**CHAPTER** 

9

# Mensuration



### 9.1 Introduction

We have learnt that for a closed plane figure, the perimeter is the distance around its boundary and its area is the region covered by it. We found the area and perimeter of various plane figures such as triangles, rectangles, circles etc. We have also learnt to find the area of pathways or borders in rectangular shapes.

In this chapter, we will try to solve problems related to perimeter and area of other plane closed figures like quadrilaterals.

We will also learn about surface area and volume of solids such as cube, cuboid and cylinder.

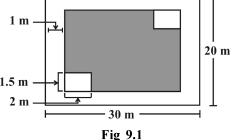
### 9.2 Let us Recall

Let us take an example to review our previous knowledge.

This is a figure of a rectangular park (Fig 9.1) whose length is 30 m and width is 20 m.

- (i) What is the total length of the fence surrounding it? To find the length of the fence we need to find the perimeter of this park, which is 100 m.

  (Check it)
- (ii) How much land is occupied by the park? To find the land occupied by this park we need to find the area of this park which is 600 square meters (m<sup>2</sup>) (How?).
- (iii) There is a path of one metre width running inside along the perimeter of the park that has to be cemented. If 1 bag of cement is required to cement 4 m<sup>2</sup> area, how many bags of cement would be required to construct the cemented path?



area of the path

We can say that the number of cement bags used =  $\frac{\text{area of the path}}{\text{area cemented by 1 bag}}$ 

Area of cemented path = Area of park – Area of park not cemented.

Path is 1 m wide, so the rectangular area not cemented is  $(30-2) \times (20-2)$  m<sup>2</sup>. That is  $28 \times 18$  m<sup>2</sup>.

Hence number of cement bags used = -----

(iv) There are two rectangular flower beds of size  $1.5 \text{ m} \times 2 \text{ m}$  each in the park as shown in the diagram (Fig 9.1) and the rest has grass on it. Find the area covered by grass.

Area of rectangular beds = -----

Area of park left after cementing the path = -----

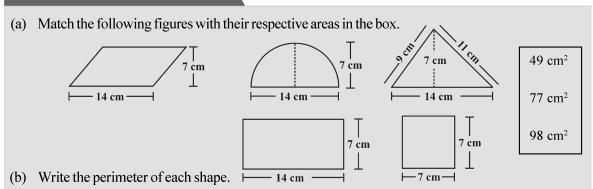
Area covered by the grass = -----

We can find areas of geometrical shapes other than rectangles also if certain measurements are given to us . Try to recall and match the following:

Diagram	Shape	Area
<i>a</i>	rectangle	$a \times a$
a a	square	b  imes h
b b	triangle	$\pi b^2$
h	parallelogram	$\frac{1}{2}b \times h$
<u>b</u>	circle	$a \times b$

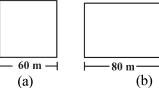
Can you write an expression for the perimeter of each of the above shapes?

# TRY THESE

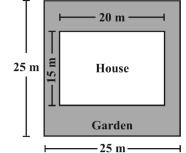


# **EXERCISE 9.1**

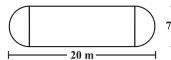
1. A square and a rectangular field with measurements as given in the figure have the same perimeter. Which field has a larger area?



2. Mrs. Kaushik has a square plot with the measurement as shown in the figure. She wants to construct a house in the middle of the plot. A garden is developed around the house. Find the total cost of developing a garden around the house at the rate of ₹ 55 per m².

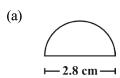


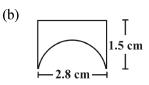
3. The shape of a garden is rectangular in the middle and semi circular at the ends as shown in the diagram. Find the area and the perimeter

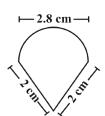


of this garden [Length of rectangle is 20-(3.5+3.5) metres].

- 4. A flooring tile has the shape of a parallelogram whose base is 24 cm and the corresponding height is 10 cm. How many such tiles are required to cover a floor of area 1080 m<sup>2</sup>? (If required you can split the tiles in whatever way you want to fill up the corners).
- 5. An ant is moving around a few food pieces of different shapes scattered on the floor. For which food-piece would the ant have to take a longer round? Remember, circumference of a circle can be obtained by using the expression  $c = 2\pi r$ , where r is the radius of the circle.







10 m

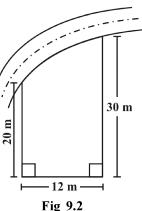
20 m

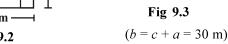
# 9.3 Area of Trapezium

Nazma owns a plot near a main road (Fig 9.2). Unlike some other rectangular plots in her neighbourhood, the plot has only one pair of parallel opposite sides. So, it is nearly a trapezium in shape. Can you find out its area?

Let us name the vertices of this plot as shown in Fig 9.3.

By drawing EC  $\parallel$  AB, we can divide it into two parts, one of rectangular shape and the other of triangular shape, (which is right angled at C), as shown in Fig 9.3.





20 m

(c)

Area of  $\triangle$  ECD =  $\frac{1}{2}h \times c = \frac{1}{2} \times 12 \times 10 = 60 \text{ m}^2$ .

Area of rectangle  $\overrightarrow{ABCE} = \overrightarrow{h} \times \overrightarrow{a} = 12 \times 20 = 240 \text{ m}^2$ .

Area of trapezium ABDE = area of  $\triangle$  ECD + Area of rectangle ABCE =  $60 + 240 = 300 \text{ m}^2$ .

We can write the area by combining the two areas and write the area of trapezium as

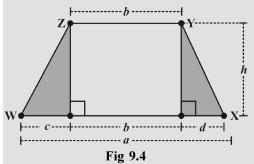
area of ABDE = 
$$\frac{1}{2}h \times c + h \times a = h\left(\frac{c}{2} + a\right)$$
  
=  $h\left(\frac{c+2a}{2}\right) = h\left(\frac{c+a+a}{2}\right)$   
=  $h\frac{(b+a)}{2}$  = height  $\frac{\text{(sum of parallel sides)}}{2}$ 

By substituting the values of h, b and a in this expression, we find  $h \frac{(b+a)}{2} = 300 \text{ m}^2$ .



# TRY THESE

1. Nazma's sister also has a trapezium shaped plot. Divide it into three parts as shown (Fig 9.4). Show that the area of trapezium WXYZ =  $h\frac{(a+b)}{2}$ .



2. If h = 10 cm, c = 6 cm, b = 12 cm, d = 4 cm, find the values of each of its parts separetely and add to find the area WXYZ. Verify it by putting the values of h, a and b in the

expression 
$$\frac{h(a+b)}{2}$$
.

# DO THIS



- 1. Draw any trapezium WXYZ on a piece of graph paper as shown in the figure and cut it out (Fig 9.5).
- 2. Find the mid point of XY by folding the side and name it A (Fig 9.6).

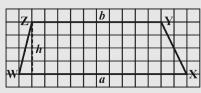
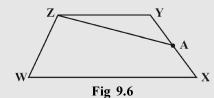
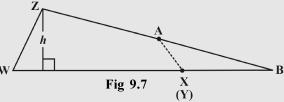


Fig 9.5



3. Cut trapezium WXYZ into two pieces by cutting along ZA. Place  $\triangle$  ZYA as shown in Fig 9.7, where AY is placed on AX.

What is the length of the base of the larger triangle? Write an expression for the area of this triangle (Fig 9.7).



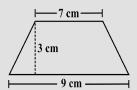
4. The area of this triangle and the area of the trapezium WXYZ are same (How?). Get the expression for the area of trapezium by using the expression for the area of triangle.

So to find the area of a trapezium we need to know the length of the parallel sides and the perpendicular distance between these two parallel sides. Half the product of the sum of the lengths of parallel sides and the perpendicular distance between them gives the area of trapezium.

### TRY THESE

Find the area of the following trapeziums (Fig 9.8).

(i)



(ii)

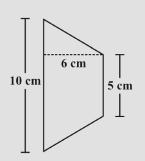




Fig 9.8

### DO THIS

In Class VII we learnt to draw parallelograms of equal areas with different perimeters. Can it be done for trapezium? Check if the following trapeziums are of equal areas but have different perimeters (Fig 9.9).



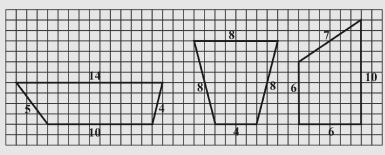


Fig 9.9

We know that all congruent figures are equal in area. Can we say figures equal in area need to be congruent too? Are these figures congruent?

Draw at least three trapeziums which have different areas but equal perimeters on a squared sheet.

