } R_2 R$$

 $\frac{1}{f} (n 1) \frac{1}{R} \frac{1}{R} (n 1) \frac{2}{R}$
 $f \frac{R}{2(n 1)} \text{ hence } f_1 \frac{R}{2(1.5 1)} R$
and $f_2 \frac{R}{2(1.7 1)} \frac{R}{1.4}$
(a) $\frac{f_1}{f_2} 1.4 f_1 : f_2 1.4 : 1$
(b) For first lens

$$f_i = rac{R}{2 \; rac{1.5}{1.6} \; 1} = rac{1.6R}{2 \; 1} = 8R$$

hence first lens become concave (diverging) For 2nd lens

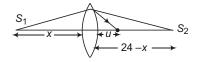
$$f_2 = rac{R}{2 \; rac{1.7}{1.6} \; 1} \; \; rac{1.6R}{2 \; \; 0.1} \; \; 8R$$

Hence 2nd lens remain convex.

19. Here *u* 10 cm acts the virtual object for the lens *v* 15 cm using $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$ $\frac{1}{15} \quad \frac{1}{10} \quad \frac{1}{f}$

On solving we get f = 30 cm.

20. Situation is shown in figure.



For Ist source direction left to right is ve Using $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$, we get $\frac{1}{v} = \frac{1}{(x)} = \frac{1}{9} = \frac{1}{v} = \frac{1}{x} = \frac{1}{9} = \dots(i)$

For 2nd source direction right to left is ve

hence
$$\frac{1}{v} = \frac{1}{24 x} \frac{1}{9}$$
 ...(ii)

On adding Eqs. (i) and (ii) we set

 $\frac{1}{x} \quad \frac{1}{24} \quad x \quad \frac{2}{9} \quad x^2 \quad 24x \quad 108 \quad 0$

hence lens can be placed at a distance of 6 cm from any source.

21. Since the object is placed at *c* of first lens hence image also form at *c* and of same magnification *i.e.v* 2*f*. Since two lens are separated by distance *f* hence the distance between 2nd lens and image is *f*. This image acts a virtual object for this lens using $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$, we get $\quad \frac{1}{v} \quad \frac{1}{f} \quad v \quad \frac{f}{2}$ and magnification $m_2 \quad \frac{v}{u} \quad \frac{f/2}{f} \quad \frac{1}{2}$

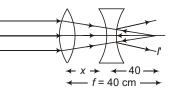
Hence image is formed at $\frac{f}{2}$ right of 2nd lens.

22. Since the object is placed at 2*f* hence image also form 2*f* by lens *i.e.*, at 60 cm. The mirror must be placed at that place that it made the final image at focus of lens. The difference is shown below.

$$O \xrightarrow{30 \text{ cm } f}_{I} = I$$

Hence the distance between lens and mirror 40 cm 15 cm 45 cm

23. The diagram is shown in figure.



The parallel ray after refraction on convergent lens meet at focus 40 cm. Let distance between two lenses is *x* then using $1 \quad 1 \quad 1 \quad x$

 $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$ for diverging lens

$$\frac{1}{(40 \ x)} \quad \frac{1}{15}$$

$$x 25 \,\mathrm{cm}$$

24. Here $f_1 = 20 \text{ cm } f_2 = 10 \text{ cm and } d = 30 \text{ cm}$

$$f_{1} = 20 \text{ cm} \quad f_{2} = 10 \text{ cm}$$

$$O \longrightarrow 30 \text{ cm} \longrightarrow 30 \text{ cm} \longrightarrow l_{1}$$

$$O \longrightarrow 0 \longrightarrow 1$$

$$O \longrightarrow 0 \longrightarrow 0$$

$$O \longrightarrow 0$$

26

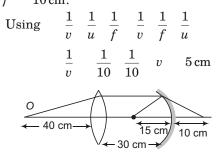
For 2nd lens

 $\frac{1}{v} \quad \frac{1}{30} \quad \frac{1}{10} \\ \frac{1}{v} \quad \frac{1}{30} \quad \frac{1}{10} \\ \frac{1}{v} \quad \frac{4}{30} \\ v \quad 7.5 \text{ cm}$

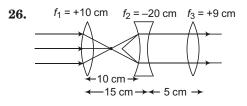
Hence image formed at 7.5 cm from 2nd lens.

25. For lens u 40 cm f 20 cm using $\frac{1}{v}$ $\frac{1}{u}$ $\frac{1}{f}$ $\frac{1}{v}$ $\frac{1}{f}$ $\frac{1}{u}$ $\frac{1}{v}$ $\frac{1}{f}$ $\frac{1}{u}$ $\frac{1}{v}$ $\frac{1}{20}$ $\frac{1}{40}$ $\frac{2}{40}$ $\frac{1}{40}$ v 40 cm

Hence the image is at 40 cm right from the lens. Since distance between mirror and lens is 30 cm. Hence for mirror v = 10 cm, f = 10 cm.



Hence image is formed at 5 cm from the mirror toward lens.



For first lens v10 cmFor 2nd lens u5 cm, f20 cm

Using
$$\frac{1}{v}$$
 $\frac{1}{u}$ $\frac{1}{f}$
 $\frac{1}{v}$ $\frac{1}{20}$ $\frac{1}{5}$
 v 4 cm
For third lens v 9 cm and f 9 cm
 $\frac{1}{v}$ $\frac{1}{(9)}$ $\frac{1}{9}$
 v

Hence the image formed at or rays become parallel.

27. Situation is shown in figure when space between two convex lenses is filled with refractive index 1.3 it become a concave lens of radii R_1 30 cm and R_2 70 cm hence it focal length is

$$\frac{1}{f} (n \ 1) \frac{1}{R_1} \frac{1}{R_2}$$

$$\frac{1}{f} (1.3 \ 1) \frac{1}{30} \frac{1}{70}$$

$$f \ 70 \text{ cm}$$

Hence the equivalent focal length of combination $\frac{1}{F}$ $\frac{1}{30}$ $\frac{1}{70}$ $\frac{1}{70}$

 $F = 30 \,\mathrm{cm}$ if

$$\begin{array}{cccc} u & 90 \, \mathrm{cm} \, \mathrm{then} \, \mathrm{using} \\ \frac{1}{F} & \frac{1}{v} & \frac{1}{u} \\ \mathrm{we} \, \mathrm{get} \, \frac{1}{30} & \frac{1}{v} & \frac{1}{90} \\ & \frac{1}{v} & \frac{1}{30} & \frac{1}{90} & \frac{2}{90} & \frac{1}{45} \\ & v & 45 \, \mathrm{cm} \end{array}$$

28.
$$n_{ice} = \frac{c}{v} = \frac{3}{2.3} \frac{10^8}{10^8} = 1.30$$

 $c = \sin^{-1} \frac{1}{n_{ice}} = \sin^{-1} \frac{1}{1.30}$ $\sin^{-1}(0.77)$

29. (a) Let angle of refraction in material 2 is
$$r$$

then $\frac{\sin}{\sin r} = \frac{1.8}{1.6} = \frac{18}{16} = \dots$ (i)

For (2) to (3) interface

$$\frac{\sin r}{\sin 90} = \frac{1.3}{1.8} = \frac{13}{18}$$

$$\sin r = \frac{13}{18} = \dots.(ii)$$
From (i) and (ii) sin = $\frac{18}{16} = \frac{13}{18}$

 $\sin \ ^1 \ \frac{13}{16}$

30. Let maximum height of liquid is *h*. From figure for critical angle *C*

$$\frac{1}{\sin C} \quad \frac{\sqrt{r^2 \quad h^2}}{r} \qquad \dots (i)$$

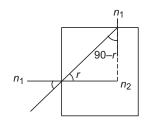
Here $r \quad 1 \text{ cm and} \quad \frac{4}{3}$ putting these
values in Eq. (i). Solving we get $h \quad \frac{4}{3} \text{ cm}$

Here $\sin_c \frac{1}{g} \frac{2}{3}$

Now if water film is poured on the glass air surface. Let emergent angle at glass water surface is *r*, then

$$\frac{\sin c}{\sin r} \quad \frac{w}{g} \quad \frac{4}{3} \quad \frac{2}{3}$$
$$\sin r \quad \frac{9}{8} \sin c \quad \frac{9}{8} \quad \frac{2}{3} \quad \frac{3}{4}$$
$$r \quad \sin^{-1} \frac{3}{4}$$

32. For total internal reflection at top surface



$$\frac{\sin (90 \quad r)}{\sin 90} \quad \frac{n_1}{n_2}$$

$$\cos r \quad \frac{n_1}{n_2}$$
and
$$\frac{\sin r}{\sin r} \quad \frac{n_2}{n_1}$$

$$\sin \quad \frac{n_2}{n_1} \sin r$$

$$\sin \quad \frac{n_2}{n_1} \sqrt{1 \quad \cos^2 r}$$

$$\frac{n_2}{n_1} \sqrt{1 \quad \frac{n_1}{n_2}^2}$$

$$\sin \quad \sqrt{\frac{n_2^2 \quad n_1^2}{n_1^2}}$$

$$\sin \quad \sqrt{\frac{n_2^2 \quad n_1^2}{n_1}} = 1$$

33. The deviation angle vary from 0° to where 90 c ...(i)

where *C* is the critical angle 4/2

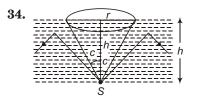
Now,
$$\sin c - \frac{w}{g} = \frac{4/3}{3/2} = \frac{8}{9}$$

From Eq. (i) $\cos \sin C$

$$\cos \frac{8}{9}$$

$$\cos \frac{1}{9} \frac{8}{9}$$

Hence deviation angle vary from 0° to $\cos^{1}\frac{8}{9}$.

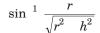


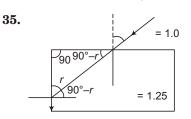
(a) Only circular patch light escapes because only those rays which are incident within a cone of semivertex angle C [Critical angle] are refracted out of the water surface. All other rays are totally internally reflected as shown in figures

 h^2

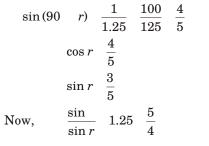
(b) Now
$$\frac{1}{\sin C} \frac{\sqrt{r^2}}{r}$$

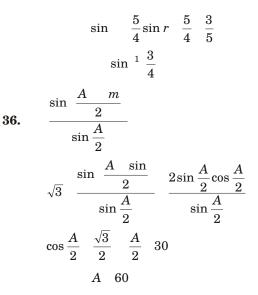
or $C \sin^{-1} \frac{1}{r}$





For maximum angle the angle 90 r at left surface must be equal to critical angle

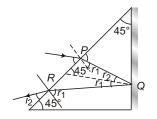




37. Here $i_1 \quad r_1 \quad 0$.

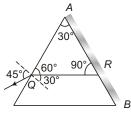
÷

Now, let other face angle of incidence is r_2



Hence the ray retrace its path.

39.



The ray retrace its path from ref. by surface 90 from geometry it is AB hence ARclear that r 30 sin *i* $\sin r$ $1/\sqrt{2}$ $\sin 45$ 1/2 $\sin 30$ 40. Depends on formula. **41.** The maximum angle will be A = 2C where Cis the critical angle $\alpha \rightarrow 1 1$ 41 01 ът

 $\sqrt{2}$

Now,
$$C \sin^{-1} \frac{1.5}{1.5}$$
 41.81
Hence $A \ 2C \ 2 \ 41.81 \ 83.62$
42. $\frac{\sin \frac{A}{2}}{\sin \frac{A}{2}}$ here $A \ 60$
 $1.5 \ \frac{\sin \frac{60}{2}}{\sin 30}$
 $0.75 \ \sin \frac{60}{2}$
 $60 \ _{m} \ 2\sin^{-1}(0.75)$
 $_{m} \ 22.8$
and not deviation 180 22.8 157.2
(b) If the system is placed in water
 $\frac{1.5}{4/3} \ \frac{4.5}{4}$
 $60 \ _{m} \ 2\sin^{-1}(1.125 \ \sin 30)$
 $_{m} \ 2\sin^{-1} \frac{1.125}{2} \ 60$
Net deviation 180 $_{m} \ 128.4$
43. $\frac{V \ R}{2}$

 $\frac{V}{V}$ $\frac{R}{1}$ $0.0305 \quad \frac{1.665 \quad 1.645}{1.645}$ 1 ν

On solving we get y = 1.656**44.** $\frac{1}{f_1}$ $\frac{2}{f_2}$ 0 $\frac{0.18}{20}$ 0.18 30 $\frac{2}{30}$ $\mathbf{2}$ 20 0.272 Now, $\frac{1}{F} \quad \frac{1}{f_1} \quad \frac{1}{f_2} \quad \frac{1}{F} \quad \frac{1}{20} \quad \frac{1}{30}$ F60 cm **45.** $\frac{1}{f_1}$ $\frac{2}{f_2}$ 0 $\frac{1}{2} \quad \frac{f_1}{f_2}$ $\frac{3}{2} \quad \frac{f_1}{f_2}$ $f_1 = \frac{3}{2}f_2$ Now, $\frac{1}{F} \quad \frac{1}{f_1} \quad \frac{1}{f_2}$ $rac{1}{150} \ rac{1}{f_2} \ rac{2}{3f_2}$ f_2 50 cm and f_1 $75\,\mathrm{cm}$ $\frac{\sin i_1}{\sin r_1}$ 46. Applying Find angle r_1 for two different refraction indices. Because i_1 65 from both the cases. Then again apply $\frac{\sin i_2}{1}$ and find i_2 . Because $r_2 \quad A \quad r_1$. sin r₂ Then apply : $(i_1 \quad i_2) \quad A$

> for two refraction indices. Then difference in deviations is :

> > 1 2

...(ii)

Objective Questions (Level-1)

- **1.** Endoscope is bases on total internal refraction Hence, correct option is (c)
- **2.** Here $A = \frac{B}{2}$

÷

is dimensionless.

 $\frac{B}{2}$ dimension of

 B^{2} B has dimension of Area

Hence, correct option is (d).

3. Shift $1 \frac{1}{2}$

 \therefore R is minimum. than other visible colour. Red colour least raised.

correct option is (c)

4. Critical angle $_C \sin^{-1} \frac{1}{2}$

 \therefore 0 is maximum for violet colour hence *c* for violet colour is least.

Hence correct option is (d)

5. We have $P = \frac{1}{f(\text{metre})}$ $\frac{100}{f(\text{cm})} = 100 \quad (n = 1) \quad \frac{1}{R} = \frac{1}{r}$ $P = \frac{100 \quad 0.6 \quad 2}{10} = 12$

Hence, correct option is (a).

6. Speed of light in water $\frac{c}{c}$

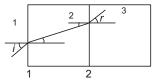
$$v_w = \frac{3 \quad 10^8}{4/3} = 2.25 \quad 10^8 \text{ m/s}$$

Hence correct option os (c).

7. Due to TIR emergent beam will turn into black.

Hence correct option is (c).

- *v n* but frequency *n* remain constant and *v* decreases hence decreases.
 Hence correct option is (b).
- 9. Using Snell's law



 \sin

sin r

On first and 2nd interface

$$\frac{\sin i}{\sin} \frac{2}{1}$$
 ...(i)

3

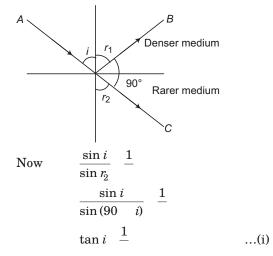
2

Multiplying (i) and (ii), we get

$$\frac{\sin i}{\sin r} \quad \frac{3}{1}$$

Hence correct option is (b).

10. We have
$$i r_1$$
 and r_2 90 i



If C is the critical angle then C $\sin^{-1} \frac{1}{2}$

$C \sin^{-1}(\tan i)$

Hence correct option is (a).

 Let angle of minimum deviation is m we know that

$$\frac{\sin \frac{A}{2}}{\sin \frac{A}{2}}$$

$$\sqrt{2} \quad \frac{\sin \frac{(60 \quad m)}{2}}{\sin 30}$$

$$\frac{1}{\sqrt{2}} \quad \sin \frac{60 \quad m}{2}$$

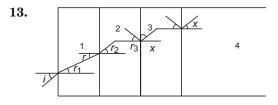
$$\frac{60 \quad m}{2} \quad 45 \quad m \quad 30$$

Hence correct option is (a).

12. We know that

Let refractive index of the liquid s n_l

Hence correct option is (b).



We have,
$$\frac{\sin i}{\sin r_1}$$
 $\frac{-1}{\cdots}$...(i)

$$\frac{\sin r_1}{\sin r_2} \quad \frac{2}{1} \qquad \qquad \dots (ii)$$

and
$$\frac{\sin r_2}{\sin r_3} - \frac{3}{2}$$
 ...(iii)
 $\frac{\sin r_3}{\sin x} - \frac{4}{3}$...(iv)

Multiplying (i), (ii), (iii) and (iv), we get

$$\frac{\sin i}{\sin x} \quad \frac{4}{2} \quad \sin x \quad -\frac{1}{4} \sin i$$

Hence correct option is (b)

14. Let radius of curvature of the lens is \boldsymbol{R}

then
$$\frac{1}{f}$$
 (*n* 1) $\frac{1}{R}$ $\frac{1}{R}$ f $\frac{R}{2(x-1)}$

Let focal length of one part is f

then
$$\frac{1}{f}$$
 $(n \ 1)$ $\frac{1}{R}$ $\frac{1}{k}$
 f $\frac{R}{(n \ 1)}$ $2f$

The focal length of the combination is

 $\frac{1}{F} \quad \frac{1}{2f} \quad \frac{1}{2f} \quad \frac{1}{2f} \quad \frac{1}{2f} \quad F \quad \frac{f}{2}$

Hence correct option is (b).

15. Here
$$P$$
 5D f 20 cm

$$\frac{1}{20}$$
 (1.5 1) $\frac{1}{R_1}$ $\frac{1}{R_2}$...(i)

and
$$\frac{1}{100} = \frac{1.5}{n_e} = 1 - \frac{1}{R_1} - \frac{1}{R_2} = \dots$$
...(ii)

Dividing Eq. (ii) by (i)
$$\frac{1}{5} - \frac{\frac{1.5}{n_l}}{0.5} - \frac{1}{10} - \frac{1}{10} - \frac{1}{n_l} - \frac{1}{n_l} - \frac{1}{n_l} - \frac{1}{n_l} - \frac{1}{3} - \frac{1}{3}$$

Hence correct option is (b).

16. We know that

$$\frac{1}{F} \quad \frac{1}{f_1} \quad \frac{1}{f_2} \quad \frac{d}{f_1 f_2}$$

 \therefore whole system is concave F = 0

$$\frac{d}{f_1 f_2} \quad \frac{1}{f_1} \quad \frac{1}{f_2} \quad d \quad f_1 \quad f_2$$

d (10 20) cm d 30 cm

Hence only possible value of the given values is 40 cm.

Hence correct option is (d).

17. Since when A 2_c total light is reflect (TIR) take place hence maximum value of A is 2 $_c$.

Hence correct option is (c).

- **18.** \therefore emergent ray is to the surface
 - $i_2 r_2 0$ r_1 r_2 A r_1 A÷ sin i Now $\sin A$

Since *i* and *A* are small

$$\sin i \sim i \text{ and } \sin A \sim A$$
$$\frac{i}{A} \quad i \quad A$$

Hence correct option is (c).

19.

$$\cdot \quad \frac{\sin \frac{A_m}{2}}{\frac{\sin \frac{A}{2}}{\sin \frac{A}{2}}}$$

$$\cot \quad \frac{A}{2} \quad \frac{\sin \quad \frac{A}{2}}{\sin \frac{A}{2}}$$

$$\frac{A}{2} \quad 90 \quad \frac{A}{2}$$

$$A \quad 180 \quad A$$

$$m \quad 180 \quad 2A$$

Hence correct option is (d).

20. Minimum deviation condition

$$r_{1} r_{2} r 90 r 90 r A 180$$

$$A 2r$$

$$r \frac{A}{2} 30$$
Now
$$\frac{\sin i}{\sin r}$$

$$\sqrt{2} \frac{\sin i}{\sin 30}$$

$$\sin i \frac{1}{\sqrt{2}}$$

$$i 45$$

~~

Hence correct option is (a).

21.
$$\frac{1}{F} = \frac{1}{f_1} = \frac{1}{f_1} = \frac{d}{f_1 f_2}$$
 ...(i)
 $= \frac{1}{2F} = \frac{1}{f_1} = \frac{1}{f_2} = \frac{2d}{f_1 f_2}$...(ii)
 $= \frac{1}{2F} = \frac{1}{f_1} = \frac{1}{f_2} = \frac{4d}{f_1 f_2}$ (iii)

$$\frac{1}{F} = \frac{1}{f_1} = \frac{1}{f_2} = \frac{1}{f_1 f_2}$$
 ...(iii)

On solving (i), (ii) and (iii) we get F2F.

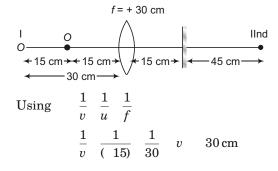
Correct option is (a).

22.
$$\left| \frac{1}{f} \right| (n \quad 1) \left| \frac{1}{R_1} \quad \frac{1}{R_2} \right|$$

$$\frac{1}{24} (1.5 \quad 1) \left| \frac{1}{R} \quad \frac{1}{2R} \right|$$
$$\frac{1}{24} \quad \frac{0.5}{2R} \quad R \quad 6 \text{ and } 2R \quad 12$$

Hence correct option is (a).

23. The system is shown in figure.



This image I_1 act as a virtual object for mirror since plane mirror form image at same distance as object. Hence the distance between object and image is (30 45) cm 75 cm.

Hence correct option is (c).

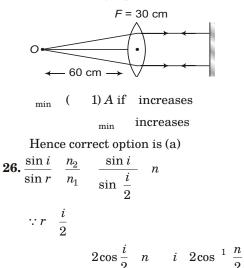
24.
$$\frac{\sin 45}{\sin r_1} \sqrt{3}$$
 ...(i)

 r_{2} 30

 $\frac{\frac{\sin r_1}{\sin r_2}}{\frac{\sin 2}{\sin r_2}} \sqrt{\frac{2}{3}}$ Multiplying Eq. (i) and (ii) $\frac{\sin 45}{\sin r_2} \sqrt{2}$ $\sin r_2 \quad \frac{1}{2}$

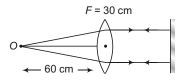
Hence correct option is (a).

25. For small angle prism



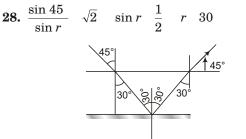
Hence correct option is (c).

27. Situation is shown in figure.



Since image after reflection form on object itself hence the object must be placed at focus of the lens. The rays after refraction by lens becomes parallel to optic axis. Hence reflection rays follow the same path and final image form on x itself. Hence x = 30 cm.

Correct option is (b).



hence total deflection 45 (45) 90 Hence correct option is (a).

