# **Chapter : 10. QUADRATIC EQUATIONS**

# **Exercise : 10A**

# **Question: 1** A

Which of the foll

### Solution:

The given equation  $x^2 - x + 3 = 0$  is a quadratic equation.

Explanation - It is of degree 2, it is in the form  $ax^2 + bx + c = 0$  (a  $\neq$  0, a, b, c are real numbers)

where a = 1, b = -1, c = 3.

### **Question: 1 B**

Which of the foll

# Solution:

The given equation  $2x^2 + \frac{5}{2}x - \sqrt{3} = 0$  equation is a quadratic equation.

Explanation - It is of degree 2, it is in the form  $ax^2 + bx + c = 0$  (a  $\neq$  0, a, b, c are real numbers)

where a = 2, b =  $\frac{5}{2}$ , c =  $-\sqrt{3}$ 

# **Question: 1 C**

Which of the foll

#### Solution:

The given equation  $\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$  is a quadratic equation.

Explanation - It is of degree 2, it is in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers) where a =  $\sqrt{2}$ , b = 7, c =  $5\sqrt{2}$ .

# Question: 1 D

Which of the foll

# Solution:

The given equation  $\frac{1}{3}x^2 + \frac{1}{5}x - 2 = 0$  is a quadratic equation.

Explanation - It is of degree 2, it is in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers)

where a = 1/3, b = 1/5, c = -2.

#### Question: 1 E

Which of the foll

# Solution:

The given equation  $x^2 - 3x - \sqrt{x} + 4 = 0$  is not a quadratic equation.

Explanation - It is not in the form of  $ax^2$  + bx + c = 0 because it has an extra term -  $\sqrt{x}$  with power 1/2

#### **Question: 1 F**

Which of the foll

# Solution:

The given equation  $x - \frac{6}{x} = 3$  is a quadratic equation.

Explanation - Given  $x - \frac{6}{x} = 3$ 

On solving the equation it gets reduced to  $x^2 - 6 = 3x$ ;  $x^2 - 3x - 6 = 0$ ; It is of degree 2 and it is in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers) where a = 1, b = -3, c = -6.

# **Question: 1 G**

Which of the foll

# Solution:

The given equation  $x + \frac{2}{x} = x^2$  is not a quadratic equation.

Explanation - Given  $x + \frac{2}{x} = x^2$ 

On getting reduced it becomes  $x^2 + 2 = x^3$ , it has degree = 3, it is not in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers).

# **Question:** 1 H

Which of the foll

# Solution:

The given equation  $x^2 - \frac{1}{x^2} = 5$  is not a quadratic equation.

Explanation - Given  $x^2 - \frac{1}{x^2} = 5$ 

On getting reduced it becomes  $x^4 - 1 = 5x^2$ ;  $x^4 - 5x^2 - 1 = 0$ 

It is not in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers)

# Question: 1 I

Which of the foll

# Solution:

The given equation  $(x + 2)^3 = x^3 - 8$  is a quadratic equation.

Explanation Given  $(x + 2)^3 = x^3 - 8$ 

On getting reduced it becomes  $x^3 + 8 + 6x^2 + 12x = x^3 - 8$ 

 $= 6x^2 + 12x + 16 = 0$ 

Now, using  $(a + b)^3 = a^3 + b^3 + 3a^2b + 3ab^2$ 

where a = 6, b = 12, c = 16

It is in the form  $ax^2 + bx + c = 0$  (a  $\neq$  0, a, b, c are real numbers)

# Question: 1 J

Which of the foll

# Solution:

The given (2x + 3)(3x + 2) = 6(x - 1)(x - 2)equation is not a quadratic equation.

Explanation - Given (2x + 3)(3x + 2) = 6(x - 1)(x - 2)

On getting reduced it becomes  $6x^2 + 4x + 9x + 6 = 6(x^2 - 2x - x + 2)$ 

 $6x^2 + 13x + 6 = 6x^2 - 18x + 12$ 

31x-6 = 0

It is not in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers)

### **Question: 1 K**

Which of the foll

### Solution:

The given equation  $\left(x + \frac{1}{x}\right)^2 = 2\left(x + \frac{1}{x}\right) + 3$  is not a quadratic equation. Explanation - Given  $\left(x + \frac{1}{x}\right)^2 = 2\left(x + \frac{1}{x}\right) + 3$ On getting reduced it becomes  $-\left(\frac{x^2+1}{x}\right)^2 = 2\left(\frac{x^2+1}{x}\right)^2 + 3$   $(x^2 + 1)^2 = 2x(x^2 + 1) + 3x^2$   $x^4 + 2x^2 + 1 = 2x^3 + 2x + 3x^2$   $x^4 - 2x^3 - x^2 - 2x + 1 = 0$ It is not in the form  $ax^2 + bx + c = 0$  (a  $\neq 0$ , a, b, c are real numbers)

### **Question: 2**

Which of the foll

#### Solution:

(i) - 1 is the root of given equation.

Explanation - Substituting value - 1 in LHS

$$= 3(-1)^2 + 2(-1) - 1$$

$$= 3 - 3 = 0 = RHS$$

Value satisfies the equation or LHS = RHS.

(ii)  $\frac{1}{2}$  is the root of the given euation  $3x^2 + 2x - 1 = 0$ 

Explanation - Substituting value in LHS

$$= 3\left(\frac{1}{3}\right)^{2} + 2\left(\frac{1}{3}\right) - 1$$
$$= \frac{1}{3} + \frac{2}{3} - 1$$

= 1 - 1 = 0 = RHS

Value satisfies the equation or LHS = RHS.

(iii)  $\frac{-1}{2}$  is not the root of given equation  $3x^2 + 2x - 1 = 0$ 

Explanation - Substituting value in LHS

$$= 3\left(\frac{-1}{2}\right)^2 + 2\left(\frac{-1}{2}\right) - 1 = 0$$
$$= \frac{3}{4} - 2$$
$$= \frac{-5}{4} \neq 0 \neq \text{RHS}$$

Value does not satisfy the equation or LHS  $\neq$  RHS.

### **Question: 3**

Find the value of

### Solution:

Given x = 1 is a root of the equation  $x^2 + kx + 3 = 0$  it means it satisfies the equation.

Substituting x = 1 in equation -

 $1^2 + k(1) + 3 = 0$ 

4 + k = 0

k = -4

Putting the value of k in the given equation :  $x^2 + kx + 3 = 0$ 

This reduced to the quadratic equation  $x^2 - 4x + 3 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1 b = -4 c = 3= 1.3 = 3 And either of their sum or difference = b = - 4 Thus the two terms are - 1 and - 3 Sum = - 1 - 3 = - 4 Product = -1. - 3 = 3 $x^2 - 4x + 3 = 0$  $x^2 - x - 3x + 3 = 0$ x(x-1)-3(x-1) = 0(x-1)(x-3) = 0x = 1 or x = 3Thus other root is 3. **Question: 4** Find the values o Solution: Given x = 3/4 or x = -2 are the roots of the equation  $ax^2 + bx - 6 = 0$ Putting  $x = \frac{3}{4}$  in the equation gives -

$$a\left(\frac{3}{4}\right)^{2} + b\left(\frac{3}{4}\right) - 6 = 0$$
  

$$\frac{9a + 12b - 96}{16} = 0;$$
  

$$9a + 12b - 96 = 0$$
  

$$3a + 4b - 32 = 0 - \dots (1)$$
  
putting x = - 2 in equation gives  

$$a(-2)^{2} + b(-2) - 6 = 0$$
  

$$4a - 2b - 6 = 0$$

2a-b-3 = 0  $2a-3 = b - \dots (2)$ Substituting (2) in (1) 3a + 4(2a-3)-32 = 0  $\Rightarrow 11a-44 = 0$   $\Rightarrow a = 4$   $\Rightarrow b = 2(4)-3 = 5$ Thus for a - 4 when  $5 = -\frac{3}{2}$  and 2 we there should also a fill be reaction 2 when 5

Thus for a = 4 or b = 5; x =  $\frac{3}{4}$  or x = -2 are the roots of the equation  $ax^2 + bx - 6 = 0$ 

# **Question: 5**

Solve each of the

# Solution:

(2x-3)(3x+1) = 0

 $6x^2 + 2x - 9x - 3 = 0$ 

2x(3x + 1)-3(3x + 1) = 0 taking common from first two terms and last two terms

(2x-3)(3x + 1) = 0

(2x-3) = 0 or (3x + 1) = 0

x = 3/2 or x = (-1)/3

Roots of equation are 3/2, (-1)/3

# **Question: 6**

Solve each of the

# Solution:

 $4x^2 + 5x = 0$ 

x(4x + 5) = 0 (On taking x common)

x = 0 or (4x + 5) = 0

 $\mathbf{x}=(-5)/4$ 

Roots of equation are 0, (-5)/4

# **Question:** 7

Solve each of the

# Solution:

 $3x^{2} - 243 = 0$   $3x^{2} = 243$   $x^{2} = 81$   $x = \sqrt{81}$  $x = \pm 9$ 

Roots of equation are 9, - 9

# **Question: 8**

Solve each of the

# Solution:

 $2x^2 + x - 6 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

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Product = a.c
For the given equation a = 2; b = 1; c = -6
= 2. - 6
= - 12
And either of their sum or difference = b
= 1
Thus the two terms are 4 and - 3
Difference = 4 - 3 = 1
Product = 4. - 3 = -12
2x^2 + x - 6 = 0
2x^2 + 4x - 3x - 6 = 0
2x(x + 2) - 3(x + 2) = 0
(2x-3)(x + 2) = 0
(2x-3) = 0 or (x + 2) = 0
x = 3/2, x = -2
Roots of equation are 3/2, - 2
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### **Question: 9**

Solve each of the

#### Solution:

 $x^2 + 6x + 5 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1, b = 6, c = 5

= 1.5 = 5

And either of their sum or difference = b

= 6

Thus the two terms are 1 and 5

Sum = 5 + 1 = 6 Product = 5.1 = 5  $x^{2} + 6x + 5 = 0$   $x^{2} + x + 5x + 5 = 0$  x(x + 1) + 5(x + 1) = 0 (x + 1)(x + 5) = 0 (x + 1) = 0 or (x + 5) = 0x = -1, x = -5 Roots of equation are - 1, - 5

#### **Question: 10**

Solve each of the

### Solution:

 $9x^2 - 3x - 2 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 9; b = -3; c = -2

= 9. - 2 = - 18

And either of their sum or difference = b

Thus the two terms are -  $6 \mbox{ and } 3$ 

- Sum = -6 + 3 = -3Product = -6.3 = -18  $9x^2 - 3x - 2 = 0$   $9x^2 - 6x + 3x - 2 = 0$ 3x(3x-2) + 1(3x-2) = 0
- (3x + 1)(3x-2) = 0
- (3x + 1) = 0 or (3x-2) = 0

x = (-1)/3 or x = 2/3

Roots of equation are (-1)/3, 2/3

# **Question: 11**

Solve each of the

# Solution:

 $x^2 + 12x + 35 = 0$ 

x(x + 7) + 5(x + 7) = 0

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1; b = 12; c = 35 = 1.35 = 35 And either of their sum or difference = b = 12 Thus the two terms are 7 and 5 Sum = 7 + 5 = 12 Product = 7.5 = 35  $x^2$  + 12x + 35 = 0  $x^2$  + 7x + 5x + 35 = 0 (x + 5)(x + 7) = 0(x + 5) = 0 or (x + 7) = 0x = -5 or x = -7

Roots of equation are - 5, - 7

# **Question: 12**

Solve each

# Solution:

 $x^{2} = 18x - 77$  $x^{2} - 18x + 77 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1; b = -18; c = 77

= 1.77 = 77

And either of their sum or difference = b

= - 18

Thus the two terms are - 7 and - 11  $\,$ 

Sum = - 7 - 11 = - 18

Product = -7. -11 = 77

 $x^2 - 18x + 77 = 0$ 

 $x^2 - 7x - 11x + 77 = 0$ 

x(x-7)-11(x-7) = 0

(x-7)(x-11) = 0

(x-7) = 0 or (x-11) = 0

$$x = 7 \text{ or } x = 11$$

Roots of equation are 7, 11

# **Question: 13**

Solve each of the

# Solution:

 $6x^2 + 11x + 3 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 6; b = 11; c = 3

= 6.3 = 18

And either of their sum or difference = b

= 11

Thus the two terms are  $9 \mbox{ and } 2$ 

Sum = 9 + 2 = 11

Product = 9.2 = 18  $6x^2 + 11x + 3 = 0$   $6x^2 + 9x + 2x + 3 = 0$  3x(2x + 3) + 1(2x + 3) = 0 (3x + 1)(2x + 3) = 0 (3x + 1) = 0 or (2x + 3) = 0 x = (-1)/3 or x = (-3)/2Roots of equation are  $\frac{-1}{2}, \frac{-3}{2}$ 

# **Question: 14**

Solve each of the

### Solution:

 $6x^2 + x - 12 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 6; b = 1; c = -12

= 6. - 12 = - 72

And either of their sum or difference = b

= 1

Thus the two terms are 9 and - 8  $\,$ 

Difference = 9 - 8 = 1

Product = 9. - 8 = -72

$$6x^2 + x - 12 = 0$$

 $6x^2 + 9x - 8x - 12 = 0$ 

3x(2x + 3) - 4(2x + 3) = 0

(2x + 3)(3x-4) = 0

(2x + 3) = 0 or (3x-4) = 0

x = (-3)/2 or x = 4/3

Roots of equation are  $\frac{-3}{2}$ ,  $\frac{4}{3}$ 

# **Question: 15**

Solve each of the

#### Solution:

 $3x^2 - 2x - 1 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 3; b = -2; c = -1

= 3. - 1 = - 3

And either of their sum or difference = b = - 2 Thus the two terms are - 3 and 1 Difference = - 3 + 1 = - 2 Product = - 3.1 = - 3  $3x^2 - 2x - 1 = 0$   $3x^2 - 3x + x - 1 = 0$  3x(x-1) + 1(x-1) = 0 (x-1)(3x + 1) = 0 (x-1) = 0 or (3x + 1) = 0 x = 1 or x = (-1)/3Roots of equation are 1, (-1)/3 Question: 16

Solve each of the

### Solution:

 $4x^{2} - 9x = 100$  $4x^{2} - 9x - 100 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 4; b = -9; c = -100= 4. - 100 = -400And either of their sum or difference = b = -9Thus the two terms are - 25 and 16 Difference = -25 + 16 = -9Product = -25.16 = -400 $4x^2 - 9x - 100 = 0$  $4x^2 - 25x + 16x - 100 = 0$ x(4x-25) + 4(4x-25) = 0(4x-25)(x+4) = 0(4x-25) = 0 or (x + 4) = 0x = 25/4 or x = -4Roots of equation are 25/4, - 4 **Question: 17** Solve each of the Solution:  $15x^2 - 28 = x$ 

 $15x^2 - x - 28 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 15; b = -1; c = -28= 15. - 28 = -420And either of their sum or difference = b = - 1 Thus the two terms are - 21 and 20 Difference = -21 + 20 = -1Product = -21.20 = -420 $15x^2 - x - 28 = 0$  $15x^2 - 21x + 20x - 28 = 0$ 3x(5x-7) + 4(5x-7) = 0(5x-7)(3x+4) = 0(5x-7) = 0 or (3x + 4) = 0x = 7/5 or x = (-4)/3Roots of equation are 7/5, - 4/3 **Question: 18** 