# 9.4 Area of a General Quadrilateral

A general quadrilateral can be split into two triangles by drawing one of its diagonals. This "triangulation" helps us to find a formula for any general quadrilateral. Study the Fig 9.10.

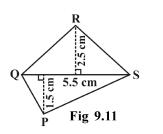
Area of quadrilateral ABCD

= (area of 
$$\triangle$$
 ABC) + (area of  $\triangle$  ADC)
$$= (\frac{1}{2} \text{AC} \times h_1) + (\frac{1}{2} \text{AC} \times h_2)$$

$$= \frac{1}{2} \text{AC} \times (h_1 + h_2)$$
Fig 9.10
$$= \frac{1}{2} d(h_1 + h_2) \text{ where } d \text{ denotes the length of diagonal AC.}$$

**Example 1:** Find the area of quadrilateral PQRS shown in Fig 9.11.

**Solution:** In this case, d = 5.5 cm,  $h_1 = 2.5$ cm,  $h_2 = 1.5$  cm,

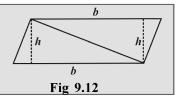


Area = 
$$\frac{1}{2} d(h_1 + h_2)$$
  
=  $\frac{1}{2} \times 5.5 \times (2.5 + 1.5) \text{ cm}^2$   
=  $\frac{1}{2} \times 5.5 \times 4 \text{ cm}^2 = 11 \text{ cm}^2$ 



### TRY THESE

We know that parallelogram is also a quadrilateral. Let us also split such a quadrilateral into two triangles, find their areas and hence that of the parallelogram. Does this agree with the formula that you know already? (Fig 9.12)



### 9.4.1 Area of special quadrilaterals

We can use the same method of splitting into triangles (which we called "triangulation") to find a formula for the area of a rhombus. In Fig 9.13 ABCD is a rhombus. Therefore, its diagonals are perpendicular bisectors of each other.

Area of rhombus ABCD = (area of  $\triangle$  ACD) + (area of  $\triangle$  ABC)

$$= (\frac{1}{2} \times AC \times OD) + (\frac{1}{2} \times AC \times OB) = \frac{1}{2}AC \times (OD + OB)$$

$$= \frac{1}{2}AC \times BD = \frac{1}{2}d_1 \times d_2 \quad \text{where } AC = d_1 \text{ and } BD = d_2 \quad A$$
Fig 9.13

In other words, area of a rhombus is half the product of its diagonals.

**Example 2:** Find the area of a rhombus whose diagonals are of lengths 10 cm and 8.2 cm.

**Solution:** Area of the rhombus =  $\frac{1}{2} d_1 d_2$  where  $d_1, d_2$  are lengths of diagonals. =  $\frac{1}{2} \times 10 \times 8.2$  cm<sup>2</sup> = 41 cm<sup>2</sup>.

# THINK, DISCUSS AND WRITE

A parallelogram is divided into two congruent triangles by drawing a diagonal across it. Can we divide a trapezium into two congruent triangles?



### TRY THESE

Find the area of these quadrilaterals (Fig 9.14).

B

4 cm

5 cm

4 cm

5 cm

4 cm

5 cm

(iii)

Fig 9.14

# 9.5 Area of a Polygon

We split a quadrilateral into triangles and find its area. Similar methods can be used to find the area of a polygon. Observe the following for a pentagon: (Fig 9.15, 9.16)

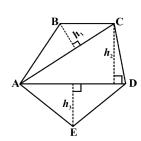


Fig 9.15

By constructing two diagonals AC and AD the pentagon ABCDE is divided into three parts. So, area ABCDE = area of  $\Delta$  ABC + area of  $\Delta$  ACD + area of  $\Delta$  AED.

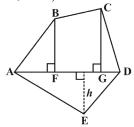


Fig 9.16

By constructing one diagonal AD and two perpendiculars BF and CG on it, pentagon ABCDE is divided into four parts. So, area of ABCDE = area of right angled  $\Delta$  AFB + area of trapezium BFGC + area of right angled  $\Delta$  CGD + area of  $\Delta$  AED. (Identify the parallel sides of trapezium BFGC.)



### TRY THESE

(i) Divide the following polygons (Fig 9.17) into parts (triangles and trapezium) to find out its area.

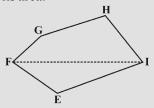
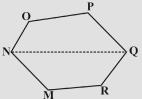


Fig 9.17



FI is a diagonal of polygon EFGHI

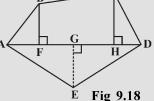
NQ is a diagonal of polygon MNOPQR

(ii) Polygon ABCDE is divided into parts as shown below (Fig 9.18). Find its area if AD = 8 cm, AH = 6 cm, AG = 4 cm, AF = 3 cm and perpendiculars BF = 2 cm, CH = 3 cm, EG = 2.5 cm.

Area of Polygon ABCDE = area of  $\triangle$  AFB + ....

Area of  $\triangle AFB = \frac{1}{2} \times AF \times BF = \frac{1}{2} \times 3 \times 2 = \dots$ 

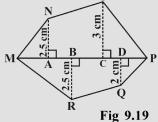
Area of trapezium FBCH = FH  $\times \frac{(BF + CH)}{2}$ 



$$= 3 \times \frac{(2+3)}{2}$$
 [FH = AH – AF]

Area of  $\triangle CHD = \frac{1}{2} \times HD \times CH = ....$ ; Area of  $\triangle ADE = \frac{1}{2} \times AD \times GE = ....$ So, the area of polygon ABCDE = ....

(iii) Find the area of polygon MNOPQR (Fig 9.19) if MP = 9 cm, MD = 7 cm, MC = 6 cm, MB = 4 cm, MA = 2 cm
NA, OC, QD and RB are perpendiculars to diagonal MP.



**Example 1:** The area of a trapezium shaped field is 480 m<sup>2</sup>, the distance between two parallel sides is 15 m and one of the parallel side is 20 m. Find the other parallel side.

**Solution:** One of the parallel sides of the trapezium is a = 20 m, let another parallel side be b, height b = 15 m.

The given area of trapezium =  $480 \text{ m}^2$ .

Area of a trapezium =  $\frac{1}{2}h(a+b)$ So  $480 = \frac{1}{2} \times 15 \times (20+b)$  or  $\frac{480 \times 2}{15} = 20+b$ or 64 = 20+b or b = 44 m

Hence the other parallel side of the trapezium is 44 m.

**Example 2:** The area of a rhombus is 240 cm<sup>2</sup> and one of the diagonals is 16 cm. Find the other diagonal.

**Solution:** Let length of one diagonal  $d_1 = 16$  cm

and

length of the other diagonal =  $d_3$ 

Area of the rhombus = 
$$\frac{1}{2} d_1 \cdot d_2 = 240$$

So,

$$\frac{1}{2}16 \cdot d_2 = 240$$
$$d_2 = 30 \text{ cm}$$

Therefore,

$$d_2 = 30 \text{ cm}$$

Hence the length of the second diagonal is 30 cm.

**Example 3:** There is a hexagon MNOPQR of side 5 cm (Fig 9.20). Aman and Ridhima divided it in two different ways (Fig 9.21).

Find the area of this hexagon using both ways.

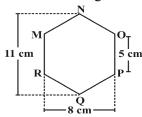
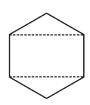
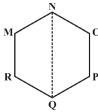


Fig 9.20



Ridhima's method



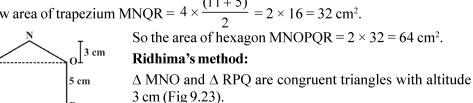
Aman's method

Fig 9.21

#### **Solution:** Aman's method:

Since it is a hexagon so NQ divides the hexagon into two congruent trapeziums. You can verify it by paper folding (Fig 9.22).

Now area of trapezium MNQR =  $4 \times \frac{(11+5)}{2} = 2 \times 16 = 32 \text{ cm}^2$ .



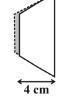


Fig 9.22

You can verify this by cutting off these two triangles and placing them on one another. Fig 9.23

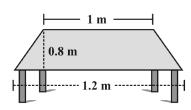
Area of 
$$\triangle$$
 MNO =  $\frac{1}{2} \times 8 \times 3 = 12 \text{ cm}^2 = \text{Area of } \triangle \text{ RPQ}$ 

Area of rectangle MOPR =  $8 \times 5 = 40 \text{ cm}^2$ .

Now, area of hexagon MNOPQR = 40 + 12 + 12 = 64 cm<sup>2</sup>.

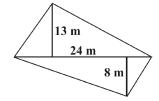
# **EXERCISE 9.2**

1. The shape of the top surface of a table is a trapezium. Find its area if its parallel sides are 1 m and 1.2 m and perpendicular distance between them is 0.8 m.