29.
$$\frac{\sin \frac{A}{2}}{\sin \frac{A}{2}}$$

$$\sqrt{\frac{3}{2}} \quad \frac{\sin \frac{90}{2}}{\sin 45}$$

$$\sin \frac{90}{2} \quad \frac{\sqrt{3}}{2} \quad \sin 60$$

$$m \quad 30$$

Hence correct option is (c)

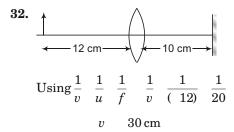
30.
$$\frac{1}{f}$$
 $(n \ 1)$ $\frac{1}{R_1}$ $\frac{1}{R_2}$
here $n \ \frac{n_{\text{air}}}{n_{\text{glass}}}$ $\frac{1}{1.5}$
 $\frac{1}{f}$ $\frac{1}{1.5}$ $1 \ \frac{1}{10}$ $\frac{1}{10}$

f 15 cm. Hence lens is concave Correct option is (a). **31.** For lens u 12 cm and F 10 cm We have $\frac{1}{v}$ $\frac{1}{u}$ $\frac{1}{f}$ $\frac{1}{v}$ $\frac{1}{12}$ $\frac{1}{10}$ v 60 cm

> Since the distance between lens and mirror is 10 cm. Hence the image formed 50 cm from convex mirror. The rays retrace its path if image is formed at the centre of curvature of the mirror *i.e.*,

$$R_{\rm convex}$$
 50 cm F $\frac{R}{2}$ 25 cm

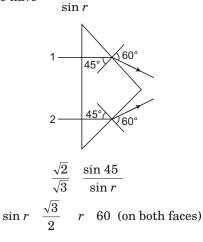
Hence the correct option is (b)



Hence the distance between mirror and this image is 40 cm. Therefore second image formed 40 cm behind the mirror.

Hence correct option is (c). $\sin i$

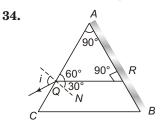
33. We have



Hence the angle between emergent ray

90 (30 30) 30

Hence correct option is (b).



Since the ray retrace its path hence ARQ = 90 RQN = r = 30 $\frac{\sin i}{\sin r}$ $\sin i = \sin r = \sqrt{2} = \sin 30$ $\sin i = \frac{1}{r} = i = 45$

$$\sin i \frac{1}{\sqrt{2}}$$
 i 45

Hence correct option is (c).

the focal length of $\frac{1}{F}$ $\frac{1}{10}$ $\frac{1}{10}$ F 5 cm Here u 7.5 cm, F 5 cm $\frac{1}{v}$ $\frac{1}{7.5}$ $\frac{1}{5}$ $\frac{1}{v}$ $\frac{7.5}{7.5}$ $\frac{5}{5}$ v 15 cm Hence $|m| \left| \frac{v}{u} \right|$ $\frac{\text{height of image}}{\text{height of object}}$ $\frac{15}{7.5}$ Height of image 2 1 cm 2 cm Hence correct option is (a). **36.** $\frac{n_2}{v}$ $\frac{n_1}{u}$ $\frac{n_2}{R}$ $\frac{1}{v}$ $\frac{3}{2}$ $\frac{1}{(v)}$ $\frac{(3/2 - 1)}{20}$ v 40 cm

Hence correct option is (a).

37.
$$\frac{1}{f} = \frac{n_g}{n_L} = 1 = \frac{1}{R_1} = \frac{1}{R_2}$$

Here R_1 30 cm and R_2 50 cm

$$\frac{1}{f}$$
 $\frac{1.5}{1.4}$ 1 $\frac{1}{30}$ $\frac{1}{50}$

On solving

f 1050 cm

Hence correct option is (d).

38. From the figure, it is clear that $1 \qquad 3 \qquad 2$

Hence correct option is (b).

Here A 60, m 60

$$\frac{\sin \frac{A}{2}}{\sin \frac{A}{2}} \frac{\sin 60}{\sin 30}$$

$$\frac{\sqrt{3}/2}{\frac{1}{2}} \sqrt{3}$$

Hence correct option is (a).

JEE Corner

39.

Assertion and Reason

1. Due to shifting of image on refraction Shayam appear nearer to Ram and light suffer two refraction. Hence, both (a) and (b) are correct but reason does not explain the assertion.

Correct option is (b).

2. Applying lens formula

÷

$$\frac{1}{v}$$
 $\frac{1}{u}$ $\frac{1}{f}$

Let u object distance from lens

 $v \quad d \quad u$ distance of image from lens.

$$v \quad u \quad d$$

$$\frac{1}{d \quad u} \quad \frac{1}{u} \quad \frac{1}{f}$$

$$u^2 \quad du \quad df \quad 0$$

$$u \quad \frac{d \quad \sqrt{d \quad 4f}}{2}$$

 $:: u ext{ is real hence } d ext{ 4} f$

Thus mean distance v = 4f, if

u = 2f, v = 2f. Hence both assertion and reason are true, and reason explain or may not explain assertion. Hence correct option is (a, b)

- **3.** Correct option is (b).
- 4. Correct option is (c).

- **5.** Since both assertion and reason are true built reason is not explain assertion Hence correct option is (b).
- 6. Using mirror formula.

$$\frac{1}{v}$$
 $\frac{1}{u}$ $\frac{1}{f}$

Here u

$$\frac{f}{v} = \frac{f}{f} \quad f \text{ (concave lens)}$$

$$\frac{1}{v} = \frac{1}{f}$$

$$v = f$$

Hence image is formed at principle focus thus assertion is false but reason is true. Hence correct option is (d).

.2

7.
$$\frac{\sin \frac{A_m}{2}}{\sin \frac{A}{2}}$$

$$\sin A / 2$$

Here A

$$\frac{\sqrt{2}}{\sqrt{2}} \quad \frac{\sin \frac{60}{2}}{\sin 30} \\
\frac{60}{2} \quad 450 \quad m \quad 30$$

60

Hence both assertion and reason are true and reason explain assertion correctly.

Correct option is (a).

8. Focal length of combination

$$\frac{1}{F} \quad \frac{1}{F_{\text{convex}}} \quad \frac{1}{F_{\text{convex}}} \quad \frac{1}{f_1} \quad \frac{1}{f_2}$$
if
$$f_1 \quad f_2$$

$$\frac{1}{f_1} \quad \frac{1}{f_2}$$

$$F \quad \text{negative}$$

Hence assertion is true. Since power is a measure of converging or divergence of a lens. Hence reason is not true. Correct option is (c).

9. Since glass slab produced a net shift. Hence *v* is increased. Thus magnified image is obtained but image may be real or virtual depending on the position of slab.

Correct option is (b)

10. In this case image distance of O_1 and O_2 are same from the lens.

$$\therefore \frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$
 and reason is trure.

Hence correct option is (d).

- 11. Assertion is false since only ray energe if refractve index of the colour less than the prism and angle of incidence is less than critical angle but reason is true. Correct option is (a).
- **12.** If two object is placed between pole and focus image is real hence assertion is true. Also reason is correct.

Hence correct option is (b)

13. Since both assertion and reason are true and reason explanation is correct.

Hence correct option is (a).

Objective Questions (Level 2)

Single option correct

1. We have

have
$$\frac{1}{\text{App. depth}}$$

 $\frac{4}{3}$ $\frac{1}{\text{App. depth}}$
App. depth $\frac{3}{4}$

Real depth

Hence the distance between bird and mirror

2
$$\frac{3}{4}$$
 $\frac{11}{4}$ m

Since plane mirror form image behind the mirror (for real object) at same distance as object hence the distance between bird and its image

$$\frac{11}{4}$$
 $\frac{11}{4}$ $\frac{11}{2}$ m

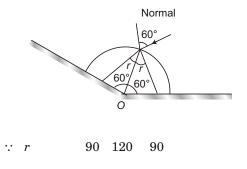
Correct option is (d).

2.
$$\frac{2}{v} \frac{1}{u} \frac{2}{R}$$

Here $u_1 \quad 1$
and $\frac{2}{1.5} \quad 1.5$
 $\frac{1.5}{v} \frac{1}{R} \quad \frac{0.5}{R} \quad v \quad 3R$

Hence correct option is (b).

3. From figure, r = 30



Hence
$$\frac{\sin 60}{\sin 30} \sqrt{3}$$

The correct option is (d).

4. The lens become diverging if

$$egin{array}{cccc} 1&2&2\\ 1&3&2&2 \end{array}$$

 2_{2} or 1

Hence correct option is (b).

5.
$$\frac{1}{v_1}$$
 $\frac{1}{16}$ $\frac{1}{f}$ v_1 $\frac{16f}{16 \ f}$
 m_1 $\frac{v_1}{16}$ $\frac{16f}{16(16 \ f)}$ $\frac{f}{(16 \ f)}$...(i)
and $\frac{1}{v_2}$ $\frac{1}{6}$ $\frac{1}{f}$ v_2 $\frac{6f}{6 \ f}$

$$2 \frac{v_2}{6}$$
 (:: image is virtual)

$$m_2 = \frac{6f}{6(6-f)} = \frac{f}{6-f}$$
 ...(ii)

f

3

3

But

Hence correct option is (d).

6. Let real depth at any instant *t* of the water is h then volume of water V R^2h

$$\frac{dV}{dt} = R^2 \frac{dh}{dt}$$
 ...(i)

Let apparent depth at this instant is h

$$\therefore \qquad \frac{\text{Real depth}}{\text{Apparent depth}}$$

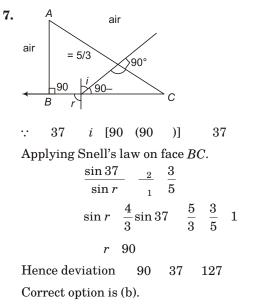
$$\frac{n_2}{n_1} \quad \frac{h}{h_1} \quad h_1 \quad \frac{n_1}{n_2} h$$
Now
$$\frac{dh}{dt} \quad x \quad \frac{n_1}{n_2} \frac{dh}{dt}$$

$$\frac{dh}{dt} \quad \frac{xn_2}{n_1} \qquad \dots (\text{ii})$$

From Eq. (i) and (ii), we get

$$rac{dV}{dt} = rac{R^2 x n_2}{n_1}$$

Hence correct option is (b).



8. Let refractive index of liquid is

For position of fish w.r.t. bird is

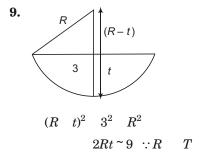
$$\frac{\text{Real depth}}{\text{App. depth}} \qquad \frac{x}{h_1} \qquad \dots (i)$$

For position of bird w.r.t. fish is

$$\frac{1}{2} \quad \frac{y}{h_2} \qquad \qquad \dots (2)$$

 $\frac{h_2}{h_1}$ From Eq. (i) and (ii) we get u

Hence correct option is (a).



$$2R \quad \frac{900 \,\mathrm{mm}}{3 \,\mathrm{mm}} \quad 300 \,\mathrm{mm}$$

R 150 mm 15 cm

Hence correct option is (a).
10.
$$\frac{1}{v_1}$$
 $\frac{1}{v_1}$ $\frac{1}{f}$ v_1 $\frac{fv_1}{v_1 f}$
 m_1 $\frac{v_1}{v_1}$ $\frac{f}{(v_1 f)}$...(i)
 $\frac{1}{v_2}$ $\frac{1}{v_2}$ $\frac{1}{f}$ v_2 $\frac{fv_2}{v_2 f}$
 m_2 $\frac{v_2}{v_2}$ $\frac{f}{2 f}$...(ii)

$$\begin{array}{cccc} \ddots & m_1 & m_2 \\ & \frac{f}{v_1 \quad f} \quad \frac{f}{v_2 f} \quad f \quad \frac{v_1 \quad v_2}{2} \end{array}$$

Hence the correct option is (d).

11.
$$\frac{1}{F} \quad \frac{1}{f_1} \quad \frac{1}{f_2} \quad \frac{d}{f_1 f_2}$$

 $F \quad \frac{f_1 f_2}{f_1 \quad f_2 \quad d}$

as d increases f_1 f_2 d decreases hence F increases. Hence image move to right.

Correct option is (b).

12. In this case, minimum deviation of ray 1 is same as ray 2.

Hence correct option is (c).

13. For critical angle at glass air surface

$$\sin_{c} \quad \frac{1}{g} \quad \frac{2}{3} \qquad \qquad \dots (i)$$

Now for glass water surface.

$$\frac{w}{g} \quad \frac{\sin c}{\sin r} \quad \frac{4/3}{3/2} \quad \frac{2}{3 \sin r}$$
$$\sin r \quad \frac{4}{3}$$

Now for water air surface

$$\frac{w}{a} \frac{\sin r}{\sin r} = \frac{4}{3} \frac{4}{3} \frac{1}{\sin r}$$
$$\sin r = 1 \quad r \quad 90$$

Hence correct option is (d).

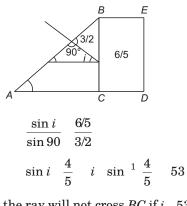
14. For limiting angle of incident emergent ray become parallel to the 2nd face

Hence correct option is (a).

15. The image form the object itself if the rays incident parallel to optical axis on the mirror *i.e.*, image of refraction is formed at . It is possible when O is placed at focus *i.e.*, d 10 cm

Hence correct option is (c).

16. The dot will appear at *c* for all values of .Since position does not in same medium.Hence correct option is (b).



Hence the ray will not cross BC if i = 53

90
$$i$$
 180
90 $i \because i$ 53
37

Hence correct option is (a).

18. For reflection at curved surface

$$\frac{1}{v} \quad \frac{1}{(x)} \quad \frac{3}{2} \quad 1 \quad \frac{1}{10}$$
$$v \quad \frac{20x}{x \quad 20}$$

This image act as virtual object for plane-glass-water surface

$$\frac{g}{20x} \frac{w(x \ 20)}{20x} \frac{g \ w}{x}$$

 $x = 20 \,\mathrm{cm}$

Hence answer is (c).

19. The ratio of focal length in the situation II and III is 1:1.

Hence correct option is (c).

20. We have
$$\frac{1}{OB} = \frac{1}{(OA)} = \frac{1}{f}$$

 $\frac{1}{OB} = \frac{1}{OA} = \frac{1}{f}$
 $f = \frac{OB.OA}{OA = OB} : OB = OA = AB$

$$f \quad \frac{OB.OA}{AB} \qquad \dots (i)$$
Now $AB^2 \quad AC^2 \quad BC^2$

$$(OA \quad OB)^2 \quad OC^2 \quad OA^2 \quad OB^2 \quad OC^2$$

$$OA^2 \quad OB^2 \quad 2OAOB \quad 20 \ C^2 \quad OA^2 \quad OB^2$$

$$OC^2 \quad OA \ OB \qquad \dots (ii)$$
Putting this value in Eq. (i) we get

q. (1), we get

$$f \quad \frac{OC^2}{AB}$$

Hence correct option is (c).

21. The shift produce

$$t \quad t \quad 1 \quad \frac{2}{w \quad g}$$

$$36 \quad 1 \quad \frac{1}{9/8} \quad \because w \quad g \quad \frac{3/2}{4/3} \quad \frac{9}{8}$$

$$\frac{36 \quad 1}{9} \quad 4 \text{ cm}$$
Hence correct option is (b).
Real depth

App. depth

22.

$$\frac{4}{3}$$
 $\frac{\text{real depth}}{10.5\,\text{cm}}$

Real depth $\frac{4}{3}$ 10.5 cm 14 cm

Hence correct option is (d).

23.
$$\therefore y_0$$
 1 cm and y_i 2 cm

$$m \quad \frac{v}{u} \quad 2 \quad \frac{v}{u}$$

Now let *x* be the position of lens then v 50 x and v (40 x).

50 x $\mathbf{2}$ $\overline{40 \quad x}$ 80 2x 50 x 3x 30 x $10\,\mathrm{cm}$

Hence correct option is (c).

- 24. If the plane surface of plano-convex lens is silvered it behave the concave mirror of focal length $f_m/2$
 - $f_m = 10 \,\mathrm{cm}$

÷

 f_e 5 cm hence R 10 cm

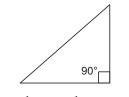
Correct option is (c).

25. Since lens made real and magnified image, hence it is a convex lens when lens dipped in water its focal length.

:: f is velens behave as concave, hence the image is virtual and magnified.

Correct option is (c).

26. The prism transmit the light for which angle of incidence(c), $2c \quad 90 \quad c \quad 45$



Hence $\frac{1}{\sin C} = \frac{1}{\sin 45} = \sqrt{2} = 1.414$

Correct option is (b).

27.
$$\frac{1}{v} \quad \frac{1}{(16)} \quad \frac{1}{f} :: |m| \quad \left| \frac{v}{u} \right| \quad 3$$

For convex lens v = 3u $\frac{1}{48} = \frac{1}{16} = \frac{1}{f} = f = 12 \text{ cm (for real image)}$

Similarly when distance is 6 cm, 3 times virtual image is formed hence mirror is convex with focal length 12 cm.

Correct option is (c).

28.
$$v_g n_g \frac{c}{g} n_g \dots$$
(i)

$$\frac{c}{w}$$
 n w

Dividing (i) and (ii)

and

$$\frac{w}{g} \quad \frac{g}{w} \quad \frac{4}{3g} \quad \frac{4}{5}$$

Hence correct option is (a).

29.
$$x \quad \frac{f_1 f_2}{f_1} \quad \frac{d(f_1 \quad d)}{f_2 \quad d} \text{ and } y \quad \frac{(f_1 \quad d)}{f_1 \quad f_2 \quad d}$$

$$f = 20 \text{ cm} \qquad f = -20$$

$$f = -20$$

$$f = -20$$

$$f = -20$$

$$f = -30$$

Here
$$f_1$$
 f_2 20 cm, d 30 cm
and 55m 0.5 cm
Putting these values we get

x 25 cm and y 0.25 cm

Correct option is (b).

30. Since for each angle of incidence at glass-air boundry remains 0° hence there will never be total internal reflection.

Correct option is (d).

31. Diameter Original diameter

$$\frac{4}{3}$$
 1 cm $\frac{4}{3}$ cm

Hence correct option is (a).

32.
$$\frac{1}{f_1}$$
 (1.5 1) $\frac{1}{20}$ $\frac{1}{20}$
 f_1 20 cm
Here u_1 30 cm
 $\frac{1}{v}$ $\frac{1}{u_1}$ $\frac{1}{f_1}$ $\frac{1}{v_1}$ $\frac{1}{20}$ $\frac{1}{30}$ v_1 60 cm
Magnification $|m_1|$ $\left|\frac{v}{u}\right|$ $\frac{60}{30}$ 2
(Inverted image)

...(ii)

For second lens. $\frac{1}{v_2}$ $\frac{1}{60}$ $\frac{1}{20}$ v_2 30 cm Magnification $|m_2|$ $\left|\frac{30}{60}\right|$ $\frac{1}{2}$

Total magnification $m_1 m_2 1$

Hence object size remains 3mm and it is formed at (120 30) cm 50 cm from first lens.

Hence correct option is (b).

33. From left hand side refraction occur from $n_2 = 2 \text{ to } n_1 = 1.$

$$n \quad \frac{n_1}{n_2} \quad \frac{1}{2} \quad 0.5$$

$$\frac{n}{v} \quad \frac{1}{u} \quad \frac{n}{R}$$

$$\frac{0.5}{v} \quad \frac{1}{10} \quad \frac{0.5}{10} \quad \frac{1}{10} \quad \frac{0.5}{10}$$

$$v \quad 10 \text{ cm}$$

Hence correct option is (a).

34. For lens
$$v = 20 \text{ cm}$$
, $f = 10 \text{ cm}$

Using
$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$
 we get $v \quad 20$ cm

This image acts virtual object for convex mirror. For mirror v (x 20)

and
$$v$$
 (20 x) and f 60 cm
Using $\frac{1}{v} = \frac{1}{u} = \frac{1}{f}$
 $\frac{1}{(20 x)} = \frac{1}{(x - 20)} = \frac{1}{60}$

After solving we get x = 20 cm.

Hence correct option is (c).

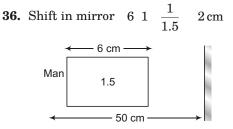
35. In this case system behave as concave mirror or focal length f_e

Now using mirror formula

$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$$
 we get

$$\frac{1}{v} \quad \frac{1}{20} \quad \frac{1}{30} \\ \frac{1}{v} \quad \frac{1}{20} \quad \frac{1}{30} \quad v \qquad 60 \,\mathrm{cm}$$

Hence correct option is (d).



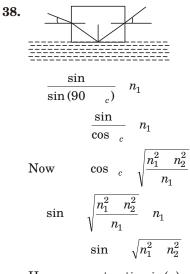
Hence man lie at 48 cm from mirror. The distance of image from observer 2 48

Hence correct option is (b).

37. Using lens formula $\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f}$ $\frac{1}{(f \quad 40)} \quad \frac{1}{(f \quad 10)} \quad \frac{1}{f}$

On solving we get f = 20 cm

Hence correct option is (c).



Hence correct option is (a).

- **39.** For mirror *u* 1 cm (taking upward direction ve)
 - $f 2 \operatorname{cm}$ $\frac{1}{v} \frac{1}{f} \frac{1}{u}$ $\frac{1}{v} \frac{1}{2} 1 \frac{1}{2}$ $v 2 \operatorname{cm}$

Hence mirror form virtual image behind mirror at 2 cm from pole. This image acts as virtual object for slab on see below the slab the shift is

$$t = 1 \quad \frac{1}{3/2} \quad 9 \quad 3 \text{ cm}$$

Hence virtual image form on object thus correct option is (a).

40. We have $\frac{2}{v} \quad \frac{1}{u} \quad \frac{2}{R}$

For real object u is ve

$$\frac{2}{v} \quad \frac{\binom{2}{2}}{R} \quad \frac{1}{u}$$

$$\therefore \qquad R \text{ is ve and } 1 \quad 2$$

$$\frac{2}{v} \quad \text{ve } \frac{1}{u}$$

$$v \quad \text{ve}$$

Hence, if $1 _2$ then these cannot be real image of real object.

Hence, correct option is (a).

41. At oil-concave surface

$$\frac{1}{f_1}$$
 (1.6 1) $\frac{1}{-}$ $\frac{1}{10}$ $\frac{1}{f_1}$ $\frac{0.6}{10}$

At other surface light goes from oil to glass

$$\begin{array}{ccccc} \frac{1}{f_2} & \frac{1.5}{1.6} & 1 & \frac{1}{10} & \frac{1}{20} \\ \\ \frac{1}{f_2} & \frac{0.3}{20 & 1.6} \end{array}$$

Let focal length of combination is ${\cal F}$

$$\frac{1}{F} \quad \frac{1}{f_1} \quad \frac{1}{f_2} \quad \frac{0.6}{10} \quad \frac{0.3}{20 \quad 1.6}$$

$$F \quad 28.57 \text{ cm}$$

Hence correct option is (d).