#### Solve each of the

### Solution:

 $4-11x = 3x^2$ 

 $3x^2 + 11x - 4 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 3; b = 11; c = -4

= 3. - 4 = - 12

And either of their sum or difference = b

= 11

Thus the two terms are 12 and - 1

Difference = 12 - 1 = 11Product = 12 - 1 = -12  $3x^{2} + 11x - 4 = 0$   $3x^{2} + 12x - 1x - 4 = 0$  3x(x + 4) - 1(x + 4) = 0 (x + 4)(3x - 1) = 0(x + 4) = 0 or (3x - 1) = 0

x = -4 or x = 1/3

Roots of equation are - 4, 1/3

#### **Question: 19**

Solve each of the

### Solution:

 $48x^2 - 13x - 1 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 48; b = -13; c = -1

 $= 48 \times -1 = -48$ 

And either of their sum or difference = b

Thus the two terms are - 16 and 3  $\,$ 

- Difference = -16 + 3 = -13
- Product = -16.3 = -48
- $48x^2 13x 1 = 0$
- $48x^2 16x + 3x 1 = 0$
- 16x(3x-1) + 1(3x-1) = 0
- (16x + 1)(3x-1) = 0
- (16x + 1) = 0 or (3x-1) = 0

$$x = (-1)/6$$
 or  $x = 1/3$ 

Roots of equation are  $\frac{-1}{6}$  or  $\frac{1}{3}$ 

# **Question: 20**

Solve each of the

# Solution:

 $x^2 + 2\sqrt{2}x - 6 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1;  $b = 2\sqrt{2}$ ; c = -6

= 1. - 6 = - 6

And either of their sum or difference = b

 $= 2\sqrt{2}$ 

Thus the two terms are  $3\sqrt{2}$  and  $-\sqrt{2}$ 

Difference =  $3\sqrt{2}-\sqrt{2} = 2\sqrt{2}$ 

Product =  $3\sqrt{2}$ .- $\sqrt{2}$  = 3.-2 = -6

 $x^2 + 2\sqrt{2}x - 6 = 0$ 

 $x^{2} + 3\sqrt{2}x - \sqrt{2}x - 3\sqrt{2}\sqrt{2} = 0$  using  $2 = \sqrt{2}\sqrt{2}$ 

 $x(x + 3\sqrt{2}) - \sqrt{2}(x + 3\sqrt{2}) = 0$ (x-\sqrt{2})(x + 3\sqrt{2}) = 0 (x-\sqrt{2}) = 0 or (x + 3\sqrt{2}) = 0 x = \sqrt{2} or x = -3\sqrt{2}

Roots of equation are  $\sqrt{2}$  or  $-3\sqrt{2}$ 

# **Question: 21**

Solve each of the

### Solution:

 $\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = \sqrt{3}$ ; b = 10;  $c = 7\sqrt{3}$ 

 $=\sqrt{3.7}\sqrt{3}=21$ 

(using  $3 = \sqrt{3} \times \sqrt{3}$ )

And either of their sum or difference = b

Thus, the two terms are 7 and 3

Sum = 7 + 3 = 10 Product = 7.3 = 21  $\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$   $\sqrt{3}x^2 + 7x + 3x + 7\sqrt{3} = 0$  (using 3 =  $\sqrt{3}.\sqrt{3}$ )  $x(\sqrt{3}x + 7) + \sqrt{3}(\sqrt{3}x + 7) = 0$   $(x + \sqrt{3})(\sqrt{3}x + 7) = 0$   $(x + \sqrt{3}) = 0$  or  $(\sqrt{3}x + 7) = 0$  $x = -\sqrt{3}$  or  $x = \frac{-7}{\sqrt{3}}$ 

Roots of equation are  $-\sqrt{3}$  or  $\frac{-7}{\sqrt{3}}$ 

# **Question: 22**

Solve each of the

# Solution:

 $\sqrt{3}x^2 + 11x + 6\sqrt{3} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = \sqrt{(3;)} b = 11; c = 6\sqrt{3}$ 

 $=\sqrt{3.6}\sqrt{3} = 3.6 = 18$ 

(using  $3 = \sqrt{3}.\sqrt{3}$ 

And either of their sum or difference = b = 11 Thus the two terms are 9 and 2 Sum = 9 + 2 = 11 Product = 9.2 = 18  $\sqrt{3}x^2 + 11x + 6\sqrt{3} = 0$   $\sqrt{3}x^2 + 9x + 2x + 6\sqrt{3} = 0$   $\sqrt{3}x(x + 3\sqrt{3}) + 2(x + 3\sqrt{3}) = 0$ (using 9 = 3.3 =  $3\sqrt{3}\sqrt{3}$ )  $(\sqrt{3}x + 2)(x + 3\sqrt{3}) = 0$   $(\sqrt{3}x + 2)(x + 3\sqrt{3}) = 0$  $x = -3\sqrt{3} \text{ or } x = \frac{-2}{\sqrt{3}}$ 

Roots of equation are  $-3\sqrt{3}$  or  $\frac{-2}{\sqrt{3}}$ 

# **Question: 23**

Solve each of the

### Solution:

 $3\sqrt{7}x^2 + 4x - \sqrt{7} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 3\sqrt{7}$ ; b = 4;  $c = -\sqrt{7}$ 

 $= 3\sqrt{7} \cdot \sqrt{7} = 3 \cdot 7 = -21$ 

(using  $7 = \sqrt{7}.\sqrt{7}$ )

And either of their sum or difference = b

= 4

Thus the two terms are 7 and - 3

Difference = 7 - 3 = 4

 $Product = 7 \times -3 = -21$ 

 $3\sqrt{7}x^2 + 4x - \sqrt{7} = 0$ 

$$3\sqrt{7}x^2 + 7x - 3x - \sqrt{7} = 0$$

(using  $7 = \sqrt{7}.\sqrt{7}$ )

 $\sqrt{7}x(3x + \sqrt{7}) - 1(3x + \sqrt{7}) = 0$ 

 $(\sqrt{7} \text{ x-1})(3x + \sqrt{7}) = 0$ 

 $(\sqrt{7} \text{ x-1}) = 0 \text{ or } (3x + \sqrt{7}) = 0$ 

$$x = 1/\sqrt{7} \text{ or } x = (-7)/\sqrt{3}$$

Roots of equation are  $x = \frac{1}{\sqrt{7}}$  or  $x = \frac{-7}{\sqrt{3}}$ 

#### **Question: 24**

Solve each of the

# Solution:

 $\sqrt{7}x^2 - 6x - 13\sqrt{7} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

$$Product = a.c$$

For the given equation  $a = \sqrt{7}$ ; b = -6;  $c = -13\sqrt{7}$ 

 $=\sqrt{7.-13}\sqrt{7} = -13.7 = -91$ 

And either of their sum or difference = b

Thus the two terms are 7 and - 13  $\,$ 

Difference = -13 + 7 = -6

Product = 7. - 13 = -91

 $\sqrt{7}x^2 - 6x - 13\sqrt{7} = 0$ 

$$\sqrt{7}x^2 - 13x + 7x - 13\sqrt{7} = 0$$

$$\sqrt{7}x^2 - 13x + 7x - 13\sqrt{7} = 0$$

 $x(\sqrt{7} x-13) + \sqrt{7} (\sqrt{7} x-13) = 0$ 

$$(x + \sqrt{7})(\sqrt{7} x - 13) = 0$$

 $(x + \sqrt{7}) = 0$  or  $(\sqrt{7} x-13) = 0$ 

$$x = -\sqrt{7} \text{ or } x = \frac{13}{\sqrt{7}}$$

Roots of equation are  $-\sqrt{7}$  or  $\frac{13}{\sqrt{7}}$ 

# **Question: 25**

Solve each of the

# Solution:

 $4\sqrt{6}x^2 - 13x - 2\sqrt{6} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 4\sqrt{6}$ ; b = -13;  $c = -2\sqrt{6}$ 

$$= 4\sqrt{6} - 2\sqrt{6} = -48$$

And either of their sum or difference = b

= - 13

Thus the two terms are - 16 and 3

Difference = -16 + 3 = -13

Product = -16.3 = -48

$$4\sqrt{6}x^2 - 13x - 2\sqrt{6} = 0$$

 $4\sqrt{6}x^2 - 16x + 3x - 2\sqrt{6} = 0$ 

 $4\sqrt{2}x(\sqrt{3}x - 2\sqrt{2}) + \sqrt{3}(\sqrt{3}x - 2\sqrt{2}) = 0$ 

(On using  $\sqrt{6} = \sqrt{3} \sqrt{2}$  and  $16 = 4.2.\sqrt{2} \sqrt{2}$ )  $\Rightarrow (4\sqrt{2} x + \sqrt{3})(\sqrt{3} x \cdot 2\sqrt{2}) = 0$   $\Rightarrow (4\sqrt{2} x + \sqrt{3}) = 0$  or  $(\sqrt{3} x \cdot 2\sqrt{2}) = 0$   $x = (-\sqrt{3})/(4\sqrt{2})$  or  $x = (2\sqrt{2})/\sqrt{3}$ Roots of equation are  $\frac{-\sqrt{3}}{4\sqrt{2}}$  or  $\frac{2\sqrt{2}}{\sqrt{3}}$ 

### **Question: 26**

Solve each of the

#### Solution:

 $3x^2 - 2\sqrt{6}x + 2 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 3; b =  $-2\sqrt{(6;)}$  c = 2 = 3.2 = 6 And either of their sum or difference = b =  $-2\sqrt{6}$ Thus the two terms are  $-\sqrt{6}$  and  $-\sqrt{6}$ Sum =  $-\sqrt{6} - \sqrt{6} = -2\sqrt{6}$ Product =  $-\sqrt{6} - \sqrt{6} = -6$  6 =  $\sqrt{6} - \sqrt{6}$   $3x^2 - 2\sqrt{6}x + 2 = 0$   $3x^2 - \sqrt{6}x - \sqrt{6}x + 2 = 0$ (On using 3 =  $\sqrt{3} \cdot \sqrt{3}$  and  $\sqrt{6} = \sqrt{3} \cdot \sqrt{2}$ )  $\sqrt{3}x(\sqrt{3}x - \sqrt{2}) - \sqrt{2}(\sqrt{3}x - \sqrt{2}) = 0$   $(\sqrt{3}x - \sqrt{2})(\sqrt{3}x - \sqrt{2}) = 0$   $x = \frac{\sqrt{2}}{\sqrt{3}}$  or  $x = \frac{\sqrt{2}}{\sqrt{3}}$ Equation has repeated roots  $\frac{\sqrt{2}}{\sqrt{3}}$ 

#### **Question: 27**

Solve each of the

### Solution:

 $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = \sqrt{3} b = -2\sqrt{2} c = -2\sqrt{3}$ 

$$=\sqrt{3.-2\sqrt{3}} = -2.3 = -6$$

And either of their sum or difference = b

 $= -2\sqrt{2}$ 

Thus the two terms are  $-3\sqrt{2}$  and  $\sqrt{2}$ Difference =  $-3\sqrt{2} + \sqrt{2} = -2\sqrt{2}$ Product =  $-3\sqrt{2} \times \sqrt{2} = -3.2 = -6$   $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$   $\sqrt{3}x^2 - 3\sqrt{2}x + \sqrt{2}x + 2\sqrt{3} = 0$ (On using  $3\sqrt{2} = \sqrt{3}\sqrt{3}\sqrt{2} = \sqrt{3}\sqrt{6}$ )  $\sqrt{3}x(x - \sqrt{6}) + \sqrt{2}(x - \sqrt{6}) = 0$ ( $\therefore 2\sqrt{3} = \sqrt{2}\sqrt{2}\sqrt{3} = \sqrt{2}\sqrt{6}$ )  $(x - \sqrt{6})(\sqrt{3}x + \sqrt{2}) = 0$  $x = \sqrt{6}$  or  $x = -\frac{\sqrt{2}}{\sqrt{3}}$ 

Roots of equation are  $\sqrt{6}$  or  $-\frac{\sqrt{2}}{\sqrt{3}}$ 

# **Question: 28**

Solve each of the

# Solution:

 $x^2 - 3\sqrt{5}x + 10 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1;  $b = -3\sqrt{5}$ ; c = 10= 1.10 = 10And either of their sum or difference = b  $= -3\sqrt{5}$ Thus the two terms are -2 $\sqrt{5}$  and - $\sqrt{5}$  $Sum = -2\sqrt{5} - \sqrt{5} = -3\sqrt{5}$ Product =  $-2\sqrt{5}$ .  $-\sqrt{5} = 2.5 = 10$  using  $5 = \sqrt{5}$ .  $\sqrt{5}$  $x^2 - 3\sqrt{5}x + 10 = 0$  $x^2 - 2\sqrt{5}x - \sqrt{5}x + 10 = 0$ (On using:  $10 = 2.5 = 2.\sqrt{5}\sqrt{5}$ )  $x(x-2\sqrt{5})-\sqrt{5}(x-2\sqrt{5}) = 0$  $(x-\sqrt{5})(x-2\sqrt{5}) = 0$  $(x-\sqrt{5}) = 0$  or  $(x-2\sqrt{5}) = 0$  $x = \sqrt{5}$  or  $x = 2\sqrt{5}$ Hence the roots of equation are  $\sqrt{5}$  or  $2\sqrt{5}$ **Question: 29** Solve each of the Solution:

 $x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$ 

 $x^2 - \sqrt{3}x - x + \sqrt{3} = 0$ 

On taking x common from first two terms and - 1 from last two

 $\mathbf{x}(\mathbf{x} \cdot \sqrt{3}) \cdot \mathbf{1}(\mathbf{x} \cdot \sqrt{3}) = \mathbf{0}$ 

 $(x-\sqrt{3})(x-1) = 0$ 

 $(x-\sqrt{3}) = 0 \text{ or } (x-1) = 0$ 

$$x = \sqrt{3}$$
 or  $x = 1$ 

Roots of equation are  $\sqrt{3}$  or 1

# **Question: 30**

Solve each of the

# Solution:

 $x^2 + 3\sqrt{3}x - 30 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1; b =  $3\sqrt{3}$ ; c = -30 = 1. - 30 = - 30 And either of their sum or difference = b =  $3\sqrt{3}$ Thus, the two terms are  $5\sqrt{3}$  and  $-2\sqrt{3}$ Difference =  $5\sqrt{3} - 2\sqrt{3} = 3\sqrt{3}$ Product =  $5\sqrt{3} - 2\sqrt{3} = -10.3 = -30$   $x^{2} + 3\sqrt{3}x - 30 = 0$   $x^{2} + 5\sqrt{3}x - 2\sqrt{3}x - 30 = 0$   $x(x + 5\sqrt{3}) - 2\sqrt{3}(x + 5\sqrt{3}) = 0.3 = \sqrt{3}\sqrt{3}$   $(x + 5\sqrt{3})(x - 2\sqrt{3}) = 0$   $(x + 5\sqrt{3}) = 0 \text{ or } (x - 2\sqrt{3}) = 0$   $x = -5\sqrt{3} \text{ or } x = 2\sqrt{3}$ Hence the roots of equation are  $-5\sqrt{3}$  or  $2\sqrt{3}$ 