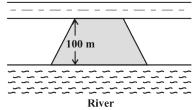


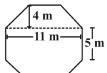


- 2. The area of a trapezium is 34 cm<sup>2</sup> and the length of one of the parallel sides is 10 cm and its height is 4 cm. Find the length of the other parallel side.
  - 3. Length of the fence of a trapezium shaped field ABCD is 120 m. If BC = 48 m, CD = 17 m and AD = 40 m, find the area of this field. Side AB is perpendicular to the parallel sides AD and BC.
- **4.** The diagonal of a quadrilateral shaped field is 24 m and the perpendiculars dropped on it from the remaining opposite vertices are 8 m and 13 m. Find the area of the field.



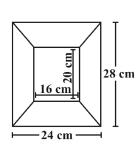
- 5. The diagonals of a rhombus are 7.5 cm and 12 cm. Find its area
- **6.** Find the area of a rhombus whose side is 5 cm and whose altitude is 4.8 cm. If one of its diagonals is 8 cm long, find the length of the other diagonal.
- 7. The floor of a building consists of 3000 tiles which are rhombus shaped and each of its diagonals are 45 cm and 30 cm in length. Find the total cost of polishing the floor, if the cost per m² is ₹ 4.
- 8. Mohan wants to buy a trapezium shaped field. Its side along the river is parallel to and twice the side along the road. If the area of this field is 10500 m<sup>2</sup> and the perpendicular distance between the two parallel sides is 100 m, find the length of the side along the river.

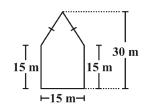




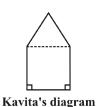
- 9. Top surface of a raised platform is in the shape of a regular octagon as shown in the figure. Find the area of the octagonal surface.
- 10. There is a pentagonal shaped park as shown in the figure.

For finding its area Jyoti and Kavita divided it in two different ways.









Find the area of this park using both ways. Can you suggest some other way of finding its area?

11. Diagram of the adjacent picture frame has outer dimensions  $=24 \text{ cm} \times 28 \text{ cm}$  and inner dimensions  $16 \text{ cm} \times 20 \text{ cm}$ . Find the area of each section of the frame, if the width of each section is same.

# 9.6 Solid Shapes

In your earlier classes you have studied that two dimensional figures can be identified as the faces of three dimensional shapes. Observe the solids which we have discussed so far (Fig 9.24).

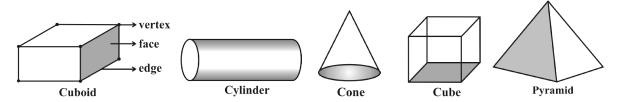
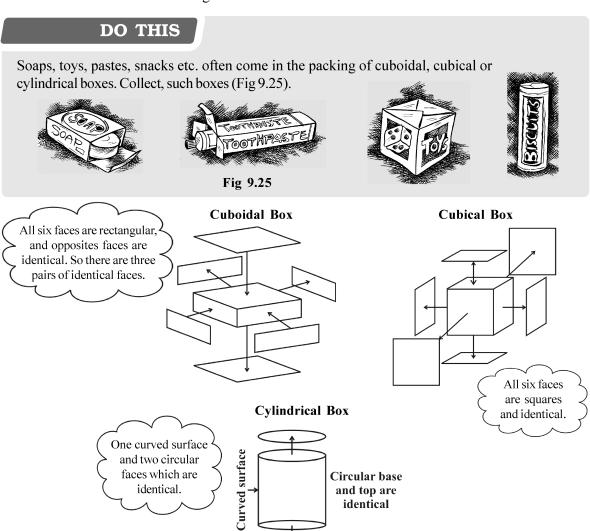


Fig 9.24

Observe that some shapes have two or more than two identical (congruent) faces. Name them. Which solid has all congruent faces?



Now take one type of box at a time. Cut out all the faces it has. Observe the shape of each face and find the number of faces of the box that are identical by placing them on each other. Write down your observations.



Fig 9.26
(This is a right circular cylinder)

Did you notice the following:

The cylinder has congruent circular faces that are parallel to each other (Fig 9.26). Observe that the line segment joining the center of circular faces is perpendicular to the base. Such cylinders are known as **right circular cylinders**. We are only going to study this type of cylinders, though there are other types of cylinders as well (Fig 9.27).



Fig 9.27 (This is not a right circular cylinder)

# THINK, DISCUSS AND WRITE



Why is it incorrect to call the solid shown here a cylinder?

# 9.7 Surface Area of Cube, Cuboid and Cylinder

Imran, Monica and Jaspal are painting a cuboidal, cubical and a cylindrical box respectively of same height (Fig 9.28).

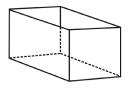






Fig 9.28

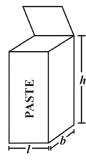
They try to determine who has painted more area. Hari suggested that finding the surface area of each box would help them find it out.

To find the total surface area, find the area of each face and then add. The surface area of a solid is the sum of the areas of its faces. To clarify further, we take each shape one by one.

### 9.7.1 Cuboid

Suppose you cut open a cuboidal box and lay it flat (Fig 9.29). We can see a net as shown below (Fig 9.30).

Write the dimension of each side. You know that a cuboid has three pairs of identical faces. What expression can you use to find the area of each face?



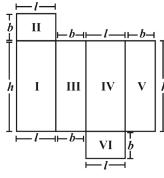


Fig 9.29

<sup>29</sup> Fig 9.30

Find the total area of all the faces of the box. We see that the total surface area of a cuboid is area I + area II + area III + area IV + area V + area VI

$$= h \times l + b \times l + b \times h + l \times h + b \times h + l \times b$$

So total surface area =  $2(h \times l + b \times h + b \times l) = 2(lb + bh + hl)$ 

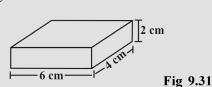
where h, l and b are the height, length and width of the cuboid respectively.

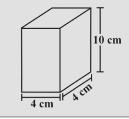
Suppose the height, length and width of the box shown above are 20 cm, 15 cm and 10 cm respectively.

Then the total surface area = 
$$2(20 \times 15 + 20 \times 10 + 10 \times 15)$$
  
=  $2(300 + 200 + 150) = 1300 \text{ m}^2$ .

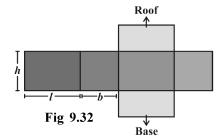
# TRY THESE

Find the total surface area of the following cuboids (Fig 9.31):





• The side walls (the faces excluding the top and bottom) make the lateral surface area of the cuboid. For example, the total area of all the four walls of the cuboidal room in which you are sitting is the lateral surface area of this room (Fig 9.32). Hence, the lateral surface area of a cuboid is given by  $2(h \times l + b \times h)$  or 2h(l + b).



# DO THIS

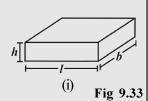
(i) Cover the lateral surface of a cuboidal duster (which your teacher uses in the class room) using a strip of brown sheet of paper, such that it just fits around the surface. Remove the paper. Measure the area of the paper. Is it the lateral surface area of the duster?

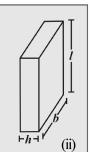


- (ii) Measure length, width and height of your classroom and find
  - (a) the total surface area of the room, ignoring the area of windows and doors.
  - (b) the lateral surface area of this room.
  - (c) the total area of the room which is to be white washed.

# THINK, DISCUSS AND WRITE

- 1. Can we say that the total surface area of cuboid = lateral surface area  $\pm 2 \times$  area of base?
- 2. If we interchange the lengths of the base and the height of a cuboid (Fig 9.33(i)) to get another cuboid (Fig 9.33(ii)), will its lateral surface area change?

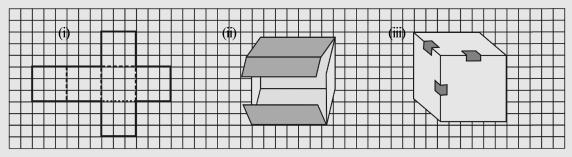


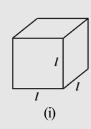


#### 9.7.2 Cube

### DO THIS

Draw the pattern shown on a squared paper and cut it out [Fig 9.34(i)]. (You know that this pattern is a net of a cube. Fold it along the lines [Fig 9.34(ii)] and tape the edges to form a cube [Fig 9.34(iii)].





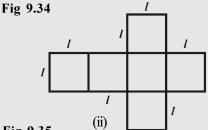


Fig 9.35

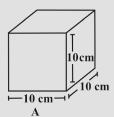
- (a) What is the length, width and height of the cube? Observe that all the faces of a cube are square in shape. This makes length, height and width of a cube equal (Fig 9.35(i)).
- (b) Write the area of each of the faces. Are they equal?
- (c) Write the total surface area of this cube.
- (d) If each side of the cube is *l*, what will be the area of each face? (Fig 9.35(ii)).

