Talent & Olympiad

Mathematics

Lines and Angles

			6.	How many rays can be drawn from a given point?		
Mult	iple Choice Question			(a) 2	(b) 5	
1.	Which of the following	are the units of an angle?		(c) 8	(d) Infinitely many	
	(a) Seconds	(b) Kilograms				
	(c) Degrees	(d) Kilometres	7.	What do we call a 169	° angle?	
				(a) An obtuse angle	(b) An acute angle	
2.	What do we call an angle which exactly measures			(c) A right angle	(d) A zero angle	
	90°?					
	(a) An obtuse angle	(b) An acute angle	8.	What happens to the	measurment of an angle	
	(c) A right angle	(d) A reflex angle		after the extension of its arms?		
				(a) Doubles	(b) Triples	
3.	What do we call an angle whose measurement is			(c) Remains the same	(d) Cannot be said	
	exactly equal to 0° ?					
	(a) An obtuse angle	(b) A straight angle	9.	In $\angle ROP$, what is the	vertex?	
	(c) A zero angle	(d) A right angle		R]	
4.	What is an angle whi	ch measures exactly 180°		() P		
	called?			(a) R	(b) P	
	(a) A zero angle	(b) A right angle		(c) O	(d) PR	
	(c) A straight angle	(d) An acute angle				
			10.	What are the two arms	ot ZDEF?	

- 5. Which instrument is used to measure or construct angles?
 - (a) Compasses (b) Scale
 - (c) Protractor (d) Set squares

- (a) \overrightarrow{ED} and \overrightarrow{EF} (b) \overrightarrow{DE} and \overrightarrow{EF}
- (c) \overrightarrow{FE} and \overrightarrow{FD} (d) \overrightarrow{DE} and \overrightarrow{FD}

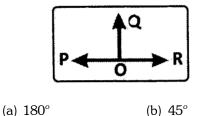
- 11. When two line segments meet at a point forming right angles, what type of segments are they called?
 - (a) Parallel segments
 - (b) Perpendicular segments
 - (c) Equal segments

(a) $\overrightarrow{AB} \perp \overrightarrow{CD}$

- (d) Bisecting segments
- **12.** How is " \overrightarrow{AB} is perpendicular to \overrightarrow{CD} " written symbolically?

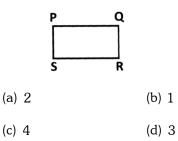
(b) $\overrightarrow{AB} \parallel \overrightarrow{CD}$

- (c) $\overrightarrow{AB} \neq \overrightarrow{CD}$ (d) $\overrightarrow{AB} = \overrightarrow{CD}$
- **13.** $\overrightarrow{OQ} \perp \overrightarrow{PR}$ What is the measure of $\angle QOR$?



- (c) 90° (d) 120°
- **14.** A line AB is parallel to the line CD. How is this symbolically written?
 - (a) $\overrightarrow{AB} \neq \overrightarrow{CD}$ (b) $\overrightarrow{AB} = \overrightarrow{CD}$
 - (c) $\overrightarrow{AB} \perp \overrightarrow{CD}$ (d) $\overrightarrow{AB} / / \overrightarrow{CD}$
- **15.** What are the lines which lie on the same plane and do not intersect at any point called?

- (a) Perpendicular lines (b) Intersecting lines
- (c) Parallel lines (d) Collinear lines
- 16. When two lines are parallel, what is the distance between them?
 - (a) Remains equal.
 - (b) Does not remain equal.
 - (c) Increases on the right.
 - (d) Decreases on the right.
- 17. What is the number of pairs of parallel lines in the given figure?



- **18.** What is the complementary angle of 20° ?
 - (a) 70°
 (b) 180°
 (c) 90°
 (d) 150°

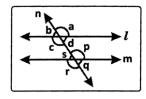
19. What is the supplementary angle of 120° ?

- (a) 20°
 (b) 90°
 (c) 60°
 (d) 180°
- **20.** What is the measure of a comple-mentary angle of an angle greater than 45° ?