42. Using formula

 $\frac{2}{v}$ $\frac{1}{u}$ $\frac{2}{R}$

For real image is ve

$$\frac{\frac{2}{v}}{\frac{1}{u}} \frac{\frac{1}{2}}{\frac{1}{R}}$$

$$\frac{1.5}{\frac{1}{v}} \frac{0.5}{\frac{1}{u}} \frac{1}{u}$$

$$\frac{1.5}{\frac{1}{2R}} \frac{1}{\frac{1}{u}} v \text{ is } \text{ ve if } u 2R$$

Hence correct option is (b).

43.
$$v \quad \frac{fu}{f \quad u}$$
 when $u \quad f$

u lend to lens

if u = 0, v = 0

Hence correct option is (d).

44. Since image formed by diverging lens is always virtual.

Hence correct option is (a)

45. If the object place at first focus the image forms at *ie*, rays incident the plane surface normally and retrace its path.

Now
$$x = f_1 = \frac{1R}{2} = \frac{60}{0.5} = 120 \,\mathrm{cm}$$

Hence correct option is (a).

46.
$$\frac{2}{v_1}$$
 $\frac{1}{u_1}$ $\frac{2}{R}$ for 2 1.6
 $\frac{1.6}{v_1}$ $\frac{1}{(2)}$ $\frac{1.6}{1}$ $\frac{1}{10}$
 $\frac{1.6}{v_1}$ $\frac{6}{10}$ $\frac{1}{2}$ $\frac{1}{10}$
 v_1 16 m
For 2 2

Hence separation between images $v_1 v_2$

(16 4) cm

 $12\,\mathrm{cm}$

Hence correct option is (a).

47. System behave a a concave mirror

Here
$$u = 10, v = 40 \text{ cm}$$

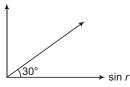
$$\frac{1}{v} \quad \frac{1}{u} \quad \frac{1}{f} \text{ we get}$$
$$\frac{1}{40} \quad \frac{1}{10} \quad \frac{1}{f}$$

More than one options correct

- **1.** Since prism are identical hence if a right prism produce deviation inverted prism produce deviation .
 - if $n \quad 2m$ deviation becomes zero.
 - if $n \quad 2m \quad 1$ deviation produce is

Hence correct options are (a) and (b).

2. sin i



 $\therefore \sin i \quad \sin r$ tan 30

if speed of light in medium *x* is *v*

then speed of light; in medium $y = \frac{v}{\sqrt{3}}$

 $\sqrt{3}$

Since *y* is denser w.r.t. *x* hence total internal reflection take place when incidence in *y*.

8 cm

Hence correct option is (a).

48. The focal length of lens combination is 2f

f

Hence
$$\frac{1}{2f} = \frac{(1.8 \quad 1.2)}{(1.2 \quad 1)} = \frac{1}{R}$$

 $\frac{1}{16} = \frac{0.6}{0.2R}$
 $R = 48 \text{ cm}$

Hence correct option is (a).

49. If plane surface is silvered the system acts a concave mirror having focal length

 $\frac{R}{2}$ 24 cm

Hence correct option is (c).

The correct options are (b) and (d).

- **3.** The correct options are (b) and (c).
- **4.** The lens form real image if D = 4F (displacement method)

$$f \quad \frac{D^2 \quad x^2}{4D}$$

and the magnification m_1m_2 1

Hence correct options are (b), (c) and (d).

5. Deviation produced by prism

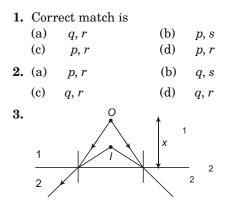
and

(1) A (1.5 1) 4 2

if the mirror is rotated 2 ray become horizontal after reflection from mirror.

Again if mirror is rotated by 1° reflection ray deviated by 2° from horizontal and after passing through prism again ray become horizontal.

Hence correct option are (a) and (b).

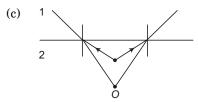


Hence image distance is less than x and virtual.

(a) *q*, *s*

Similarly as in (a) the correct match for

(b) *q*, *r*



(c)
$$p, s$$

(d) p, r

4. (a) q, (b) r(c) r(d) p5. Since $\frac{1}{f}$ (n 1) $\frac{1}{R_1}$ $\frac{1}{R_2}$ here n 1.5 for (a) n 1.4 $\frac{1}{f}$ $\frac{1.5}{1.4}$ 1 $\frac{1}{R_1}$ $\frac{1}{R_2}$ f is ve

hence

(a) p, s :: f increases, power decreases

(b) q, s :: f is ve and increase in magnification

Similarly

- (c) q, s and
- (d) *p*, *s*
- **6.** For real object at 2*c* convex lens form image at 2*c* similarly for virtual object concave lens does.

(a)
$$q, s$$
 (b) q, r

(c)
$$q, r$$
 (d) q, r

28 Interference and Diffraction of Light

Introductory Exercise 28.1

1. Because they are incoherent *ie*, does not $I = 10 - 6 = 2\cos^2 \frac{1}{2} - 1 = I_0$ remain constant. $10 \quad 12\cos^2{-7} \quad 6 \quad I_0$ 2. Since laser is highly coherent and monochromatic source of light **3.** $I I_0 \cos^2 / 2$ 4 $12\cos^2 \frac{1}{2} I_0$ $\frac{3I_0}{4}$ $I_0 \cos^2 / 2$ $4I_0 \ 1 \ 3\cos^2\frac{1}{2}$ $\cos /2 \frac{\sqrt{3}}{2}$ Now, $I_{\text{max}} = \frac{I_0}{\alpha}$ $I \quad \frac{4}{9}I_{\text{max}} \quad 1 \quad 3\cos^2\frac{1}{9}$ $\frac{1}{2}$ $\frac{1}{6}$ $\overline{3}$ 6. $x \frac{yd}{D}$ (1) t $x \quad \overline{2} \quad \overline{2} \quad \overline{3} \quad \overline{6}$ if $t = \frac{1}{2(1)}$ $x \frac{yd}{D}$ But $x \frac{yd}{D} = \frac{1}{2}$ $y \quad \frac{D \quad x}{d} \quad \frac{D}{d} \quad \frac{D}{6}$ For maxima x n $y = \frac{1.2 \ 600 \ 10^{9}}{0.25 \ 10^{2} \ 6} \ 48 \ m$ $\frac{yd}{D}$ 2n $\frac{1}{2}$ **4.** 2 t n $\frac{1}{2}$ for minimum thickness n 1 This become minima. For minima $x n \frac{1}{2}$ $t = \frac{3}{4} = \frac{3}{4} = 1.5$ cm $\frac{yd}{2}$ $\frac{1}{2}$ n $\frac{1}{2}$ **5.** Here a_1 3 a and a_2 a $\frac{yd}{D}$ *n* this become maxima. R^2 $(3a)^2$ $(a)^2$ 2 3a a cos $I \quad 9I_0 \quad I_0 \quad 6I_0 \cos \theta$ Hence maxima and minima interchanged. $I \ [10 \ 6\cos]I_0$

are

7. For two slit experiment

$$d\sin \quad n\\ \sin \quad \frac{n}{d}$$

But

n 6

8. Since amplitude of each wave is equal. The amplitude of resultant wave is zero if waves are equally displaced in phase

ie,
$$\frac{360}{8}$$
 45

Hence phase difference must be 45°

AIEEE Corner

Subjective Question (Level-1)

1. R^2 a_1^2 a_2^2 $2a_1a_2\cos$	$\overline{2}$
(i) $R 2a, a_1 a_2 a$ $4a^2 a^2 a^2 2a^2 \cos a^2$	Now, $\frac{2}{-} x$
$\cos 1 0$	$\frac{2}{2}$ $\frac{2}{x}$
(ii) $2a^2 2a^2 2a^2 \cos \theta$	
90	$\frac{x}{4}$
(iii) $a^2 2a^2 2a^2 \cos \cos \frac{1}{2} 120$	But $x \frac{yd}{D}$
$(iv) 0 2a^2 2a^2 \cos 180$	$y \frac{D x}{d}$
9	$y \frac{1m}{4 1mm} \frac{1 500 10^{9}}{4 10^{3}}$
2. $\frac{I_{\max}}{I_{\min}} = \frac{(a_1 a_2)^2}{(a_1 a_2)^2} = \frac{\frac{a_1}{a_2} 1}{\frac{a_1}{a_2} 1}$	$4 \text{ 1mm} 4 \text{ 10}^{-1}$ y 1.25 10 4 m
$\frac{1}{a_2}$	4. $I = I_{\text{max}} \cos^2 \frac{1}{2}$
$\frac{I_{\max}}{I_{\min}} = \frac{\frac{5}{3}}{\frac{5}{2}}^{2} = \frac{8^{2}}{2^{2}} = 16$	(a) $\frac{I_{\text{max}}}{2}$ $I_{\text{max}} \cos^2 \frac{1}{2}$ $\frac{1}{2}$
$I_{\min} = \frac{5}{3 - 1} + \frac{2}{2}$	Now $\frac{2}{-}$ x
$I_{\rm max}: I_{\rm min}$ 16:1	$x \frac{1}{4} \text{ and } x \frac{yd}{D} \qquad \frac{D}{4d}$
3. $I I_{\max} \cos^2 \frac{1}{2}$	(b) $\frac{1}{4}I_{\text{max}}$ $I_{\text{max}}\cos^2\frac{1}{2}$
$rac{{I_{\max }}}{2}$ ${I_{\max }}\cos ^2rac{1}{2}$	$\cos \frac{1}{2}$ $\cos \frac{1}{3}$ $\frac{2}{3}$
$\begin{array}{c}\cos-2&\cos-4\end{array}$	$\frac{2}{2}$ x

$$\frac{2}{3} \quad \frac{2}{3} \quad x \quad x \quad \frac{3}{3}$$
Now $x \quad \frac{yd}{D} \quad y \quad \frac{D}{3d}$
5. (a) $I \quad I_{\max} \cos^2 \frac{1}{2}$

$$I_{\max} \quad I_0 \text{ and } 60$$

$$I \quad I_0 \cos^2 30 \quad \frac{3}{4} I_0 \quad 0.75I_0$$
(b) $\frac{2}{3} \quad x$

$$\frac{3}{3} \quad \frac{2}{3} \quad x$$

$$x \quad \frac{1}{6} \quad \frac{480}{6} \text{ nm}$$

$$x \quad 80 \text{ nm}$$
6. $A \quad B \quad 6m$

For constructive interference difference wavelength 0, ,2

 $6 \quad d_{AB} \quad 5$ ÷

Hence only constructive interference occur at 0

$$x \quad \frac{5}{2}$$
m 2.5 m

For destructive interference

6 Only possibility at

Which occur at x = 1 m and x = 4 m from A.

 $,\frac{3}{2}$

 $\frac{c}{n} \quad \frac{3 \quad 10^8}{120 \quad 10^6} \quad 2.5 \,\mathrm{m}$ 7. The wavelength

For constructive interference

x (9 x) n, where n = 0, 1, 2...*x* 4.5, 5.75, 7, 8.25

The other points are 3.25, 2, .75

8. In Young's double slit experiment

$$w \quad \frac{D}{d}$$
2.82 10 ³m $\frac{2.2}{.460 \quad 10^{-3}}$

9. x_n for bright fringe is given by

$$x_n \quad \frac{nD}{d}$$

$$x_1 \quad \frac{D}{d} \text{ and } x_2 \quad \frac{2D}{d}$$

$$x \quad \frac{D}{d} \text{ the angular separation}$$

$$\sin(\quad) \quad \frac{x}{D} \quad \frac{5}{d} \quad \frac{5}{2} \quad \frac{10}{10}^{\frac{7}{3}} \quad 2.5 \quad 10^{-4}$$

$$(\quad) \quad \sin^{-1}[0.00025]$$

$$0.014$$

${\bf 10.}~{\rm When}~{\rm whole}~{\rm appratus}~{\rm is}~{\rm immersed}~{\rm in}~{\rm water}$

$$n_{w} \quad \frac{4}{3} \quad 700 \quad 10^{-9} \text{ m}$$

$$w \quad \frac{D}{d} \quad \frac{48 \quad 10^{-2} \quad 4 \quad 7 \quad 10^{-7}}{3 \quad 25 \quad 10^{-5}} \quad 0.90 \text{ mm}$$
11. $w_{1} \quad \frac{D_{1}}{d} \text{ and } w_{2} \quad \frac{D_{2}}{d}$

$$w_{1} \quad w_{2} \quad \frac{(D_{1} \quad D_{2})}{d}$$
3 $\quad 10^{-5} \quad \frac{1.5 \quad 10^{-2}}{10^{-3}}$
 $\frac{3}{1.5} \quad \frac{10^{-8}}{10^{-2}} \quad 2 \quad 10^{-6} \text{m} \quad 2 \text{ m}$
12. For bright fringe $x_{n} \quad \frac{Dn}{d}$
For first light (480 nm) the third order Bright fringe is $x_{3} \quad \frac{1 \quad 3 \quad 480 \quad 10^{-9}}{5 \quad 10^{-3}}$
For second light (600 nm)
$$x_{3} \quad \frac{1 \quad 3 \quad 600 \quad 10^{-9}}{5 \quad 10^{-3}}$$

13. Fringe width :

$$\frac{D}{d}$$

$$\frac{(500 \ 10^{9})(75 \ 10^{2})}{(0.45 \ 10^{3})} \text{ m}$$

$$0.83 \ 10^{3} \text{ m}$$

$$0.83 \text{ mm}$$

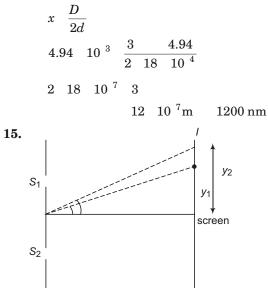
Distance between second and third dark line one fringe width 0.83 mm.

14. For first order bright fringe

$$x \quad \frac{D}{d}$$
4.94 10³ $\frac{3 \quad 600 \quad 10^{-9}}{d}$

$$d \quad \frac{18 \quad 10^{-7}}{4.94 \quad 10^{-3}} \quad \frac{18}{5.94} \quad 10^{-4} \text{ m}$$

Let for wavelength first dark fringe is obtained at this point for first dark fringe



For dark fringe

 $d\sin((2n-1)\frac{1}{2})$

For first dark fringe n = 1 and for 2nd, n = 2

$$d \sin \frac{1}{2}$$

$$d \sin \frac{3}{2} \sin \frac{1}{2d}$$

$$\frac{y_1}{\sqrt{D^2 y_1^2}} = \frac{1}{2d}$$
and
$$\frac{y_2}{\sqrt{D^2 y_1^2}} = \frac{3}{2d}$$

$$\frac{y_1}{\sqrt{(35 \ 10^{\ 2})^2 \ y_1^2}} = \frac{550 \ 10^{\ 9}}{2 \ 1.8 \ 10^{\ 6}} \dots (i)$$

and
$$\frac{y_2}{\sqrt{(35 \ 10^2)^2 \ y_2^2}} = \frac{3 \ 550 \ 10}{2 \ 1.8 \ 10^6}$$

On solving $y_2 \quad y_1 \quad 12.6 \text{ cm}$

16. Wavelength of source
$$\sqrt{2 meV}$$

$$\frac{6.62 \quad 10^{-34}}{\sqrt{2 \quad 9.1 \quad 10^{-31} \quad 100 \quad 1.6 \quad 10^{-19}}}$$

$$\frac{1.24 \quad 10^{-10} \text{ m}}{d} = \frac{3 \quad 1.24 \quad 10^{-10}}{10 \quad 10^{-10}} \text{ m} = 36.6 \text{ cm}$$

17. Given 546 nm 5.46 10 7 m, D 1 m

d 0.3 mm 0.3 10 3 m

(a) At distance $y = 10 \text{ mm} = 10^{-3} \text{m}$ from the central fringe path difference will be

y
$$\frac{y.d}{D}$$
 $\frac{10 \ 10^{3} \ 0.3 \ 10^{3}}{1}$
3 10^{6} m

Corresponding phase difference

$$\frac{2}{-}$$
 x $\frac{2}{5.46 \ 10^{-7}}$ 3 10 ⁶ rad

1978

$$I \quad I_{0} \cos^{2} \frac{1978}{2} \qquad I_{0} \cos^{2} 989$$

$$I \quad 3 \quad 10^{-4} I_{0}$$
(b) Fringe width $w \quad \frac{D}{d}$

$$w \quad \frac{5.46}{0.3} \frac{10^{-7}}{10^{-3}} 1.82 \text{ mm}$$
Number of fringes $\frac{10 \text{ mm}}{1.82 \text{ mm}} 5.49$

Hence the number of fringe is five.

18. Shift due to sheet of thickness 10 and refractive index 1.6 is

$$x_{1} \quad \frac{(1) tD}{d}$$

$$x_{1} \quad (1.6 \quad 1) \quad \frac{10 \quad 10^{-6} \quad 1.5}{1.5 \quad 10^{-3}}$$

$$x_{1} \quad 0.6 \quad 10 \quad 10^{-3} \quad 6 \quad 10^{-3} \text{m}$$

Shift due to sheet of thickness 15 and refractive index 1.2 is

Since these shifts are in opposite direction of central maxima hence net shift

$$x$$
 x_1 x_2 6 10 ³m 3 10 ³m
3 10 ³m 3 mm

19. Let is the wavelength of light D is screen distance from source and d is the separation between slits (all are in metres)

Shift
$$x = \frac{(1) tD}{d}$$

 $x = \frac{(1.6 \ 1) \ 1.964 \ 10^{-6} \ D}{d}$

$$x = \frac{1.1784 D}{d} = 10^{-6} m$$

Now when *t* is removed and *D* is doubled the distance between successive maximum (or minima) *i.e.*, fringe width

$$w \quad \frac{2D}{d}$$

but according to question x w

$$\frac{1.178 \quad 10^{6}D}{d} \quad \frac{2D}{d}$$
0.589 \quad 10^{6}m \quad 589 \nm

20. Let *n* bright fringe (5500 Å) concide with 10th

bright fringe of 6000 Å

Similarly first bright fringe concide with 1st fringe. Now fringe width

 $w = \frac{14.74 \quad 12.5}{10} = 0.224 \text{ mm}$

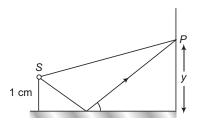
Hence position of 10th bright fringe

 $14.74 \quad 0.224 \approx 14.55 \,\mathrm{mm}$

Position of zero order bright fringe

 $12.75 \quad 0.224 \approx 12.25 \,\mathrm{mm}$

21. Here *d* ~ 1 cm



D 100 m 500 nm For first dark fringe

$$y = \frac{100 500 10^{9}}{2 10^{2}}$$

y 2.5 mm

22. The destructive interference will be 2 t n for thinnest n 1

- **23.** Here t 0.485 m, t 485 nm, n 1.53
 - (a) Condition for constructive interference in refractive system
 - $2 t n \frac{1}{2}$ where, n 1, 2

For *n* 1, 1 4 *t* 4 1.53 485 2968.2 mm

which does not lie in visible region put

n 2, 3,

- we get 424 nm, 594 nm, ...
- (b) For structive interference in transmitted system

2 t n, putting n 1, 2,

only 495 nm is lie in visible region.

24. For constructive interference

$$2 t n \frac{1}{2} \text{ for } t \text{ to be minimum } n 1$$
$$t \frac{6000}{4 1.3} 1154 \text{ Å}$$

25. For destructive interference

$$2 t n \text{ for } t \text{ to be minimum}$$

$$n 1$$

$$t \frac{1}{2} \frac{800}{2} \dots (i)$$

For constructive interference

1600
$$(2n \ 1)$$

For n = 1, 600 nm which does not lie in visible region

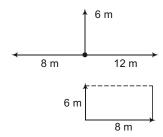
For
$$n \ 2$$

 $1600 \ 3$
 $\frac{1600}{3} \ 533 \text{ nm}$
for $n \ 3$, $\frac{1600}{5} \ 320 \text{ nm}$ which does lie
in visible
Hence 533 nm

Objective Questions (Level-1)

(Single option correct)

1. Using phasor method



$$R \quad \sqrt{8^2 \quad 6^2} \quad 10 \,\mathrm{m}$$

Hence correct option is (b).

2. Here
$$\frac{I_1}{I_2}$$
 B^2
 I_{max} $[\sqrt{I_1} \quad \sqrt{I_1}]^2$
 I_{min} $[\sqrt{I_1} \quad \sqrt{I_2}]$

$$\begin{array}{cccc} \frac{I_{\min}}{I_{\max}} & \frac{\sqrt{\frac{I_{1}}{I_{2}}} & 1}{\sqrt{\frac{I_{1}}{I_{2}}}} & 1 & \frac{1}{1}^{2} \\ \frac{(I_{\max} & I_{\min})}{(I_{\max} & I_{\min})} & \frac{1}{2} & \frac{1}{2} \\ \frac{I_{\max} & I_{\min}}{I_{\max}} & \frac{1}{2} \end{array}$$

Hence, correct option is (d).

3. For *n*th dark fringe

$$x_n$$
 (2n 1) $\frac{D}{2d}$

For 1st dark fringe n = 1

$$x_{1} \quad \frac{D}{2d}$$
Angular position $\sin^{-1} \frac{x_{1}}{D}$

$$\sin^{-1} \frac{2a}{2a}$$

$$\sin^{-1} \frac{5460 \quad 10^{-10}}{2 \quad 0.1 \quad 10^{-3}}$$

$$\sin^{-1} [273 \quad 10^{-5}]$$

$$\sin^{-1} [0.00273]$$

$$0.16$$
Hence correct option is (b)
For 10th bright fringe $x_{10} \quad \frac{10D}{d}$
For 6th dark fringe $x_{6} \quad (2 \quad 6 \quad 1) \frac{D}{2d}$
But
$$\frac{11}{2a} D \quad \frac{10D}{d}$$

$$- \frac{20}{11}$$
But
$$- \frac{20}{11} \quad 1.8$$

Hence correct option is (a).

5. Shift
$$\frac{(1)tD}{d}$$

 $\frac{(1.5 \ 1) \ 10 \ 10^{6} \ 100 \ 10^{2}}{2.5 \ 10^{3}}$
 $\frac{5 \ 10^{6}}{2.5 \ 10^{3}} \ 2 \ 10^{3} \text{m} \ 2 \text{mm}$
Hence correct option is (a).
6. $x_{n} \ \frac{Dn}{d}$ for *n*th bright fringe
 $x_{n} \ \frac{D}{2d}(2n \ 1)$ for *n*th dark fringe
 $x \ x_{n} \ x_{n} \ \frac{D}{2d}[2n \ 2n \ 1]$
 $x \ \frac{D}{2d}$

Hence correct option is (c).

 $\overline{2d}$

7. Since at centre path difference for all colour is always zero hence centre will be white.

Hence correct option is (a).

8.
$$n_1$$
 1 n_2 2
60 4000 n_2 6000 n_2 40
Hence correct option is (a).
9. Initial fringe width w_1 $\frac{D}{d}$
Final fringe width w_2 $\frac{(D \ 5 \ 10^2)}{d}$
 $|w| |w_2 |w_1| = \frac{D}{d} = 5 \ 10^2$
 $3 \ 10^5 = \frac{10^3}{10^3} = 5 \ 10^2$
 $\frac{3 \ 10^6}{5} = 6000 \text{ Å}$

Hence correct option is (a).