Can we say that the total surface area of a cube of side l is  $6l^2$ ?

### TRY THESE



Find the surface area of cube A and lateral surface area of cube B (Fig 9.36).



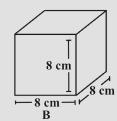


Fig 9.36

# THINK, DISCUSS AND WRITE

(i) Two cubes each with side b are joined to form a cuboid (Fig 9.37). What is the surface area of this cuboid? Is it  $12b^2$ ? Is the surface area of cuboid formed by joining three such cubes,  $18b^2$ ? Why?

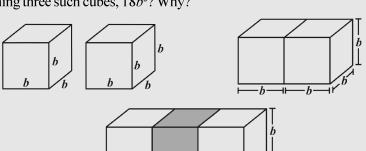


Fig 9.37

(ii) How will you arrange 12 cubes of equal length to form a cuboid of smallest surface area?

-*b*—⊢

(iii) After the surface area of a cube is painted, the cube is cut into 64 smaller cubes of same dimensions (Fig 9.38). How many have no face painted? 1 face painted? 2 faces painted? 3 faces painted?

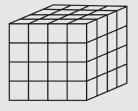


Fig 9.38

### 9.7.3 Cylinders

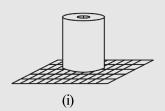
Most of the cylinders we observe are right circular cylinders. For example, a tin, round pillars, tube lights, water pipes etc.

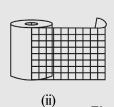
### DO THIS

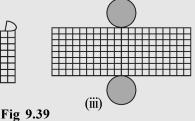
(i) Take a cylindrical can or box and trace the base of the can on graph paper and cut it [Fig 9.39(i)]. Take another graph paper in such a way that its width is equal to the height of the can. Wrap the strip around the can such that it just fits around the can (remove the excess paper) [Fig 9.39(ii)].



Tape the pieces [Fig 9.39(iii)] together to form a cylinder [Fig 9.39(iv)]. What is the shape of the paper that goes around the can?









Of course it is rectangular in shape. When you tape the parts of this cylinder together, the length of the rectangular strip is equal to the circumference of the circle. Record the radius (r) of the circular base, length (l) and width (h) of the rectangular strip. Is  $2\pi r =$  length of the strip. Check if the area of rectangular strip is  $2\pi rh$ . Count how many square units of the squared paper are used to form the cylinder. Check if this count is approximately equal to  $2\pi r (r + h)$ .

(ii) We can deduce the relation  $2\pi r(r+h)$  as the surface area of a cylinder in another way. Imagine cutting up a cylinder as shown below (Fig 9.40).

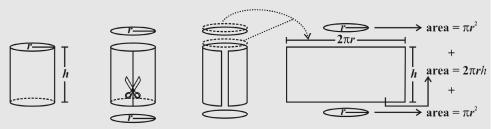


Fig 9.40

**Note:** We take  $\pi$  to be  $\frac{22}{7}$  unless otherwise stated.

The lateral (or curved) surface area of a cylinder is  $2\pi rh$ .

The total surface area of a cylinder = 
$$\pi r^2 + 2\pi rh + \pi r^2$$
  
=  $2\pi r^2 + 2\pi rh$  or  $2\pi r (r + h)$ 

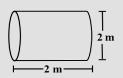


### TRY THESE

Find total surface area of the following cylinders (Fig 9.41)



Fig 9.41





# THINK, DISCUSS AND WRITE

Note that lateral surface area of a cylinder is the circumference of base × height of cylinder. Can we write lateral surface area of a cuboid as perimeter of base × height of cuboid?

**Example 4:** An aquarium is in the form of a cuboid whose external measures are  $80 \text{ cm} \times 30 \text{ cm} \times 40 \text{ cm}$ . The base, side faces and back face are to be covered with a coloured paper. Find the area of the paper needed?

**Solution:** The length of the aquarium = l = 80 cm

Width of the aquarium = b = 30 cm

Height of the aquarium = h = 40 cm

Area of the base = 
$$l \times b = 80 \times 30 = 2400 \text{ cm}^2$$

Area of the side face = 
$$b \times h = 30 \times 40 = 1200 \text{ cm}^2$$

Area of the back face = 
$$l \times h = 80 \times 40 = 3200 \text{ cm}^2$$



Required area = Area of the base + area of the back face

$$+(2 \times \text{area of a side face})$$

$$= 2400 + 3200 + (2 \times 1200) = 8000 \text{ cm}^2$$

Hence the area of the coloured paper required is 8000 cm<sup>2</sup>.

**Example 5:** The internal measures of a cuboidal room are  $12 \text{ m} \times 8 \text{ m} \times 4 \text{ m}$ . Find the total cost of whitewashing all four walls of a room, if the cost of white washing is  $₹ 5 \text{ per m}^2$ . What will be the cost of white washing if the ceiling of the room is also whitewashed.

**Solution:** Let the length of the room = l = 12 m

Width of the room = 
$$b = 8 \text{ m}$$

Height of the room = 
$$h = 4$$
 m

Area of the four walls of the room = Perimeter of the base  $\times$  Height of the room

$$= 2 (l + b) \times h = 2 (12 + 8) \times 4$$

$$= 2 \times 20 \times 4 = 160 \text{ m}^2.$$

Cost of white washing per  $m^2 = 7$ 

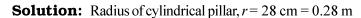
Hence the total cost of white washing four walls of the room =  $₹(160 \times 5) = ₹800$ 

Area of ceiling is 
$$12 \times 8 = 96 \text{ m}^2$$

Cost of white washing the ceiling = 
$$\neq$$
 (96 × 5) =  $\neq$  480

So the total cost of white washing = 
$$₹ (800 + 480) = ₹ 1280$$

**Example 6:** In a building there are 24 cylindrical pillars. The radius of each pillar is 28 cm and height is 4 m. Find the total cost of painting the curved surface area of all pillars at the rate of  $\mathbb{Z}$  8 per m<sup>2</sup>.



height, 
$$h = 4 \text{ m}$$

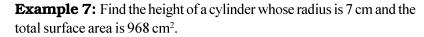
curved surface area of a cylinder =  $2\pi rh$ 

curved surface area of a pillar = 
$$2 \times \frac{22}{7} \times 0.28 \times 4 = 7.04 \text{ m}^2$$

curved surface area of 24 such pillar = 
$$7.04 \times 24 = 168.96 \text{ m}^2$$

cost of painting an area of 
$$1 \text{ m}^2 = \text{ } 8$$

Therefore, cost of painting 1689.6 
$$m^2$$
 = 168.96 × 8 = ₹ 1351.68



**Solution:** Let height of the cylinder = 
$$h$$
, radius =  $r$  = 7cm

Total surface area = 
$$2\pi r (h + r)$$





i.e., 
$$2 \times \frac{22}{7} \times 7 \times (7 + h) = 968$$
  
 $h = 15 \text{ cm}$ 

Hence, the height of the cylinder is 15 cm.

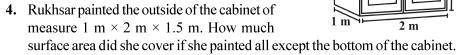


# **EXERCISE 9.3**

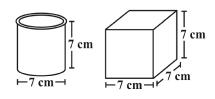
- 1. There are two cuboidal boxes as shown in the adjoining figure. Which box requires the lesser amount of material to make?
- 2. A suitcase with measures 80 cm ×

  48 cm × 24 cm is to be covered with

  a tarpaulin cloth. How many metres of tarpaulin of width 96 cm is required to cover 100 such suitcases?
- **3.** Find the side of a cube whose surface area is 600 cm<sup>2</sup>.



**5.** Daniel is painting the walls and ceiling of a cuboidal hall with length, breadth and height of 15 m, 10 m and 7 m respectively. From each can of paint 100 m<sup>2</sup> of area is painted. How many cans of paint will she need to paint the room?

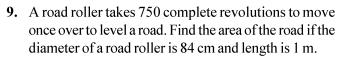


50 cm

50 cm

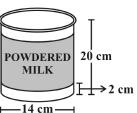
1.5 m

- **6.** Describe how the two figures at the right are alike and how they are different. Which box has larger lateral surface area?
- 7. A closed cylindrical tank of radius 7 m and height 3 m is made from a sheet of metal. How much sheet of metal is required?
- **8.** The lateral surface area of a hollow cylinder is 4224 cm<sup>2</sup>. It is cut along its height and formed a rectangular sheet of width 33 cm. Find the perimeter of rectangular sheet?



10. A company packages its milk powder in cylindrical container whose base has a diameter of 14 cm and height 20 cm. Company places a label around the surface of the container (as shown in the figure). If the label is placed 2 cm from top and bottom, what is the area of the label.