	(a) Less than 45°	(b) Equal to 45°		(b) Alternate angles	
	(c) Greater than 45°	(d) Equal to 90°		(c) Vertically opposite	angles
				(d) Interior angle o	n the same side of the
21.	Which of the following	is true?		transversal	
	(a) Two acute angles a	re supplementary.			
	(b) Two obtuse angles	are supplementary.	25.	What type of angles a	re 'c' and 'p'?
	(c) Two right angles are		(a) Corresponding and	gles	
	(d) Two reflex angles are supplementary.			(b) Alternate angles	
				(c) Vertically opposite	angles
22.	Find the angle which is a complement of itself.			(d) Interior angles o	on the same side of the
	(a) 30°	(b) 45°		transversal	
	(c) 90°	(d) 180°			
			26.	Which of the following	g is a pair of corresponding
23.	Which of the following angles is a supplement of itself?			angles?	
				(a) d and c	(b) s and r
	(a) 90°	(b) 180°		(c) c and r	(d) p and q
	(c) 45°	(d) 110°			
			27.	Which of the follow	ng is a pair of vertically
	(24 - 30): Observe the given figure in which $l \parallel m$			opposite angles?	
				(a) a and b	(b) a and p

that follow.

24. What type of angles are 'a' and 'p'?



and n is the transversal and answer the questions

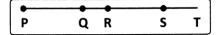
(a) Corresponding angles

28. If the measure of 'c' is $110^\circ\,$ what is the measure of 's'? (a) 45° (b) 110° (c) 70° (d) 180°

(d) p and r

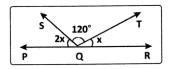
(c) s and r

- **29.** If the measure of $b = 70^{\circ}$, what is the measure of s?
 - (a) 110° (b) 70°
 - (c) 90° (d) 180°
- **30.** If $b = 70^\circ$, what is the measure of b + p?
 - (a) 180°
 (b) 110°
 (c) 90°
 (d) 70°
- 31. The angle between the two blades of a scissors is 194°. What type of an angle is it?(a) straight angle(b) reflex angle
 - (c) obtuse angle (d) complete angle
- **32.** Observe the figure given,



Which of the following is true if PQ = RS?

- (a) PQ + QR = RS (b) PR = QS
- (c) PQ + QS = RS (d) PQ RS = QR
- **33.** PQR is a straight line.

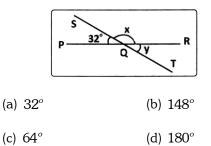


What is the value of x?

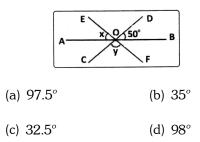
(a) 20°	(b)	25°
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(c) 15° (d) 30°

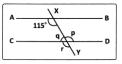
34. In the given figure, what is the measure of x?



35. In the figure, \overline{AB} , \overline{CD} and \overline{EF} are three straight lines that interesect at O. If y is thrice x, find the value of y.



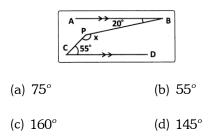
36. In the figure, $AB \parallel CD$ and XY is the transversal.



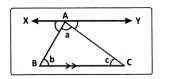
Which of the following is incorrect?

(a)
$$p = 115^{\circ}$$
 (b) $q = 115^{\circ}$
(c) $q = 65^{\circ}$ (d) $r = 115^{\circ}$

37. Find the angle x in the given figure, if AB || CD

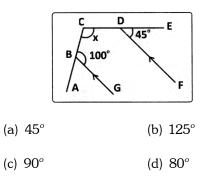


38. Through the vertex A of $\triangle ABC$, a line XY is drawn parallel to BC.

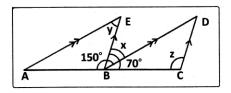


Which of the following is correct?