4.

$$10. \frac{I_{\max}}{I_{\min}} \frac{49}{9}$$

$$Now \frac{I_{\max}}{I_{\min}} \frac{\sqrt{I_1}}{\sqrt{I_1}} \frac{\sqrt{I_2}}{\sqrt{I_2}}^2 \frac{\sqrt{I_1}}{\sqrt{I_2}} \frac{1}{2} \frac{1}{\sqrt{I_2}}^2$$

$$\frac{I_{\max}}{I_{\min}} \frac{\sqrt{\frac{49}{9}}}{\sqrt{\frac{49}{9}} \frac{1}{1}} \frac{1}{2} \frac{\frac{7}{3}}{\frac{7}{3}} \frac{1}{1} \frac{100}{16}$$

$$\frac{I_{\max}}{I_{\min}} \frac{25}{4}$$

Hence correct option is (a)

11.
$$x_n \quad \frac{Dn}{d}$$

 $x_3 \quad \frac{3D}{d} \quad 7.5 \quad 10^{-3} \text{m}$
 $\frac{7.5 \quad 10^{-3} \quad 0.2 \quad 10^{-3}}{3 \quad 1}$

Assertion and Reason

1. We have $I = 4I_0 \cos^2 \frac{1}{2}$ if $\frac{2}{3}$

we get $I = I_0$

Hence assertion is true.

Now path difference $-\frac{1}{2}$ phase difference

Path difference $\frac{2}{2}$ $\frac{2}{3}$ $\frac{3}{3}$

Hence reason is true.

But reason is not the explanation of assertion. Hence correct option is (b).

2. Here assertion and reason are both true but reason is not correct explanation of assertion. Correct option is (b).

 $0.5 \ 10^{-6} \ 500 \ nm$

Hence correct option is (b).

12. Let *n*th fringe of 6500 Å concide with *n* th fringe of 5200 Å.

$$\begin{array}{cccc} x_n & \frac{Dn & 6500 \text{ \AA}}{d} & \frac{Dn}{d} & 5200 \text{ \AA} \\ \frac{n}{n} & \frac{5200}{6500} & \frac{4}{5} \end{array}$$

It means 4th fringe of 6500 Å coincide with 5th fringe of 5200 Å hence the distance

$$x \quad \frac{4 \quad 120 \quad 10^{\ 2} \quad 6500 \quad 10^{\ 10}}{2 \quad 10^{\ 3}}$$

x 0.156 cm

Hence correct option is (a).

- **13.** Since number of minima does not depends on orientation hence $n_1 \quad n_2$ Hence correct option is (a).
- **3.** Assertion is wrong since fringes are symmetrical *ie*, fringes obtained both above and below point *O*. Reason is true.

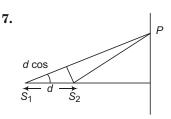
Correct option is (a).

- **4.** Here both assertion and reason are true and reason correctly explain assertion. Hence correct option is (a).
- **5.** Both assertion and reason are true and reason correctly explain the assertion.

Hence correct option is (a).

6. Assertion is true since locus of all fringes is circle. But reason is wrong since fringes may have any shape.

Correct option is (c).



Path difference at point *P* is $x \ d \cos x$ The path difference decreases as increases. \therefore as increases, $\cos x$ decreases Hence order of fringe $n \ \frac{d \cos x}{d}$ decreases

as we go above *P*. Hence assertion is wrong (false).

For 11th order maxima path differenc is more hence reason is true but assertion is false correct option is (d).

8. Here assertion is true and reason is false and reason does not correctly explain assertion. Correct option is (c).

9.
$$\because d \sin n$$

 $\sin \frac{n}{d} \operatorname{but} \frac{d}{4} = 4$
 $\sin \frac{n}{4}$
Now if 30
 $n = 4 \sin 30$

Hence assertion is true.

Also reason is true and does not correctly explain assertion correct option is (b).

 $\mathbf{2}$

10. Here assertion is false. Since shift $\frac{(1)tD}{d}$ is independent of .

Hence shift of red colour shift of violet colour.

and reason is true

 $\frac{k}{4}$

Objective Questions (Level 2)

1.
$$I \quad 4I_0 \cos^2 \frac{x}{-1}$$

 $I_0 \quad 4I_0 \cos^2 \frac{x_1}{-1}$
 $x_1 \quad \frac{1}{3} \qquad \dots(i)$
and $2I_0 \quad 4I_0 \cos^2 \frac{x_2}{-1}$
 $x_2 \quad \frac{1}{4} \qquad \dots(ii)$
 $x \quad x_1 \quad x_2 \quad \frac{1}{3} \quad \frac{1}{4} \quad \frac{12}{-12}$

2.
$$I \quad 4I_0 \cos^2 \frac{x}{-} \quad k \cos^2 \frac{x}{-}$$

 $I \quad k \cos^2 - k \qquad \dots (i)$

$$rac{I}{4}$$
 $k\cos^2$ $rac{x}{}$

$$k\cos^{2} \frac{x}{-1}$$

$$\cos \frac{x}{2} \frac{1}{2}$$

$$\frac{x}{-1}\cos^{-1}\frac{1}{2}$$

$$\frac{x}{-3} \text{ or } \frac{x}{-3}\frac{2}{3}$$

$$x \frac{1}{-3} \text{ or } x \frac{2}{-3}$$

Hence correct option is (b).

3. Light of wavelength is strongly reflected if

$$2ut \quad n \quad \frac{1}{2} \qquad n \quad 0, 1, 2 \qquad \dots (i)$$

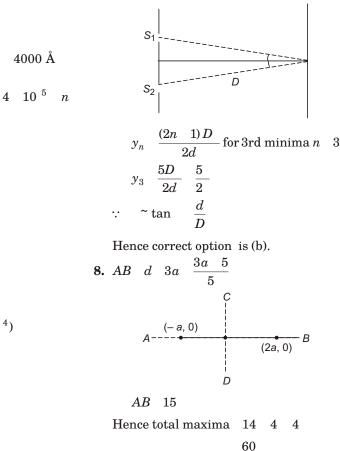
2ut 2 1.5 5 10 ⁷m 1.5 10 ⁶m Putting 400 nm in eq. (1) and using eq. (ii)

 $x \quad \cos^{-1} \sqrt{\frac{3}{4}} \quad x \quad -\cos^{-1} \sqrt{\frac{3}{4}}$ *x* 0.20 mm Hence correct option is (d). **6.** Number of fringes shifted (1

$$\frac{4}{0.5}$$
 6 10 ⁷m t
t 4.8 m

Hence correct option is (a).

7. For *n*th order minima



Hence correct option is (a).

Putting 700 1.5 10 6 m $n \frac{1}{2}$ 7 10 7 n 1.66 Hence n can take values 2 and 3. From (i) if n = 2, $\frac{4ut}{2 - 2 - 1}$ 600 nm if $n \quad 3$ 429 nm only 600 is given in the options. Hence correct option is (b). **4.** $x_n = \frac{D n}{d} = \frac{100 - 10^{-2}}{0.01 - 10^{-3}} = n$ $x_n = \frac{n}{10^{5}}$ For 4000 Å $x_n = \frac{n - 4000 - 10^{-10} \text{ m}}{10^{-5}} = 4 - 10^{-5} = n$ 0.04 n $x_n \quad 4n \text{ mm}$ Similarly for 7000 Å x_n 7 n mm n 5,6 hence only x = 55000 Å Passes through hole Hence correct option is (b). 5. $I \quad 4I_0 \cos^2 \frac{x}{-1}$ where \overline{d} $\frac{1 \quad 6000 \quad 10^{10}}{1 \quad 10^{3}} \quad (6 \quad 10^{4})$ $75\% I_0 I_0 \cos^2 \frac{x}{-1}$ $\frac{3}{16} \cos^2 \frac{x}{x}$ $\frac{\sqrt{3}}{4}$ cos $\frac{x}{3}$

1.5 10⁶ m $n \frac{1}{2}$ 4 10⁷ m

n 3.25

1) t

4 $\frac{(1.5 \ 1) \ t}{6000 \ \text{\AA}}$

9.
$$I \quad 4I_0 \cos^2 \frac{x}{-1}$$

 $I \quad 4I_0 \cos^2 - \frac{1}{4}$
 $I \quad 4I_0 \cos^2 \frac{1}{4}$
 $\frac{4I_0}{2} \quad 2I_0$
 $\frac{I_0}{I} \quad \frac{1}{2}$

Hence correct option is (b).

10.
$$I I_0 \cos^2 - (1) t$$

at
$$I \qquad I \quad I_0$$

Hence correct variation is (c)

11.
$$I_{0} \cos^{2} \frac{x}{-1}$$

 $\frac{3}{4}I_{0} I_{0} \cos^{2} \frac{x}{-1}$
 $\frac{x}{6}$
 $x - \frac{1}{6} but x (-1) t$
(1.5 1) $t - \frac{1}{6}$
 $t - \frac{6000}{3} Å$
 $t - 2000 Å - 0.2 m$
Hence correct option is (a).
12. Net shift $(-1 - 1)t - (-2 - 1)t$

2. Net shift
$$\begin{pmatrix} 1 \\ 1 \end{pmatrix} t \begin{pmatrix} 2 \\ 2 \end{pmatrix} t$$

(1 $_{2}$) t (1.52 1.40) t

Net shift 0.12 10.4 m

12 104 10⁹m $1248 \quad 10^{-9} m$ 1248 nmNet shift nwhere n is ve integer 1248 п Now, for 416 n 3 For 624 , n 2 Hence correct option is (c). 6300 Å 1.33 m 13. $w \quad \frac{D}{d \quad n}$ 1 mm 1.33 $63 \quad 10^{8} \quad 1.33 \text{ m}$ 10 ³ 1.33 0.63 mm Hence correct option is (a).

$$14. \quad x \quad \frac{7D}{nd} \quad \frac{3D}{nd} \quad 4 \quad \frac{D}{nd}$$

x 4 0.63 mm 2.52 mm

Correct option is (a).

15.
$$x$$
 2 of fridge width

$$(1) t \quad \frac{2 \quad 0.63 \text{ mm}}{2} \\ t \quad \frac{2 \quad 0.63}{0.53} \quad 1.57 \text{ mm}$$

Hence correct option is (b).

16. Since on introducing thin glass sheet fringe width does not change hence fringe width 0.63 mm.

The correct option is (a).

56

More than one options correct

1. At centre path difference between all colours is zero hence cnetre is white since violet has least wavelength hence next to central will be violet and since intensity is different for different for colours hence there will be not a completely dark fringe

Hence correct options, are (b), (c) and (d).

- 2. Correct options are (a), (c) and (d).
- **3.** $\therefore I \quad 4I_0 \cos^2 \frac{1}{2}$ at centre $0 \quad I \quad 4I_0$

and at distance 4 mm above o is again maxima hence its intensity is also $4I_0$.

Hence correct options are (a) and (c).

Match the Columns

1. ∵ <i>I</i>	$4I_0\cos^2{-\over 2}$		
if	60	Ι	$3I_0$
if	90	Ι	$2I_0$
if	0	Ι	$4I_0$
if	120	Ι	I_0

Hence correct match is

(a) s;(b) q;(c) p;(d) r

2. $x = \frac{1}{2}$

$$\begin{array}{c}
2 \\
\frac{2}{-} x \text{ if } x \frac{3}{3} \\
\frac{2}{3} 120 \\
\text{if } x \frac{6}{6} \\
60 \text{ if } x \frac{1}{4}, \quad 90 \\
\text{Using } I 4I_0 \cos^2 \frac{1}{2}
\end{array}$$

The correct match are

- 4. The correct options, are (a), (c) and (d)Since phase difference constantLight should be monochromatic.
- **5.** Since in this case fringe pattern shift upward hence the correct options are (a), (b) and (c).
- **6.** \therefore $n_{1 \ 1}$ $n_{2 \ 2}$ for maxima

Using this option (a) is satisfied and $(2n_1 \ 1)_1 \ (2n_2 \ 1)_2$ for minima Using this 3rd option is satified Hence correct options are (a) and (c).

(a) q; (b) p; (c) r; (d) s

3. Distance between third order maxima and central maxima $\frac{3D}{d}$ 3w

Distance between 3rd order minima and central

Maxima 3
$$\frac{1}{2} \frac{D}{d}$$
 2.5 $\frac{D}{d}$ 2.5 w

Distance between first minima and forth order

maxima
$$\frac{4D}{d}$$
 $\frac{D}{2d}$ 2.5 w

Distance between first minima and forth order

maxima
$$\frac{4D}{d}$$
 $\frac{D}{2d}$ $3.5w$

Distance between 2nd order maxima and fifth order minima $4.5 w \ 2w \ 2.5 w$

hence correct match is

(a) q; (b) p; (c) r; (d) p

(a) *p*

Similarly for other the correct match

(b)
$$r, s; (c) p; (d) p$$

5. When $y = \frac{D}{2d}$ there will a dark fringe at 0.

hence (a) q

when
$$y \quad \frac{D}{6d} \quad 3 \quad \frac{D}{2d}$$

The intensity becomes 3I

(b)
$$p$$

when $y = \frac{D}{4d}$ Intensity $2I$
(c) s

when
$$y = \frac{D}{3d}$$
 Intensity I
(d) r

6. When a thin plate (transparent) is placed in front of S_1 zero order fringe shift above from O hence

(a) *r*

When S_1 is closed interference disappear and uniform illuminance is obtained on screen hence

Similarly (c) r, s and

When *s* is removed and two real sources s_1 and s_2 emitting light of same wavelength are placed interference disappear. Since sources become non-cohrrent hence (d) p, q

29. Modern Physics I

Introductory Exercise 29.1

3. For H-atom $r_n = \frac{0}{me^2} n^2 h^2$ **1.** The positron has same mass m as the electron. The reduced mass of electron positron atom is $u_n \quad \frac{e^2}{2 \circ nh}$ $rac{m}{m}rac{m}{m}rac{1}{2}\mathrm{m}$ $T_n = \frac{2 r_n}{\mu} = 2 \frac{n^2 h^2 + 2 n h}{m a^2 a^2}$ $R_H = \frac{me^4}{8 {}^2_0 ch^3}$ $\frac{4_{0}n^{3}h^{3}}{me^{4}}$ $R_P \quad \frac{R_H}{2}$ $r_n = \frac{1}{T_n} = \frac{me^4}{4 {\ }_0^2 n^3 h^3}$ $rac{1}{H}$ R_{H} $rac{1}{2^{2}}$ $rac{1}{3^{2}}$ $r_1 = \frac{me^4}{4 e^2 h^3}$ $rac{1}{R_{P}}$ R_{P} $rac{1}{2^{2}}$ $rac{1}{3^{2}}$ ${}^{1} \quad \frac{9.1 \quad 10^{\ 31} \quad (1.6 \quad 10^{\ 19})^4}{4 \quad (8.85 \quad 10^{\ 12})^2 \quad (6.6 \quad 10^{\ 34})^3}$ $-\frac{P}{H}$ $\frac{R_{H}}{R_{P}}$ 2 $_{1}$ 6.58 $10^{15} \,\mathrm{Hz}$ $_{p}$ 2 $_{H}$ 2 6563 Å 13126 Å $_{2}$ $\frac{1}{2^{3}}$ $\frac{1}{8}$ $\frac{6.58 \ 10^{15}}{8}$ 1.31 m $0.823 \quad 10^{15} \text{ Hz}$ (b) $\frac{1}{r} R \frac{1}{1^2} \frac{1}{2^2}$ $\frac{1}{\frac{1}{He}} \frac{1}{\frac{H}{H}} z^2 \qquad {}_{He} \frac{\frac{H}{2^2}}{\frac{2^2}{2^2}} \frac{6563 \text{ \AA}}{2^2}$ $\frac{c}{-}$ 3 10⁸ R $\frac{3}{4}$ 164 nm He $\frac{9 \quad 10^8 \quad 1.097 \quad 10^7}{4}$ **2.** $\frac{1}{n} = R \frac{1}{n^2} + \frac{1}{n^2}$ for largest wavelength n = 3 $\frac{1}{2}$ R $\frac{1}{4}$ $\frac{1}{9}$ $2.46 \quad 10^{15} \, \mathrm{Hz}$ (c) Number of revolutions $\frac{36}{5R} \quad \frac{36}{5 \quad 1.097 \quad 10^7}$ v_2 T 0.823 10¹⁵ 1 10⁸ $8.23 \quad 10^6$ revolution 656 nm

4. Reduce mass
$$\frac{m m_p}{m m_p} = \frac{207 \text{ m} \cdot 1836 \text{ m}}{(207 \text{ m} \cdot 1836 \text{ m})} = 186 \text{ m}$$

$$r_1 \quad 4 \quad _0 \quad \frac{h^2}{4^{-2} e^2} \quad 4 \quad _0 \quad \frac{h^2}{4^{-2}(186m) e^2}$$

Putting the value we get

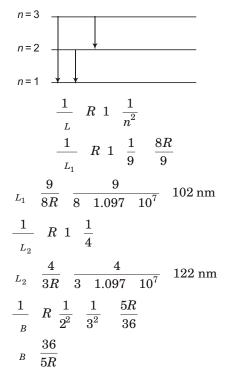
$$r_{1} \quad 2.55 \quad 10^{-13} \text{m}$$
$$E_{1} \quad \frac{e^{4}}{8 \quad _{0}^{2} h^{2}} \quad 2810 \text{ eV}$$

Ionization energy E_1 2.81 keV

5. (a)
$$\frac{h}{mv} = \frac{6.6 \times 10^{-34}}{46 \times 10^{-3} \times 30} = 4.8 \times 10^{-34} \text{ m}$$

(b) $\frac{6.6 \times 10^{-34}}{9.1 \times 10^{-31} \times 10^7} = 7.3 \times 10^{-11} \text{ m}$

6. (a) After absorbing 12.3 eV the atom excited to n = 3 state



$$B = \frac{36}{5 \ 1.097 \ 10^7} \ 653 \text{ nm}$$
7. $K = K = L = L = \frac{K - K}{K - K}$

$$\frac{c}{K} = \frac{c}{K} = \frac{c}{L} = L = \frac{0.71 \ 0.63}{0.71 \ 0.63}$$

$$\frac{1}{L} = \frac{1}{K} = \frac{1}{K} = L = 5.59 \text{ nm}$$
8. $\frac{hc}{E}$

$$E_2 = -2870 \text{ eV}$$

$$K = E_1$$

$$K = \frac{6.6 \ 10^{-34} \ 3 \ 10^8}{(E_1 \ 2870) \ 1.6 \ 10^{-19}}$$
0.71 $10^{-9} = \frac{6.6 \ 10^{-34} \ 3 \ 10^8}{(E_1 \ 2870) \ 1.6 \ 10^{-19}}$
Solving this we get
$$E_1 = 4613 \text{ eV}$$

$$K_B = \frac{6.6 \ 10^{-34} \ 3 \ 10^8}{(4613 \ E_3) \ 1.6 \ 10^{-19}} = 0.63$$
Solving this we get $E_3 = 2650 \text{ eV}$
9. $31 = \frac{4E}{h} = f$

$$(...(i))$$

$$\frac{1}{12} = \frac{3E}{h} = \frac{3}{4} = \frac{4E}{h} = \frac{3f}{4}$$

Introductory Exercise 29.2

1. $eV_0 \quad \frac{hc}{dc} \quad W$ $eV_0 = \frac{6.6 \quad 10^{-34} \quad 3 \quad 10^8}{2 \quad 10^{-7} \quad 1.6 \quad 10^{-19}} \quad 4.3 \text{ eV}$ eV_0 6.2 eV 4.3 eV 1.9 eV V_0 1.9 volt **2.** P 1.5 mW 1.5 10 3 W 5. Energy of each photon $\frac{6.62 \quad 10 \quad {}^{34} \quad 3 \quad 10^8}{4 \quad 10 \quad {}^7}$ 4.96 10¹⁹ J Number of photons incident per second $\frac{P}{\text{Energy of each photon}} \quad \frac{1.5 \quad 10^{-3}}{4.96 \quad 10^{-19}}$ $\sim 3 \ 10^{15}$ The number of photoelectrons produce $0.1\% \ \ 3 \ \ 10^{15} \ \ 3 \ \ 10^{12}$ Current i 3 10^{12} 1.6 10 19 A 4.8 10⁷ A 0.48 A **3.** K_{max} hf W hf hf₀ K_{max} $(f f_0)$

4. $K_{\text{max}} \quad \frac{hc}{W}$ $\frac{6.62 \quad 10^{\ 34} \quad 3 \quad 10^8}{2 \quad 10^{\ 7} \quad 1.6 \quad 10^{\ 19}} \quad 3 \ \ eV$ [6.20 3]eV 3.20 eV The minimum kinetic energy 0. K_{\max} $h[f f_0]$ $1.2 \, \text{eV} \quad h[f \quad f_0]$...(i) 4.2 eV $h[1.5f f_0]$...(ii) Dividing Eq. (i) and Eq. (ii) $\frac{124}{42} \quad \frac{f}{1.5f} \quad \frac{f_0}{f_0}$ $3f \ 2f_0 \ 7f \ 7f_0$ $5f_0 4f$ $f_0 = \frac{4}{5}f = 0.8f$ 1.2 1.6 10¹⁹ 6.62 10³⁴ $\frac{f_0}{0.8}$ f_0 $\frac{1.2 \quad 1.6 \quad 10^{\ 19}}{6 \ 62 \quad 10^{\ 34}} \quad \frac{2f_0}{8} \quad \frac{f_0}{4}$ f_0 1.16 10¹⁵Hz

Subjective Questions (Level I)

1. Here 280 nm 28 10 ⁸ m $E \frac{hc}{28} \frac{6.6 \cdot 10^{-34}}{28 \cdot 10^{-8}} J$ $E \frac{19.8 \cdot 10^{-34}}{28} J \frac{198 \cdot 10^{-19}}{28} J$ $E \frac{198 \cdot 10^{-19}}{28} eV \frac{198}{28} \frac{10^{-19}}{1.6} \sim 4.6 eV$ We have $E mc^2 m \frac{E}{c^2} \frac{198 \ 10^{\ 19}}{28 \ 9 \ 10^{16}}$ $m \ 8.2 \ 10^{\ 36} \text{ kg}$ Momentum $p \ mc \ 8.2 \ 10^{\ 36} \ 3 \ 10^8$ $2.46 \ 10^{\ 27} \text{ kg-m/s}$ 2. Intensity of light at a distance 2 m From the source $\frac{1}{4} \frac{1}{(2)^2} \frac{1}{16} \text{ W/m}^2$ Let plate area is A

Energy incident on unit time is

$$E_1 \quad \frac{1}{16}A$$

Energy of each photon

$$\frac{6.6 \quad 10^{-34} \quad 3 \quad 10^8}{4.8 \quad 10^{-7}}$$

Number of photons striking per unit area

$$n \quad \frac{\frac{1}{16}}{A \quad 6.6 \quad 10^{-34} \quad 3 \quad 10^{-7}}$$

$$4.82 \quad 10^{16} \text{ per m}^2 \text{ s}$$
3. Here $p \quad 8.24 \quad 10^{-28} \text{ kg-m/s}$

(a) Energy of photon E pc

Energy (in eV) 1.54 eV

(b) Wavelength

$$\frac{h}{p} \quad \frac{6.6}{8.24} \quad \frac{10}{10}^{\frac{34}{28}} \quad 804 \text{ nm}$$

This wavelength in Infrared region.