# **Question: 31**

Solve each of the

# Solution:

 $\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = \sqrt{2}$ ; b = 7;  $c = 5\sqrt{2}$ 

 $=\sqrt{2}.5\sqrt{2} = 2.5 = 10$ And either of their sum or difference = b = 7 Thus the two terms are 5 and 2 Sum = 5 + 2 = 7Product = 5.2 = 10 $\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$  $\sqrt{2}x^2 + 5x + 2x + 5\sqrt{2} = 0$  $x(\sqrt{2}x + 5) + \sqrt{2}(\sqrt{2}x + 5) = 0$  $(\sqrt{2}x + 5)(x + \sqrt{2}) = 0$  $(\sqrt{2}x + 5) = 0 \text{ or } (x + \sqrt{2}) = 0$  $x = \frac{-5}{\sqrt{2}} \text{ or } x = -\sqrt{2}$ 

Hence the roots of equation are  $\frac{-5}{\sqrt{2}}$  or  $-\sqrt{2}$ 

# **Question: 32**

Solve each of the

# Solution:

 $5x^2 + 13x + 8 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 5; b = 13; c = 8

= 5.8 = 40

And either of their sum or difference = b

= 13

~

Thus the two terms are 5 and 8

Sum = 5 + 8 = 13  
Product = 5.8 = 40  
$$5x^{2} + 5x + 8x + 8 = 0$$

$$5x(x + 1) + 8(x + 1) = 0$$

(x + 1)(5x + 8) = 0

(x + 1) = 0 or (5x + 8) = 0

$$x = -1 \text{ or } x = \frac{-8}{5}$$

Hence the roots of equation are  $-1 \text{ or } \frac{-8}{5}$ 

# **Question: 33**

Solve each of the

### Solution:

$$x^{2} - (1 + \sqrt{2})x + \sqrt{2} = 0$$
$$x^{2} - x - \sqrt{2}x + \sqrt{2} = 0$$

On taking x common from first two terms and - 1 from last two

$$x(x-1) - \sqrt{2}(x-1) = 0$$
  
(x - \sqrt{2})(x - 1) = 0  
(x - \sqrt{2}) = 0 or (x - 1) = 0  
x = -1 or x = \sqrt{2}

Hence the roots of equation are  $-1 \text{ or } \sqrt{2}$ 

# **Question: 34**

Solve each of the

### Solution:

 $9x^2 + 6x + 1 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 9; b = 6; c = 1

$$= 9.1 = 9$$

And either of their sum or difference = b

= 6

Thus the two terms are  $3 \mbox{ and } 3$ 

Sum = 3 + 3 = 6

Product = 3.3 = 9

```
9x^2 + 6x + 1 = 0
```

 $9x^2 + 3x + 3x + 1 = 0$ 

3x(3x + 1) + 1(3x + 1) = 0

(3x + 1)(3x + 1) = 0

(3x + 1) = 0 or (3x + 1) = 0

$$x = \frac{-1}{3} \text{ or } x = \frac{-1}{3}$$

Hence the equation has repeated roots  $x = \frac{-1}{3}$ 

# **Question: 35**

Solve each of the

# Solution:

 $100x^2 - 20x + 1 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 100; b = -20; c = 1 = 100.1 = 100 And either of their sum or difference = b = -20 Thus the two terms are - 10 and - 10 Sum = -10 - 10 = -20 Product = -10. - 10 = 100 100x<sup>2</sup> - 20x + 1 = 0 100x<sup>2</sup> - 10x - 10x + 1 = 0 10x(10x-1)-1(10x-1) = 0 (10x-1)(10x-1) = 0 (10x-1) = 0 or (10x-1) = 0 x =  $\frac{1}{2}$  or x =  $\frac{1}{2}$ 

$$x = \frac{1}{10} \text{ or } x = \frac{1}{10}$$

Roots of equation are repeated  $\frac{1}{10}$ 

# **Question: 36**

Solve each of the

# Solution:

$$2x^2 - x + \frac{1}{8} = 0$$

$$16x^2 - 8x + 1 = 0$$
 (taking LCM)

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 16; b = -8; c = 1

= 16.1 = 16

And either of their sum or difference = b

= - 8

Thus the two terms are - 4 and - 4

```
Sum = -4 - 4 = -8

Product = -4 - 4 = 16

16x^2 - 8x + 1 = 0

16x^2 - 4x - 4x + 1 = 0

4x(4x-1)-1(4x-1) = 0

(4x-1)(4x-1) = 0

(4x-1) = 0 \text{ or } (4x-1) = 0

x = \frac{1}{4} \text{ or } x = \frac{1}{4}
```

The equation has repeated roots  $\frac{1}{4}$ 

# **Question: 37**

Solve each of the

# Solution:

 $10x - \frac{1}{x} = 3 \text{ taking LCM}$  $10x^2 - 1 - 3x = 0$  $10x^2 - 3x - 1 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 10; b = -3; c = -1 = 10. -1 = -10 And either of their sum or difference = b = -3 Thus the two terms are - 5 and 2 Difference = -5 + 2 = -3 Product = -5.2 = -10  $10x^2 - 3x - 1 = 0$   $10x^2 - 5x + 2x - 1 = 0$  5x(2x-1) + 1(2x-1) = 0 (5x + 1)(2x-1) = 0 (5x + 1) = 0 or (2x-1) = 0 $x = \frac{-1}{5}$  or  $x = \frac{1}{2}$ 

# **Question: 38**

Solve each of the

# Solution:

 $\frac{2}{x^2} - \frac{5}{x} + 2 = 0$ 2 - 5x + 2x<sup>2</sup> = 0 2x<sup>2</sup> - 5x + 2 = 0

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 2; b = -5; c = 2

= 2.2 = 4

And either of their sum or difference = b

= - 5

Thus the two terms are - 4 and - 1

Difference = -4 - 1 = -5Product = -4 - 1 = 4  $2x^2 - 5x + 2 = 0$   $2x^2 - 4x - x + 2 = 0$  2x(x-2)-1(x-2) = 0 (2x-1)(x-2) = 0 (2x-1) = 0 or (x-2) = 0 $x = 2 \text{ or } x = \frac{1}{2}$ 

Hence the roots of equation are2 or  $\frac{1}{2}$ 

# **Question: 39**

Solve each of the

### Solution:

 $2x^2 + ax - a^2 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 2; b = a;  $c = -a^2$ 

$$= -2.a^2 = -2 a^2$$

And either of their sum or difference = b

= a

Thus the two terms are 2a and - a

Difference = 
$$2a - a = a$$
  
Product =  $2a - a = -2a^2$   
 $2x^2 + ax - a^2 = 0$   
 $2x^2 + 2ax - ax - a^2 = 0$   
 $2x (x + a) - a (x + a) = 0$   
 $(2x-a) (x + a) = 0$   
 $(2x-a) = 0 \text{ or } (x + a) = 0$   
 $x = \frac{a}{2} \text{ or } x = -a$ 

Hence the roots of equation are  $\frac{a}{2}$  or -a

# **Question: 40**

Solve each of the

# Solution:

 $4x^2 + 4bx - (a^2 - b^2) = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 4 b = 4b c = -(a^2 - b^2)$ = 4. - (a<sup>2</sup> - b<sup>2</sup>) = -4a<sup>2</sup> + 4b<sup>2</sup> And either of their sum or difference = b = 4b Thus the two terms are 2(a + b) and - 2(a - b) Difference = 2a + 2b - 2a + 2b = 4b Product = 2(a + b). - 2(a - b) = -4(a<sup>2</sup> - b<sup>2</sup>) using a<sup>2</sup> - b<sup>2</sup> = (a + b) (a - b) 4x<sup>2</sup> + 4bx - (a<sup>2</sup> - b<sup>2</sup>) = 0  $\Rightarrow 4x^2 + 2(a + b)x - 2(a - b) - (a + b) (a - b) = 0$   $\Rightarrow 2x[2x + (a + b)] - (a - b) [2x + (a + b)] = 0$   $\Rightarrow [2x + (a + b)] [2x - (a - b)] = 0$   $\Rightarrow [2x + (a + b)] = 0 \text{ or } [2x - (a - b)] = 0$  $x = \frac{-(a + b)}{2} \text{ or } x = \frac{a - b}{2}$ 

Hence the roots of equation are  $\frac{-(a+b)}{2}$  or  $\frac{a-b}{2}$ 

### **Question: 41**

Solve each of the

# Solution:

 $4x^2 - 4a^2x + (a^4 - b^4) = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 4;  $b = -4a^2$ ;  $c = (a^4 - b^4)$ 

$$= 4. (a^4 - b^4)$$

 $= 4a^4 - 4b^4$ 

And either of their sum or difference = b

$$= -4a^{2}$$

Thus the two terms are -  $2(a^2 + b^2)$  and -  $2(a^2 - b^2)$ 

Difference = 
$$-2(a^2 + b^2) - 2(a^2 - b^2)$$
  
=  $-2a^2 - 2b^2 - 2a^2 + 2b^2$   
=  $-4a^2$   
Product =  $-2(a^2 + b^2) - 2(a^2 - b^2)$   
=  $4(a^2 + b^2)(a^2 - b^2)$   
=  $4. (a^4 - b^4)$   
( $\therefore$  using  $a^2 - b^2 = (a + b) (a - b)$ )  
=  $4x^2 - 4a^2x + (a^4 - b^4) = 0$ 

$$\Rightarrow 4x^{2} - 4a^{2}x + ((a^{2})^{2} - (b^{2})^{2}) = 0$$
  
(: using  $a^{2} - b^{2} = (a + b) (a - b))$   
$$\Rightarrow 4x^{2} - 2(a^{2} + b^{2}) x - 2(a^{2} - b^{2}) x + (a^{2} + b^{2}) (a^{2} - b^{2}) = 0$$
  
$$\Rightarrow 2x [2x - (a^{2} + b^{2})] - (a^{2} - b^{2}) [2x - (a^{2} + b^{2})] = 0$$
  
$$\Rightarrow [2x - (a^{2} + b^{2})] [2x - (a^{2} - b^{2})] = 0$$
  
$$\Rightarrow [2x - (a^{2} + b^{2})] = 0 \text{ or } [2x - (a^{2} - b^{2})] = 0$$
  
$$x = \frac{a^{2} + b^{2}}{2} \text{ or } x = \frac{a^{2} - b^{2}}{2}$$

Hence the roots of given equation are  $\frac{a^2 + b^2}{2}$  or  $\frac{a^2 - b^2}{2}$ 

### **Question: 42**

Solve each of the

#### Solution:

 $x^2 + 5x - (a^2 + a - 6) = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1; b = 5;  $c = -(a^2 + a - 6)$ 

= 1. - (a<sup>2</sup> + a - 6)= - (a<sup>2</sup> + a - 6)

And either of their sum or difference = b

Thus the two terms are (a + 3) and - (a - 2)

Difference = a + 3 - a + 2

= 5

Product = (a + 3). - (a - 2)

= - [(a + 3)(a - 2)]

 $= - (a^2 + a - 6)$ 

 $x^2 + 5x - (a^2 + a - 6) = 0$ 

 $\Rightarrow x^{2} + (a + 3)x - (a - 2)x - (a + 3)(a - 2) = 0$ 

 $\Rightarrow x[x + (a + 3)] - (a - 2) [x + (a + 3)] = 0$ 

 $\Rightarrow$  [x + (a + 3)] [x - (a - 2)] = 0

 $\Rightarrow$  [x + (a + 3)] = 0 or [x - (a - 2)] = 0

 $\Rightarrow$  x = - (a + 3) or x = (a - 2)

Hence the roots of given equation are -(a + 3) or (a - 2)

#### **Question: 43**

Solve each of the

### Solution:

 $x^2 - 2ax - (4b^2 - a^2) = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation  $a = 1 b = -2a c = -(4b^2 - a^2)$  $= 1. - (4b^2 - a^2)$  $= -(4b^2 - a^2)$ And either of their sum or difference = b = - 2a Thus the two terms are (2b - a) and -(2b + a)Difference = 2b - a - 2b - a= - 2a Product = (2b - a) - (2b + a)(∵ using  $a^2 - b^2 = (a + b) (a - b))$  $= -(4b^2 - a^2)$  $x^2 - 2ax - (4b^2 - a^2) = 0$  $\Rightarrow x^{2} + (2b - a)x - (2b + a)x - (2b - a)(2b + a) = 0$  $\Rightarrow x[x + (2b - a)] - (2b + a)[x + (2b - a)] = 0$  $\Rightarrow [x + (2b - a)] [x - (2b + a)] = 0$  $\Rightarrow$  [x + (2b - a)] = 0 or [x - (2b + a)] = 0  $\Rightarrow$  x = (a - 2b) or x = (a + 2b)

Hence the roots of given equation are (a - 2b) or x = (a + 2b)

### **Question: 44**

Solve each of the

### Solution:

 $x^2 - (2b - 1)x + (b^2 - b - 20) = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1; b = -(2b - 1);  $c = b^2 - b - 20$ 

$$= 1(b^2 - b - 20)$$

 $= (b^2 - b - 20)$ 

And either of their sum or difference = b

= -(2b - 1)

Thus the two terms are -(b - 5) and -(b + 4)

Sum = -(b - 5) - (b + 4)

= -b + 5 - b - 4

= -2b + 1

= - (2b - 1)

Product = -(b - 5) - (b + 4)

= (b - 5) (b + 4)  $= b^{2} - b - 20$   $x^{2} - (2b - 1)x + (b^{2} - b - 20) = 0$   $\Rightarrow x^{2} - (b - 5)x - (b + 4)x + (b - 5)(b + 4) = 0$   $\Rightarrow x[x - (b - 5)] - (b + 4)[x - (b - 5)] = 0$   $\Rightarrow [x - (b - 5)] [x - (b + 4)] = 0$   $\Rightarrow [x - (b - 5)] = 0 \text{ or } [x - (b + 4)] = 0$   $\Rightarrow x = (b - 5) \text{ or } x = (b + 4)$ 

Hence the roots of equation are (b - 5) or (b + 4)

#### **Question: 45**

Product = a.c

Solve each of the

#### Solution:

 $x^2 + 6x - (a^2 + 2a - 8) = 0$ 

 $abx^{2} + (b^{2} - ac)x - bc = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

For the given equation a = 1; b = 6;  $c = -(a^2 + 2a - 8)$  $= 1. - (a^2 + 2a - 8)$  $= -(a^2 + 2a - 8)$ And either of their sum or difference = b = 6Thus the two terms are (a + 4) and - (a - 2)Difference = a + 4 - a + 2= 6Product = (a + 4) - (a - 2) $= -(a^2 + 2a - 8)$  $\Rightarrow x^{2} + 6x - (a^{2} + 2a - 8) = 0$  $\Rightarrow x^{2} + (a + 4)x - (a - 2)x - (a + 4)(a - 2) = 0$  $\Rightarrow x [x + (a + 4)] - (a - 2) [x + (a + 4)] = 0$  $\Rightarrow$  [x + (a + 4)] [x - (a - 2)] = 0  $\Rightarrow$  [x + (a + 4)] = 0 or [x - (a - 2)] = 0 x = -(a + 4) or x = (a - 2)Hence the roots of equation are -(a + 4) or (a - 2)**Question: 46** Solve each of the Solution:  $abx^{2} + (b^{2} - ac)x - bc = 0$ 