# 9.8 Volume of Cube, Cuboid and Cylinder

Amount of space occupied by a three dimensional object is called its **volume**. Try to compare the volume of objects surrounding you. For example, volume of a room is greater than the volume of an almirah kept inside it. Similarly, volume of your pencil box is greater than the volume of the pen and the eraser kept inside it.

Can you measure volume of either of these objects?

Remember, we use square units to find the area of a region. Here we will use cubic units to find the volume of a solid, as cube is the most convenient solid shape (just as square is the most convenient shape to measure area of a region).

For finding the area we divide the region into square units, similarly, to find the volume of a solid we need to divide it into cubical units.

Observe that the volume of each of the adjoining solids is 8 cubic units (Fig 9.42).

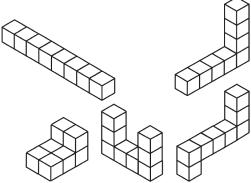


Fig 9.42

We can say that the volume of a solid is measured by counting the number of unit cubes it contains. Cubic units which we generally use to measure volume are

We now find some expressions to find volume of a cuboid, cube and cylinder. Let us take each solid one by one.

### 9.8.1 Cuboid

Take 36 cubes of equal size (i.e., length of each cube is same). Arrange them to form a cuboid. You can arrange them in many ways. Observe the following table and fill in the blanks.

	cuboid	length	breadth	height	$l \times b \times h = V$
(i)	12 units 3 units	12	3	1	$12 \times 3 \times 1 = 36$
(ii)			ii		

(iii)	į	ł	į	
(iv)	:	:	::	



What do you observe?

Since we have used 36 cubes to form these cuboids, volume of each cuboid is 36 cubic units. Also volume of each cuboid is equal to the product of length,

breadth and height of the cuboid. From the above example we can say volume of cuboid  $= l \times b \times h$ . Since  $l \times b$  is the area of its base we can also say that,

Volume of cuboid = area of the base  $\times$  height

# DO THIS



Take a sheet of paper. Measure its area. Pile up such sheets of paper of same size to make a cuboid (Fig 9.43). Measure the height of this pile. Find the volume of the cuboid by finding the product of the area of the sheet and the height of this pile of sheets.

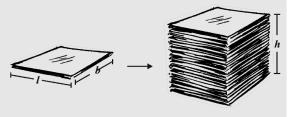


Fig 9.43

This activity illustrates the idea

that volume of a solid can be deduced by this method also (if the base and top of the solid are congruent and parallel to each other and its edges are perpendicular to the base). Can you think of such objects whose volume can be found by using this method?



### TRY THESE

Find the volume of the following cuboids (Fig 9.44).



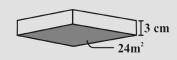


Fig 9.44

### 9.8.2 Cube

The cube is a special case of a cuboid, where l = b = h. Hence, volume of cube =  $l \times l \times l = l^3$ 

## TRY THESE

Find the volume of the following cubes

- (a) with a side 4 cm
- (b) with a side 1.5 m



# DO THIS

Arrange 64 cubes of equal size in as many ways as you can to form a cuboid. Find the surface area of each arrangement. Can solid shapes of same volume have same surface area?

# THINK, DISCUSS AND WRITE

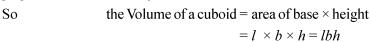
A company sells biscuits. For packing purpose they are using cuboidal boxes: box A $\rightarrow$ 3 cm × 8 cm × 20 cm, box B $\rightarrow$  4 cm × 12 cm × 10 cm. What size of the box will be economical for the company? Why? Can you suggest any other size (dimensions) which has the same volume but is more economical than these?



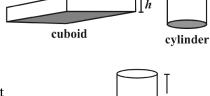
### 11.8.3 Cylinder

We know that volume of a cuboid can be found by finding the product of area of base and its height. Can we find the volume of a cylinder in the same way?

Just like cuboid, cylinder has got a top and a base which are congruent and parallel to each other. Its lateral surface is also perpendicular to the base, just like cuboid.



Volume of cylinder = area of base × height  
= 
$$\pi r^2 \times h = \pi r^2 h$$

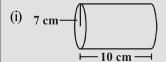


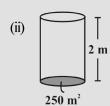
area of base

 $(=\pi r^2)$ 

#### TRY THESE

Find the volume of the following cylinders.







# 9.9 Volume and Capacity

There is not much difference between these two words.

- (a) Volume refers to the amount of space occupied by an object.
- (b) Capacity refers to the quantity that a container holds.

**Note:** If a water tin holds 100 cm<sup>3</sup> of water then the capacity of the water tin is 100 cm<sup>3</sup>.

Capacity is also measured in terms of litres. The relation between litre and cm<sup>3</sup> is,  $1 \text{ mL} = 1 \text{ cm}^3$ ,  $1 \text{ L} = 1000 \text{ cm}^3$ . Thus,  $1 \text{ m}^3 = 1000000 \text{ cm}^3 = 1000 \text{ L}$ .

**Example 8:** Find the height of a cuboid whose volume is 275 cm<sup>3</sup> and base area is 25 cm<sup>2</sup>.

**Solution:** Volume of a cuboid = Base area  $\times$  Height

Hence height of the cuboid = 
$$\frac{\text{Volume of cuboid}}{\text{Base area}}$$
  
=  $\frac{275}{25} = 11 \text{ cm}$ 

Height of the cuboid is 11 cm.

**Example 9:** A godown is in the form of a cuboid of measures  $60 \text{ m} \times 40 \text{ m} \times 30 \text{ m}$ . How many cuboidal boxes can be stored in it if the volume of one box is  $0.8 \text{ m}^3$ ?

**Solution:** Volume of one box =  $0.8 \text{ m}^3$ 

Volume of godown = 
$$60 \times 40 \times 30 = 72000 \text{ m}^3$$

Number of boxes that can be stored in the godown =  $\frac{\text{Volume of the godown}}{\text{Volume of one box}}$  $= \frac{60 \times 40 \times 30}{0.8} = 90,000$ 

Hence the number of cuboidal boxes that can be stored in the godown is 90,000.

**Example 10:** A rectangular paper of width 14 cm is rolled along its width and a cylinder of radius 20 cm is formed. Find the volume of the cylinder (Fig 9.45). (Take  $\frac{22}{7}$  for  $\pi$ )

**Solution:** A cylinder is formed by rolling a rectangle about its width. Hence the width of the paper becomes height and radius of the cylinder is 20 cm.

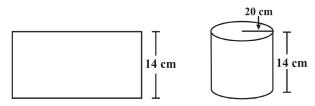


Fig 9.45

Height of the cylinder = 
$$h = 14$$
 cm  
Radius =  $r = 20$  cm

Volume of the cylinder = V = 
$$\pi r^2 h$$
  
=  $\frac{22}{7} \times 20 \times 20 \times 14 = 17600 \text{ cm}^3$ 

Hence, the volume of the cylinder is 17600 cm<sup>3</sup>.

**Example 11:** A rectangular piece of paper 11 cm × 4 cm is folded without overlapping to make a cylinder of height 4 cm. Find the volume of the cylinder.

**Solution:** Length of the paper becomes the perimeter of the base of the cylinder and width becomes height.

Let radius of the cylinder = r and height = h

Perimeter of the base of the cylinder =  $2\pi r = 11$ 

or

$$2 \times \frac{22}{7} \times r = 11$$

Therefore,

$$r = \frac{7}{4}$$
 cm

 $r = \frac{7}{4}$  cm Volume of the cylinder =  $V = \pi r^2 h$ 

$$= \frac{22}{7} \times \frac{7}{4} \times \frac{7}{4} \times 4 \text{ cm}^3 = 38.5 \text{ cm}^3.$$

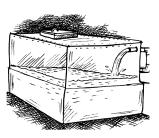
Hence the volume of the cylinder is 38.5 cm

# **EXERCISE 9.4**

- 1. Given a cylindrical tank, in which situation will you find surface area and in which situation volume.
  - (a) To find how much it can hold.
  - (b) Number of cement bags required to plaster it.
  - (c) To find the number of smaller tanks that can be filled with water from it.
- 2. Diameter of cylinder A is 7 cm, and the height is 14 cm. Diameter of cylinder B is 14 cm and height is 7 cm. Without doing any calculations can you suggest whose volume is greater? Verify it by finding the volume of both the cylinders. Check whether the cylinder with greater volume also has greater surface area?
- 14 cm 14 cm 7 cm В
- 3. Find the height of a cuboid whose base area is 180 cm<sup>2</sup> and volume is 900 cm<sup>3</sup>?
- 4. A cuboid is of dimensions  $60 \text{ cm} \times 54 \text{ cm} \times 30 \text{ cm}$ . How many small cubes with side 6 cm can be placed in the given cuboid?
- 5. Find the height of the cylinder whose volume is 1.54 m<sup>3</sup> and diameter of the base is 140 cm?
- **6.** A milk tank is in the form of cylinder whose radius is 1.5 m and length is 7 m. Find the quantity of milk in litres that can be stored in the tank?
- 7. If each edge of a cube is doubled,
  - (i) how many times will its surface area increase?
  - (ii) how many times will its volume increase?