4. We have $c \ f \ f \ \frac{c}{6} \ \frac{3 \ 10^8 \,\mathrm{m/s}}{6 \ 10^{7} \mathrm{m}}$

 $\begin{array}{ccc} f & 5 & 10^{14} \, \mathrm{Hz} \\ \mathrm{We \ have \ } p & \displaystyle \frac{E}{t} & E & pt \ \mathrm{power \ per \ sec} \\ \mathrm{energy} \end{array}$

$$\begin{array}{cccccc} P & E \\ 75 & (h & v) & n \\ & & 75 \\ \hline 6.6 & 10 & ^{34} & 5 & 10^{14} \\ n & 2.3 & 10^{20} \text{ photons/sec} \end{array}$$

5. (a) E = 2.45 MeV $2.45 = 1.6 = 10^{-19} = 10^6$ J $E \quad h \qquad \frac{E}{h} \quad \frac{3.92}{6.6} \quad \frac{10^{-13}}{10^{-34}}$ $5.92 \quad 10^{20} \text{ Hz}$ (b) We have *c* $\frac{3 \quad 10^8}{5.92 \quad 10^{20}} \quad 5.06 \quad 10^{-13} \ m$ 6. We have $p \sqrt{2mK}$ $p_1 \quad \sqrt{2mK_1} \text{ and } p_2 \quad \sqrt{2mK_2}$ $rac{p_1}{p_2} \quad \sqrt{rac{K_1}{K_2}}$ $rac{1}{2}$ $\sqrt{rac{K_1}{K_2}}$ [:: p_2 $2p_1$] $K_2 = 4K_1$ (b) $E_1 \quad p_1 c \text{ and } E_2 \quad p_2 c \quad E_2 \quad 2 p_1 c$ $E_2 \quad 2E_1$ 7. (a) Since power energy per unit line let *n* be the number of photons nc10 --

(b) Force exerted on that surface

$$F \quad \frac{P}{c} \quad \frac{10}{3 \quad 10^8} \quad 3.33 \quad 10^8 \text{ N}$$

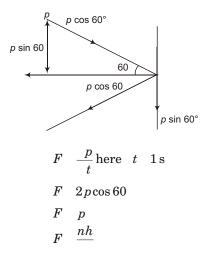
8. Absorbing (power) light 70% of incident light

$$P_{a} \quad 70\% \text{ of } 10 \text{ W} \quad 7 \text{ W}$$
Refractive power $30\% \text{ of } 10 \text{ W}$

$$P_{R} \quad 3 \text{ W}$$
The force exerted $\frac{P_{a}}{c} \quad \frac{2P_{R}}{c}$

$$\frac{7}{2} \quad \frac{2}{3} \quad \frac{13}{3} \quad 10^{8}$$

$$4.3 \quad 10^{-8} \text{ N}$$



where n is number of photons striking per second

$$F \quad \frac{1 \quad 10^{19} \quad 6.63 \quad 10^{34}}{663 \quad 10^{9}} \quad 10^{8} \,\mathrm{N}$$

10. Here output energy 60 W/s

Pressure
$$p = \frac{2 \quad 60}{3 \quad 10^8} \quad 4 \quad 10^{-7} \text{ N}$$

de-Broglie wavelength

11. Here m 5 g m 5 10 3 kg, v 340 m/s

by de-Broglie hypothesis wavelength

$$\frac{h}{mv} = \frac{6.62 \quad 10^{-34}}{5 \quad 10^{-3} \quad 340}$$

3.9 = 10^{-34} m

Since is too small. No wave like property is exhibit.

12.(a)
$$_{e} \frac{h}{m_{e}v} \frac{6.6 \ 10^{34}}{9.1 \ 10^{31} \ 4.7 \ 10^{6}}$$

1.55 10^{10} m
(b) $_{p} \frac{6.6 \ 10^{34}}{1836 \ 9.1 \ 10^{31} \ 4.7 \ 10^{6}}$
8.44 10^{14} m

13. (a)
$$\frac{h}{p}$$
 p $\frac{h}{c}$ $\frac{6.6 \ 10^{-34}}{2.8 \ 10^{-10}}$
 p 2.37 10^{-24} kgm/s
(b) $\therefore p^2 \ 2m_e K \ K \ \frac{p^2}{2m_e}$
 $K \ \frac{(2.37 \ 10^{-24})^2}{2 \ 9.1 \ 10^{-31}}$
 K 3.07 10^{-18} J
 $K (\text{in eV}) \ \frac{K \ \text{in } J}{1.6 \ 10^{-19}} \ \frac{3.07 \ 10^{-18}}{1.6 \ 10^{-19}}$
 $K \ 19.2 \ \text{eV}$
14. Here T 273 20 293 K
 $v_{\text{rms}} \ \sqrt{\frac{3RT}{M}} \ \frac{h}{Mv_{\text{rms}}}$
 $\frac{h}{\sqrt{3MRT}}$
 $6.6 \ 10^{-34}$

$$\overline{ \sqrt{3 \ 1836 \ 9.1 \ 10^{\ 31} \ 8.31 \ 293} } \\ 1.04 \ \text{\AA}$$

15. For hydrogen like atom

$$E K ext{ Here } E 3.4 ext{ eV} K 3.4 ext{ eV} 3.4 ext{ 1.6 } 10^{-19} ext{ J} \frac{h}{p} \frac{h}{\sqrt{2m_e K}} \frac{6.6 ext{ 10 }^{-34}}{\sqrt{2 ext{ 9.1 } 10^{-31} ext{ 3.4 } 1.6 ext{ 10 }^{-19}}} 6.663 ext{ Å}$$

16. In Bohr model the velocity of electron in *n*th orbit is given by

$$U_n = rac{e^2}{2_0 nh}$$

Putting the values of e, 0, h and n 1, we get

$$U_1 \ \ 2.19 \ \ 10^7 \, {
m m/s} \ {
m and} \ U_4 \ \ {2.19 \over 4} \, {
m m/s} \ {
m m/s}$$

 $\begin{array}{cccc} & 1.33 & 10 \ ^9 \mathrm{m} \\ \end{array}$ The radius of first Bohr orbit $r_1 & 0.529 & 10 \ ^{10} \\ \end{array}$ The radius of fourth Bohr orbit $r_4 & 16 & 0.529 & 10 \ ^{10} \\ & 2 \ r_1 & 2 & 3.14 & 0.529 & 10 \ ^{10} \\ & & 3.32 & 10 \ ^{10} \mathrm{m} & _1 \end{array}$

Bohr Atomic Model and Emission Spectrum

17. For hydrogen like atom we can write

$$e_n \quad \frac{z^2}{n^2} (13.6 \,\mathrm{eV})$$

For lithium atom z = 3 we get

$$E_n = \frac{9}{n^2} (13.6 \,\mathrm{eV}) = \frac{122.4}{n^2} \,\mathrm{eV}$$

The ground state energy is for n = 1

$$E_1 = \frac{122.4}{1^2} \,\mathrm{eV} = 122.4 \,\mathrm{eV}$$

Ionization potential E_1 122.4 eV

18. For hydrogen atom we can write

(a) E K K 3.4 eV

(b) PE 2K 2 3.4 6.8 eV

Since potential energy depends upon refrence hence it will changed.

19. Binding energy of an electron in He-atom is E_0 24.6 eV. *ie*, the energy required to remove one electron from He-atom 24.6 eV

Now, He-atom becomes He and energy of He ion is given by

$$E_n = \frac{z^2(13.6)}{n^2}$$
 for He z 2, we get

 E_1 4 13.6 54.4 eV.

Hence energy required to remove this electron 54.4 eV, thus total energy 24.6 54.4 79 eV **20.** For hydrogen atom $E_n = \frac{13.6 \,\mathrm{eV}}{n^2}$

Putting
$$n = 3$$
, we get
 $E_3 = \frac{13.6 \text{ eV}}{9} = 1.51 \text{ eV}$

Hence hydrogen atom is in third excited state the angular momentum

$$L \quad \frac{nh}{2} \quad \frac{3h}{2} \quad \frac{3}{2} \quad \frac{6.62}{2} \quad \frac{10}{34}$$

$$L \quad 3.16 \quad 10^{-34} \text{ kg} \text{m}^2/\text{s}$$
21. We have
$$\frac{hc}{E} \quad \frac{6.6}{10} \quad \frac{10}{34} \quad 3 \quad 10^8}{E}$$

$$E \quad \frac{6.6}{1023} \quad \frac{10}{10} \quad \frac{10}{10} \quad (\text{in Joule})$$

$$E \quad \frac{6.6}{1023} \quad \frac{10}{10} \quad \frac{34}{1.6} \quad 3 \quad 10^8}{10^{10}} \quad (\text{in V})$$

$$\approx 12.1 \text{ eV}$$

$$E_n \quad E_1 \quad 12.1 \text{ eV} \text{ But } E_1 \quad 13.6 \text{ eV}$$

$$E_n \sim 1.51 \text{ eV}$$
For H-atom $E_n \quad \frac{13.6}{n^2} \quad 1.51 \quad \frac{13.6}{n^2}$

$$n \quad 3$$

Hence atom goes to 3rd excited state. The possible transition are $(3 \ 2, 3 \ 1, and 2 \ 1)$ *ie*, 3 transitions are possible and the largest wavelength 1023 Å

22. For hydrogen like atom

$$E_n = \frac{z^2}{n^2} (13.6) \,\mathrm{eV}$$

For Li z 3 $E_n = \frac{122.4}{n^2} \text{eV} = E_1 = 122.4 \text{ eV}$ $E_3 = \frac{122.4}{9} \text{eV} = 13.6 \text{ eV}$ $E = E_3 = E_1 = (122.4 = 13.6) \text{ eV} = 108.8 \text{ eV}$ $\frac{hc}{E} = \frac{6.6 = 10^{-34} - 3 = 10^8}{108.8 = 1.6 = 10^{-19}} = 113.74 \text{ Å}$

23. The excited state energy He atom will be equal to the sum of energies of the photons having wavelength 108.5 nm and 30.4 nm.

For He atom
$$E_n = \frac{z^2(13.6)}{n^2} eV$$

For He z 2

$$E_n \quad \frac{54.4}{n^2} \text{ eV}$$

$$E_1 \quad 54.4 \text{ eV}$$

$$E_n \quad E_1 \quad 54.4 \quad 1 \quad \frac{1}{n^2} \text{ eV} \quad \dots \text{(ii)}$$

From Eqs. (i) and (ii), we get

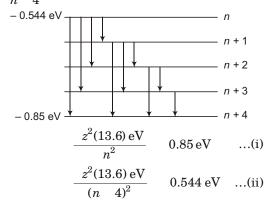
52.3 54.4 1
$$\frac{1}{n^2}$$

1 $\frac{1}{n^2}$ 0.96
 n 5

24. For hydrogen like atom

$$E_n \quad \frac{z^2}{n^2} (13.6) \,\mathrm{eV}$$

Let for ten transitions quantum numbers of energy levels are n, n = 1, n = 2, n = 3 and n = 4



$$\frac{(n \quad 4)^2}{n^2} \quad \frac{0.85}{0.544} \quad 1.5625$$
$$\frac{n \quad 4}{n} \quad 1.25$$
$$1 \quad \frac{4}{n} \quad 1.25$$
$$\frac{4}{n} \quad 0.25$$
$$n \quad \frac{4}{0.25} \quad 16$$

Putting this value of *n* in Eq. (i)

$$\frac{z^{2}(13.6)}{(16)^{2}} = 0.85$$

$$z^{2} = \frac{256 - 0.85}{13.6}$$

$$z^{2} = 16 - z - 4$$

Hence atom no. of atom is 4

We know that $E = \frac{hc}{c}$

 $\frac{hc}{E}$ for smallest wavelength E is maximum

$$\frac{6.6 \quad 10^{34} \quad 3 \quad 10^8}{[\quad 0.544 \quad (\quad 0.85)] \quad 1.6 \quad 10^{-19}}$$

40441 Å

25.	Here E_1 15.6 eV	v^2 m $^2r^2$
	Here E_1 15.6 eV (a) Hence ionization potential E_1 15.6 eV (b) We have $\frac{hc}{E}$ for short wavelength E is maximum $\frac{6.6 \ 10^{-34} \ 3 \ 10^8}{0 \ (-5.3) \ 1.6 \ 10^{-19}} \sim 2335 \text{ Å}$ (c) Excitation potential for $n \ 3$ state is $E_3 \ E_1 \ 3.08 \ 15.6 \ 12.52 \text{ V}$ (d) From $n \ 3$ to $n \ 1$ $E \ E_3 \ E_1 \ 3.08 \ 15.6 \ 12.52 \text{ eV}$ We know $\frac{hc}{E}$ $\frac{1}{hc} \ \frac{E}{6.6 \ 10^{-34} \ 3 \ 10^8}{6.6 \ 10^{-34} \ 3 \ 10^8}$ $1.01 \ 10^7 (m^{-1})$ (a) $E_1 \ 6.52 \text{ eV}$	But by Bohr's postulate mvr $\frac{nh}{2}$ $m^{2}v^{2}r^{2}$ $\frac{n^{2}h^{2}}{4^{2}}$ $m^{3-2}r^{4}$ $\frac{n^{2}h^{2}}{4^{2}m^{3-2}}$ r^{4} $\frac{n^{2}h^{2}}{4^{2}m^{3-2}}$ $r \sqrt{n}$ 28. $\frac{1}{\kappa}$ $R(z \ 1)^{2}$ 1 $\frac{1}{2^{2}}$ $\frac{1}{0}$ $\frac{1}{\kappa}$ $R(z \ 1)^{2}$ 1 $\frac{1}{3^{2}}$ $\frac{\kappa}{\kappa}$ $\frac{3}{4}$ $\frac{9}{8}$ $\frac{27}{32}$ κ $\frac{27}{32}$ κ $\frac{27}{32}$ 0
20.	$\begin{array}{rl} 860 \ \mathrm{nm} & 8600 \ \mathrm{\AA} \\ \mathrm{Energy \ of \ this \ photon} \\ & \frac{12375 \ (\mathrm{eV})}{8600} & 1.44 \ \mathrm{eV} \\ \mathrm{hence \ internal \ energy \ of \ atom \ after \\ absorbing \ this \ photon \ is \ given \ by \\ E_i E_1 1.44 \ \mathrm{eV} 6.52 1.44 \\ & 5.08 \ \mathrm{eV} \\ \mathrm{(b)}_{\ 2} \frac{12375 \ (\mathrm{eV})}{4200} 2.95 \ \mathrm{eV} \\ \mathrm{hence \ internal \ energy \ of \ the \ atom \ after \\ emission \ of \ this \ photon \ is \ given \ by \\ E_i E_1 2.95 \ \mathrm{eV} (\ 2.68 2.95) \ \mathrm{eV} \end{array}$	29. $_{0} \frac{hc}{eV}$ $_{0_{1}} \frac{6.6 10^{34} 3 10^{8}}{1.6 10^{19} 25 10^{3}}$ $_{0_{1}} 49.5 \text{ pm}$ $_{0_{2}} 2 0_{1} 2 49.5 \text{ pm} 99 \text{ pm}$ $[1 \text{ pm} 10^{12} \text{ m}]$ 30. $f_{K} (2.48 10^{15}) \text{ Hz} (z 1)^{2}$ $\frac{3 10^{8}}{\kappa} 2.48 10^{15} (2 1)^{2}$ $\frac{3 10^{8}}{0.76 10^{10} 2.58 10^{15}} (z 1)^{2}$ $z 1) \sim 40 z 41$ hc
27.	$E_{i} = 5.63 \text{ eV}$ Heve $U = \frac{1}{2}m^{-2}r^{2}$ $F = \left \frac{dU}{dr}\right = m^{2-2}r$ But $\frac{mv^{2}}{r} = m^{2-2}r$	31. $_{i} \frac{hc}{eV}$ 26 pm when V_{f} 1.5 V $_{f} \frac{f}{e} \frac{(i 26)}{1.5 V} \frac{1}{1.5 eV} \frac{12}{1.5} \frac{1}{1.5} \frac{1}{i}$

$$2^{2}r$$

Photoelectric effect

 This difference equal to n = 3 $n \quad 1$ transition.

36.
$$K_{\text{max}}$$
 h W
 $K_{\text{max}} = \frac{6.6 \quad 10^{-34} \quad 1.5 \quad 10^{15}}{1.6 \quad 10^{-19}} = 3.7$
 $K_{\text{max}} = 6.18 \quad 3.7 \quad 2.48 \text{ eV}$

37. Here work function

$$W(\text{in eV}) \quad \frac{12375}{5000 \text{ Å}} \quad 2.475 \text{ eV}$$

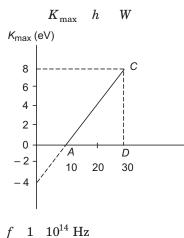
$$K_{\text{max}} \quad \frac{eV_0}{\Delta} \quad 3 \text{ eV}$$

$$K_{\text{max}} \quad \frac{hc}{\Delta} \quad W$$

$$3 \quad \frac{12375}{(\text{in Å})} \quad 2.475$$

$$\frac{12375}{5.475} \quad 2260 \text{ Å}$$

38. Comparing the given graph with



threshold frequency $10 \ 10^{14} \, {\rm Hz}$ (a) _o $10^{15}~{
m Hz}$

(b) W = 4 eV

(c)
$$h$$
 slope of the graph

$$\frac{CD}{AD} = \frac{8 \text{ eV}}{20 \text{ } 10^{14} \text{ Hz}}$$

$$h \quad \frac{8 \quad 1.6 \quad 10^{-19}}{2 \quad 10^{15}} \quad 6.4 \quad 10^{-34} \text{ J-s}$$
39. Here $\frac{v_{1(\text{max})}}{u_{2(\text{max})}} \quad \frac{3}{1}$
Using Einstein equation, $K_{\text{max}} \quad \frac{hc}{-} \quad W$,
we get
 $\frac{1}{2} m v_{\text{max}}^2 \quad \frac{hc}{-} \quad W$

where m is the mass of photoelectron

$$\frac{1}{2}m[v_{1(\max)}]^2 = \frac{hc}{1} = W$$
 ...(i)

and
$$\frac{1}{2}m[v_{2(\max)}]^2 \frac{hc}{2} W$$
 ...(ii)

Dividing Eq. (i) and Eq. (ii), we get

$$\frac{v_{1 \max}}{v_{2 \max}} \stackrel{2}{=} \frac{\frac{hc}{1}}{\frac{hc}{2}} \stackrel{W}{W} \qquad (3)^{2} \stackrel{\frac{hc}{1}}{\frac{hc}{2}} \stackrel{W}{W}$$
$$\frac{\frac{9hc}{2}}{\frac{hc}{2}} \stackrel{hc}{1} \quad 8W$$
$$hc \stackrel{9}{=} \frac{1}{6000} \stackrel{1}{\frac{3000}} \quad 8W$$
$$\frac{6.6 \quad 10^{-34} \quad 3 \quad 10^{8} \quad 7}{6000 \quad 10^{-10} \quad 1.6 \quad 10^{-19}} \quad 8W$$
$$W \quad 1.81 \text{ eV}$$

Putting the value of W in Eq. (i)

$$\frac{1}{2}m(u_{1\,\text{max}})^2 \quad \frac{hc}{3000 \quad 10^{-10}}$$

$$\frac{1.81 \quad 1.6 \quad 10^{-19}}{2 m(u_{1 \max})^2} \quad \frac{6.62 \quad 10^{-34} \quad 3 \quad 10^8}{3 \quad 10^7}$$

~ ~

T7

$$(u_{1 \max})^2 \quad \frac{3.724 \quad 10^{-19} \quad 2}{9.1 \quad 10^{-31}}$$

$$1.81 \quad 1.6 \quad 10^{-19} \quad \because \quad m_e \quad 9.1 \quad 10^{-31}$$

$$u_{1 \max} \quad 9 \quad 10^5 \text{ m/s}$$
and $v_{2 \max} \quad \frac{1}{3} v_{1 \max} \quad 3 \quad 10^5 \text{ m/s}$

40. Here intensity $I = 2 \text{ W/m}^2$ and

Area A 1 10
4
m²

Energy incident per unit time on the metal surface

Energy of each photon 10.6 eV

Number of photons incident on surface $2 10^{15}$

$$\frac{1.6}{1.6}$$
 10.6

Number of photoelectrons emitted

$$\frac{0.53}{100} \quad \frac{2}{1.6} \quad \frac{10^{15}}{10.6}$$

 $6.25 \quad 10^{11} \text{ per second}$

Minimum KE 0

Maximum KE (10.6 5.6) eV 5 eV

41.
$$K_{\text{max}} \quad \frac{hc}{m} \quad W$$

$$K_{\max} = \frac{6.6 \cdot 10^{34} \cdot 3 \cdot 10^8}{180 \cdot 10^{-9}} = 2 \cdot 1.6 \cdot 10^{-19}$$

$$\frac{1}{2} m_e v_{\max}^2 = \frac{6.6 \cdot 3 \cdot 10^{-18}}{18} = 2 \cdot 1.6 \cdot 10^{-19}$$

$$\frac{1}{2} m_e v_{\max}^2 = 11 \cdot 10^{-19} \cdot 3.2 \cdot 10^{-19}$$

$$7.2 \cdot 10^{-19} \text{ J}$$

$$v_{\text{max}} = \sqrt{\frac{2}{9.1} \frac{7.2}{10} \frac{10}{^{31}}} \frac{1.25}{1.25} \frac{10^6}{1.6} \text{ m/s}$$

$$r = \frac{mv_{\text{max}}}{eB} = \frac{9.1}{1.6} \frac{10}{10} \frac{^{31}}{19} \frac{1.25}{5} \frac{10^6}{10^{5}}$$

$$r = 0.148 \text{ m}$$
The given equation is

Light consist of two different frequencies.

$$\begin{array}{c} \text{Maximum frequency} \\ \frac{8 \quad 10^{15}}{2} \quad 1.27 \quad 10^{15} \, \text{Hz} \end{array}$$

For maximum KE we will use Einstein's equation

$$(\text{KE})_{\text{max}}$$
 3.27 eV

43. Here $E = E_0 \sin 1.57 = 10^7 (x - ct)$ frequency of the wave

$$\frac{1.57 \quad 3 \quad 10^{15}}{2 \quad 3.14} \quad 0.75 \quad 10^{15}$$

We have

42.

$$eV_0 = \frac{6.6 \quad 10^{-34} \quad 0.75 \quad 10^{15}}{1.8 \quad 10^{-19}} = 1.9 \ eV_0$$

 V_0 1.2 V

Objective Questions (Level-1)

1. Einstein photo electric equation is

$$K_{\max}$$
 h W

its slope h planck constant which is same for all metals and independent of intensity of radiation.