- (a) b = y
- (b) *c* = *x*
- (c) a = b
- (d) a + b + c = x + a + y
- **39.** Find the unknown angle x in the figure.



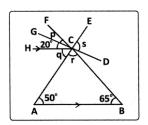
40. Observe the figure given.



Compute the sum of x, y and z.

- (a) 180° (b) 70°
- (c) 190° (d) 80°

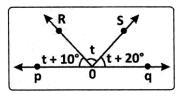
- **41.** If the angles $(2a-10)^{\circ}$ and $(a-11)^{\circ}$ are complementary, what is the value of 'a'?
 - (a) 37° (b) 27°
 - (c) 17° (d) 7°
- **42.** If \overrightarrow{OP} is a ray standing on a line \overrightarrow{OR} such that $\angle POQ = \angle POR$, what is the measure $\angle POQ$?
 - (a) 45° (b) 60°
 - (c) 75° (d) 90°
- **43.** In the figure, ACE, BCF and DCG are straight lines and *AB* || HC.



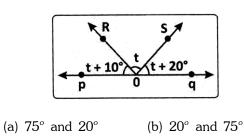
Find the angles p, q, r and s.

	р	q	r	S
(A)	45°	50°	65°	50°
(B)	45°	65°	50°	50°
(C)	45°	65°	50°	65°
(D)	45°	50°	65°	65°

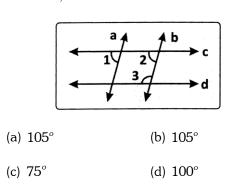
44. In the figure given, what is the value of $\angle t$?



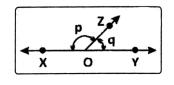
- (a) 30° (b) 40°
- (c) 50° (d) 60°
- **45.** In the figure given, if *AB* || CD, what are the respective values of 'p' and 'q'?



- (c) 25° and 70° (d) 70° and 25°
- **46.** In the figure given, a || b and c || d. If $\angle 1 = 75^\circ$, what is the measure of $\angle 3$?

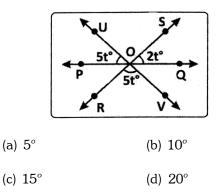


47. In the figure given, $\angle XOZ$ and $\angle YOZ$ form a linear pair. If $p - q = 80^{\circ}$ what are the respective values of p and q?

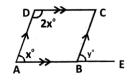


(a) 50° and 130°
(b) 130° and 50°
(c) 120° and 60°
(d) 60° and 120°

48. In the figure given, what is the value of 't'?



49. Given ABE is a straight line.

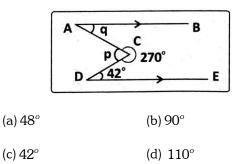


Find angle y.

(a)	60°	(b)	120°
(~,	~ ~	(*)	

(c) 150° (d) 30°

50. In the given figure, what is the measure of q?



Solution

- (C) A common unit of measurement of angles is degrees.
- (C) An angle which exactly measures 90° is called a right angle.

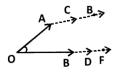


3. (C) Not available

- **4.** (C) Not available
- **5.** (C) Not available
- (D) An infinite number of rays can be drawn from a point.



- (A) An angle which lies between 90° and 180° is called as an obtuse angle. So, 169° is an obtuse angle.
- (C) Extending the arms of an angle does not affect the angle between them.



- **9.** (C) The vertex of an angle is the common point of the rays that form the arms of an angle. Here, it is 0.
- **10.** (A) \overleftarrow{ED} and \overleftarrow{EF} are the two arms of $\angle DEF$.