**8.** Water is pouring into a cubiodal reservoir at the rate of 60 litres per minute. If the volume of reservoir is 108 m<sup>3</sup>, find the number of hours it will take to fill the reservoir.



# WHAT HAVE WE DISCUSSED?

- 1. Area of
  - (i) a trapezium = half of the sum of the lengths of parallel sides × perpendicular distance between them.
  - (ii) a rhombus = half the product of its diagonals.
- 2. Surface area of a solid is the sum of the areas of its faces.
- 3. Surface area of

a cuboid = 
$$2(lb + bh + hl)$$

a cube = 
$$6l^2$$

a cylinder = 
$$2\pi r(r+h)$$

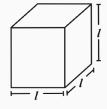
- **4.** Amount of region occupied by a solid is called its **volume**.
- 5. Volume of

a cuboid = 
$$l \times b \times h$$

a cube = 
$$l^3$$

a cylinder = 
$$\pi r^2 h$$

- 6. (i)  $1 \text{ cm}^3 = 1 \text{ mL}$ 
  - (ii)  $1L = 1000 \text{ cm}^3$
  - (iii)  $1 \text{ m}^3 = 1000000 \text{ cm}^3 = 1000 \text{L}$







# 1. CUBES AND CUBE ROOTS

# **EXERCISE 1.1**

- 1. (ii) and (iv)
- 2. (i) 3
- (ii) 2 (ii) 2
- (iii) 3
- (iv) 5
- (v) 10

- **3.** (i) 3
- (iii) **5**
- (iv) 3
- (v) 11

**4.** 20 cuboids

### EXERCISE 1.2

- **1.** (i) 4
- (ii) 8 (viii) 36
- (iii) 22
- (iv) 30
- (v) 25
- (vi) 24

- (vii) 48
- (ix) 56
- (iii) False
- (iv) False
- (v) False
- (vi) False

(vii) True

2. (i) False (ii) True

**3.** 11, 17, 23, 32

# 2. EXPONENTS AND POWERS

### EXERCISE 2.1

- 1. (i)  $\frac{1}{9}$  (ii)  $\frac{1}{16}$
- (iii) 32
- 2. (i)  $\frac{1}{(-4)^3}$

- (ii)  $\frac{1}{2^6}$  (iii)  $(5)^4$  (iv)  $\frac{1}{(3)^2}$  (v)  $\frac{1}{(-14)^3}$

- **3.** (i) 5 (ii)  $\frac{1}{2}$  (iii) 29 (iv) 1 (v)  $\frac{81}{16}$
- **4.** (i) 250 (ii)  $\frac{1}{60}$  **5.** m = 2 **6.** (i) -1 (ii)  $\frac{512}{125}$

7. (i)  $\frac{625t^4}{2}$  (ii) 5<sup>5</sup>

# **EXERCISE 2.2**

- 1. (i)  $8.5 \times 10^{-12}$
- (ii)  $9.42 \times 10^{-12}$
- (iii)  $6.02 \times 10^{15}$

- (iv)  $8.37 \times 10^{-9}$
- (v)  $3.186 \times 10^{10}$

- **2.** (i) 0.00000302
- (ii) 45000

(iii) 0.00000003

- (iv) 1000100000
- (v) 5800000000000
- (vi) 3614920

- 3. (i)  $1 \times 10^{-6}$
- (ii)  $1.6 \times 10^{-19}$
- (iii)  $5 \times 10^{-7}$

- (iv)  $1.275 \times 10^{-5}$
- (v)  $7 \times 10^{-2}$
- 4.  $1.0008 \times 10^2$

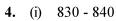
# 3. DATA HANDLING

# **EXERCISE 3.1**

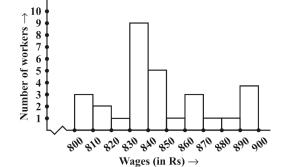
1. (b), (d). In all these cases data can be divided into class intervals.

2.	Shopper	Tally marks	Number
	W	HHHHHHI	28
	M	####	15
	В	7	5
	G	## ##	12

3.	Interval	Tally marks	Frequency
	800 - 810		3
	810 - 820	П	2
	820 - 830		1
	830 - 840	<del>/</del>	9
	840 - 850	7	5
	850 - 860		1
	860 - 870	Ш	3
	870 - 880	1	1
	880 - 890		1
	890 - 900	1111	4
		Total	30



(ii) 10



**5.** (i) 4 - 5 hours

(ii) 34

(iii) 14

<sup>(</sup>iii) 20

# **EXERCISE 3.2**

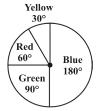
- (i) 200 (ii) Lightmusic (iii) Classical - 100, Semi classical - 200, Light - 400, Folk - 300
- Winter (ii) Winter 150°, Rainy 120°, Summer 90°

Winter

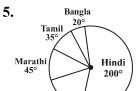
Rainy

1209

3.



- Hindi (i)
- (ii) 30 marks
- (iii) Yes



English

# EXERCISE 3.3

- Outcomes  $\rightarrow$  A, B, C, D 1. (a)
  - HT, HH, TH, TT (Here HT means Head on first coin and Tail on the second coin and so on).
- 2. Outcomes of an event of getting
  - (i) (a) 2, 3, 5
- (b) 1, 4, 6
- (ii) (a) 6
- (b) 1, 2, 3, 4, 5

- 3. (a)  $\frac{1}{5}$  (b)  $\frac{1}{13}$  (c)  $\frac{4}{7}$ 4. (i)  $\frac{1}{10}$  (ii)  $\frac{1}{2}$  (iii)  $\frac{2}{5}$  (iv)  $\frac{9}{10}$

- 5. Probability of getting a green sector =  $\frac{3}{5}$ ; probability of getting a non-blue sector =  $\frac{4}{5}$
- **6.** Probability of getting a prime number =  $\frac{1}{2}$ ; probability of getting a number which is not prime =  $\frac{1}{2}$

Probability of getting a number greater than  $5 = \frac{1}{6}$ 

Probability of getting a number not greater than  $5 = \frac{5}{6}$ 

# 4. DIRECT AND INVERSE PROPORTIONS

### **EXERCISE 4.1**

- **1.** No
- Parts of red pigment 7 12 20 8 32 56 96 160 Parts of base

**3.** 24 parts

**4.** 700 bottles

5.  $10^{-4}$  cm: 2 cm

**6.** 21 m

7. (i)  $2.25 \times 10^7$  crystals

(ii)  $5.4 \times 10^6$  crystals

8. 4 cm

(i) 6 m

(ii) 8 m 75 cm 10. 168 km

# EXERCISE 4.2

1. (i), (iv), (v)

**2.**  $4 \rightarrow 25,000$ ;  $5 \rightarrow 20,000$ ;  $8 \rightarrow 12,500$ ;  $10 \rightarrow 10,000$ ;  $20 \rightarrow 5,000$ Amount given to a winner is inversely proportional to the number of winners.

3.  $8 \rightarrow 45^{\circ}$ ,  $10 \rightarrow 36^{\circ}$ ,  $12 \rightarrow 30^{\circ}$ 

(i) Yes

(ii) 24°

(iii) 9

**4.** 6

**5.** 4

**6.** 3 days

7. 15 boxes

8. 49 machines

**9.**  $1\frac{1}{2}$  hours

**10.** (i) 6 days (ii) 6 persons **11.** 40 minutes

# 5. INTRODUCTION TO GRAPHS

# EXERCISE 5.1

36.5° C **1.** (a)

(b) 12 noon

(c) 1 p.m, 2 p.m.

- 36.5° C; The point between 1 p.m. and 2 p.m. on the x-axis is equidistant from the two points (d) showing 1 p.m. and 2 p.m., so it will represent 1.30 p.m. Similarly, the point on the y-axis, between 36° C and 37° C will represent 36.5° C.
- 9 a.m. to 10 a.m., 10 a.m. to 11 a.m., 2 p.m. to 3 p.m.

**2.** (a) (i) ₹ 4 crore

(ii) ₹8 crore

(i) ₹7 crore (b)

(ii) ₹ 8.5 crore (approx.)