Hence correct option is (d).

2. Since current is directly proportional to intensity therefore as current is increased

intensity is increased since $_{\min} = \frac{1}{V}$, if V is decreased $_{\min}$ is increased. Hence correct option is (c).

3. For hydrogen atom (Bohr's model) *n*th orbital speed $v_n = \frac{e^2}{2_{-0}nh}$

For first orbit
$$n = 1$$

 $v_1 = \frac{e^2}{2_{-0} - h}$
 $\frac{(1.6 - 10^{-19})^2}{2 - 8.85 - 10^{-12} - 6.62 - 10^{-34}}$
 $v \sim \frac{1}{137} = 3 - 10^8 - \frac{c}{137}$

Hence correct option is (c).

$$4. \ _{86}A^{22} \ _{3} \ _{80}X^{210} \ ^{4} \ _{84}B^{210}$$

Hence correct option is (b)

5. _{min}(in Å)
$$\frac{12375}{V(\text{in volt})} = \frac{12375}{20 \ 1000} \approx 0.62 \text{ Å}$$

Hence correct option is (c).

6. We have
$$\frac{1}{2} m_e v_{max}^2$$
 eV
 $v_{max} = \sqrt{\frac{2eV}{m}}$
 $\sqrt{\frac{2 \ 1.6 \ 10^{\ 19} \ 18 \ 1000}{9.1 \ 10^{\ 31}}}$
 $v_{max} \approx 8 \ 10^7 \text{m/s}$

Hence correct option is (a).

7. For hydrogen atom $v_n = \frac{e^2}{2_0 nh}$ $v_2 = \frac{e^2}{2_0 2h}, v_3 = \frac{e^2}{2_0 3h}$ $\frac{v_2}{v_3} = \frac{3}{2}$

Let $_2$ and $_3$ are the de-Broglie wavelengths

$$\begin{array}{c}
\frac{h}{mv_2} \\
\frac{2}{3} \\
\frac{mv_2}{n} \\
\frac{1}{mv_3} \\
\frac{2}{3} \\
\frac{2}{3}
\end{array}$$

Hence correct option is (a).

8. For hydrogen like atom

$$E_n \quad \frac{z^2}{n^2} (13.6 \,\mathrm{eV})$$

For ground state n = 1

$$\begin{array}{cccc} & E_1 & z^2 & 13.6\,{\rm eV} \\ {\rm But} & E_1 & 122.4\,{\rm eV} \\ & 122.4\,{\rm eV} & z^2 & 13.6\,{\rm eV} \\ & z^2 & 9 \\ & z & 3 \end{array}$$

Hence it is Li^2

The correct option is (c).

9.
$$\min_{\min} \frac{hc}{eV} = \min_{\min} 100 = \frac{V}{V} 100$$

10. $E_n = \frac{z^2}{n^2} (13.6 \text{ eV})$ for first excited state n = 2

$$E_2 \quad \frac{z^2}{4} (13.6) \text{ eV}$$

13.6 eV $\frac{z^2}{4}$ 13.6 eV

z 2

Hence it is He

Correct option is (a).

11.
$$_{\min}(in \text{ Å}) = \frac{12375}{V(in \text{ volt})}$$

 $V = \frac{12375}{1} = 12.375 = 10^3 \text{ V}$
 $V = 12.4 \text{ eV}$

Hence correct option is (c).

12. We have
$$\frac{h}{p}$$

 $p \quad \frac{h}{-} \quad \frac{6.62}{0.5} \quad \frac{10}{10}^{-34}$
13.26 10^{-24} kg-m/s
Hence correct option is (c).
13. $W \quad \frac{hc}{0} = 0 \quad \frac{6.6}{1.6} \quad \frac{10}{10}^{-34} \quad \frac{3}{1.6} \quad \frac{10^8}{1.6}$

₀ 7750 Å

Hence correct option is (a).

14. For H-like atom Balmer series is $\frac{1}{2} z^2 R \frac{1}{2^2} \frac{1}{n^2}$

For third Balmer line n = 5

$$\frac{1}{1085 \ 10^{10}} \ z^2 \ 109 \ 10^7 \ \frac{1}{4} \ \frac{1}{5^2}$$
$$z^2 \ \frac{100 \ 1000}{1085 \ 1.097 \ 21} \ 4$$

z 2

Binding energy (13.6) $z^2 eV$ 13.6 4 eV54.4 eV

Hence correct option is (a).

15. If V_1 0 then total energy KE

KE 13.6 eV

and the energy difference between two states $10.2\,\mathrm{eV}$

Hence total energy in this state

13.6 10.2 23.8 eV

The correct option is (c).

16.
$$eV_0 = \frac{hc}{3300}$$
 W ...(i)

$$2eV_0 = \frac{hc}{2200}$$
 ...(ii)

Substracted Eq. (i) from Eq. (ii), we get

$$eV_0 \quad hc \quad \frac{3300 \quad 2200}{3300 \quad 2200}$$

$$-\frac{hc}{3 \quad 2200 \quad 10^{-10}}$$

$$V_0 \quad \frac{6.6 \quad 10^{-34} \quad 3 \quad 10^8}{3 \quad 2200 \quad 1.6 \quad 10^{-19} \quad 10^{-10}}$$

$$-\frac{30}{16} \quad \frac{15}{8}$$

$$V_0 \quad \frac{15}{8} \text{ V}$$

Hence the correct option is (c).

17.
$$E \stackrel{hc}{=} W$$
 ...(i)

$$4E \quad \frac{hc}{3} \quad W$$
$$4E \quad \frac{3hc}{3} \quad W \qquad \dots (ii)$$

From Eqs. (i) and (ii) $4 \frac{hc}{m} W \frac{3hc}{m} W$ $\frac{hc}{m} 3W$

$$W \quad \frac{hc}{3}$$

Hence correct option is (b).

18.

By Moseley's law

$$\sqrt{f} \quad a(z \quad b) \text{ for } K \quad \text{line } b \quad 1$$

$$\sqrt{f} \quad a(z \quad 1)$$

$$\sqrt{f} \quad a(31 \quad 1) \quad a \quad 30 \qquad \dots(i)$$
and

$$\sqrt{f} \quad a(51 \quad 1) \quad 9 \quad 50$$

$$\sqrt{\frac{f}{f}} \quad \frac{3}{5}$$

$$f \quad \frac{25f}{9}$$

Hence correct option is (a).

19.
$$\sqrt{f} \quad \sqrt{(RC)} (z \quad 1) \sqrt{\frac{1}{12} \quad \frac{1}{n^2}}$$

for *K*, *n* = 2

Correct option is (a).

20.
$$\frac{1}{2}$$
 $R \frac{1}{2^2}$ $\frac{1}{n^2}$ here $n = 3$
 $\frac{1}{2}$ $R \frac{1}{2^2}$ $\frac{1}{3^2}$ $\frac{9}{9} \frac{4}{4}$ $R = \frac{5R}{36}$
 $\frac{36}{5R}$

Hence correct option is (c)

Hence correct option is (c).

22.
$$5eV_0 \quad \frac{hc}{m} \quad W \qquad \dots$$
(i)

$$eV_0 \quad \frac{hc}{3} \quad W \qquad \qquad \dots (ii)$$

$$\frac{5hc}{3} \quad 5W \quad \frac{hc}{3} \quad W$$
$$\frac{5hc}{3} \quad \frac{hc}{3} \quad 4W$$
$$\frac{hc}{3} \frac{(5 \quad 3)}{3} \quad 4W$$
$$\frac{2hc}{3} \quad 4W$$

 $W \quad \frac{hc}{6}$

Hence correct option is (a).

23.
$$eV_0 \quad h[2V_0 \quad V_0] \quad hV_0 \qquad \dots$$
(i)

$$eV \quad h[3V_0 \quad V_0] \quad h \quad 2V_0 \quad 2hV_0 \quad ...$$
(ii)
From Eqs. (i) and (ii)

$$eV \quad 2 \quad eV_0 \quad V \quad 2V_0$$

Hence correct option is (b).

24. For H-atom Lyman series is

$$\frac{1}{2} \quad R \quad \frac{1}{1^2} \quad \frac{1}{n^2}$$
$$v \quad \frac{c}{2} \quad RC \quad \frac{1}{1^2} \quad \frac{1}{n^2}$$

For H-like atom

$$RC \ \frac{1}{12} \quad \frac{1}{n^2} \qquad z^2$$

For Li , n = 3 $3^2 = 9 v$ Hence correct option is (c).

25. Ground state energy of H-atom 13.6 eV

For Li atom
$$E_n = \frac{(13.6) eV}{n^2} z^2$$

13.6 eV $\frac{13.6 eV}{n^2}$
 $n = 3$

Hence correct option is (c).

26.
$$\frac{1}{2}mv_1^2$$
 h_1 W ...(i)

$$\frac{1}{2}mv_2^2$$
 h_2 W ...(ii)

$$\frac{1}{2}m[v_1^2 \quad v_2^2] \quad h[_1 \quad _2]$$
$$v_1^2 \quad v_2^2 \quad \frac{2h}{m}[_1 \quad _2]$$

Hence correct option is (b).

27. For Lyman series $\frac{1}{2} R \frac{1}{2} \frac{1}{2}$

$$= R \frac{1}{1^2} \frac{1}{n^2}$$

For largest wavelength n = 2

$$\frac{1}{2} \quad R \quad \frac{1}{1^2} \quad \frac{1}{2^2}$$
$$\frac{1}{2} \quad R \quad 1 \quad \frac{1}{4}$$
$$\frac{4}{3R}$$

For He atom

Hence correct option is (b).

28. We have
$$\sqrt{\frac{1}{4}}$$
 $\sqrt{\frac{3R}{4}}$ $(z \ 1)$
 $\sqrt{\frac{1}{4}}$ $\sqrt{\frac{3 \ 1.0973 \ 10^7}{4}}$ $(92 \ 1)$
 $\frac{4}{3 \ 91 \ 91 \ 1.0973 \ 10^7}$ 0.15 Å

Hence correct option is (c).

29. For K, K and L of X-rays

$$\begin{matrix} K & K & L \\ Y_2 & Y_1 & Y_3 \end{matrix}$$

Hence correct option is (b).

30. We have
$$\frac{h}{\sqrt{2mqV}}$$

 $p \quad \frac{h}{\sqrt{2m_p eV}} \text{ and } \quad \frac{h}{\sqrt{2m_{e}}V}$
 $-\frac{p}{\sqrt{\frac{2m}{m_p}}} \quad \sqrt{\frac{2}{\frac{4m_p}{m_p}}} \quad \sqrt{8} \quad 2\sqrt{2}$

Hence correct option is (c).

31. We have,
$$_{e} \quad \frac{h}{\sqrt{2m_{e}E_{1}}} \qquad \frac{h}{\sqrt{2m} E_{2}}$$

 $_{p} \quad \frac{h}{\sqrt{2m_{p}E_{3}}} \because m \quad m_{p} \quad m_{e}$

and $e p :: E_1 E_3 E_2$ Hence correct option is (a).

32. KE in ground state $13.6 \,\mathrm{eV}$

Total energy in n KE Energy difference between n to n 1 Total energy

13.6 eV 13.6 eV 27.2 eV

Hence correct option is (b).

33. Here P 1000 W, 880 kHz 880 10^3 Hz

Let n is the number of photon p emitted per second

$$n \quad \frac{P}{h} \quad \frac{1000}{6.62 \quad 10^{-34} \quad 880 \quad 10^3}$$
$$1.7 \quad 10^{30}$$

Correct option is (b).

34. Here 3000 Å 3 10^{-7}m

Energy of incident radiation $E = \frac{hc}{m}$ joule

$$E \quad \frac{hc}{1.6 \quad 10^{-19}} \text{(in eV)}$$
$$E \quad \frac{6.62 \quad 3 \quad 10^{-26}}{3 \quad 1.6 \quad 10^{-26}} \quad 4.125 \text{ eV}$$

 $\therefore E$ work function hence no emission of electrons it means sphere remain natured.

Hence correct option is (c).

35.
$$\therefore E_n = \frac{13.6 \text{ eV}}{n^2}$$
 for $n = 5$
 $E_5 = \frac{13.6 \text{ eV}}{5^2} = 0.54 \text{ eV}$

Hence correct option is (a).

36.
$$K_{\text{max}} = E = W = (6.2 + 4.2) \text{ eV} = 2 \text{ eV}$$

$$K_{\rm max}$$
 2 1.6 10 ¹⁹ J
3.2 10 ¹⁹ J

Hence correct option is (b).

37.
$$\frac{6.62 \quad 10^{34}}{5200 \quad 10^{10}}$$
 9.1 10³¹ *v*
v $\frac{6.625 \quad 10^{27}}{5.2 \quad 9.1 \quad 10^{31}} \sim 1400 \, \text{m/s}$

Hence correct option is (c).

38.
$$K_{\text{max}} = \frac{6.62 \ 10^{\ 3^4} \ 3 \ 10^8}{3000 \ 10^{\ 10} \ 1.6 \ 10^{\ 19}} \ 1 \ \text{eV}$$

 $K_{\text{max}} = 3.14 \ \text{eV} = 3.14 \ 1.6 \ 10^{\ 19} \ \text{J}$
 $\frac{1}{2} m_e v_{\text{max}}^2 = 3.14 \ 1.6 \ 10^{\ 19}$
 $v_{\text{max}} = \sqrt{\frac{3.14 \ 3.2 \ 10^{\ 19}}{9.1 \ 10^{\ 31}}} \sim 10^6 \text{m/s}$

Hence correct option is (d).

JEE Corner

- 1. Here both assertion and reason are true and reason explain correctly assertion. Correct option is (a).
- **2.** For photon $E \quad \frac{hc}{c}$ and $p \quad \frac{E}{c}$

If is doubled, E and p are reduced to half. Hence assertion is true. Since speed of photon is always c. Hence reason is false. Hence correct option is (c).

- **3.** If frequency is increased keeping intensity constant photoelectron emitted the plate reach other plate in less time hence saturation current can be increased. Reason can be true or not hence correct option is (a, b).
- **4.** Here both assertion and reason is true and reason correctly explain assertion. Hence correct option is (a).
- **5.** Here assertion is true since possible transition are 6 3, 6 4, 6 5, 5 3, 5 4, and 4 3. According to reason total $\frac{n(n-1)}{2}$ transition has $n-3 = \frac{6 (3-1)}{2} = 6$ it may explain or may not explain assertion Hence correct option is (a, b)
- 6. We have

$$eV_0$$
 $h[$ $_0]$

$$V_0 = \frac{h}{e} = 0 = \frac{h}{e} = 0$$
 ...(i)

if 2_{0}_{0} does not become double hence assertion is false but reason is true. Hence correct option is (d).

- **7.** Here both assertion and reason are true and reason may or may not explain assertion correct option is (a, b).
- 8. Here assertion and reason are both true.

$$\therefore \quad \lim_{\min} \quad \frac{hc}{eV} \text{ if } V \quad \text{ increases}$$

_{min} decreases

but reason is not correct explanation of assertion hence correct option is (b).

$$9. \quad \because \quad E_n \quad \frac{13.6}{n_2}$$

$$E_2 \quad E_1$$

Hence assertion is true and E

 $\frac{v}{2}$

Κ

v is more in n = 2

Here reason is also true but it is not correct explanation of assertion hence correct option is (b).

10. Here assertion is false but reason is true. Hence correct option is (a).

Objective Questions (Level 2)

1.
$$F_a = F_c = \frac{GmM}{r^2} = \frac{mv^2}{r}$$
 ...(i)
and $mvr = \frac{nh}{2}$...(ii)

From Eq. (ii) $v \frac{nh}{2 mr}$

Putting this value in Eq. (i)

$$\frac{GM}{r} = \frac{h^2 h^2}{4^{-2} m^2 r^2}$$

$$r = \frac{n^2 h^2}{4^{-2} m^2 GM}$$
KE = $\frac{1}{2} m v^2 = \frac{1}{2} \frac{m}{r} \frac{GM}{r} = \frac{GMm}{2r}$
PE = $\frac{GMm}{r}$

$$E = KE = PE$$

$$E = \frac{GMm}{2r} = \frac{GMm}{2n^2 h^2}$$

$$E = \frac{2^{-2} G^2 M^2 m^3}{n^2 h^2} \text{ for ground state } n = 1$$

$$E = \frac{2^{-2} G^2 M^2 m^3}{n^2}$$

Hence correct option is (b).

2. We have $_{n} i_{n}A_{n} \frac{e}{T_{n}} r_{n}^{2}$ $n \frac{e}{2} \frac{r_{n}^{2} u_{n}}{2} \frac{e u_{n} r_{n}}{2}$ $n e \frac{v_{1}}{n} \frac{r_{1} n^{2}}{2} \frac{e v_{1} r_{1}}{2} n$ $2 \frac{e v_{1} r_{1} 2}{2}$ and $1 \frac{e v_{1} r_{1}}{2} 1$ $1 \frac{2}{2}$

Hence magnetic moment decreases two times correct option is (b).

3. For H-like atom
$$E_n = \frac{(13.6)Z^2 eV}{n^2}$$

Here $E_2 = \frac{(13.6)z^2}{4}$ and $E_1 = 13.6 z^2$
 $E_2 = E_1 = 40.8 eV$
 $13.6Z^2 = 1 = \frac{1}{4} = 40.8$
 $Z^2 = \frac{408}{13.6} = \frac{4}{3} = Z^2 = 4$
 $Z = 2$

Energy needed to remove the electron from ground state is

$$E_1$$
 (13.6) Z^2 13.6 4 54.4 eV

Hence correct option is (a).

÷

$$i_n \quad \frac{e}{T_n} \quad \frac{e}{2 r_n} \quad \frac{ev_n}{2 r_n}$$
$$u_n \quad \frac{1}{n} \text{ and } r_n \quad \frac{1}{n^2}$$
$$i_n \quad \frac{1}{n^3} \quad \frac{i_2}{i_1} \quad \frac{1}{2^3}$$
$$i_1 \quad 8i_2$$

Hence current increases 8 times correct option is (c).

- **5.** Since five dark lines are possible hence atom is excited to n = 6 state.
 - The number of transition in emission line $\frac{n(n-1)}{2}$

Number of emission transition
$$\frac{6}{2}$$
 15

Hence correct option is (c).

6. $A_n = r_n^2$ for hydrozen atom $r_n = kn^2$

where *k* is constant.

$$egin{array}{ccc} A_n & k^2 n^4 \ A_1 & k^2 & rac{A_n}{A_1} & n^4 \end{array}$$

0 4

Taking log both sides log $\frac{A_n}{A_1} = 4 \log_n$

Hence it is a straight line with slope 4 Correct option is (b)

7. For hydrogen atom $i_n = \frac{1}{n^3}$ and

$$B_{n} \quad \frac{i_{n}}{r_{n}} \quad B_{n} \quad k \frac{1}{n^{5}} \qquad [\because r_{n} \quad n^{2}]$$
$$B_{2} \quad \frac{k}{2^{5}} \text{ and } B_{1} \quad k$$
$$\frac{B_{2}}{B_{1}} \quad \frac{1}{2^{5}} \quad \frac{1}{32}$$
$$B_{1} \quad 32 B_{2}$$

Hence magnatic field increases 32 times. The correct option is (d).

8. For H-atom Lyman series is given by

$$\frac{1}{2} \quad R \quad \frac{1}{1^2} \quad \frac{1}{n^2} \quad \text{for first line } n \quad 2$$
$$\frac{1}{2} \quad R \quad 1 \quad \frac{1}{2^2}$$
$$\frac{1}{2} \quad \frac{3R}{4}$$

Momentum of photon P_p $\frac{h}{-}$

Let momentum of atom p_A

 \therefore Initial momentum was zero. Hence using momentum conservation law, we get

$$egin{array}{cccc} p_A & p_B & Mv & rac{h}{2} & rac{3hR}{4} \ & v & rac{3hR}{4M} \end{array}$$

Hence the correct option is (a).

9. Light wave equation is

 $200 \text{ V/m} \sin (1.5 \quad 10^{15} \text{ sec}^{-1}) t$ $\cos (0.5 \quad 10^{15} \text{ sec}^{-1}) t$ Here maximum frequency $\frac{1.5 \quad 10^{15}}{2}$

Maxmum incident energy

$$\frac{1.5 \quad 10^{15}}{2} \quad \frac{6.6 \quad 10^{-34}}{1.6 \quad 10^{-19}}$$

0.98 eV

Since work function $2 \, eV$ maximum energy hence no emission of electrons.

Thus correct option is (d).

10. Since in Balmer series of H-like atom wavelengths (in visible region) are found same or smaller hence the gas was initially in second excited state.

Correct option is (c).

11. For H-atom T_H 2 n^3

and for H-like atom

$$T_x \quad \frac{2 n^3}{z^2}$$

For H-atom in ground state $T_H = 2$ For H-like atom in first excited state

$$T_{x} \quad \frac{(2 \) \quad 2^{3}}{z^{2}} \quad \frac{2 \quad 8}{z^{2}}$$

But $T_{H} \quad 2T_{x} \quad 2 \quad \frac{2 \quad 2 \quad 8}{z^{2}}$
 $z^{2} \quad 16$
 $z \quad 4$

Hence correct option is (c).

12. For K line of X-ray

$$\frac{1}{c} \frac{a^2}{c} (z \ 1)^2$$

 $\therefore z$ (atomic No.) for Pb²⁰⁴, Pb²⁰⁶, Pb²⁰⁸ are same hence $1 \ 2 \ 3$. Hence correct option is (c).

13. The correct option is (d).

14. Since
$$E_n = \frac{13.6 \text{ eV}}{n^2}$$

 $E_1 = 13.6 \text{ eV}$
and first excited state $E_2 = \frac{13.6}{4} \text{ eV}$

$$E_2$$
 3.4 eV

 $E \quad E_2 \quad E_1 \quad 10.2\,\mathrm{if}\,K \quad 10.2\,\mathrm{eV}$

The electron collide elastically with H-atom in ground state.

The correct option is (c).

15. For Lyman series $\frac{1}{n} = R \frac{1}{1^2} + \frac{1}{n^2}$ here n = 3 $\frac{1}{n} = R + 1 + \frac{1}{2}$

$$\frac{1}{2} \quad \frac{8R}{9}$$

$$P_{\text{photon}} \quad \frac{h}{2} \quad \frac{8Rh}{9}$$

But

$$v = \frac{\frac{P_{\text{Photon}}}{P_{\text{H-atom}}}}{\frac{8Rh}{9}} \frac{M_p}{M_p} \frac{v}{V}$$

v = 4 m/s

Hence correct option is (a).

16. Power VI 150 10^3 10 10^3 1500 W The 99% power heated the target hence

Heating power $\frac{99}{100}$ 1500 15 99 W

The rate at which target is heated per sec. (in cal)

$$\frac{15 \ 99}{4.2} \sim 355 \qquad \because 1J \quad \frac{1}{4.2} \text{cal}$$

Hence correct option is (c).