 $abx^2 + b^2x - acx - bc = 0$ 

bx (ax + b) - c (ax + b) = 0 taking bx common from first two terms and -c from last two

(ax + b) (bx - c) = 0

(ax + b) = 0 or (bx - c) = 0

$$x = \frac{-b}{a} \text{ or } x = \frac{c}{a}$$

Hence the roots of equation are  $\frac{-b}{a}$  or  $\frac{c}{a}$ 

# **Question: 47**

Solve each of the

# Solution:

 $x^{2} - 4ax - b^{2} + 4a^{2} = 0$   $x^{2} - 4ax - ((b)^{2} - (2a)^{2}) = 0$ {using  $a^{2} - b^{2} = (a + b)(a - b)$ }  $x^{2} - (b + 2a)x + (b - 2a)x - (b + 2a)(b - 2a) = 0$   $\Rightarrow x [x - (b + 2a)] + (b - 2a) [x - (b + 2a)] = 0$   $\Rightarrow [x - (b + 2a)] [x + (b - 2a)] = 0$   $\Rightarrow [x - (b + 2a)] = 0 \text{ or } [x + (b - 2a)] = 0$   $\Rightarrow x = (b + 2a) \text{ or } x = -(b - 2a)$  $\Rightarrow x = (2a + b) \text{ or } x = (2a - b)$ 

Hence the roots of equation are (2a + b) or (2a - b)

### **Question: 48**

Solve each of the

### Solution:

 $4x^{2} - 2a^{2}x - 2b^{2}x + a^{2}b^{2} = 0$ 2x (2x - a<sup>2</sup>) - b<sup>2</sup>(2x - a<sup>2</sup>) = 0

(On taking 2x common from first two terms and  $-b^2$  from last two)

0

$$\Rightarrow (2x - a^{2}) (2x - b^{2}) = 0$$
  
$$\Rightarrow (2x - a^{2}) = 0 \text{ or } (2x - b^{2}) =$$
  
$$\Rightarrow x = \frac{a^{2}}{2} \text{ or } x = \frac{b^{2}}{2}$$

Hence the roots of equation are  $\frac{a^2}{2}$  or  $\frac{b^2}{2}$ 

#### **Question: 49**

Solve each of the

### Solution:

 $12abx^2 - (9a^2 - 8b^2)x - 6ab = 0$ 

$$12abx^2 - 9a^2 x + 8b^2 x - 6ab = 0$$

3ax(4bx - 3a) + 2b(4bx - 3a) = 0 taking 3ax common from first two terms and 2b from last two (4bx - 3a) (3ax + 2b) = 0 (4bx - 3a) = 0 or (3ax + 2b) = 0

$$x = \frac{3a}{4b} \text{ or } x = \frac{-2b}{3a}$$

Hence the roots of equation are  $x = \frac{3a}{4b}$  or  $x = \frac{-2b}{3a}$ 

### **Question: 50**

Solve each of the

### Solution:

 $a^2b^2x^2 + b^2x - a^2x - 1 = 0$ 

 $b^2x(a^2x + 1) - 1(a^2x + 1) = 0$  taking  $b^2x$  common from first two terms and - 1 from last two

 $(a^2x + 1)(b^2x - 1) = 0$ 

 $(a^2x + 1) = 0$  or  $(b^2x - 1) = 0$ 

$$x = \frac{-1}{a^2} \text{ or } x = \frac{1}{b^2}$$

Hence the roots of equation are  $\frac{-1}{a^2}$  or  $\frac{1}{b^2}$ 

### **Question: 51**

Solve each of the

### Solution:

 $9x^2 - 9(a + b)x + (2a^2 + 5ab + 2b^2) = 0$ 

Using the splitting middle term - the middle term of the general equation  $Ax^2 + Bx + C$  is divided in two such values that:

Product = AC

For the given equation A = 9, B = -9(a + b),  $C = 2a^2 + 5ab + 2b^2$ 

 $= 9(2a^{2} + 5ab + 2b^{2}) = 9(2a^{2} + 4ab + ab + 2b^{2}) = 9[2a(a + 2b) + b(a + 2b)] = 9(a + 2b)(2a + b) = 3(a + 2b)3(2a + b)$ Also, 3(a + 2b) + 3(2a + b) = 9(a + b)Therefore, 9x<sup>2</sup> - 9 (a + b) x + (2 a<sup>2</sup> + 5ab + 2b<sup>2</sup>) = 0 9x<sup>2</sup> - 3(2a + b)x - 3(a + 2b)x + (a + 2b) (2a + b) = 0

3x[3x - (2a + b)] - (a + 2b)[3x - (2a + b)] = 0

[3x - (2a + b)][3x - (a + 2b)] = 0

[3x - (a + 2b)] = 0 or [3x - (2a + b)] = 0

$$x = \frac{a+2b}{3} \text{ or } x = \frac{2a+b}{3}$$

Hence the roots of equation are  $\frac{a+2b}{3}$  or  $\frac{2a+b}{3}$ 

# **Question: 52**

Solve each of the

# Solution:

 $\frac{\frac{16}{x} - 1}{\frac{15}{x+1}} = \frac{15}{x+1} = 1$ 

 $\frac{16x+16-15x}{x(x+1)} = 1 \text{ taking LCM}$   $\frac{x + 16}{x^2 + x} = 1$   $x^2 + x = x + 16 \text{ cross multiplying}$   $x^2 - 16 = 0$   $x^2 - (4)^2 = 0 \text{ using } a^2 - b^2 = (a + b)(a - b)$  (x + 4) (x - 4) = 0 (x + 4) = 0 or (x - 4) = 0 x = 4 or x = -4

Hence the roots of equation are 4, - 4.

# **Question: 53**

Solve each of the

# Solution:

 $\frac{4}{x} - 3 = \frac{5}{2x+3}$   $\frac{4}{x} - \frac{5}{2x+3} = 3$   $\frac{8x+12-5x}{x(2x+3)} = 3 \text{ taking LCM}$   $\frac{3x+12}{2x^2+3x} = 3$   $\frac{3(x+4)}{2x^2+3x} = 3$   $\frac{x+4}{2x^2+3x} = 1$   $x+4 = 2x^2 + 3x \text{ cross multiplying}$   $2x^2 + 2x - 4 = 0 \text{ taking 2 common}$   $x^2 + x - 2 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 1 c = -2

And either of their sum or difference = b

= 1

Thus the two terms are 2 and - 1  $\,$ 

Difference = 2 - 1 = 1

Product = 2. - 1 = -2

 $\mathbf{x}^2 + \mathbf{x} - 2 = 0$ 

 $x^2 + 2x - x - 2 = 0$ 

x(x + 2) - (x + 2) = 0

(x + 2) (x - 1) = 0(x + 2) = 0 or (x - 1) = 0x = -2 or x = 1

Hence the roots of equation are - 2 or 1.

# **Question: 54**

Solve each of the

# Solution:

 $\frac{3}{x+1} - \frac{2}{3x-1} = \frac{1}{2}, x \neq -1, \frac{1}{3}$  $\frac{3}{x+1} - \frac{2}{3x-1} = \frac{1}{2}$  $\frac{9x-3-2x-2}{(x+1)(3x-1)} = \frac{1}{2} \text{ taking LCM}$  $\frac{7x-5}{3x^2+2x-1} = \frac{1}{2}$ 

 $3x^2 + 2x - 1 = 14x - 10$  cross multiplying

 $3x^2 - 12x + 9 = 0$  taking 3 common

 $x^2 - 4x + 3 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -4 c = 3

= 1.3 = 3

And either of their sum or difference = b

= - 4

Thus the two terms are - 3 and - 1

Sum = - 3 - 1 = - 4

Product = -3. -1 = 3

 $x^2 - 4x + 3 = 0$ 

 $x^2 - 3x - x + 3 = 0$ 

x(x - 3) - 1(x - 3) = 0

(x - 3) (x - 1) = 0

(x - 3) = 0 or (x - 1) = 0

x = 3 or x = 1

Hence the roots of equation are 3 or 1.

# **Question: 55**

Solve each of the

# Solution:

 $\frac{1}{x-1} - \frac{1}{x+5} = \frac{6}{7}$  $\frac{x+5-x+1}{(x-1)(x+5)} = \frac{6}{7} \text{ taking LCM}$ 

 $\frac{6}{(x-1)(x+5)} = \frac{6}{7}$  $\frac{6}{x^2+4x-5} = \frac{6}{7}$  $x^2 + 4x - 5 = 7 \text{ cross multiplying}$  $x^2 + 4x - 12 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 4 c = -12

= 1. - 12 = - 12

And either of their sum or difference = b

```
= 4
```

Thus the two terms are 6 and - 2  $\,$ 

Difference = 6 - 2 = 4

Product = 6. - 2 = -12

 $x^2 + 4x - 12 = 0$ 

 $x^2 + 6x - 2x - 12 = 0$ 

x(x + 6) - 2(x + 6) = 0

(x + 6)(x - 2) = 0

(x + 6) = 0 or (x - 2) = 0

x = -6 or x = 2

Hence the roots of equation are - 6 or 2.

# **Question: 56**

Solve each of the

### Solution:

 $\frac{1}{2a+b+2x} = \frac{1}{2a} + \frac{1}{b} + \frac{1}{2x}$   $\frac{1}{2a+b+2x} - \frac{1}{2x} = \frac{1}{2a} + \frac{1}{b}$   $\frac{2x-2a-b-2x}{2x(2a+b+2x)} = \frac{1}{2a} + \frac{1}{b} \text{ taking LCM}$   $\frac{-(2a+b)}{4x^2 + 4ax + 2bx} = \frac{2a+b}{2ab}$   $4x^2 + 4ax + 2bx = -2ab \text{ cross multiplying}$   $4x^2 + 4ax + 2bx + 2ab = 0$  4x(x+a) + 2b(x+a) = 0 taking 4x common from first two terms and 2b from last two (x+a) (4x+2b) = 0 (x+a) = 0 or (4x+2b) = 0  $x = -a \text{ or } x = \frac{-b}{2}$ 

Hence the roots of equation are  $-a \text{ or } \frac{-b}{2}$ 

### **Question: 57**

Solve each of the

#### Solution:

 $\frac{x+3}{x-2} - \frac{1-x}{x} = 4\frac{1}{4}$   $\frac{x(x+3) - (1-x)(x-2)}{x(x-2)} = \frac{17}{4} \text{ taking LCM}$   $\frac{x^2 + 3x - (x-2-x^2+2x)}{x^2-2x} = \frac{17}{4}$   $\frac{x^2 + 3x + x^2 - 3x + 2}{x^2 - 2x} = \frac{17}{4}$   $\frac{2x^2 + 2}{x^2 - 2x} = \frac{17}{4}$   $8x^2 + 8 = 17x^2 - 34x \text{ cross multiplying}$   $-9x^2 + 34x + 8 = 0$   $9x^2 - 34x - 8 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 9 b = -34 c = -8

= 9. - 8 = - 72

And either of their sum or difference = b

= - 34

Thus the two terms are - 36 and 2  $\,$ 

Difference = -36 + 2 = -34

Product = -36.2 = -72

 $9x^2 - 34x - 8 = 0$ 

 $9x^2 - 36x + 2x - 8 = 0$ 

9x(x - 4) + 2(x - 4) = 0

(9x + 2)(x - 4) = 0

$$x = 4 \text{ or } x = \frac{-2}{9}$$

Hence the roots of equation are 4 or  $\frac{-2}{2}$ 

# **Question: 58**

Solve each of the

# Solution:

Given:  $\frac{3x-4}{7} + \frac{7}{3x-4} = \frac{5}{2}$ ,  $x \neq \frac{4}{3}$  $\frac{(3x-4)^2 + 49}{7(3x-4)} = \frac{5}{2}$  taking LCM  $\frac{9x^2 - 24x + 16 + 49}{7(3x - 4)} = \frac{5}{2} \text{ using } (a - b)^2 = a^2 + b^2 - 2ab$  $\frac{9x^2 - 24x + 65}{21x - 28} = \frac{5}{2} \text{ cross multiplying}$  $18x^2 - 48x + 130 = 105x - 140$ 

 $18x^2 - 153x + 270 = 0$  taking 9 common

 $2x^2 - 17x + 30 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 2 b = -17 c = 30

= 2.30 = 60

And either of their sum or difference = b

= - 17

Thus the two terms are - 12 and - 5  $\,$ 

Sum = - 12 - 5 = - 17

Product = -12. - 5 = 60

 $2x^2 - 17x + 30 = 0$ 

 $2x^2 - 12x - 5x + 30 = 0$ 

2x(x - 6) - 5(x - 6) = 0

(x - 6) (2x - 5) = 0

(x - 6) = 0 or (2x - 5) = 0

$$x = 6 \text{ or } x = \frac{5}{2}$$

Hence the roots of equation are  $6 \text{ or } x = \frac{5}{2}$ 

# **Question: 59**

Solve each of the

# Solution:

Given:  $\frac{x}{x-1} + \frac{x-1}{x} = 4\frac{1}{4}$   $\frac{(x-1)^2}{x(x-1)} = \frac{17}{4}$  taking LCM  $\frac{x^2 + x^2 - 2x + 1}{x(x-1)} = \frac{17}{4}$  using  $(a - b)^2 = a^2 + b^2 - 2ab$   $\frac{2x^2 - 2x + 1}{x^2 - 1} = \frac{17}{4}$  $8x^2 - 8x + 4 = 17x^2 - 17x$  cross multiplying

$$9x^2 - 9x - 4 = 0$$

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 9 b = -9 c = -4

= 9. - 4 = - 36 And either of their sum or difference = b = - 9 Thus the two terms are - 12 and 3 Sum = - 12 + 3 = - 9 Product = - 12.3 = - 36 9x<sup>2</sup> - 9x - 4 = 0 9x<sup>2</sup> - 12x + 3x - 4 = 0 3x(3x - 4) + 1(3x - 4) = 0 (3x - 4) (3x + 1) = 0 (3x - 4) = 0 or (3x + 1) = 0  $x = \frac{4}{3} \text{ or } x = \frac{-1}{3}$ 

Hence the roots of equation are  $\frac{4}{3}$  or  $\frac{-1}{3}$ 

### **Question: 60**

Solve each of the

### Solution:

Given:  $\frac{x}{x+1} + \frac{x+1}{x} = 2\frac{4}{15}$  taking LCM  $\frac{x^2 + x^2 + 2x + 1}{x(x+1)} = \frac{34}{15}$   $\frac{2x^2 + 2x + 1}{x^2 + x} = \frac{34}{15}$   $30x^2 + 30x + 15 = 34x^2 + 34x$  cross multiplying

 $4x^2 + 4x - 15 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 4 b = 4 c = -15