₹4 crore

(d) 2005

(i) 7 cm **3.** (a)

(ii) 9 cm

(b) (i) 7 cm (ii) 10 cm

2 cm (d) 3 cm (c)

(e) Second week (f) First week

(g) At the end of the 2nd week

Tue, Fri, Sun **4.** (a)

(b) 35° C

(c) 15° C

(d) Thurs

4 units = 1 hour**6.** (a)

(b)  $3\frac{1}{2}$  hours

(c) 22 km

- (d) Yes; This is indicated by the horizontal part of the graph (10 a.m. - 10.30 a.m.)
- Between 8 a.m. and 9 a.m. (e)
- 7. (iii) is not possible

### **EXERCISE 5.2**

- 1. Points in (a) and (b) lie on a line; Points in (c) do not lie on a line
- 2. The line will cut x-axis at (5, 0) and y-axis at (0, 5)
- **3.** O(0, 0), A(2, 0), B(2, 3), C(0, 3), P(4, 3), Q(6, 1), R(6, 5), S(4, 7), K(10, 5), L(7, 7), M(10, 8)
- **4.** (i) True
- (ii) False
- (iii) True

### **EXERCISE 5.3**

(i) 20 km (ii) 7.30 a.m. 1. (b)

(c) (i) Yes (ii) ₹200 (iii) ₹3500

**2.** (a) Yes (b) No

# 6. FACTORISATION

# **EXERCISE 6.1**

1. (i) 12 (ii) 2*y* 

(iii) 14*pq* 

(iv) 1

(vi) 5xy(x-3y) (vii)  $5(2a^2-3b^2+4c^2)$ 

(v) 6ab (vi) 4x

(vii) 10 (viii)  $x^2y^2$ 

**2.** (i) 7(x-6)

(ii) 6(p-2q) (iii) 7a(a+2) (iv)  $4z(-4+5z^2)$ 

(v) 10 lm(2l+3a)(viii) 4a(-a+b-c)

(ix) xyz(x+y+z)

(x) xy(ax + by + cz)

3. (i) (x+8)(x+y)

(ii) (3x+1)(5y-2)

(iii) (a+b)(x-y)

(iv) (5p+3)(3q+5)

(v) (z-7)(1-xy)

EXERCISE 6.2

1. (i)  $(a+4)^2$ 

(ii)  $(p-5)^2$  (iii)  $(5m+3)^2$  (iv)  $(7y+6z)^2$ 

(v)  $4(x-1)^2$ 

(vi)  $(11b-4c)^2$  (vii)  $(l-m)^2$  (viii)  $(a^2+b^2)^2$ 

(v) 4(x-1) (vi) (11b-4c) (vii) (1-4c) (vii) (1-4c) (viii) (1-4c) (viii) (1-4c) (viii) (1-4c) (viiii) (1-4c) (viiiii) (1-4c) (viiiii) (1-4c) (viiii) (1-4c)

(iii) (7x-6)(7x+6)

(vi) (3xy-4)(3xy+4)

(vii) (x-y-z)(x-y+z) (viii) (5a-2b+7c)(5a+2b-7c)(ii)  $7(p^2 + 3q^2)$  (iii)  $2x(x^2 + y^2 + z^2)$ 

3. (i) x(ax + b)(iv)  $(m^2 + n^2)(a + b)$ 

(v) (l+1)(m+1)

(vi) (y+9)(y+z)

(vii) (5y+2z)(y-4)

(viii) (2a+1)(5b+2)

(ix) (3x-2)(2y-3)

**4.** (i)  $(a-b)(a+b)(a^2+b^2)$  (ii)  $(p-3)(p+3)(p^2+9)$ 

(iii)  $(x-y-z)(x+y+z)[x^2+(y+z)^2]$  (iv)  $z(2x-z)(2x^2-2xz+z^2)$ 

(v)  $(a-b)^2(a+b)^2$ 

5. (i) (p+2)(p+4)

(ii) (q-3)(q-7) (iii) (p+8)(p-2)

### **EXERCISE 6.3**

1. (i)  $\frac{x^3}{2}$  (ii) -4y (iii) 6pqr (iv)  $\frac{2}{3}x^2y$  (v)  $-2a^2b^4$ 2. (i)  $\frac{1}{3}(5x-6)$  (ii)  $3y^4-4y^2+5$  (iii) 2(x+y+z)

(iv)  $\frac{1}{2}(x^2 + 2x + 3)$  (v)  $q^3 - p^3$ 

**3.** (i) 2x - 5 (ii) 5 (iii) 6y (iv) xy (v) 10abc

**4.** (i) 5(3x+5)

(ii) 2y(x+5) (iii)  $\frac{1}{2}r(p+q)$  (iv)  $4(y^2+5y+3)$ 

(v) (x+2)(x+3)

**5.** (i) y+2 (ii) m-16 (iii) 5(p-4) (iv) 2z(z-2) (v)  $\frac{5}{2}q(p-q)$  (vi) 3(3x-4y) (vii) 3y(5y-7)

### EXERCISE 6.4

1. 
$$4(x-5) = 4x-20$$

**2.** 
$$x(3x + 2) = 3x^2 + 2x$$
 **3.**  $2x + 3y = 2x + 3y$ 

$$3. \ 2x + 3y = 2x + 3y$$

**4.** 
$$x + 2x + 3x = 6x$$

$$3. \ 3y + 2y + y - 1y = y$$

**6.** 
$$3x + 2x = 5x$$

**4.** 
$$x + 2x + 3x = 6x$$
 **5.**  $5y + 2y + y - 7y = y$  **6.**  $3x + 2x = 5x$  **7.**  $(2x)^2 + 4(2x) + 7 = 4x^2 + 8x + 7$  **8.**  $(2x)^2 + 5x = 4x^2 + 5x$  **9.**  $(3x + 2)^2 = 9x^2 + 12x + 4$ 

$$3. (2x)^2 + 5x = 4x^2 + 5x$$

9. 
$$(3x + 2)^2 = 9x^2 + 12x + 4$$

**10.** (a) 
$$(-3)^2 + 5(-3) + 4 = 9 - 15 + 4 = -2$$
 (b)  $(-3)^2 - 5(-3) + 4 = 9 + 15 + 4 = 28$ 

(b) 
$$(-3)^2 - 5(-3) + 4 = 9 + 15 + 4 = 28$$

(c) 
$$(-3)^2 + 5(-3) = 9 - 15 = -6$$

11. 
$$(y-3)^2 = y^2 - 6y + 9$$

$$b - 3b^2$$

**12.** 
$$(z+5)^2 = z^2 + 10z + 25$$

13. 
$$(2a+3b)(a-b) = 2a^2 + ab - 3b$$

**14.** 
$$(a+4)(a+2) = a^2 + 6a + 8$$

**15.** 
$$(a-4)(a-2) = a^2 - 6a + 8$$

$$3x^2$$
**10**  $\frac{3}{3} = \frac{3}{3}$ 

13. 
$$(2a+3b)(a-b) = 2a^2 + ab - 3b^2$$

14.  $(a+4)(a+2) = a^2 + 6a + 8$ 

15.  $(a-4)(a-2) = a^2 - 6a + 8$ 

16.  $\frac{3x^2}{3x^2} = 1$ 

17.  $\frac{3x^2 + 1}{3x^2} = \frac{3x^2}{3x^2} + \frac{1}{3x^2} = 1 + \frac{1}{3x^2}$ 

18.  $\frac{3x}{3x+2} = \frac{3x}{3x+2}$ 

19.  $\frac{3}{4x+3} = \frac{3}{4x+3}$ 

20.  $\frac{4x+5}{4x} = \frac{4x}{4x} + \frac{5}{4x} = 1 + \frac{5}{4x}$ 

$$18. \quad \frac{3x}{3x+2} = \frac{3x}{3x+2}$$

$$19. \ \frac{3}{4x+3} = \frac{3}{4x+3}$$

**20.** 
$$\frac{4x+5}{4x} = \frac{4x}{4x} + \frac{5}{4x} = 1 + \frac{5}{4x}$$

**21.** 
$$\frac{7x+5}{5} = \frac{7x}{5} + \frac{5}{5} = \frac{7x}{5} + 1$$

# 7. VISUALISING SOLID SHAPES

### EXERCISE 7.1

1. (a) 
$$\rightarrow$$
 (iii)  $\rightarrow$  (iv)

$$(b) \rightarrow (i) \rightarrow (v)$$

$$(c) \rightarrow (iv) \rightarrow (ii)$$

$$(d) \rightarrow (v) \rightarrow (iii)$$

$$(e) \rightarrow (ii) \rightarrow (i)$$

2. (a) (i) 
$$\rightarrow$$
 Front, (ii)  $\rightarrow$  Side, (iii)  $\rightarrow$  Top