17.
$$E_n = \frac{13.6 \text{ eV} z^2}{n^2}$$

 $E_3 = \frac{13.6 \text{ eV}}{9} z^2 \text{ and } E_4 = \frac{13.6 \text{ eV}}{16} z^2$
 $E = E_4 = E_3 = (13.6) \text{ eV} = z^2 \frac{1}{9} = \frac{1}{16}$
 $E = \frac{13.6(\text{eV}) - 2^2 - 7}{16 - 9} = 32.4 \text{ eV}$

$$z^2 = \frac{16 \quad 32.4 \quad 9}{13.6 \quad 7} \quad 49$$

z 7

Hence correct option is (d).

$$18. \qquad \frac{h}{p} \quad \frac{h}{\sqrt{2m_p K}} \quad \frac{h}{\sqrt{2m_p eV}}$$

10¹³
$$\frac{6.6 \ 10^{34}}{\sqrt{2} \ 1836 \ 9.1 \ 10^{31} \ 1.6 \ 10^{19} \ V}$$
$$V \ 8.15 \ 10^4 \ \text{volt}$$

Hence correct option is (b).

19. Since
$$E_n = \frac{1}{n^2}$$
 and $L_n = n$
Hence $E_n = \frac{1}{L_{n^2}}$

The correct option is (d).

20. Since
$$_n \quad \frac{eu_n r_n}{2} \because u_n \quad \frac{1}{n} \text{ and } r_n \quad n^2$$

 $_n \quad kn$
Where k is constant for H-atom
For ground state $_1 \quad k \quad 1 \quad k \quad \dots(i)$
For third excited state n $\quad 4$
 $_2 \quad k \quad 4 \quad 4k \quad \dots(ii)$
From Eqs. (i) and (ii) we get $_2 \quad 4 \quad 1$

Hence correct option is (d).

21. By conservation of momentum

$$M_H v (M_H M_H) v v \frac{v}{2}$$

Let initial KE of H-atom
$$K$$

Final KE of each-H-atom $\frac{K}{2}$
For excitation $\frac{K}{2}$ E_2 E_1 $\frac{13.6}{4}$ 13.6
 $\frac{K}{2}$ 10.2 eV
 K 20.4 eV

Hence correct option is (a).

22. We know that for H-like atom

$$\begin{array}{rcrr}
 E_n & K_n & K_n & 3.4 \text{ eV} \\
 & \frac{h}{p} & \frac{h}{\sqrt{2m_e K}} \\
 & \frac{6.6 & 10^{-34}}{\sqrt{2} & 9.1 & 10^{-31} & 3.4 & 1.6 & 10^{-19}} \\
 & 6.6 \text{ Å}
 \end{array}$$

Hence both options (a) and (b) are correct.

Hence answer is (c) both are correct.

23-25. 0.6e
$$\frac{hc}{4950 \ 10^{10}}$$
 W ...(i)
1.1 e $\frac{hc}{2}$ W ...(ii)

Subtracting Eq. (i) from Eq. (ii) we get

23. W 1.9 eV

Hence correct option is (c).

24. 4111 Å

Hence correct option is (c)

25. Since magnatic field does not change the KE of electrons hence retarding potential remain same.

Hence correct option is (c).

$$26. (KE)_{max} \quad 5 \, \text{eV} \quad 3 \, \text{eV} \quad 2 \, \text{eV}$$

$$\begin{array}{ccc} 2 & 1.6 & 19 \text{ J} \\ \\ \text{min} & \displaystyle \frac{h}{p} & \displaystyle \frac{h}{\sqrt{2m_eK}} \end{array}$$

$$\begin{array}{c} \text{min} & \frac{6.6 \quad 10^{-34}}{\sqrt{2 \quad 9.1 \quad 10^{-31} \quad 2 \quad 1.6 \quad 10^{-19}}} \\ & 8.69 \text{ \AA} \end{array}$$

Hence correct option is (b).

27. Photo emission will stop when potential of sphere becomes stopping potential

$$\frac{1}{4_{0}}\frac{q}{r} = 2V$$
(KE)_{max} eV₀

hence V_0 2

Since

$$q = 8 _{0} r \text{ coulomb}$$

Hence correct option is (b)

28. Let t be the time for photo emission $\frac{1}{4_0}$ $\frac{q}{r}$ t 2

$$t \quad \frac{8 \quad 0}{q}r$$

Intensity of light at 0.8 from source

 $I = \frac{3.2 \times 10^{-3}}{4 \times (0.8)^2} \approx 4 \times 10^{-4} \,\mathrm{W/m^2}$

Energy incident on the sphere in unit time

 E_1 (8 10 ³)² 4 10 ⁴ 8.04 10 ⁸ W Energy of each photon

$$E_2$$
 5 1.6 10 ¹⁹ 8 10 ¹⁹ J

Total number of photons incident on the sphere per second

$$\frac{E_1}{E_2} \quad \frac{8.04}{8} \quad \frac{10}{19}^{8} \quad 10^{11}$$

Since 10^6 photons emit one electron.

Hence the total number of photoelectron per sec is $n_2 \quad \frac{n_1}{10^1} \quad \frac{10^{11}}{10^6} \quad 10^5$ Therefore, $q \quad n_2 \quad e \quad t \quad 10^5 \quad 1.6 \quad 10^{-19} \quad t$

$$t \quad \frac{2}{9} \quad \frac{8}{1.6} \quad \frac{10}{10^{5}} \quad t \quad 111 \,\mathrm{s}$$

Hence correct option is (c).

More than one options are correct

1. Since $_{0} \frac{hc}{eV}$ if v increases $_{0}$ decreases hence the interval between $_{K}$ and $_{0}$ as

well as $_{K}$ and $_{0}$ increases.

The correct options are (b) and (c).

2.
$$R \quad n^2, V \quad \frac{1}{n} \text{ and } E \quad \frac{1}{n^2} \text{ for Bohr model of}$$

H-atom

$$VR \quad n \text{ and } rac{V}{E} \quad n$$

Hence, the correct options are (a) and (c).

3. For Bohr model of H-atom

$$L$$
 n , r n^2 and T n^3
Hence $\frac{rL}{T}$ is independent of n
 $\frac{L}{T}$ $\frac{1}{n^2}$ and $\frac{T}{r}$ n, L n^3

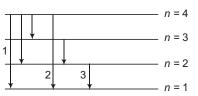
Hence correct options are (a), (b) and (c).

4.
$$\therefore \quad \frac{h}{mv} \text{ and } \quad \frac{h}{\sqrt{2mK}}$$

Hence heavy particle has smallest wavelength when speed and KE both particle are same.

The correct options are (a) and (c).

5. Since there are six different wavelength



Hence, final state will be n = 4.

Since two wavelengths are longer than $_0$ [(From n 4 3 and n 3 2)]

Hence initial state was n = 2

and there are three transitions shown as (1), (2) and (3) belonging to Lymen series. Hence correct options are (a), (b) and (d).

6. $:: \sqrt{f} \quad a(z \quad b)$

÷

$$\sqrt{f}$$
 versus *z* is a straight line

$$f \quad \frac{c}{-} \quad \sqrt{\frac{1}{-}} \quad \frac{a}{\sqrt{c}}(z \quad b)$$

hence $\sqrt{\frac{1}{2}}$ versus z is a straight line

$$a^2(z b)$$

 $\log f \log a^2 \log (z \ b)$ which is a straight line

Hence correct options are (a), (b) and (c).

Match the Columns :

1. Lymen series lies in UV region, Balmer series lies in visible region and Paschen and Brackelt series lie in infrared region. Hence

2. For H-atom
$$E_n = \frac{13.6}{n^2} e^{\sqrt{n^2}}$$

$$E_2 = \frac{13.6}{2^2} \mathrm{eV} = \frac{13.6}{4} \mathrm{eV}$$

Ionization energy from first excited state of H-atom

$$E = E_2 = \frac{13.6}{4} \text{eV} \qquad \dots \text{(i)}$$

For He ion

$$E_{H(\text{He})} = \frac{(13.6) \text{ eV}}{n^2} = Z^2 \text{ for He} = z = 2$$

 $E_n(\text{He}) = \frac{13.6 \text{ eV}}{n^2} = 4$

Ionization energy of He atom from ground state (13.6) eV 4 4*E* 4 from Eq. (i)

 $E_2(\text{He}) = \frac{(13.6)\,\text{eV} - 4}{4}$ (13.6) eV But $E_2 = K_2 = K_2$ (13.6) and \overline{U} 2K 2 (13.6) $2 \quad 4E$ From Eq. (i) KE in ground state of He ion (13.6) eV 4 4*E* 4 16*E* Ionisation energy from Ist executive state $\frac{13.6\,\mathrm{eV}}{4}$ 4 13.6 eV 4E Hence correct match are (a) r s p (b) (c) (d) p (d) **3.** K_{max} h W and $V_0 = \frac{h}{e} = \frac{W}{e}$ Slope of line 1 is h, Y_1 W Slope of line 2 is $\frac{h}{\rho}$, $Y_2 = \frac{W}{\rho}$ Hence correct match are (a) q р (b) (c) r (d) s 4. $T \quad \frac{2}{v} : r \quad \frac{n^2}{z} \quad U \quad \frac{z}{n}$ $T \quad \frac{n^3}{r^2}$ (a) r \therefore L n (b) s $\therefore \qquad V \quad \frac{z}{n}$ (c) s $R \quad \frac{n^2}{z}$ ÷ (d) q

8E

5. Balmer series is

 $\frac{1}{n}$ R $\frac{1}{2^2}$ $\frac{1}{n^2}$ n 3, 4, 5... For 2nd line n = 4 and B $\frac{1}{4}$ $\frac{1}{4}$ $\frac{1}{16}$ R 163R $rac{1}{B_1}$ R $rac{1}{2^2}$ $rac{1}{3^2}$ $_{B_1}$ $\frac{36}{5R}$ $\frac{36}{5 \frac{16}{2}}$ $\frac{36}{16} \frac{3}{16}$ 27 B_1 20 (a) *p* $\frac{1}{B_3} R \frac{1}{2^2} \frac{1}{5^2} \frac{R}{25} \frac{(25 \ 4)}{25} \frac{21R}{100}$ $B_3 = \frac{100}{21R} = \frac{100}{21} = \frac{100}{21}$ $\frac{100 \quad 3}{21 \quad 16} \quad \frac{25}{28}$ 28 (b) (s) For Lyman series $\frac{1}{r}$ R $\frac{1}{1^2}$ $\frac{1}{n^2}$ n 2, 3, 4 $rac{1}{L_1}$ R $rac{1}{1^2}$ $rac{1}{2^2}$ $L_1 \quad \frac{4}{3R}$ $_{L_1} \quad \frac{5}{16} \quad \frac{}{4} \qquad \text{(c)} \quad q$ $\frac{1}{L_2}$ R 1 $\frac{1}{9}$ $\frac{8R}{9}$ $L_2 = \frac{9}{8R} = \frac{9}{8 \cdot \frac{16}{2}} = \frac{9}{16} \cdot \frac{3}{16} \cdot \frac{27}{128}$ (d) s

6. The proper match are

(a) *s*

:: X-ray is inverse process of photoelectric effect [high energy electrons convert in electromagnetic radiation]

(b) p \therefore c $\frac{1}{V}$ (c) q

 \because Wavelength of continuos X-ray depends on voltage

7. $:: (\text{KE})_{\text{max}}$ *f* and stopping potential *f*

 \therefore stopping potental f hence it remains same

(b) *s*

 \therefore Current is directly proportional to Intensity. Hence sat current increases but stopping potential does not chase

(c)
$$q, s$$

 \therefore (KE)_{max} hf W and stopping potential
 $\frac{hf}{e} \frac{W}{e}$

If W is decreased $\left(\mathrm{KE}\right)_{\max}$ and stopping potential increased

Modern Physics II

Introductory Exercise 30.1

0.223**1.** $R_0 = N_0 = 8000 \, \mathrm{Bq}$ 4 3600 $R_1 = N = 1000 \, \text{Bq}$ 1.55 10 5 /s $\frac{R_1}{R_0} \ \ \frac{1}{8} \ \ \frac{N}{N_0} \ \ e^{-t} \ \ \, \log 8 \ \ t$ $T_{1/2} = \frac{0.693}{1.55} = \frac{0.693}{1.55} = 12.4 \text{ h}$ $3\log 2 \quad {\log 2 \over T_{1/2}} \quad 9$ (b) R_0 10 mci 10 3.7 10¹⁰ 10 ³ Bq 3.7 10⁸ Bq $T_{1/2} = \frac{9}{3} = 3 \text{ days}$ $R_0 = N_0$ $N_0 \quad \frac{R_0}{1.55} \quad \frac{3.7 \quad 10^8}{1.55 \quad 10^{5}}$ Average, life 1.44 $T_{1/2}$ 1.44 3 4.33 days **2.** $R_0 = N_0$ $2.39 \quad 10^{13} \text{ (atoms)}$ $40 \quad 3.7 \quad 10^{10} \quad 10^{-6} \quad \frac{0.693}{64.8} \quad N_0$ (c) $R R_0 e^{t}$ 10 mCi $e^{\frac{0.693}{12.4}}$ ³⁰ 1.87 mCi $N_0 \quad \frac{40 \quad 64.8 \quad 3.7 \quad 10^4}{0.693}$ **4.** *R*₀ N_0 $13.83 \quad 10^7$ $\frac{R_0}{N_0} \quad \frac{6 \quad 10^{11} \mathrm{Bq}}{10^{15}}$ $N N_0 e^{-t}$ Now, $N_{10} \quad N_0 e^{ rac{0.693 \quad 10}{64.8} }$ $6 \ 10^{4}/s$ $T_{1/2} = \frac{0.693}{6} = \frac{0.693}{6 \times 10^{-4}} = 1.16 \times 10^3 \mathrm{s}$ 13.83 $10^7 e^{\frac{0.693 \ 10}{64.8}}$ $N_{12} \quad 13.83 \quad 10^7 \quad e^{ \underbrace{ 0.693 \quad 12 }_{ 64.8 } }$ **5.** $N_x N_y N_0$ $\begin{array}{ccc} T_{1/2x} & 50 \min \text{ and } T_{1/2y} & 100 \min \\ N_x & (N_0) \ \frac{1}{2}^n N_0 \ \frac{1}{2}^4 & \frac{N_0}{16} \end{array}$ N_{10} N_{12} 13.83 10^7 $N_{y} \quad N_{0} \quad \frac{1}{2}^{n} \quad N_{0} \quad \frac{1}{2}^{2} \quad \frac{N_{0}}{4}$ 9.47 10^9 nuclei $\frac{N_x}{N_y} \stackrel{\underline{N_0}}{\underline{16}} \frac{1}{4}$ **3.** (a) R_0 10 mCi, R 8 mCi $\frac{R_0}{R}$ e^{t} $\log \frac{10}{9}$ 4 3600

4.002602) u

Introductory Exercise 30.2

 $E Mc^2$ Here, $P = 10^9 \text{ J/s} = 10^9 24 60 \text{ J/day}$ $M = \frac{10^9 \quad 24 \quad 60}{(3 \quad 10^8)^2} \quad 9.6 \quad 10^{-4} \, \mathrm{kg}$ $\frac{10^9 \text{ J/s}}{200 \ 10^6 \ 1.6 \ 10^{\ 19}}$ **2.** Number of fission $3.125 \ 10^{19}$ **3.** Given reaction is $_{92}U^{238}$ $_{90}Th^{234}$ $_{2}He^{4}$

M (238.050784 234.043593

- M 0.0004589 u
- M 931.5 MeV E0.0004589 931.5 4.27 MeV
- 4. Complete reactions are (a) ${}_{3}\text{Li}^{6} {}_{1}\text{H}^{2} {}_{4}\text{Be}^{7} {}_{0}n^{1}$ (b) $_{17}Cl^{35}$ $_{1}H^{1}$ $_{16}S^{32}$ $_{2}He^{4}$ (c) $_{4}Be^{9}$ $_{2}He^{4}$ $3(_{2}He^{4})$ $_{0}n^{1}$ (d) $_{35}Br^{79}$ $_{1}H^{2}$ $_{36}Kr^{79}$ $2(_{0}n^{1})$

60s

365 24 3600

AIEEE Corner

Subjective Questions (Level 1)

Radioactivity

1. (a) Initially the rate of distingration is
 2. We have
$$A = N$$
 $\frac{dN}{dt}_{0} = N_{0}$
 6 $10^{11} = 1 = 10^{15}$

 After 5 min $\frac{dN}{dt} = N$
 6 $10^{11} = 1 = 10^{15}$
 $\frac{N_{0}}{N} = \frac{\frac{dN}{dt}}{\frac{dN}{dt}} = \frac{4750}{2700}$
 1.76

 $\frac{N_{0}}{N} = \frac{\frac{dN}{dt}}{\frac{dN}{dt}} = \frac{4750}{2700}$
 1.76

 Now $N = N_{0} e^{-t}$ or
 $\frac{\log \frac{N}{N_{0}}}{t}$
 $\frac{2.3026}{t} \log_{10} \frac{N_{0}}{N}$
 $\frac{0.693}{5.3 \text{ gr}} = \frac{0.693}{5.3 \text{ gr}}$
 $\frac{0.113 / \text{min}}{(b) \text{ Half-life}} = \frac{0.693}{0.25} = \frac{0.693}{0.113} = 6.132 \text{ min}$
 $N = \frac{8 - 3.7 - 10^{10} - 5.3 - 365 - 24}{0.693}$

1.

$$\begin{array}{r} 6.023 & 10^{-9} \text{ huclei} & 60 \text{ g} \\ 1 & \frac{60 \text{ g}}{6.023 & 10^{23}} \\ \text{Hence 7.2} & 10^{19} \text{ nuclei} \\ & \frac{60 & 7.2 & 10^{19}}{6.023 & 10^{23}} & 7.11 & 10^{-3} \text{ g} \end{array}$$

1 . 00

4. Number of decay per second

1 023

0 000

- $\frac{m}{M} \quad N_A \qquad \frac{1}{238} \quad 6 \quad 10^{23} \quad \frac{0.693}{4.5 \quad 10^9 \text{ yr}}$ $6 \ 10^{23}$ 0.693 60 60s $1.23 \quad 10^4 \text{ decay/s}$
- 5. Probability of decay

$$\begin{array}{cccc} P & (1 & e^{-t}) & (1 & e^{-t/T_{\text{mean}}}) \\ P & (1 & e^{-5/10}) & 1 & e^{-2} & 0.39 \end{array}$$

6. Since initially no Pb nuclei is present and after time *t* the ratio of $\frac{N_v}{N_{\rm Pb}}$ 3

It means $\frac{1}{4}$ of original $\overset{238}{U}$ nuclei decays. N N₀e^t

Hence

$$N_0 \quad \frac{N_0}{4} \qquad N_0 e$$
$$\frac{3}{4} \quad e^{-t}$$
$$t \quad \frac{\log 4 \quad \log 3}{2}$$

$$t = rac{(\log 4 - \log 3)}{0.693} = 4.5 - 10^9 ext{ yr}$$

 $t = 1.88 - 10^9 ext{ yr}$

7.
$$(R_1)_{0P_{39}} = {}_14N_0$$

$$(R_{2})_{tP_{33}} = N_{0} e^{\frac{\log 2}{25}} = 60 = 365$$

$$R = (R_{1})_{tP_{32}} = (R_{2}) t_{P_{33}}$$

$$N_{0} = 4 = e^{\frac{\log 2}{14}} = 60 = 365$$

$$= 2 e^{\frac{\log 2}{25}} = 60 = 365$$

$$= \frac{3 \text{ mCi}}{(4_{1} = 2)}$$

$$= 4 = e^{\frac{\log 2}{14}} = \frac{60 = 365}{14} = 2e^{\frac{\log 2}{25}} = 60 = 365$$

$$\frac{3 \text{ mCi}}{4 \log 2} \frac{\log 2}{25}$$

$$\frac{4 \log 2}{14} e^{\frac{\log 2}{60} \frac{60}{365}} \frac{\log 2}{25} e^{\frac{\log 2}{25} 60 \frac{365}{5}}$$

0.205 mCi

- 8. Complete reactions are $_{86} {\rm RN}^{222}$ (a) $_{88}$ Ra 226 (b) ₈ O¹⁹ $_{o}F^{19}$ е (c) ₁₃Al²⁵ $_{12}\mathrm{Mg}^{25}$ е
- **9.** Only reaction (b) is possible.
- **10.** E (7 1.000783 7 1.00867 14.00307 $931.5\,\mathrm{MeV}$

E 104.72 MeV

11.
$$E [8m_p \ 8m_n \ m(_8O^{16})]$$
 931.5

12. (a) Number of nuclei in kg

$$\frac{6.023 \quad 10^{23}}{235} \quad 1$$

Energy
$${6.023 \quad 10^{23} \over 235}$$
 200 10⁶ 1.6 10 ¹⁹
8.09 10¹³J

(b) Mass
$$\frac{8.09 \quad 10^{13} \text{J}}{30 \quad 10^{3} \text{J/g}}$$
$$\frac{8.09 \quad 10^{13}}{30 \quad 10^{3}} \text{g}$$
$$\frac{8.09}{3} \quad 10^{9} \quad \frac{1}{10^{3}} \text{kg}$$
$$2.7 \quad 10^{6} \text{kg}$$

13. Applying conservation of momentum

$$\begin{array}{rcl}
M & v & M_{\rm Ti} v_{\rm Ti} \\
v_{\rm Ti} & \frac{M & v}{M_{\rm Ti}} \\
K & \frac{1}{2}M & v^2 & 6.802 \,{\rm MeV} \\
K_{\rm Ti} & \frac{1}{2}M_{\rm Ti} & v_{\rm Ti}^2 & \frac{1}{2}M_{\rm Ti} & \frac{M^2 v^L}{M_{\rm Ti}^2} \\
K_{\rm Ti} & \frac{M}{M_{\rm Ti}} & \frac{1}{2}M & v^2 \\
& \frac{4}{208} & 6.802 \,{\rm MeV} \\
& \frac{1}{52} & 6.802 & 0.1308 \,{\rm MeV}
\end{array}$$

14. Power 100 MW 10^8 W 10^8 J/s $\frac{10^8}{1.6 \ 10^{\ 13}} \frac{10^{21}}{1.6} \frac{\text{MeV}}{\text{s}}$ Energy per fission 185 MeV Hence number of fissions $\frac{10^{21}}{1.6 \ 185}$ / s. Number of nuclei in 1 kg

$$U^{235} = \frac{6.023 \times 10^{26}}{235}$$
Hence $t = \frac{6.023 \times 10^{26}}{235 \times 10^{26}}$

15. (a) The given reaction is ${}_{1}\text{H}^{2}$ ${}_{1}\text{H}^{2}$ ${}_{1}\text{H}^{3}$ ${}_{1}\text{H}^{1}$ M $[2m({}_{1}\text{H}^{2})$ $m({}_{1}\text{H}^{3})$ $m({}_{1}\text{H}^{1})]$

- M 17.57 MeV
- **16.** The given reaction is
 - He⁴ He⁴ Be⁸ M (2 4.0026 8.0053) u (8.0052 8.0053) u M (0.0001) u
 - \therefore *M* is negative this reaction is not energetically favourable
 - E M 931.5
 1 10⁴ 931.5 MeV
 93.15 keV
- **17.** Number of nuclei in 1 kg water $6.023 \quad 10^{26}$

Heavy water
$$\frac{\overline{\begin{array}{c} 18 \\ 6.023 \quad 10^{26} \\ 18 \end{array}}}{\begin{array}{c} 1.5 \quad 10^{2} \\ 100 \end{array}} \\ \frac{6.023 \quad 1.5}{18} \quad 10^{22} \end{array}$$

Energy realesed per fission

 $(2 \ 2.014102 \ 3.016049 \ 1.007825) \ 931.5$

 $3200\,\mathrm{MJ}$

1. Since during decay a neutron in the nucleus is transformed into a proton, an electron and an antineutrino as $n P e^{-1}$.