- (B) Perpendicular segments meet at a point forming right angles.
- **12.** (A) Not available
- **13.** (C) Not available
- 14. (D) Not available
- **15.** (C) Not available
- **16.** (A) The distance between the parallel lines is the

same.
$$\overleftarrow{m}^{l}$$

- 17. (A) There are two pairs of parallel lines as the opposite sides of a rectangle are parallel.
- **18.** (A) Complementary angles add up to $90^{\circ} \cdot \angle PQR = 20^{\circ} \Rightarrow$ Its complementary angle is $90^{\circ} - 20^{\circ} = 70^{\circ}$
- **19.** (C) The sum of supplementary angles is 180° . $\angle ABC = 120^{\circ} \Rightarrow$ Its supplementary angles add up to 180° .
- **20.** (A) Not available
- **21.** (C) Not available
- **22.** (B) Not available
- **23.** (A) Not available
- 24. (A) 1 || m, n is the transversal, 'a' is an exterior angle and 'p' is an interior angle both on the same side of n.

So, 'a' and 'p' are corresponding angles.

25. (B) l || m, n is the transversal, 'c' and 'p' are both interior angles, but on different sides of n. So, 'c' and 'p' are alternate angles.

- 26. (C) c and r are corresponding angles as 'c' interior and 'r' is exterior angle both on the same side of 'n'.
- 27. (D) p and r are vertically opposite angles formed at the intersection of n and m.
- **28.** (C) c and s are interior angles on the same side of transversal, which are supplementary. So, if $c = 110^{\circ}$, 's' measures $180^{\circ} 110^{\circ} = 70^{\circ}$.
- **29.** (B) Not available
- **30.** (A) Not available
- **31.** (B) Not available
- **32.** (B) Not available
- **33.** (A) Not available
- **34.** (B) PR is a straight line and so, $x = 180^{\circ} - 32^{\circ} = 148^{\circ}$.
- **35.** (A) From the figure,
 - $\angle AOC = 50^{\circ}$

(Vertically opposite angles)

Given y is thrice x, we have

 $x + 50^{\circ} + y = 180^{\circ}$

(Angle on a straight line)

 $\Rightarrow x + 50^\circ + 3x = 180^\circ$

$$\Rightarrow x = \frac{130^{\circ}}{4} = 32.5^{\circ}$$

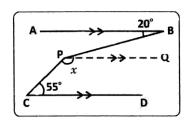
$$\therefore$$
 $y = 3x = 3(32.5) = 97.5^{\circ}$

36. (B) 115° and q are interior angles on the same side of the transversal.

So, $115^{\circ} + q = 180^{\circ}$

$$\Rightarrow q = 180^\circ - 115^\circ = 65^\circ$$

37. (D) Draw $PQ \parallel AB$ and CD.



	From the figure,
	$x = 20^{\circ} + (180^{\circ} - 55^{\circ})$
	<i>PQ</i> AB CD.
	$\Rightarrow x = 20^{\circ} + 125^{\circ} = 145^{\circ}$
38.	(D) $a+b+c = 180^{\circ}$
	(Sum of angles in a triangle)
	Also, $x + a + y = 180^{\circ}$
	(Angle on a straight line)
	$\therefore a+b+c = x+a+y$
39.	(B) <i>DF</i> CH BG
	$\Rightarrow a+b=x \text{ and } a=45^{\circ}$
	(Corresponding angles)
	$b = 180^{\circ} - 100^{\circ} = 80^{\circ}$
	(Angles on the same side of transversal.)
	$\Rightarrow x = a + b = 45^{\circ} + 80^{\circ} = 125^{\circ}$
40 .	(C) From the figure,
	$150 - x + 70 - x + x = 180^{\circ}$
	$\Rightarrow x = 220^{\circ} - 180^{\circ} = 40^{\circ}$
	Since $AE \mid \mid BD$, $AE \mid \mid BD$, $y = x$ as they are
	alternate angles.
	In $\triangle BCD$, $\angle BDC = x$ (Alternate angles)

$$70 - x + x + z = 180^{\circ} \implies z = 110^{\circ}$$

∴ The required sum

 $= x + y + z = 40^{\circ} + 40^{\circ} + 110^{\circ} = 190^{\circ}$

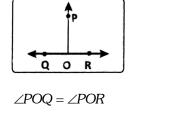
41. (A) Given, the angles $(2a-10)^{\circ}$ and $(a-11)^{\circ}$ are complementary angles.