(b) (i) 
$$\rightarrow$$
 Side, (ii)  $\rightarrow$  Front, (iii)  $\rightarrow$  Top  
(d) (i)  $\rightarrow$  Front, (ii)  $\rightarrow$  Side, (iii)  $\rightarrow$  Top

(c) (i) 
$$\rightarrow$$
 Front, (ii)  $\rightarrow$  Side, (iii)  $\rightarrow$  Top  
3. (a) (i)  $\rightarrow$  Top, (ii)  $\rightarrow$  Front, (iii)  $\rightarrow$  Side

(a) (i) 
$$\rightarrow$$
 From, (ii)  $\rightarrow$  Side, (iii)  $\rightarrow$  Top

(b) (i) 
$$\rightarrow$$
 Side, (ii)  $\rightarrow$  Front, (iii)  $\rightarrow$  Top  
(d) (i)  $\rightarrow$  Side, (ii)  $\rightarrow$  Front, (iii)  $\rightarrow$  Top

(c) (i) 
$$\rightarrow$$
 Top, (ii)  $\rightarrow$  Side, (iii)  $\rightarrow$  Front

(e) (i) 
$$\rightarrow$$
 Front, (ii)  $\rightarrow$  Top, (iii)  $\rightarrow$  Side

#### EXERCISE 7.3

- 1. (i) No (ii) Yes (iii) Yes
- 2. Possible, only if the number of faces are greater than or equal to 4
- 3. only (ii) and (iv)
- 4. (i) A prism becomes a cylinder as the number of sides of its base becomes larger and larger.
  - (ii) A pyramid becomes a cone as the number of sides of its base becomes larger and larger.
- 5. No. It can be a cuboid also
- 7. Faces  $\rightarrow$  8, Vertices  $\rightarrow$  6, Edges  $\rightarrow$  30

# 8. COMPARING QUANTITIES

#### EXERCISE 8.1

- **1.** (a) 1:2 (b) 1:2000
- (c) 1:10
- **2.** (a) 75% (b)  $66\frac{2}{3}$ %
- **3.** 28% students **4.** 25 matches **5.** ₹ 2400
- **6.** 10%, cricket  $\rightarrow$  30 lakh; football  $\rightarrow$  15 lakh; other games  $\rightarrow$  5 lakh

### **EXERCISE 8.2**

1	<b>Ŧ</b>	1	1	Λ	Λ	Λ	r
1.	<	1,	,4	υ,	v	υ	U

2. 80%

**3.** ₹ 34.80

4. ₹18,342.50

**6.** ₹ 2,835

7. Loss of ₹ 1,269.84

### **8.** ₹ 14,560

**9.** ₹ 2,000

### **10.** ₹ 5,000

**11.** ₹ 1,050

## **EXERCISE 8.3**

(b) Amount = ₹ 22,869; Interest = ₹ 4869

(c) Amount = ₹ 70,304, Interest = ₹ 7,804

(d) Amount = ₹8,736.20, Interest = ₹736.20 (e) Amount = ₹10,816, Interest = ₹816

**2.** ₹ 36,659.70

**3.** Fabina pays ₹ 362.50 more

**5.** (ii) ₹63,600 (ii) ₹67,416

**6.** (ii) ₹92,400 (ii) ₹92,610

7. (i) ₹8,820

(ii) ₹ 441

8. Amount = ₹ 11,576.25, Interest = ₹ 1,576.25 Yes.

**9.** ₹ 4,913

**10.** (i) About 48,980 (ii) 59,535

**11.** 5,31,616 (approx)

**12.** ₹ 38,640

# 9. MENSURATION

### EXERCISE 9.1

1. (a)

**2**. ₹ 17,875

3. Area =  $129.5 \text{ m}^2$ ; Perimeter = 48 m

**4.** 45000 tiles

**5.** (b)

### **EXERCISE 9.2**

1.  $0.88 \,\mathrm{m}^2$ 

2. 7 cm

3.  $660 \,\mathrm{m}^2$ 

4.  $252 \text{ m}^2$ 

5.  $45 \text{ cm}^2$ 

**6.**  $24 \text{ cm}^2$ , 6 cm

**7.** ₹810

**8.** 140 m

**9.** 119 m<sup>2</sup>

10. Area using Jyoti's way =  $2 \times \frac{1}{2} \times \frac{15}{2} \times (30 + 15) \text{ m}^2 = 337.5 \text{ m}^2$ ,

Area using Kavita's way =  $\frac{1}{2} \times 15 \times 15 + 15 \times 15 = 337.5 \text{ m}^2$ 

11.  $80 \text{ cm}^2$ ,  $96 \text{ cm}^2$ ,  $80 \text{ cm}^2$ ,  $96 \text{ cm}^2$ 

## **EXERCISE 9.3**

**2.** 144 m

**3.** 10 cm

**4.** 11 m<sup>2</sup>

Similarity  $\rightarrow$  Both have same heights. Difference  $\rightarrow$  one is a cylinder, the other is a cube. The cube has larger lateral surface area

7.  $440 \,\mathrm{m}^2$ 

**8.** 322 cm

9.  $1980 \text{ m}^2$ 

**10.** 704 cm<sup>2</sup>

### EXERCISE 9.4

1. (a) Volume

(b) Surface area

(c) Volume

2. Volume of cylinder B is greater; Surface area of cylinder B is greater.

4. 450

**5.** 1 m

**6.** 49500 L

7. (i) 4 times (ii) 8 times

**8.** 30 hours

### JUST FOR FUN

### 1. More about Pythagorean triplets

We have seen one way of writing pythagorean triplets as 2m,  $m^2 - 1$ ,  $m^2 + 1$ .

A pythagorean triplet a, b, c means  $a^2 + b^2 = c^2$ . If we use two natural numbers m and n(m > n), and take  $a = m^2 - n^2$ , b = 2mn,  $c = m^2 + n^2$ , then we can see that  $c^2 = a^2 + b^2$ .

Thus for different values of m and n with m > n we can generate natural numbers a, b, c such that they form Pythagorean triplets.

For example: Take, m = 2, n = 1.

Then,  $a = m^2 - n^2 = 3$ , b = 2mn = 4,  $c = m^2 + n^2 = 5$ , is a Pythagorean triplet. (Check it!)

For, m = 3, n = 2, we get,

a = 5, b = 12, c = 13 which is again a Pythagorean triplet.

Take some more values for *m* and *n* and generate more such triplets.

- 2. When water freezes its volume increases by 4%. What volume of water is required to make 221 cm<sup>3</sup> of ice?
- **3.** If price of tea increased by 20%, by what per cent must the consumption be reduced to keep the expense the same?
- **4.** Ceremony Awards began in 1958. There were 28 categories to win an award. In 1993, there were 81 categories.
  - (i) The awards given in 1958 is what per cent of the awards given in 1993?
  - (ii) The awards given in 1993 is what per cent of the awards given in 1958?
- **5.** Out of a swarm of bees, one fifth settled on a blossom of *Kadamba*, one third on a flower of *Silindhiri*, and three times the difference between these two numbers flew to the bloom of *Kutaja*. Only ten bees were then left from the swarm. What was the number of bees in the swarm? (Note, *Kadamba*, *Silindhiri* and *Kutaja* are flowering trees. The problem is from the ancient Indian text on algebra.)
- **6.** In computing the area of a square, Shekhar used the formula for area of a square, while his friend Maroof used the formula for the perimeter of a square. Interestingly their answers were numerically same. Tell me the number of units of the side of the square they worked on.
- 7. The area of a square is numerically less than six times its side. List some squares in which this happens.
- **8.** Is it possible to have a right circular cylinder to have volume numerically equal to its curved surface area? If yes state when.
- 9. Leela invited some friends for tea on her birthday. Her mother placed some plates and some *puris* on a table to be served. If Leela places 4 *puris* in each plate 1 plate would be left empty. But if she places 3 *puris* in each plate 1 *puri* would be left. Find the number of plates and number of *puris* on the table.
- 10. Is there a number which is equal to its cube but not equal to its square? If yes find it.
- 11. Arrange the numbers from 1 to 20 in a row such that the sum of any two adjacent numbers is a perfect square.

#### Answers

- 2.  $212\frac{1}{2}$  cm<sup>3</sup>
- 3.  $16\frac{2}{3}\%$
- **4.** (i) 34.5% (ii) 289%

- **5.** 150
- **6.** 4 units
- 7. Sides = 1, 2, 3, 4, 5 units

8. Yes, when radius = 2 units

- 9. Number of puris = 16, number of plates = 5
- **10.** -1 **11.** One of the ways is, 1, 3, 6, 19, 17, 8 (1 + 3 = 4, 3 + 6 = 9 etc.). Try some other ways.