Hence Correct option is (c).

2. Since nuclear force is same for all nucleons. Hence F_1 F_2 F_3

Correct option is (a)..

3. Given reaction is ${}_{90}X^{200}$ ${}_{80}Y^{168}$

Difference in mass number 200 168 32 Hence Number of -particles $\frac{32}{4}$ 8 Difference in atomic number 10 hence number of -particles 6 Hence correct option is (d).

4. The reaction is

 ${}_{92}U^{235} {}_{0}n^{1} {}_{54}Xe^{138} {}_{38}Sr^{94} {}_{3}({}_{0}n^{1})$ The correct option is (b) three neutrons.

5. The reactions are *A* and *C* 2 After one atomic number reduced by 2 and after 2 atomic number increased by.

Hence A and C are isotopes Correct option is (d).

6. Here m_p 1.00785 u, m_n 1.00866 u

and
$$m = 4.00274$$
 u
 $m = 2(m_p = m_n) = m$
 $m = [2(1.00785 = 1.00866) = 4.00274]$ u
 $m = 0.03028$ u
 $E = m = 931.5$ MeV

0.3028 931.5 28.21 MeV

Hence correct option is (c).

7.
$$N \quad N_0 \quad \frac{7}{8} N_0 \quad \frac{1}{8} N_0$$

But
$$N = N_0 = \frac{1}{2}^n = \frac{1}{8}N_0 = N_0 = \frac{1}{2}^n$$

 $n = 3$
 $3 = T_{1/2} = \frac{8}{3}s$

Hence correct option is (d).

8. $N \quad N_0 e^{-t}$ for mean life $t = \frac{1}{2}$

$$N \quad N_0 e \quad \frac{1}{e} \quad \frac{N_0}{e}$$

Hence the fraction disintegrated

$$\frac{N_0 N}{N_0} \quad 1 \quad \frac{1}{e}$$

Correct option is (b).

9.
$$N \quad N_0 \quad \frac{7}{8} N_0 \quad \frac{1}{8} N_0$$

But $N \quad N_0 \quad \frac{1}{2}^n$
 $\frac{1}{8} \quad \frac{1}{2}^n \quad n \quad 3$
Hence half life $T_{1/2} \quad \frac{15 \min}{3} \quad 5 \min$

Correct option is (a).

10. Since radioactive substance loses half of its activity in 4 days it means its half life

$$T_{1/2} \quad 4 \text{ days}$$
Now $A \quad 5\% \text{ of } A_0$

$$A \quad \frac{1}{20}A_0$$

$$\frac{A}{A_0} \quad \frac{1}{20}$$
But
$$A \quad A_0 e^{-t} \quad \frac{1}{20} e^{-t}$$

$$\log 20 \quad t \quad t \quad \frac{\log 20}{20}$$

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But
$$\frac{\log_e 2}{T_{1/2}}$$

 $t \quad T_{1/2} \frac{\log_e 20}{\log_e 2} \quad T_{1/2} \frac{\log_{10} 20}{\log_{10} 2} = 4.32$ 4

t 17.3 days

Hence correct option is (c).

11. Total energy released per sec

 $1.6 \,\mathrm{MW}$ $1.6 \,10^6 \,\mathrm{J/s}$

Energy released per fission 200 MeV

200 10^{6} 1.6 10^{19} J 2 1.6 10^{11} J

Number of fission per second

$$\frac{1.6 \quad 10^6}{2 \quad 1.6 \quad 10^{\ 11}} \quad 5 \quad 10^{16}/s$$

Hence correct option is (a).

 $\begin{array}{rcrcrcr} \textbf{12.} & \because R & R_0 A^{1/3} \\ & \text{Volume} & \frac{4}{3} & R^3 & \frac{4}{3} & R_0^3 A \\ & \text{Mass of nucleus} & A & 1.67 & 10 & {}^{27} \text{ kg} \\ & \text{Density} & \frac{\text{mass}}{\text{volume}} & \frac{A & 1.67 & 10 & {}^{27} \text{ kg}}{\frac{4}{3} & R_0^3 A} \\ & & \frac{1.67 & 10 & {}^{27} \text{ kg}}{\frac{4}{3} & R_0^3} \end{array}$

: is independent of A, hence ratio of densities $\frac{-1}{2}$ 1.

Correct option is (d).

Assertion and Reason

- 1. Here both assertion and reason are true but reason does not explain assertion. Hence correct option is (b).
- **2.** Here assertion is false but reason is true since for heavier nucleus binding energy per nucleon is least.

Correct option is (d).

13.
$$N N_0 e^{-t} \frac{N}{N_0} e^{-t}$$

$$\frac{N}{N_0} e^{-\frac{0.693}{6.93} 10} e^{-1} \frac{1}{e}$$

Fractional change

$$\frac{N_0 N}{N_0} = 1 - \frac{1}{e} \approx 0.63$$

п

Hence correct option is (b).

14. Since radioactive substance reduce to about 6% it means $N = \frac{N_0}{16}$

We have
$$N(N_0) \frac{1}{2}$$

$$\frac{1}{16} \quad \frac{1}{2}^n \quad n \quad 4$$

4 $T_{1/2}$ 2 h $T_{1/2}$ 30 min

Hence correct option is (a).

15. Probability of a nucleus for survival of time *t*.

$$p_{(\text{survival})} = \frac{N}{N_0} = \frac{N_0 e^{-t}}{N_0} = e^{-t}$$

For one mean life $t = \frac{1}{2}$

$$P_{\text{survival}} e^{\frac{1}{2}} e^{1} \frac{1}{e}$$

Hence Correct option is (a).

- **3.** Here both assertion and reason are true but reason is not correct explanation of assertion. Hence correct option is (b).
- **4.** Here a ssertion is true but reason is false since electromagnetic waves are produced by accelerating charge particles.

Correct option is (c).

5. Here assertion is wrong since -decay process is $n \ p \ e^- \ \overline{v}$

but reason is true hence correct option is (d).

- **6.** Here assertion is true but reason is false. Correct option is (c).
- 7. Here both assertion and reason are true and reason may or may not be true. Correct option is (a, b)
- **8.** Both assertion and reason are true but reason is not correct explanation of assertion. Hence correct option is (b).

- 9. Here reason is true but assertion is false
 ∴ 1 amu 931.5 MeV
 Correct option is (d)
- **10.** Both assertion and reason are true but reason does not correctly explain assertion. Hence correct option is (b).
- **11.** Here both assertion and reason are true and reason may or may not be correct explanation of assertion .

Hence correct options are (a, b).

Objective Questions (Level 2)

Single option correct

1. Let initially substance have N_i nuclei then

$$N \quad N_i e^{-t} \\ \frac{dN}{dt} \quad N_i e^{-t}$$

At $t \quad t$

At

we get

$$\frac{dN}{dt} \qquad N_i e^{-t} \qquad \dots (i)$$

At
$$t \quad 4t$$

 $\frac{dN}{dt} = N_i e^{-4t} = \frac{N_0}{16}$...(ii)

Dividing Eq. (i) and Eq. (ii) we get

$$e^{3 t} 16 ...(iii)$$
Now at $t \frac{11}{2} t$

$$\frac{dN}{dt} = N_i e^{\frac{11}{2}t}$$

$$N_i e^{\frac{8 t}{2}} e^{\frac{3 t}{2}}$$

$$\frac{N_i e^{4 t}}{\sqrt{e^{3 t}}} \frac{N_0}{16 \sqrt{16}}$$

From Eqs. (ii) and (iii) N_0

Hence, correct option is (b).

Hence correct option is (c).

3. From graph it is clear that number of nucleons in X is N_3 and binding energy per nucleon is E_3 for Y nucleon is N_2 and BE per nucleon is E_2 .

Hence $X Y E_3N_3 E_2N_2$ Similerly $W E_1N_1$ The reaction is W = X = YThe energy released is $(E_3N_3 = E_2N_2 = E_1N_1)$ Hence Correct option is (b). 4. Energy (110 8.2 90 8.2 200 7.4) 200 (8.2 7.4)

200 0.8 160 MeV

Hence correct option is (d).

5. The reaction is

 ${}_{1}\text{H}^{2}$ ${}_{1}\text{H}^{2}$ ${}_{2}\text{He}^{4}$ energy Energy (4 7 2 1.1) MeV (28 4.4) 23.6 MeV

- Hence Correct option is (b).
- 6. Total energy released per second

 $16 \ 10^{6} W$

- $16 \ 10^6 \, \text{J/s}$
- Energy per fission 200 MeV

 - 2 1.0 10
- :: Efficiency 50%

Hence power (energy converted per second)

Hence correct option is (d).

7.
$$\frac{dN}{dt}$$
 A N

 $\because \text{After time } N \text{ become}$

$$\begin{array}{rcl} \text{conservation} & \frac{dN}{dt} & 0 \\ N & \frac{A}{log 2} & \frac{AT}{log 2} \\ \hline T & \end{array}$$

Hence correct option is (d).

8. By conservation of momentum

$$\begin{array}{ccc} M_{\rm H}\, v & (M_{\rm H} & M_{\rm H}) \\ v & \displaystyle \frac{v}{2} \end{array}$$

Let initial KE of H-atom K

Final KE of each H-atom $\frac{\pi}{2}$

For excitation

Hence correct option is (c).

9. Let us suppose just before the death no radioactive atoms were present hence original activity A_0 is given as

$$A_0 = N_0$$
 ...(i)

After death the radioactivity decreases exponentially *ie*,

$$A \quad \frac{dN}{dt} \qquad N \qquad N_0 e^{-t} \qquad \dots (ii)$$

Dividing eq. (ii) by eq. (i) we get

$$\frac{A}{A_0} e^{-t}$$

or $t \log \frac{A_0}{A}$ or $t - \frac{1}{2} \log \frac{A_0}{A}$
Now A_0 15 decay/min/gram
 $A - \frac{375}{200}$ decay/min/g
but $\frac{0.693}{5730 \text{ yr}}$

$$t \quad \frac{5730}{0.693} \quad \log \frac{15 \quad 200}{375} \quad \frac{5730}{0.693} \quad \log \frac{200}{25}$$
$$t \quad \frac{5730}{0.693} \quad \log 8$$
$$\frac{5730}{0.693} \quad 3 \log 2 \quad 5730 \quad 3$$
$$t \quad 17190 \text{ yr}$$

Hence correct option is (c).

10.
$$N_P = N_0 e^{-(t_1 - t)}$$
 ...(i)

and
$$N_Q \quad N_0 e^{-t}$$

Now $A_P \quad N_P \text{ and } A_Q \quad N_Q$
 $\frac{A_P}{A_Q} \quad \frac{N_P}{N_Q} e^{-t_1}$
 $t_1 \quad \log \quad \frac{A_Q}{A_P}$
 $t_1 \quad \frac{1}{\log \quad \frac{A_Q}{A_P}} \quad T \log \quad \frac{A_Q}{A_P}$

Hence correct option is (b).

11. The given reactions are

$${}_{1}\mathrm{H}^{2}$$
 ${}_{1}\mathrm{H}^{2}$ ${}_{1}\mathrm{H}^{3}$ ${}_{2}\mathrm{H}\mathrm{e}^{4}$ n
 ${}_{1}\mathrm{H}^{2}$ ${}_{1}\mathrm{H}^{3}$ ${}_{2}\mathrm{H}\mathrm{e}^{4}$ n
 ${}_{3}\mathrm{1}\mathrm{H}^{2}$ ${}_{2}\mathrm{H}\mathrm{e}^{4}$ n p

Mass defect

Energy Released

 $0.026 \ \ 931 \, MeV \ \ 3.87 \ \ 10 \ ^{12} J$

This energy produced by the three deutronatoms. Total energy released by

 $10^{40} \ deutrons$

 $\frac{10^{40}}{3} \quad 3.87 \quad 10^{-12} \, J \quad 1.29 \quad 10^{28} \, J$

The average power $P - 10^{16}\,{\rm W} - 10^{16}\,{\rm J/s}$

Therefore total time to exhaust all deutrons of the star will be

$$t = \frac{1.29 - 10^{28}}{10^{16}} \mathrm{s} = 10^{12} \mathrm{s}.$$

Hence correct option is (c).

12.
$$N_1 \quad N_0 e^{-1^t} \quad N_0 e^{-\frac{\log 2}{t_1}t} \qquad \dots (i)$$

$$N_2 N_0 e^{-2t} N_0 e^{-\frac{\log 2}{t_2}t}$$
 ...(ii)

$$R_1 = {}_1N_1 = \dots$$
...(iii)

$$R_2 _2 _2 _2 N_2$$
 ...(iv)

Let after time $t, R_1 = R_2$ then

and

$$\begin{array}{cccc} & \frac{R_1}{R_1} & 1 \\ \\ -\frac{1}{2} & \frac{N_1}{N_2} & 1 \\ \\ & \frac{-1}{2} & \frac{N_2}{N_1} & e^{\log 2 \frac{t_2 - t_1}{t_1 t_2} - t} \\ & \log \frac{t_2}{t_1} & t - \log 2 - \frac{t_2 - t_1}{t_1 t_2} \\ & t_1 & \frac{t_1 t_2}{0.693 \left(t_2 - t_1\right)} - \log \frac{t_2}{t_1} \end{array}$$

Hence Correct option is (a).

13. The given reaction is ${}_Z X^{232} \qquad {}_{90} Y^A$

$$_{Z}X^{232}$$
 $_{90}Y^{A}$ $_{2}\text{He}^{4}$
Z 92 and A 228

: Initially X is in rest hence momentum of -particle after decay will be equal and opposite of Y.

$$\begin{array}{ccc} M_{Y}v_{Y} & M v \\ v_{Y} & \frac{M}{M_{Y}}v \end{array}$$

Total kinetic energy

$$\begin{split} K_T & \frac{1}{2} (M \ v^2 \ M_Y v_Y^2) \\ K_T & \frac{1}{2} \ M \ v^2 \ M_y \frac{M^2 v^2}{M_Y^2} \end{split}$$

$$egin{array}{ccccc} K_T & rac{1}{2}M v^2 & 1 & rac{M}{M_Y} \ K_T & K & 1 & rac{4}{228} \end{array}$$

$$K \qquad \frac{232}{228} K_T$$

Hence Correct option is (b).

K_T K

14. Energy of emitted photon 7 MeV

: Initial nucleus is stationary

Applying conservation of momentum principle

$$O \mathbf{P}_{nuc} \mathbf{P}_{photon} \mathbf{P}_{nuc} \mathbf{P}_{photon}$$

$$|\mathbf{P}_{nuc}| | \mathbf{P}_{photon}|$$

$$P_{nuc} \frac{11.2}{3} \quad 10^{-21} \text{ kg-m/s}$$

Mass of nucleus 24 amu

But $P_{\rm nuc}^2 = 2mK_{\rm nuc}$

$$K_{
m nuc} = rac{P_{
m nuc}^2}{2m} = rac{11.2}{9} rac{11.2}{24} rac{10}{1.66} rac{42}{10} rac{27}{27}$$
 Joule

$$K_{\rm nucc} = \frac{11.2 \quad 11.2 \quad 10^{-42}}{18 \quad 24 \quad 1.66 \quad 10^{-27} \quad 1.6 \quad 10^{-19}} \, {\rm eV}$$

1.1 keV

Hence correct option is (b).

15. Let time interval between two instants is t_1 then

$$N_1 \quad N_0 e^{-(t - t_1)}$$

Hence Correct option is (c).

16. The given reaction is

and

 ${}_{1}H^{3}$ ${}_{1}H^{1}$ $_{1}H^{2}$ $_{1}\text{H}^{2}$ $M = [2m(_1H^2) m(_1H^3) m(_1H^1)]$ (2 2.014102 3.016049 1.007825) amu 4.33 10 ³amu *E* 4.33 10⁻³ 931.5 MeV 4 MeV

Hence correct option is (c).

17. Number of fusion required to generate 1 kWh

$$\frac{1 \quad 10^3 \quad 3600}{4 \quad 10^6 \quad 1.6 \quad 10^{19}}$$
$$\frac{36 \quad 10^{18}}{6.4} \quad 5.6 \quad 10^{18} \quad 10^{18}$$

Hence correct option is (b).

18. The energy released 4 MeV

This energy produced by two atoms.

Hence energy produced per atom $2 \, MeV \, 2 \, 1.6 \, 10^{-13} J$

Hence number of atom fused to produced 1 kWJ

$$\frac{36 \quad 10^5}{2 \quad 1.6 \quad 10^{13}} \quad \frac{18}{1.6} \quad 10^{18}$$

Mass of deutrium which contain

 $\frac{18}{1.6}$ $10^{18}\,\mathrm{atom}$

$$-\frac{18 \quad 10^{18}}{1.6 \quad 6.02 \quad 10^{23}} \quad 3.7 \quad 10^{-5} \text{ kg}.$$

Hence correct option is (c).

More Than one Option is Correct

$$\begin{array}{cccc} \mathbf{1.} & x & N_0, y & N_0 \\ & & \frac{x}{y} & \frac{N_0}{N_0} & \mathbf{1} \end{array}$$

where is decay constant

Hence $\frac{x}{y}$ is constant throught.

$$\therefore \qquad \frac{x}{y} \quad \frac{1}{2} \quad \frac{1}{\frac{0.693}{T}} \quad \frac{T}{0.693}$$
$$\frac{x}{y} \quad T, \ xy \quad (N_0)^2$$

For one half life $N = \frac{N_0}{2}$

$$(xy)_T \qquad \frac{N_0}{2}^2 \quad \frac{N_0^2}{4} \quad \frac{xy}{4}$$

Hence correct options are (a), (b) and (d).

- **2.** The correct options are (a), (b), (c) and (d).
- 3. A nucleus in excited state emits a high energy photon called as -ray. The reaction is

 X^{*} Χ

Hence by gamma radiation atomic number and mass number are not changed. Since after emission of one atomic number reduced by $2(2^{4})$ and after 2 atomic number is increased by (2). Hence correct options are (a), (b) and (c).

4. Here half lives are *T* and 2T and $N_x = N_0$,

 $N_y = N_0$ after 4T for first substance 4 half lives and after 4T the second substance 2 Half lines.

$$N_{x} \quad N_{0} \quad \frac{1}{2}^{4} \quad \frac{N_{0}}{16}$$

$$N_{y} \quad N_{0} \quad \frac{1}{2}^{2} \quad \frac{N_{0}}{4}$$

$$x \quad \frac{N_{x}}{N_{y}} \quad \frac{N_{0}/16}{N_{0}/4} \quad \frac{1}{4}$$

Let their activity are R_x and R_y .

$$R_x \xrightarrow{x} N_x \text{ and } R_y \xrightarrow{y} N_y$$

$$y \xrightarrow{R_x} \xrightarrow{x} \frac{N_x}{y} \xrightarrow{N_y} \frac{0.693}{\frac{T}{2000}} \frac{1}{4}$$

$$\frac{R_x}{R_y} \xrightarrow{y} \frac{1}{2}$$

Hence correct options are (b) and (c).

5. Since nuclear forces are vary short range charge independent, no electromagnetic and they exchange (*n* p or p *n*). Hence the correct options are (a), (b), (c) and (d).

6. ::
$$R \quad R_0 A^{1/3}$$

$$\frac{M}{4/3 R^3} \frac{A 1.67 10^{27} \text{ kg}}{\frac{4}{3} R_0^3 A}$$

is independent of A.

But
$$\frac{1.67 \quad 10^{27} \text{ kg}}{\frac{4}{3} \quad 3.14 \quad (1.3 \quad 10^{15})^3}$$
$$1.8 \quad 10^{17} \text{ kg/m}^3$$

Hence correct options are (b) and (c).

Match the Columns

1. Here $N_0 = x$, let is the decay constant.

$$N N_{0}e^{t} xe^{t}$$

$$\left|\frac{dN}{dt}\right| xe^{t} \text{ but } \left|\frac{dN}{dt}\right|_{t=0} y$$

$$y xe^{0} x$$

$$\frac{y}{x}$$
Hence
(a) s
Half life $T_{1/2} \quad \frac{\log 2}{\frac{y}{x}} \quad \frac{\log 2}{\frac{y}{x}} \quad \frac{x}{y} \log 2$
Hence
(b) p
We have activity $R \quad N \quad xe^{-t}$
at $t \quad \frac{1}{e}$

$$R \quad xe^{-\frac{1}{2}} \quad xe^{-1} \quad \frac{x}{e}$$
but $x \quad y$

$$R \quad \frac{y}{e}$$
Hence
(c) r
Number of nuclei after time $t \quad \frac{1}{e}$
Hence
(x) r
Number of nuclei after time $t \quad \frac{1}{e}$

(d)

Thus correct match is

 \mathbf{s}

- (a) s
- (b) r
- (c) r
- (d) s

2. In reaction P = P = Q energy is released

: Binding energy increases when two or more lighter nucleus combine to form haviour nucleus.

Hence correct match is

(a) p

Similerly for reaction

Correct match is

(b) p

for reaction

P R 2Q from graph BE per nucleon increases.

Hence energy is released.

Correct match is

(c) p

For the reaction

 $P \quad Q \quad R$

We will check energy process if BE per nucleon is given. Hence data is not sufficient correct match is

(d) s

- **3.** Since *A* and *B* are radioactive nuclei of (*A B*) decreases with time. Hence correct match is
 - (a) q

 $\therefore A$ is converted into *B* and *B* is converted into *C* and decay rate of *A B* and *B C* are not known. Hence correct match is

(b) s

Since at time passes A is converted to Band B is converted to C. Hence nuclei of (B C) increases. Correct match is

(c) p

Similarly the correct match for (d) is

(d) s

4. After emission of 1 particle mass no decreased by 4 but after emission of 1 particle atomic number will increase or decrease by 1. Hence for (a)

- (a) p, s
- (b) p, r

 \mathbf{s}

- (c)
- (d) q, r

5. For

(a)

р

Since BE per nucleon of heavy nuclei is about 7.2 MeV. Hence

(b) s

X-ray photon have wavelength about 1 Å the energy of this wavelength is of order of 10 keV.

 \because Visible light energy of order of $2\,\text{eV}.$ Hence

(d) q

⁽c) r