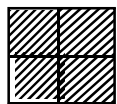
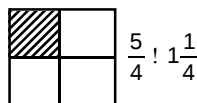


$$\frac{1}{4} = \frac{4}{16}$$



+



FRACTION

Comparison of two fractions

eg: $\frac{4}{7}$ $\frac{3}{7}$ → Compare numerator
 → Denominator same
 eg: $\frac{5}{4}$ $\frac{5}{3}$ → Numerator same
 → Compare denominator
 eg: $\frac{1}{3}$ $\frac{2}{5}$ → Find L.C.M. of denominators
 L.C.M. of (3,5) = 15
 $\frac{1 \times 5}{3 \times 5} = \frac{5}{15}$; $\frac{2 \times 3}{5 \times 3} = \frac{6}{15}$

Decimal fraction

Denominator is 10, 100, 1000, 10000 ...

eg: $\frac{1}{10}$; $\frac{3}{100}$ e.t.c.

Improper fraction

denominator > numerator

eg: $\frac{7}{5}$

converted into

Mixed fraction

[combination of whole no. and a proper fraction]

$\frac{7}{5} = 1\frac{2}{5}$; $14\frac{2}{3} = \frac{14 \times 3 + 2}{3} = \frac{44}{3}$

Proper fraction

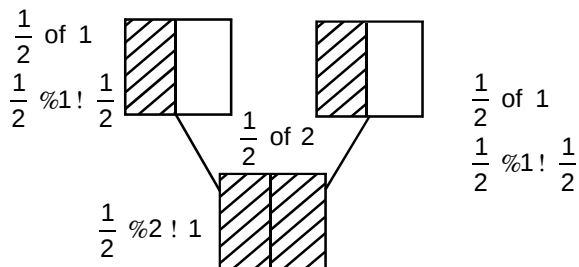
numerator < denominator

eg: $\frac{5}{7}$

Equivalent fractions

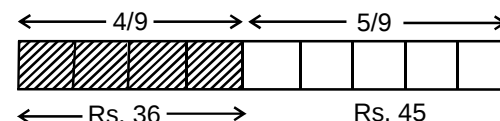
$\frac{3}{5} = \frac{3 \times 2}{5 \times 2} = \frac{6}{10}$
 $\frac{3}{5} = \frac{3 \times 3}{5 \times 3} = \frac{9}{15}$
 $\frac{6}{10} = \frac{6 \div 2}{10 \div 2} = \frac{3}{5}$
 $\frac{9}{15} = \frac{9 \div 3}{15 \div 3} = \frac{3}{5}$

Fraction as an operator



Operation on Fraction

eg: After spending $\frac{4}{9}$ of her money, Nidhi had Rs. 45 left. How much did she spend



Addition

$3\frac{1}{4}$ kg ∇ $1\frac{1}{6}$ kg $\frac{13}{4}$ kg ∇ $\frac{7}{6}$ kg
 L.C.M. (4,6) = 12
 $\frac{(13 \times 3 + 7 \times 2) \text{ kg}}{12} = \frac{53}{12} \text{ kg} = 4\frac{5}{12} \text{ kg}$

eg: $4\frac{1}{2} + 3\frac{1}{5} + \frac{1}{3} = \frac{9}{2} + \frac{16}{5} + \frac{1}{3}$
 $= \frac{9 \times 15 + 16 \times 6 + 1 \times 10}{2 \times 5 \times 3} = \frac{24}{5} = 4\frac{4}{5}$

Subtraction

$2\frac{2}{5} - 1\frac{1}{4} = \frac{12}{5} - \frac{5}{4}$ L.C.M. (5,4) = 20
 $\frac{12 \times 4 - 5 \times 5}{20} = \frac{48 - 25}{20} = \frac{23}{20} = 1\frac{3}{20}$

eg: $1\frac{14}{11} - 14\frac{2}{3} - 2\frac{2}{5} + \frac{1}{4} = \frac{15}{11} - \frac{44}{3} - \frac{12}{5} + \frac{1}{4}$
 $= \frac{15 \times 44 - 12 \times 9}{11 \times 3} - \frac{20}{1} + \frac{27}{5}$
 $= \frac{20 \times 5 - 27 \times 1}{5} = \frac{73}{5}$

Multiplication

(i) Fraction by fraction

Product of numerator
 Product of denominator
 eg: $\frac{3}{4} \times \frac{5}{7} = \frac{3 \times 5}{4 \times 7} = \frac{15}{28}$

(ii) Fraction by whole number

$\frac{3}{4} \times 2 = \frac{3 \times 2}{4 \times 1} = \frac{3 \times 1}{2 \times 1} = \frac{3}{2}$

* Product of two proper fraction is less than each of the fraction.
 * Value of product of two improper fraction is more than each of the two fractions

Division

(i) $3 - \frac{5}{4} = \frac{3}{1} - \frac{5}{4} = \frac{12}{4} - \frac{5}{4} = \frac{7}{4}$
 (ii) $\frac{5}{4} - 3 = \frac{5}{4} - \frac{3}{1} = \frac{5}{4} - \frac{12}{4} = -\frac{7}{4}$
 (ii) $\frac{1}{3} - \frac{5}{6} = \frac{1}{3} - \frac{5}{6} = \frac{2}{6} - \frac{5}{6} = -\frac{3}{6} = -\frac{1}{2}$

* Reciprocal or multiplicative inverse of a non-zero fraction

$\frac{a}{b}$ is $\frac{b}{a}$ ie $\frac{a}{b} \times \frac{b}{a} = 1$

* Multiplicative inverse of 1 is 1
 Reciprocal of 0 does not exist.