 $\therefore (2a-10)^{\circ} + (a-11)^{\circ} = 90^{\circ}$

 $\therefore a = 37^{\circ}$

42. (D) Given OP is a ray on line QR.

Also $\angle POQ = \angle POR$.



$$\angle POQ + \angle POR = 180^{\circ}$$
(ii)

.....(i)

From (1) and (2), we have

 $2\angle POQ = 180^{\circ}$

$$\Rightarrow \angle POQ = \frac{180^{\circ}}{2} = 90^{\circ}$$

43. (A) In $\triangle ABC$, $r = 180^{\circ} - 50^{\circ} - 65^{\circ} = 65^{\circ}$

 $HC \parallel AB \Rightarrow q = 50^{\circ}$. (Alternate angles)

s = q (Vertically opposite angles) Hence,

Since BCF is a straight line,

$$p + 20^{\circ} + q + r = 180^{\circ} \implies p = 45^{\circ}$$
$$\therefore \quad p = 45^{\circ}, q = 50^{\circ}, r = 65^{\circ}$$

and $s = 50^{\circ}$ are the required values.

R t + 10° t + 20° q

In the given figure,

$$t + 10^\circ + t + t + 20^\circ = 180^\circ$$

 $\Rightarrow t = 50^{\circ}$

45. (D) The lines AB and EF intersect at G.

 $\therefore \angle EGB = \angle AGF$

(Vertically opposite angles)

$$\Rightarrow \angle AGF = 65^{\circ}$$

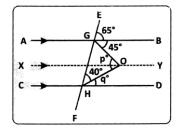
Since $AB \parallel CD$,

$$\angle GHD = \angle AGH = \angle AGF$$

$$\Rightarrow \angle GHD = 65^{\circ}$$

$$\Rightarrow \angle GHO + \angle OHD = 65^{\circ}$$

$$\Rightarrow q^\circ = 65^\circ - 40^\circ = 25^\circ$$



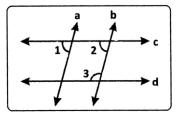
Draw a line XY through 'O' parallel to AB and CD.

Since XY || AB, $\angle XOG = \angle BGO$ $\Rightarrow \angle XOG = 45^{\circ}$ (Alternate angles) and XY || CD $\Rightarrow \angle XOH = \angle OHD$ $\Rightarrow \angle XOH = 25^{\circ}$ But $p = 45^{\circ} + 25^{\circ} = 70^{\circ}$

44.

- :. $p = 70^{\circ} \& q = 25^{\circ}$
- **46.** (A) Given $a \parallel b$ and $c \parallel d$ and $\angle 1 = 75^{\circ}$

Since $a \parallel b$, $\angle 1 = \angle 2$



Also $c \mid\mid d, \Rightarrow \angle 2 + \angle 3 = 180^{\circ}$

$$\therefore \quad \angle 3 = 105^{\circ}$$

- **47.** (B) Not available
- **48.** (C) Not available
- **49.** (A) Given $AD \parallel BC \Rightarrow x = y$

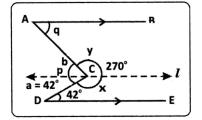
(Corresponding angles)

Also $AB \parallel CD \Longrightarrow x + 2x = 180^{\circ}$

- \Rightarrow $x = 60^{\circ}$ and $y = 60^{\circ}$
- **50.** Clearly $p = 360^{\circ} 270^{\circ} = 90^{\circ}$

(Angles at a point)

Through C, draw a line Z parallel to AB and DE.



: $42^{\circ} + x = 180^{\circ}$ and $q + y = 180^{\circ}$

$$\Rightarrow x = 180^\circ - 42^\circ = 138^\circ$$

- \therefore $y = 270^{\circ} 138^{\circ} = 132^{\circ}$
- : $q = 180^{\circ} 132^{\circ} = 48^{\circ}$