= 4. - 15 = - 60

And either of their sum or difference = b

= 4

Thus the two terms are 10 and - 6

Difference = 10 - 6 = 4

Product = 10. - 6 = -60

 $4x^2 + 4x - 15 = 0$ 

 $4x^2 + 10x - 6x - 15 = 0$ 

2x(2x + 5) - 3(2x + 5) = 0

(2x + 5)(2x - 3) = 0

(2x + 5) = 0 or (2x - 3) = 0

$$x = \frac{-5}{2} \text{ or } x = \frac{3}{2}$$

Hence the roots of equation are  $\frac{-5}{2}$  or  $\frac{3}{2}$ 

# **Question: 61**

Solve each of the

#### Solution:

Given:  $\frac{x-4}{x-5} + \frac{x-6}{x-7} = 3\frac{1}{3}$ ,  $x \neq 5,7$   $\frac{(x-7)(x-4) + (x-5)(x-6)}{(x-5)(x-7)} = \frac{10}{3}$  taking LCM  $\frac{x^2 - 11x + 28 + x^2 - 11x + 30}{x^2 - 12x + 35} = \frac{10}{3}$   $\frac{2x^2 - 22x + 58}{x^2 - 12x + 35} = \frac{10}{3}$   $\frac{x^2 - 11x + 29}{x^2 - 12x + 35} = \frac{5}{3}$   $3x^2 - 33x + 87 = 5x^2 - 60x + 175$  cross multiplying  $2x^2 - 27x + 88 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 2 b = -27 c = 88

= 2.88 = 176

And either of their sum or difference = b

= - 27

Thus the two terms are - 16 and - 11  $\,$ 

Sum = - 16 - 11 = - 27

Product = -16. - 11 = 176

 $2x^2 - 27x + 88 = 0$ 

 $2x^2 - 16x - 11x + 88 = 0$ 

2x(x - 8) - 11(x - 8) = 0

$$(x - 8)(2x - 11) = 0$$

(x - 8) = 0 or (2x - 11) = 0

$$x = 8 \text{ or } x = \frac{11}{2} = 5\frac{1}{2}$$

Hence the roots of equation are 8 or  $5\frac{1}{2}$ 

#### **Question: 62**

Solve each of the

# Solution:

Given:  $\frac{x-1}{x-2} + \frac{x-3}{x-4} = 3\frac{1}{3}$ 

 $\frac{(x-1)(x-4) + (x-2)(x-3)}{(x-2)(x-4)} = \frac{10}{3} \text{ taking LCM}$   $\frac{x^2 - 5x + 4 + x^2 - 5x + 6}{x^2 - 6x + 8} = \frac{10}{3}$   $\frac{2x^2 - 10x + 10}{x^2 - 6x + 8} = \frac{10}{3}$   $\frac{x^2 - 5x + 5}{x^2 - 6x + 8} = \frac{5}{3} \text{ cross multiplying}$   $3x^2 - 15x + 15 = 5x^2 - 30x + 40$   $2x^2 - 15x + 25 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 2 b = -15 c = 25 = 2.25 = 50 And either of their sum or difference = b = -15 Thus the two terms are - 10 and - 5 Sum = -10 - 5 = -15 Product = -10. - 5 = 50  $2x^2 - 15x + 25 = 0$   $2x^2 - 10x - 5x + 25 = 0$  2x(x - 5) - 5(x - 5) = 0 (x - 5)(2x - 5) = 0 (x - 5) = 0 or (2x - 5) = 0 $x = 5 \text{ or } x = \frac{5}{2}$ 

Hence the roots of equation are 5 or  $\frac{5}{2}$ 

# **Question: 63**

Solve each of the

# Solution:

Given:  $\frac{1}{x-2} + \frac{2}{x-1} = \frac{6}{x}$ ,  $x \neq 0, 1, 2$   $\frac{(x-1)+2(x-2)}{(x-2)(x-1)} = \frac{6}{x}$  taking LCM  $\frac{3x-5}{x^2-3x+2} = \frac{6}{x}$  cross multiplying  $3x^2 - 5x = 6x^2 - 18x + 12$  $3x^2 - 13x + 12 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

### Product = a.c

For the given equation a = 3 b = -13 c = 12

= 3.12 = 36And either of their sum or difference = b = -13 Thus the two terms are - 9 and - 4 Sum = -9 - 4 = -13 Product = -9. - 4 = 36  $3x^2 - 13x + 12 = 0$  $3x^2 - 9x - 4x + 12 = 0$ 3x (x - 3) - 4(x - 3) = 0(x - 3) (3x - 4) = 0 $x = 3 \text{ or } x = \frac{4}{3}$ 

Hence the roots of equation are 3 or  $\frac{4}{3}$ 

## **Question: 64**

Solve each of the

### Solution:

Given:  $\frac{1}{x+1} + \frac{2}{x+2} = \frac{5}{x+4}$   $\frac{(x+2)+2(x+1)}{(x+2)(x+1)} = \frac{5}{x+4}$  taking LCM  $\frac{3x+4}{x^2+3x+2} = \frac{5}{x+4}$   $(3x+4)(x+4) = 5x^2 + 15x + 10$  cross multiplying  $3x^2 + 16x + 16 = 5x^2 + 15x + 10$  $2x^2 - x - 6 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 2 b = -1 c = -6

= 2. - 6 = - 12

And either of their sum or difference = b

```
= - 1
```

Thus the two terms are -  $4 \mbox{ and } 3$ 

Difference = -4 + 3 = -1

Product = -4.3 = 12

 $2x^2 - x - 6 = 0$ 

 $2x^{2} - 4x + 3x - 6 = 0$ 2x(x - 2) + 3(x - 2) = 0

(x - 2) (2x + 3) = 0

(x - 2) = 0 or (2x + 3) = 0

$$x = 2 \text{ or } x = \frac{-3}{2}$$

Hence the roots of equation are 2 or  $\frac{-3}{2}$ 

#### **Question: 65**

Solve each of the

#### Solution:

Given:  $3\left(\frac{3x-1}{2x+3}\right) - 2\left(\frac{2x+3}{3x-1}\right) = 5$   $\frac{3(3x-1)^2 - 2(2x+3)^2}{(2x+3)(3x-1)} = 5$  taking LCM  $\frac{3(9x^2 - 6x+1) - 2(4x^2 + 12x+9)}{(2x+3)(3x-1)} = 5$  using  $(a + b)^2 = a^2 + b^2 + 2ab$ ;  $(a - b)^2 = a^2 + b^2 - 2ab$   $\frac{27x^2 - 18x + 3 - 8x^2 - 24x - 18}{6x^2 + 7x - 3} = 5$   $\frac{19x^2 - 42x - 15}{6x^2 + 7x - 3} = 5$   $19x^2 - 42x - 15 = 30x^2 + 35x - 15$  cross multiplying  $11 x^2 + 77x = 0$  11x(x + 7) = 0 taking 11x common 11x = 0 or (x + 7) = 0x = 0 or x = -7

Hence the roots of equation are 0, - 7

### **Question: 66**

Solve each of the

#### Solution:

Given:  $3\left(\frac{7x+1}{5x-3}\right) - 4\left(\frac{5x-3}{7x+1}\right) = 11$  $\frac{3(7x+1)^2 - 4(5x-3)^2}{(7x+1)(5x-3)} = 11 \text{ taking LCM; using } (a + b)^2 = a^2 + b^2 + 2ab$   $\frac{3(49x^2 + 14x + 1) - 4(25x^2 - 30x + 9)}{(7x+1)(5x-3)} = 11$   $\frac{147x^2 + 42x + 3 - 100x^2 + 120x - 36}{35x^2 - 16x - 3} = 11$   $\frac{47x^2 + 162x - 33}{35x^2 - 16x - 3} = 11$   $47x^2 + 162x - 33 = 385x^2 - 176x - 33 \text{ cross multiplying}$   $338x^2 - 338x = 0$  338x(x - 1) = 0 taking 338x common 338x = 0 or (x - 1) = 0 x = 1 or x = 0Hence the roots of equation are 1, 0

**Question: 67** 

Solve each of the

#### Solution:

Given:  $\left(\frac{4x-3}{2x+1}\right) - 10\left(\frac{2x+1}{4x-2}\right) = 3$  $\frac{(4x-3)^2-10(2x+1)^2}{(2x+1)(4x-3)} = 3 \text{ taking LCM; using } (a+b)^2 = a^2 + b^2 + 2ab$  $\frac{(16x^2 - 24x + 9) - 10(4x^2 + 4x + 1)}{8x^2 - 6x + 4x - 3} = 3$  $\frac{16x^2 - 24x + 9 - 40x^2 - 40x - 10}{8x^2 - 6x + 4x - 3} = 3$  $\frac{-24x^2 - 64x - 1}{8x^2 - 6x + 4x - 3} = 3$  $-24x^2 - 64x - 1 = 3(8x^2 - 2x - 3)$  cross multiplying  $-24x^2 - 64x - 1 = 24x^2 - 6x - 9$  $48 x^2 + 58x - 8 = 0$  taking 2 common  $24 x^2 + 29x - 4 = 0$ Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that: Product = a.cFor the given equation a = 24 b = 29 c = -4= 24. - 4 = - 96 And either of their sum or difference = b = 29Thus the two terms are 32 and - 3 Difference = 32 - 3 = 29Product = 32. - 3 = -96 $24 x^2 + 29x - 4 = 0$  $24 x^2 + 32x - 3x - 4 = 0$ 8x(3x + 4) - 1(3x + 4) = 0(3x + 4)(8x - 1) = 0(3x + 4) = 0 or (8x - 1) = 0 $x = \frac{-4}{3}$  or  $x = \frac{1}{8}$ Hence the roots of equation are  $\frac{-4}{3}$  or  $\frac{1}{8}$ **Ouestion: 68** Solve each of the Solution:

Given: 
$$\left(\frac{x}{x+1}\right)^2 - 5\left(\frac{x}{x+1}\right) + 6 = 0 \cdots \cdots (1)$$
  
Let  $\frac{x}{x+1} = y$   
 $y^2 - 5y + 6 = 0$  substituting value for y in (1)

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1 b = -5 c = 6= 1.6 = 6And either of their sum or difference = b= - 5 Thus the two terms are - 3 and - 2 Difference = -3 - 2 = -5Product = -3. -2 = 6 $y^2 - 5y + 6 = 0$  $y^2 - 3y - 2y + 6 = 0$ y(y - 3) - 2(y - 3) = 0(y - 3)(y - 2) = 0(y - 3) = 0 or (y - 2) = 0y = 3 or y = 2Case I: if y = 3 $\frac{x}{x+1} = 3$ x = 3x + 32x + 3 = 0x = -3/2Case II: if y = 2 $\frac{x}{x+1} = 2$ x = 2x + 2x = - 2  $x = \frac{-3}{2}$  or = -2Hence the roots of equation are  $\frac{-3}{2}$  or -2

#### **Question: 69**

Solve each of the

### Solution:

Given: 
$$\frac{a}{(x-b)} + \frac{b}{(x-a)} = 2$$
  
 $\frac{a}{(x-b)} + \frac{b}{(x-a)} - 2 = 0$   
 $\left[\frac{a}{(x-b)} - 1\right] + \left[\frac{b}{(x-a)} - 1\right] = 0$ 

taking - 1 with both terms

$$\frac{a - (x - b)}{(x - b)} + \frac{b - (x - a)}{(x - a)} = 0$$

taking LCM

$$(a-x+b)\left[\frac{1}{(x-b)}+\frac{1}{(x-a)}\right] = 0$$

taking common (a - x - b)

$$(a-x + b)\left[\frac{(x-a) + (x-b)}{(x-b)(x-a)}\right] = 0$$

taking LCM

(a - x + b)[2x - (a + b)] = 0(a - x + b) = 0 or [2x - (a + b)] = 0 $x = a + b \text{ or } x = \frac{a + b}{2}$ 

Hence the roots of equation are a + b or  $\frac{a+b}{2}$ 

### **Question: 70**

Solve each of the

### Solution:

Given: 
$$\frac{a}{(ax-1)} + \frac{b}{(bx-1)} = (a + b)$$
  
 $\frac{a}{(ax-1)} + \frac{b}{(bx-1)} - a - b = 0$   
 $\left[\frac{a}{(ax-1)} - b\right] + \left[\frac{b}{(bx-1)} - a\right] = 0$   
 $\frac{a - b(ax-1)}{(ax-1)} + \frac{b - a(bx-1)}{(bx-1)} = 0$ 

taking LCM

$$\frac{a - bax + b}{(ax - 1)} + \frac{b - abx + a}{(bx - 1)} = 0$$
  
(a + b - abx)  $\left[\frac{1}{(ax - 1)} + \frac{1}{(bx - 1)}\right] = 0$ 

taking common (a + b - abx)

$$(a + b - abx) \left[ \frac{(bx - 1) + (ax - 1)}{(ax - 1)(bx - 1)} \right] = 0$$

taking LCM

$$(a + b - abx)\left[\frac{(a + b)x - 2}{(ax - 1)(bx - 1)}\right] = 0$$
  
(a + b - abx)[(a + b)x - 2] = 0  
(a + b - abx) = 0 or [(a + b)x - 2] = 0  
$$x = \frac{a + b}{ab} \text{ or } x = \frac{2}{a + b}$$

Hence the roots of equation are  $\frac{a+b}{ab}$  or  $\frac{2}{a+b}$ 

#### **Question: 71**

Solve each of the

### Solution:

Given:  $3^{(x + 2)} + 3^{-x} = 10$   $3^x \cdot 3^2 + \frac{1}{3^x} = 10 - \dots + (1)$ Let  $3^x = y - \dots + (2)$   $9y + \frac{1}{y} = 10$  substituting for y in (1)  $9y^2 - 10y + 1 = 0$ Using the splitting middle term - the middle term - te

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 9 b = -10 c = 1

= 9.1 = 9

And either of their sum or difference = b

= - 10

Thus the two terms are - 9 and - 1  $\,$ 

Sum = - 9 - 1 = - 10

Product = -9. -1 = 9

 $9y^2 - 9y - 1y + 1 = 0$ 

9y(y - 1) - 1(y - 1) = 0

(y - 1) (9y - 1) = 0

$$(y - 1) = 0 \text{ or } (9y - 1) = 0$$

y = 1 or y = 1/9

 $3^{x} = 1$  or  $3^{x} = 1/9$ 

On putting value of y in equation (2)

 $3^{x} = 3^{0}$  or  $3^{x} = 3^{-2}$ 

x = 0 or x = -2

Hence the roots of equation are 0, - 2

### **Question: 72**

Solve each of the

### Solution:

Given:  $4^{(x + 1)} + 4^{(1 - x)} = 10$   $4^{x} \cdot 4 + 4 \cdot \frac{1}{4^{x}} = 10 \cdot \dots \cdot (1)$ Let  $4^{x} = y \cdot \dots \cdot (2)$   $4y + \frac{4}{y} = 10$  substituting for y in (1)  $4y^{2} \cdot 10y + 4 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is

divided in two such values that: Product = a.cFor the given equation a = 4 b = -10 c = 4= 4.4 = 16And either of their sum or difference = b = -10Thus the two terms are - 8 and - 2 Sum = - 8 - 2 = - 10 Product = -8. -2 = 16 $4y^2 - 10y + 4 = 0$  $4y^2 - 8y - 2y + 4 = 0$ 4y(y - 2) - 2(y - 2) = 0(y - 2) (4y - 2) = 0(y - 2) = 0 or (4y - 2) = 0y = 2 or y = 1/2substituting the value of y in (2)  $4^{x} = 2 \text{ or } 4^{x} = 2^{-1}$  $2^{2x} = 2^1$  or  $2^{2x} = 2^{-1}$ 2x = 1 or 2x = -1 $x = \frac{1}{2} \text{ or } x = \frac{-1}{2}$ 

Hence the roots of equation are  $\frac{1}{2}$  or  $\frac{-1}{2}$ 

# **Question: 73**

Solve each of the

# Solution:

Given:  $2^{2x} - 3 \cdot 2^{(x+2)} + 32 = 0$  $(2^x)^2 - 3 \cdot 2^x \cdot 2^2 + 32 = 0 - \dots - (1)$ 

Let  $2^{x} = y - \dots + (2)$ 

substituting for y in (1)

 $y^2 - 12y + 32 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -12 c = 32

= 1.32 = 32

And either of their sum or difference = b

= - 12

Thus the two terms are - 8 and - 4  $\,$ 

Sum = - 8 - 4 = - 12

Product = -8. -4 = 32  $y^2 - 8y - 4y + 32 = 0$  y(y - 8) - 4(y - 8) = 0 (y - 8) (y - 4) = 0 (y - 8) = 0 or (y - 4) = 0 y = 8 or y = 4  $2^x = 8$  or  $2^x = 4$ substituting the value of y in (2)  $2^x = 2^3$  or  $2^x = 2^2$  x = 2 or x = 3Hence the roots of equation are 2, 3

# **Exercise : 10B**

### **Question: 1**

Solve each of the

### Solution:

Given:  $x^2 - 6x + 3 = 0$   $x^2 - 6x = -3$   $x^2 - 2.x.3 + 3^2 = -3 + 3^2$  (adding 3<sup>2</sup> on both sides)  $(x - 3)^2 = -3 + 9 = 6$  using  $a^2 - 2ab + b^2 = (a - b)^2$   $x - 3 = \pm \sqrt{6}$  (taking square root on both sides)  $x - 3 = \sqrt{6}$  or  $x - 3 = -\sqrt{6}$ 

 $x = 3 + \sqrt{6} \text{ or } x = 3 - \sqrt{6}$ 

Hence the roots of equation are  $3 + \sqrt{6}$  or  $3 - \sqrt{6}$ 

# **Question: 2**

Solve each of the

# Solution:

Given:  $x^2 - 4x + 1 = 0$   $x^2 - 4x = -1$   $x^2 - 2.x.2 + 2^2 = -1 + 2^2$  (adding  $2^2$  on both sides)  $(x - 2)^2 = -1 + 4 = 3$  using  $a^2 - 2ab + b^2 = (a - b)^2$  $x - 2 = \pm\sqrt{3}$  (taking square root on both sides)

$$x - 2 = \sqrt{3} \text{ or } x - 2 = -\sqrt{3}$$

$$x = 2 + \sqrt{3} \text{ or } x = 2 - \sqrt{3}$$

Hence the roots of equation are 2 +  $\sqrt{3}$  or 2 -  $\sqrt{3}$ 

### **Question: 3**

Solve each of the

Given:  $x^2 + 8x - 2 = 0$   $x^2 + 8x = 2$   $x^2 + 2.x.4 + 4^2 = 2 + 4^2$  (adding 4<sup>2</sup> on both sides)  $(x + 4)^2 = 2 + 16 = 18$  using a<sup>2</sup> + 2ab + b<sup>2</sup> = (a + b)<sup>2</sup>  $x + 4 = \pm\sqrt{18} = \pm 3\sqrt{2}$  (taking square root on both sides)  $x + 4 = 3\sqrt{2}$  or  $x + 4 = -3\sqrt{2}$   $x = -4 + 3\sqrt{2}$  or  $x = -4 - 3\sqrt{2}$ Hence the roots of equation are  $-4 + 3\sqrt{2}$  or  $-4 - 3\sqrt{2}$ 

#### **Question: 4**

Solve each of the

#### Solution:

Given:  $4x^2 + 4\sqrt{3}x + 3 = 0$   $4x^2 + 4\sqrt{3}x = -3$   $(2x)^2 + 2.2x.\sqrt{3} + (\sqrt{3})^2 = -3 + (\sqrt{3})^2$  (adding  $(\sqrt{3})^2$  on both sides)  $(2x + \sqrt{3})^2 = -3 + 3$  using  $a^2 + 2ab + b^2 = (a + b)^2$   $(2x + \sqrt{3})^2 = 0$   $(2x + \sqrt{3})(2x + \sqrt{3}) = 0$  $x = \frac{-\sqrt{3}}{2}$  or  $x = \frac{-\sqrt{3}}{2}$ 

Hence the equation has repeated roots  $\frac{-\sqrt{3}}{2}$ 

### **Question:** 5

Solve each of the

## Solution:

Given:  $2x^2 + 5x - 3 = 0$ 

 $4x^2 + 10x - 6 = 0$  (multiplying both sides by 2)

$$4x^2 + 10x = 6$$

 $(2x)^{2} + 2.2x \cdot \frac{5}{2} + \left(\frac{5}{2}\right)^{2} = 6 + \left(\frac{5}{2}\right)^{2} (adding \left(\frac{5}{2}\right)^{2} on both sides)$   $\left(2x + \frac{5}{2}\right)^{2} = 6 + \frac{25}{4} using a^{2} + 2ab + b^{2} = (a + b)^{2}$   $\left(2x + \frac{5}{2}\right)^{2} = \frac{25 + 24}{4} = \frac{49}{4} = \left(\frac{7}{2}\right)^{2}$   $2x + \frac{5}{2} = \pm \frac{7}{2} (taking square root on both sides)$   $2x + \frac{5}{2} = \frac{7}{2} \text{ or } 2x + \frac{5}{2} = -\frac{7}{2}$ 

$$2x = \frac{7}{2} - \frac{5}{2} \text{ or } 2x = -\frac{7}{2} - \frac{5}{2}$$
$$2x = 1 \text{ or } 2x = -6$$
$$x = \frac{1}{2} \text{ or } x = -3$$

Hence the roots of equation are  $x = \frac{1}{2}$  or x = -3

# **Question: 6**

Solve each of the

### Solution:

Given:  $3x^2 - x - 2 = 0$  $9x^2 - 3x - 6 = 0$  (multiplying both sides by 3)

 $9x^2 - 3x = 6$ 

$$(3x)^{2} - 2.3x \cdot \frac{1}{2} + \left(\frac{1}{2}\right)^{2} = 6 + \left(\frac{1}{2}\right)^{2} (adding \left(\frac{1}{2}\right)^{2} on both sides)$$

$$\left(3x - \frac{1}{2}\right)^{2} = 6 + \frac{1}{4} = \frac{25}{4} = \left(\frac{5}{2}\right)^{2} using a^{2} - 2ab + b^{2} = (a - b)^{2}$$

$$3x - \frac{1}{2} = \pm \frac{5}{2} (taking square root on both sides)$$

$$3x - \frac{1}{2} = \frac{5}{2} \text{ or } 3x - \frac{1}{2} = -\frac{5}{2}$$

$$3x = \frac{5}{2} + \frac{1}{2} = \frac{6}{2} = 3 \text{ or } 3x = -\frac{5}{2} + \frac{1}{2} = -\frac{4}{2} = -2$$

$$x = 1 \text{ or } x = \frac{-2}{3}$$

Hence the roots of equation are1 or  $\frac{-2}{3}$ 

### **Question:** 7

Solve each of the

### Solution:

Given:  $8x^2 - 14x - 15 = 0$ 

 $16x^2 - 28x - 30 = 0$  (multiplying both sides by 2)

$$16x^2 - 28x = 30$$

$$(4x)^{2} - 2.4x \cdot \frac{7}{2} + \left(\frac{7}{2}\right)^{2} = 30 + \left(\frac{7}{2}\right)^{2} (adding \left(\frac{7}{2}\right)^{2} on both sides)$$

$$\left(4x - \frac{7}{2}\right)^{2} = 30 + \frac{49}{4} = \frac{169}{4} = \left(\frac{13}{2}\right)^{2} using a^{2} - 2ab + b^{2} = (a - b)^{2}$$

$$4x - \frac{7}{2} = \pm \frac{13}{2} (taking square root on both sides)$$

$$4x - \frac{7}{2} = \frac{13}{2} \text{ or } 4x - \frac{7}{2} = -\frac{13}{2}$$

$$4x = \frac{13}{2} + \frac{7}{2} = \frac{20}{2} = 10 \text{ or } 4x = -\frac{13}{2} + \frac{7}{2} = -\frac{6}{2} = -3$$

$$x = \frac{5}{2} \text{ or } x = \frac{-3}{4}$$

Hence the roots of equation are  $\frac{5}{2}$  or  $\frac{-3}{4}$ 

#### **Question: 8**

Solve each of the

#### Solution:

Given:  $7x^2 + 3x - 4 = 0$ 

 $49x^2 + 21x - 28 = 0$  (multiplying both sides by 7)

$$(7x)^{2} + 2.7x \cdot \frac{3}{2} + \left(\frac{3}{2}\right)^{2} = 28 + \left(\frac{3}{2}\right)^{2} (adding \left(\frac{3}{2}\right)^{2} on both sides)$$

$$\left(7x + \frac{3}{2}\right)^{2} = 28 + \frac{9}{4} = \frac{121}{4} = \left(\frac{11}{2}\right)^{2} using a^{2} + 2ab + b^{2} = (a + b)^{2}$$

$$7x + \frac{3}{2} = \pm \frac{11}{2} (taking square root on both sides)$$

$$7x + \frac{3}{2} = \frac{11}{2} \text{ or } 7x + \frac{3}{2} = -\frac{11}{2}$$

$$7x = \frac{11}{2} - \frac{3}{2} = \frac{8}{2} = 4 \text{ or } 7x = -\frac{11}{2} - \frac{3}{2} = \frac{-14}{2} = -7$$

$$x = -1 \text{ or } x = \frac{4}{7}$$

Hence the roots of equation are  $-1 \text{ or } \frac{4}{7}$ 

### **Question: 9**

Solve each of the

# Solution:

Given:  $3x^2 - 2x - 1 = 0$  $9x^2 - 6x = 3$  (multiplying both sides by 3)  $(3x)^2 - 2.3x \cdot 1 + (1)^2 = 3 + (1)^2$  (adding (1)<sup>2</sup> on both sides)  $(3x-1)^2 = 3 + 1 = 4 = (2)^2 using a^2 - 2ab + b^2 = (a - b)^2$  $3x - 1 = \pm 2$  (taking square root on both sides) 3x - 1 = 2 or 3x - 1 = -23x = 3 or 3x = -1 $x = -1 \text{ or } x = \frac{-1}{3}$ Hence the roots of equation are -1 or  $\frac{-1}{3}$ **Ouestion: 10** 

Solve each of the

## Solution:

Given:  $5x^2 - 6x - 2 = 0$  $25x^2 - 30x - 10 = 0$  (multiplying both sides by 5)  $25x^2 - 30x = 10$  $(5x)^2 - 2.5x.3 + (3)^2 = 10 + (3)^2$  (adding (3)<sup>2</sup>on both sides)  $(5x-2)^2 = 10 + 9 = 19$  using  $a^2 - 2ab + b^2 = (a - b)^2$ 

 $5x - 3 = \pm \sqrt{19}$  (taking square root on both sides)

$$5x - 3 = \sqrt{19} \text{ or } 5x - 3 = -\sqrt{19}$$
$$5x = 3 + \sqrt{19} \text{ or } 5x = 3 - \sqrt{19}$$
$$x = \frac{3 + \sqrt{19}}{5} \text{ or } x = \frac{3 - \sqrt{19}}{5}$$

Hence the roots of equation are  $\frac{3+\sqrt{19}}{5}$  or  $\frac{3-\sqrt{19}}{5}$ 

### **Question: 11**

Solve each of the

#### Solution:

Given:  $\frac{2}{x^2} - \frac{5}{x} + 2 = 0$   $\frac{2 - 5x + 2x^2}{x^2} = 0$   $2x^2 - 5x + 2 = 0$   $4x^2 - 10x + 4 = 0$   $4x^2 - 10x = -4$  (multiplying both sides by 2)  $(2x)^2 - 2.2x \cdot \frac{5}{2} + (\frac{5}{2})^2 = -4 + (\frac{5}{2})^2$  (adding  $(\frac{5}{2})^2$  on both sides)  $(2x - \frac{5}{2})^2 = -4 + \frac{25}{4} = \frac{9}{4} = (\frac{3}{2})^2$  using  $a^2 - 2ab + b^2 = (a - b)^2$   $2x - \frac{5}{2} = \pm \frac{3}{2}$  (taking square root on both sides)  $2x - \frac{5}{2} = \frac{3}{2}$  or  $2x - \frac{5}{2} = -\frac{3}{2}$   $2x = \frac{3}{2} + \frac{5}{2} = \frac{8}{2} = 4$  or  $2x = -\frac{3}{2} + \frac{5}{2} = \frac{2}{2} = 1$ x = 2 or  $x = \frac{1}{2}$ 

Hence the roots of equation are 2 or  $\frac{1}{2}$ 

# **Question: 12**

Solve each of the

## Solution:

 $4x^{2} + 4bx = (a^{2} - b^{2})$   $(2x)^{2} + 2.2x \cdot b + b^{2} = a^{2} - b^{2} + b^{2} \text{ (adding b}^{2}\text{ on both sides)}$   $(2x + b)^{2} = a^{2} \text{ using } a^{2} + 2ab + b^{2} = (a + b)^{2}$   $2x + b = \pm a \text{ (taking square root on both sides)}$  2x + b = -a or 2x + b = a

$$x = \frac{-(a+b)}{2} \text{ or } x = \frac{a-b}{2}$$

Hence the roots of equation are  $\frac{-(a+b)}{2}$  or  $\frac{a-b}{2}$ 

#### **Question: 13**

Solve each of the

#### Solution:

Given : 
$$x^2 - (\sqrt{2} + 1)x + \sqrt{2} = 0$$
  
 $x^2 - (\sqrt{2} + 1)x = -\sqrt{2}$   
 $x^2 - 2.x.(\frac{\sqrt{2}+1}{2}) + (\frac{\sqrt{2}+1}{2})^2 = -\sqrt{2} + (\frac{\sqrt{2}+1}{2})^2 (adding(\frac{\sqrt{2}+1}{2})^2 on both sides)$   
 $\left(x - (\frac{\sqrt{2}+1}{2})\right)^2 = \frac{-4\sqrt{2}+2+1+2\sqrt{2}}{4} = \frac{2-2\sqrt{2}+1}{4} = (\frac{\sqrt{2}-1}{2})^2 using a^2 - 2ab + b^2 = (a - b)^2$   
 $x - (\frac{\sqrt{2}+1}{2}) = (\frac{\sqrt{2}+1}{2}) or x - (\frac{\sqrt{2}+1}{2}) = -(\frac{\sqrt{2}+1}{2}) taking square root on both sides$   
 $x = (\frac{\sqrt{2}+1}{2}) + (\frac{\sqrt{2}-1}{2}) or x = (\frac{\sqrt{2}+1}{2}) - (\frac{\sqrt{2}-1}{2})$   
 $x = \sqrt{2} or x = 1$ 

Hence the roots of equation are  $\sqrt{2}$  or 1

### **Question: 14**

Solve each of the

#### Solution:

Given:  $\sqrt{2}x^2 - 3x - 2\sqrt{2} = 0$   $2x^2 - 3\sqrt{2}x - 4 = 0$  (multiplying both sides by  $\sqrt{2}$ )  $2x^2 - 3\sqrt{2}x = 4$   $(\sqrt{2}x)^2 - 2.\sqrt{2}x.\frac{3}{2} + (\frac{3}{2})^2 = 4 + (\frac{3}{2})^2$  [Adding  $(\frac{3}{2})^2$  on both sides]  $(\sqrt{2}x - \frac{3}{2})^2 = 4 + \frac{9}{4} = \frac{25}{4} = (\frac{5}{2})^2$  using  $a^2 - 2ab + b^2 = (a - b)^2$   $\sqrt{2}x - \frac{3}{2} = \pm \frac{5}{2}$  (taking square root on both sides)  $\sqrt{2}x - \frac{3}{2} = \frac{5}{2}$  or  $\sqrt{2}x - \frac{3}{2} = -\frac{5}{2}$   $\sqrt{2}x = \frac{5}{2} + \frac{3}{2} = \frac{8}{2} = 4$  or  $\sqrt{2}x = -\frac{5}{2} + \frac{3}{2} = -1$   $\sqrt{2}x = 4$  or  $\sqrt{2}x = -1$  $x = \frac{4}{\sqrt{2}} = 2\sqrt{2}$  or  $x = \frac{-1}{\sqrt{2}}$ 

Hence the roots of equation are  $2\sqrt{2}$  or  $\frac{-1}{\sqrt{2}}$ 

# **Question: 15**

Solve each of the

### Solution:

Given:  $\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$ 

 $3x^2$  +  $10\sqrt{3}x$  + 21 = 0 (multiplying both sides with  $\sqrt{3}$  )

 $3x^{2} + 10\sqrt{3}x = -21$   $(\sqrt{3}x)^{2} + 2.\sqrt{3}x.5 + 5^{2} = -21 + 5^{2} [Adding 5^{2}on both sides]$   $(\sqrt{3}x + 5)^{2} = -21 + 25 = 4 = 2^{2} using a^{2} + 2ab + b^{2} = (a + b)^{2}$   $\sqrt{3}x + 5 = \pm 2 (taking square root on both sides)$   $\sqrt{3}x + 5 = 2 \text{ or } \sqrt{3}x + 5 = -2$   $\sqrt{3}x = 2 - 5 \text{ or } \sqrt{3}x = -2 - 5$   $\sqrt{3}x = -3 \text{ or } \sqrt{3}x = -7$  $x = -\sqrt{3} \text{ or } x = \frac{-7}{\sqrt{3}}$ 

Hence the roots of equation are  $-\sqrt{3}$  or  $\frac{-7}{\sqrt{3}}$ 

#### **Question: 16**

By using the meth

#### Solution:

 $2x^{2} + x + 4 = 0$   $4x^{2} + 2x + 8 = 0 \text{ (multiplying both sides by 2)}$   $4x^{2} + 2x = -8$   $(2x)^{2} + 2.2x \cdot \frac{1}{2} + \left(\frac{1}{2}\right)^{2} = -8 + \left(\frac{1}{2}\right)^{2} [\text{Adding} \left(\frac{1}{2}\right)^{2} \text{ on both sides}]$   $\left(2x + \frac{1}{2}\right)^{2} = -8 + \frac{1}{4} = -\frac{31}{4} < 0 \text{ using } a^{2} + 2ab + b^{2} = (a + b)^{2}$ But  $\left(2x + \frac{1}{2}\right)^{2}$  cannot be negative for any real value of x So there is no real value of x satisfying the given equation. Hence the given equation has no real roots.

# **Exercise : 10C**

#### **Question: 1 A**

Find the discrimi

#### Solution:

Given:  $2x^2 - 7x + 6 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 2, b = - 7, c = 6

Discriminant D =  $b^2 - 4ac$ 

 $= (-7)^2 - 4.2.6$ 

= 49 - 48 = 1

#### **Question: 1 B**

Find the discrimi

#### Solution:

Given:  $3x^2 - 2x + 8 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 3, b = - 2, c = 8

Discriminant D =  $b^2 - 4ac$ 

 $= (-2)^2 - 4.3.8$ 

= 4 - 96 = - 92

# **Question: 1 C**

Find the discrimi

### Solution:

Given:  $2x^2 - 5\sqrt{2}x + 4 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 2b = -5\sqrt{2}c = 4$$

Discriminant D =  $b^2 - 4ac$ 

$$=(-5\sqrt{2})^2-4.2.4$$

= 50 - 32 = 18

# **Question: 1 D**

Find the discrimi

# Solution:

Given:  $\sqrt{3}x^2 + 2\sqrt{2}x - 2\sqrt{3} = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = \sqrt{3} b = 2\sqrt{2} c = -2\sqrt{3}$$

Discriminant D =  $b^2 - 4ac$ 

$$=(2\sqrt{2})^2-4.\sqrt{3}.-2\sqrt{3}$$

= 8 + 24 = 32

### **Question: 1 E**

Find the discrimi

## Solution:

Given: (x - 1)(2x - 1) = 0

 $2x^2 - 3x + 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 2, b = -3, c = -1

Discriminant D =  $b^2 - 4ac$ 

 $= (-3)^2 - 4.2.1$ 

= 9 - 8 = 1

# **Question: 1 F**

Find the discrimi

### Solution:

Given:  $1 - x = 2x^2$ 

 $2x^2 + x - 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

 $= (1)^2 - 4.2. - 1$ 

= 1 + 8 = 9

## **Question: 2**

Find the roots of

## Solution:

Given:  $x^2 - 4x - 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (-4)^2 - 4.1. - 1$$

$$= 16 + 4 = 20 > 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-4) + \sqrt{20}}{2 \times 1} = \frac{4 + 2\sqrt{5}}{2} = \frac{2(2 + \sqrt{5})}{2} = (2 + \sqrt{5})$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-4) - \sqrt{20}}{2 \times 1} = \frac{4 - 2\sqrt{5}}{2} = \frac{2(2 - \sqrt{5})}{2} = (2 - \sqrt{5})$$
$$x = (2 + \sqrt{5}) \text{ or } x = (2 - \sqrt{5})$$

Hence the roots of equation are  $(2 + \sqrt{5})$  or  $(2 - \sqrt{5})$ 

# **Question: 3**

Find the roots of

### Solution:

Given:  $x^2 - 6x + 4 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (6)^2 - 4.1.4$$

$$= 36 - 16 = 20 > 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-6) + \sqrt{20}}{2 \times 1} = \frac{6 + 2\sqrt{5}}{2} = \frac{2(3 + \sqrt{5})}{2} = (3 + \sqrt{5})$$

$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-6) - \sqrt{20}}{2 \times 1} = \frac{6 - 2\sqrt{5}}{2} = \frac{2(3 - \sqrt{5})}{2} = (3 - \sqrt{5})$$
$$x = (3 + \sqrt{5}) \text{ or } x = (3 - \sqrt{5})$$

Hence the roots of equation are  $(3 + \sqrt{5})$  or  $(3 - \sqrt{5})$ 

### **Question: 4**

Find the roots of

### Solution:

Given:  $2x^2 + x - 4 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 2, b = 1, c = -4$$

Discriminant D =  $b^2 - 4ac$ 

$$= (1)^2 - 4.2. - 4$$

$$= 1 + 32 = 33 > 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-1 + \sqrt{33}}{2 \times 2} = \frac{-1 + \sqrt{33}}{4}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-1 - \sqrt{33}}{2 \times 2} = \frac{-1 - \sqrt{33}}{4}$$
$$x = \frac{-1 + \sqrt{33}}{4} \text{ or } x = \frac{-1 - \sqrt{33}}{4}$$

Hence the roots of equation are  $\frac{-1+\sqrt{33}}{4}$  or  $\frac{-1-\sqrt{33}}{4}$ 

## **Question: 5**

Find the roots of

#### Solution:

Given:  $25x^2 + 30x + 7 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 25, b = 30, c = 7

Discriminant D =  $b^2 - 4ac$ 

$$= (30)^2 - 4.25.7$$

$$= 900 - 700 = 200 > 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-30 + \sqrt{200}}{2 \times 25} = \frac{-30 + 10\sqrt{2}}{50} = \frac{10(-3 + \sqrt{2})}{50} = \frac{(-3 + \sqrt{2})}{50}$$

$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-30 - \sqrt{200}}{2 \times 25} = \frac{-30 - 10\sqrt{2}}{50} = \frac{10(-3 - \sqrt{2})}{50}$$
$$= \frac{(-3 - \sqrt{2})}{5}$$
$$x = \frac{(-3 + \sqrt{2})}{5} \text{ or } x = \frac{(-3 - \sqrt{2})}{5}$$

Hence the roots of equation are  $\frac{(-3+\sqrt{2})}{5}$  or  $\frac{(-3-\sqrt{2})}{5}$ 

### **Question: 6**

Find the roots of

# Solution:

Given:  $16x^2 = 24x + 1$ 

 $16x^2 - 24x - 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (-24)^2 - 4.16. - 1$$

$$= 576 + 64 = 640 > 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-24) + \sqrt{640}}{2 \times 16} = \frac{24 + 8\sqrt{10}}{32} = \frac{8(3 + \sqrt{10})}{32}$$
$$= \frac{(3 + \sqrt{10})}{4}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-24) - \sqrt{640}}{2 \times 16} = \frac{24 - 8\sqrt{10}}{32} = \frac{8(3 - \sqrt{10})}{32}$$
$$= \frac{(3 - \sqrt{10})}{4}$$
$$x = \frac{(3 + \sqrt{10})}{4} \text{ or } x = \frac{(3 - \sqrt{10})}{4}$$

Hence the roots of equation are  $\frac{(3+\sqrt{10})}{4}$  or  $\frac{(3-\sqrt{10})}{4}$ 

### **Question:** 7

Find the roots of

# Solution:

Given:  $15x^2 - 28 = x$ 

 $15x^2 - x - 28 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

 $= (-1)^2 - 4.15. - 28$ 

= 1 + 1680 = 1681 > 0

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-1) + \sqrt{1681}}{2 \times 15} = \frac{1 + 41}{30} = \frac{42}{30} = \frac{7}{5}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-1) - \sqrt{1681}}{2 \times 15} = \frac{1 - 41}{30} = \frac{-40}{30} = \frac{-4}{30}$$
$$x = \frac{7}{5} \text{ or } x = \frac{-4}{3}$$

Hence the roots of equation are  $\frac{7}{5}$  or  $\frac{-4}{3}$ 

### **Question: 8**

Find the roots of

#### Solution:

Given:  $2x^2 - 2\sqrt{2}x + 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 2b = -2\sqrt{2}c = 1$$

Discriminant D =  $b^2 - 4ac$ 

$$=(-2\sqrt{2})^2-4.2.1$$

$$= 8 - 8 = 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-2\sqrt{2})}{2 \times 2} = \frac{2\sqrt{2}}{4} = \frac{\sqrt{2}}{2} = \frac{\sqrt{2}}{\sqrt{2}\sqrt{2}} = \frac{1}{\sqrt{2}}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-2\sqrt{2})}{2 \times 2} = \frac{2\sqrt{2}}{4} = \frac{\sqrt{2}}{2} = \frac{\sqrt{2}}{\sqrt{2}\sqrt{2}} = \frac{1}{\sqrt{2}}$$
$$x = \frac{1}{\sqrt{2}} \text{ or } x = \frac{1}{\sqrt{2}}$$

Hence these are the repeated roots of the equation  $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$ 

#### **Question: 9**

Find the roots of

### Solution:

Given:  $\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = \sqrt{2}b = 7c = 5\sqrt{2}$$

Discriminant D =  $b^2 - 4ac$ 

$$= (7)^2 - 4.\sqrt{2}.5\sqrt{2}$$

$$= 49 - 40 = 9 > 0$$

Hence the roots of equation are real.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-7 + \sqrt{9}}{2 \times \sqrt{2}} = \frac{-7 + 3}{2 \times \sqrt{2}} = \frac{-4}{2\sqrt{2}} = -\sqrt{2}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-7 - \sqrt{9}}{2 \times \sqrt{2}} = \frac{-7 - 3}{2 \times \sqrt{2}} = \frac{-10}{2\sqrt{2}} = \frac{-5\sqrt{2}}{2}$$
$$x = -\sqrt{2} \text{ or } x = \frac{-5\sqrt{2}}{2}$$

Hence the roots of equation are  $-\sqrt{2}$  or  $\frac{-5\sqrt{2}}{2}$ 

# **Question: 10**

Find the roots of

### Solution:

Given:  $\sqrt{3}x^2 + 10x - 8\sqrt{3} = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = \sqrt{3} b = 10 c = -8\sqrt{3}$$

Discriminant D =  $b^2 - 4ac$ 

$$= (10)^2 - 4.\sqrt{3}.-8\sqrt{3}$$

$$= 100 + 96 = 196 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{196} = 14$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-10 + \sqrt{196}}{2 \times \sqrt{3}} = \frac{-10 + 14}{2 \times \sqrt{3}} = \frac{4}{2\sqrt{3}} = \frac{2}{\sqrt{3}} = \frac{2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$
$$= \frac{2\sqrt{3}}{3}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-10 - \sqrt{196}}{2 \times \sqrt{3}} = \frac{-10 - 14}{2 \times \sqrt{3}} = \frac{-24}{2\sqrt{3}} = \frac{-12}{\sqrt{3}}$$
$$= \frac{-12}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{-12\sqrt{3}}{3} = -4\sqrt{3}$$
$$x = \frac{2\sqrt{3}}{3} \text{ or } x = -4\sqrt{3}$$

Hence the roots of equation are  $\frac{2\sqrt{3}}{3}$  or  $-4\sqrt{3}$ 

### **Question: 11**

Find the roots of

#### Solution:

Given: 
$$\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$$

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = \sqrt{3} b = -2\sqrt{2} c = -2\sqrt{3}$$

$$=(-2\sqrt{2})^2-4.\sqrt{3}.-2\sqrt{3}$$

= 8 + 24 = 32 > 0

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{32} = 4\sqrt{2}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-2\sqrt{2}) + 4\sqrt{2}}{2 \times \sqrt{3}} = \frac{6\sqrt{2}}{2 \times \sqrt{3}} = \frac{2\sqrt{3}\sqrt{3}\sqrt{2}}{2 \times \sqrt{3}} = \sqrt{6}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-2\sqrt{2}) - 4\sqrt{2}}{2 \times \sqrt{3}} = \frac{-2\sqrt{2}}{2 \times \sqrt{3}} = \frac{-\sqrt{2}}{\sqrt{3}}$$
$$x = \sqrt{6} \text{ or } x = \frac{-\sqrt{2}}{\sqrt{3}}$$

Hence the roots of equation are  $\sqrt{6}$  or  $\frac{-\sqrt{2}}{\sqrt{3}}$ 

### **Question: 12**

Find the roots of

# Solution:

Given:  $2x^2 + 6\sqrt{3}x - 60 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 2b = 6\sqrt{3}c = -60$$

Discriminant D =  $b^2 - 4ac$ 

$$= (6\sqrt{3})^2 - 4.2. -60$$

$$= 180 + 480 = 588 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{588} = 14\sqrt{3}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(6\sqrt{3}) + 14\sqrt{3}}{2 \times 2} = \frac{8\sqrt{3}}{4} = 2\sqrt{3}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(6\sqrt{3}) - 14\sqrt{3}}{2 \times 2} = \frac{-20\sqrt{3}}{4} = -5\sqrt{3}$$
$$x = 2\sqrt{3} \text{ or } x = -5\sqrt{3}$$

Hence the roots of equation are  $2\sqrt{3}$  or  $-5\sqrt{3}$ 

#### **Question: 13**

Find the roots of

### Solution:

Given  $4\sqrt{3}x^2 + 5x - 2\sqrt{3} = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 4\sqrt{3}b = 5c = -2\sqrt{3}$$

$$=(5)^2-4.4\sqrt{3}.-2\sqrt{3}$$

= 25 + 96 = 121 > 0

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{121} = 11$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-5 + 11}{2 \times 4\sqrt{3}} = \frac{6}{8 \times \sqrt{3}} = \frac{3}{4 \times \sqrt{3}} = \frac{\sqrt{3}}{4}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-5 - 11}{2 \times 4\sqrt{3}} = \frac{-16}{8 \times \sqrt{3}} = \frac{-2}{\sqrt{3}}$$
$$x = \frac{\sqrt{3}}{4} \text{ or } x = \frac{-2}{\sqrt{3}}$$

Hence the roots of equation are  $\frac{\sqrt{3}}{4}$  or  $\frac{-2}{\sqrt{3}}$ 

### **Question: 14**

Find the roots of

### Solution:

Given:  $3x^2 - 2\sqrt{6}x + 2 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 3b = -2\sqrt{6}c = 2$$

Discriminant D =  $b^2 - 4ac$ 

$$= (-2\sqrt{6})^2 - 4.3.2$$

$$= 24 - 24 = 0$$

$$\sqrt{D} = 0$$

Hence the roots of equation are real and repeated.

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-2\sqrt{6}) + 0}{2 \times 3} = \frac{2\sqrt{6}}{6} = \frac{\sqrt{6}}{3} = \frac{\sqrt{2}\sqrt{3}}{\sqrt{2}\sqrt{3}} = \sqrt{\frac{2}{3}}$$

$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-2\sqrt{6}) - 0}{2 \times 3} = \frac{2\sqrt{6}}{6} = \frac{\sqrt{6}}{3} = \frac{\sqrt{2}\sqrt{3}}{\sqrt{2}\sqrt{3}} = \sqrt{\frac{2}{3}}$$

Hence the roots of equation are  $\sqrt{\frac{2}{3}}$ ,  $\sqrt{\frac{2}{3}}$ 

# **Question: 15**

Find the roots of

#### Solution:

Given:  $2\sqrt{3}x^2 - 5x + \sqrt{3} = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 2\sqrt{3}b = -5c = \sqrt{3}$$

 $= (-5)^2 - 4.2\sqrt{3}.\sqrt{3}$ = 25 - 24 = 1 > 0

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{1} = 1$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-5) + 1}{2 \times 2\sqrt{3}} = \frac{6}{4 \times \sqrt{3}} = \frac{\sqrt{3}}{2}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-5) - 1}{2 \times 2\sqrt{3}} = \frac{4}{4 \times \sqrt{3}} = \frac{1}{\sqrt{3}}$$
$$x = \frac{\sqrt{3}}{2} \text{ or } x = \frac{1}{\sqrt{3}}$$

Hence the roots of equation are  $\frac{\sqrt{3}}{2}$  or  $\frac{1}{\sqrt{3}}$ 

### **Question: 16**

Find the roots of

### Solution:

Given:  $x^2 + x + 2 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

 $= (1)^2 - 4.1.2$ 

= 1 - 8 = - 7 < 0

Hence the roots of equation do not exist

### **Question: 17**

Find the roots of

### Solution:

Given:  $2x^2 + ax - a^2 = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 2, B = a, C = -a^2$$

Discriminant D =  $B^2 - 4AC$ 

$$= (a)^2 - 4.2. - a^2$$

$$= a^2 + 8 a^2 = 9a^2 \ge 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{9a^2} = 3a$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-a + 3a}{2 \times 2} = \frac{2a}{4} = \frac{a}{2}$$

$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-a - 3a}{2 \times 2} = \frac{-4a}{4} = -a$$
$$x = \frac{a}{2} \text{ or } x = -a$$

Hence the roots of equation are  $\frac{a}{2}$  or -a

#### **Question: 18**

Find the roots of

# Solution:

Given:  $x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 1b = -(\sqrt{3} + 1)c = \sqrt{3}$$

Discriminant D =  $b^2 - 4ac$ 

$$D = \left[ -\left(\sqrt{3} + 1\right) \right]^2 - 4.1 \cdot \sqrt{3} = 3 + 1 + 2\sqrt{3} - 4\sqrt{3} = 3 - 2\sqrt{3} + 1$$
$$D = \left(\sqrt{3} - 1\right)^2 > 0$$
Using a<sup>2</sup> - 2ab + b<sup>2</sup> = (a - b)<sup>2</sup>

Thus the roots of given equation are real.

$$\sqrt{D} = \sqrt{3} - 1$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-[-(\sqrt{3} + 1)] + (\sqrt{3} - 1)}{2 \times 1} = \frac{\sqrt{3} + 1 + \sqrt{3} - 1}{2}$$
$$= \frac{2\sqrt{3}}{2} = \sqrt{3}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-[-(\sqrt{3} + 1)] - (\sqrt{3} - 1)}{2 \times 1} = \frac{\sqrt{3} + 1 - \sqrt{3} + 1}{2} = \frac{2}{2}$$

 $x = 1 \text{ or } x = \sqrt{3}$ 

Hence the roots of equation are 1,  $\sqrt{3}$ 

# **Question: 19**

Find the roots of

# Solution:

Given:  $2x^2 + 5\sqrt{3}x + 6 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 2b = 5\sqrt{3}c = 6$$

Discriminant D =  $b^2 - 4ac$ 

$$=(5\sqrt{3})^2-4.2.6$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{27} = 3\sqrt{3}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(5\sqrt{3}) + 3\sqrt{3}}{2 \times 2} = \frac{-2\sqrt{3}}{4} = \frac{-\sqrt{3}}{2}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(5\sqrt{3}) - 3\sqrt{3}}{2 \times 2} = \frac{-8\sqrt{3}}{4} = -2\sqrt{3}$$
$$x = \frac{-\sqrt{3}}{2} \text{ or } x = -2\sqrt{3}$$

Hence the roots of equation are  $\frac{-\sqrt{3}}{2}$  ,  $-2\sqrt{3}$ 

# **Question: 20**

Find the roots of

#### Solution:

Given:  $3x^2 - 2x + 2 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 3, b = -2, c = 2$$

Discriminant D =  $b^2 - 4ac$ 

$$= (-2)^2 - 4.3.2$$

= 4 - 24 = -20 < 0

Hence the roots of equation do not exist

#### **Question: 21**

Find the roots of

#### Solution:

Given:  $x + \frac{1}{x} = 3$ 

taking LCM

$$\frac{x^2 + 1}{x} =$$

cross multiplying

3

$$x^2 + 1 = 3x$$

$$x^2 - 3x + 1 = 0$$

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

 $= (-3)^2 - 4.1.1$ 

$$= 9 - 4 = 5 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{5}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-3) + \sqrt{5}}{2 \times 1} = \frac{3 + \sqrt{5}}{2}$$

$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-3) - \sqrt{5}}{2 \times 1} = \frac{3 - \sqrt{5}}{2}$$
$$x = \frac{3 + \sqrt{5}}{2} \text{ or } x = \frac{3 - \sqrt{5}}{2}$$

Hence the roots of equation are  $\frac{3+\sqrt{5}}{2}$ ,  $\frac{3-\sqrt{5}}{2}$ 

#### **Question: 22**

Find the roots of

### Solution:

Given:  $\frac{1}{x} - \frac{1}{x-2} = 3$  $\frac{x-2-x}{x(x-2)} = 3$  taking LCM  $\frac{-2}{x^2 - 2x} = 3$ 

 $3x^2 - 6x + 2 = 0$  cross multiplying

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 3, b = -6, c = 2$$

Discriminant D =  $b^2 - 4ac$ 

$$= (-6)^2 - 4.3.2$$
$$= 36 - 24 = 12 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{12} = 2\sqrt{3}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-6) + 2\sqrt{3}}{2 \times 3} = \frac{6 + 2\sqrt{3}}{6} = \frac{3 + \sqrt{3}}{3}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-6) - 2\sqrt{3}}{2 \times 3} = \frac{6 - 2\sqrt{3}}{6} = \frac{3 - \sqrt{3}}{3}$$
$$x = \frac{3 + \sqrt{3}}{3} \text{ or } x = \frac{3 - \sqrt{3}}{3}$$

Hence the roots of equation are  $\frac{3+\sqrt{3}}{3}$  or  $\frac{3-\sqrt{3}}{3}$ 

### **Question: 23**

Find the roots of

# Solution:

Given:  $x - \frac{1}{x} = 3, x \neq 0$ 

 $\frac{x^2-1}{x} = 3$  taking LCM

 $x^2 - 3x - 1 = 0$  cross multiplying

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 1, b = - 3, c = - 1

 $= (-3)^2 - 4.1. - 1$ 

= 9 + 4 = 13 > 0

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{13}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(-3) + \sqrt{13}}{2 \times 1} = \frac{3 + \sqrt{13}}{2}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(-3) - \sqrt{13}}{2 \times 1} = \frac{3 - \sqrt{13}}{2}$$
$$x = \frac{3 + \sqrt{13}}{2} \text{ or } \frac{3 - \sqrt{13}}{2}$$

Hence the roots of equation are  $\frac{3+\sqrt{13}}{2}$  or  $\frac{3-\sqrt{13}}{2}$ 

# **Question: 24**

Find the roots of

# Solution:

Given: 
$$\frac{m}{n}x^2 + \frac{n}{m} = 1 - 2x$$
$$\frac{m^2x^2 + n^2}{mn} = 1 - 2x$$

taking LCM  $m^2x + n^2 = mn - 2mnx$ 

On cross multiplying

$$m^2x + 2mnx + n^2 - mn = 0$$

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = m^2$$
,  $b = 2mn$ ,  $c = n^2 - mn$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (2mn)^2 - 4.m^2. (n^2 - mn)$$

$$= 4m^2n^2 - 4m^2n^2 + 4m^3n > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{4m^3n} = 2m\sqrt{mn}$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-(2mn) + 2m\sqrt{mn}}{2 \times m^2} = \frac{2m(-n + \sqrt{mn})}{2 \times m^2} = \frac{(-n + \sqrt{mn})}{m}$$
$$\beta = \frac{-b - \sqrt{D}}{2a} = \frac{-(2mn) - 2m\sqrt{mn}}{2 \times m^2} = \frac{2m(-n - \sqrt{mn})}{2 \times m^2} = \frac{(-n - \sqrt{mn})}{m}$$
$$x = \frac{(-n + \sqrt{mn})}{m} \text{ or } x = \frac{(-n - \sqrt{mn})}{m}$$

Hence the roots of equation are  $\frac{(-n+\sqrt{mn})}{m}$  or  $\frac{(-n-\sqrt{mn})}{m}$ 

### **Question: 25**

Given:  $36x^2 - 12ax + (a^2 - b^2) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 36, B = -12a, C = a^2 - b^2$$

Discriminant D =  $B^2 - 4AC$ 

 $= (-12a)^2 - 4.36.(a^2 - b^2)$ 

$$= 144a^2 - 144a^2 + 144b^2 = 144b^2 > 0$$

Hence the roots of equation are real.

 $\sqrt{D} = \sqrt{144b^2} = 12b$ 

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-(-12a) + 12b}{2 \times 36} = \frac{12(a+b)}{72} = \frac{(a+b)}{6}$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-(-12a) - 12b}{2 \times 36} = \frac{12(a-b)}{72} = \frac{(a-b)}{6}$$
$$x = \frac{(a+b)}{6} \text{ or } x = \frac{(a-b)}{6}$$

Hence the roots of equation are  $\frac{(a+b)}{6}$  or  $\frac{(a-b)}{6}$ 

### **Question: 26**

Find the roots of

### Solution:

Given:  $x^2 - 2ax + (a^2 - b^2) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 1, B = -2a, C = a^2 - b^2$$

Discriminant D =  $B^2 - 4AC$ 

$$= (-2a)^{2} - 4.1.(a^{2} - b^{2})$$
$$= 4a^{2} - 4a^{2} + 4b^{2} = 4b^{2} > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{4b^2} = 2b$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-(-2a) + 2b}{2 \times 1} = \frac{2(a + b)}{2} = a + b$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-(-2a) - 2b}{2 \times 1} = \frac{2(a - b)}{2} = a - b$$
$$x = (a + b) \text{ or } x = (a - b)$$

Hence the roots of equation are (a + b) or (a - b)

# **Question: 27**

Find the roots of

#### Solution:

Given:  $x^2 - 2ax - (4b^2 - a^2) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 1, B = -2a, C = -(4b^2 - a^2)$$

Discriminant D =  $B^2 - 4AC$ 

$$= (-2a)^2 - 4.1. - (4b^2 - a^2)$$

$$= 4a^2 - 4a^2 + 16b^2 = 16b^2 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{16b^2} = 4b$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-(-2a) + 4b}{2 \times 1} = \frac{2(a + 2b)}{2} = a + 2b$$

$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-(-2a) - 4b}{2 \times 1} = \frac{2(a - 2b)}{2} = a - 2b$$

x = (a + 2b) or x = (a - 2b)

Hence the roots of equation are (a + 2b) or (a - 2b)

### **Question: 28**

Find the roots of

## Solution:

Given:  $x^2 + 6x - (a^2 + b^2 - 8) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

A = 1, B = 6, C = 
$$-(a^2 + b^2 - 8)$$
  
Discriminant D = B<sup>2</sup> - 4AC  
=  $(6)^2 - 4.1. - (a^2 + b^2 - 8)$   
=  $36 + 4a^2 + 8a - 32 = 4a^2 + 8a + 4$   
=  $4(a^2 + 2a + 1)$   
=  $4(a + 1)^2 > 0$  Using  $a^2 + 2ab + b^2 = (a + b)^2$ 

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{4(a + 1)^2}$$
  
= 2(a + 1)

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-6 + 2(a + 1)}{2 \times 1} = \frac{2a - 4}{2} = a - 2$$
  
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-6 - 2(a + 1)}{2 \times 1} = \frac{-2a - 8}{2} = -a - 4 = -(a + 4)$$
  
$$x = (a - 2) \text{ or } x = -(4 + a)$$

Hence the roots of equation are (a - 2) or -(4 + a)

# **Question: 29**

Given:  $x^2 + 5x - (a^2 + a - 6) = 0$ Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$   $A = 1, B = 5, C = -(a^2 + a - 6)$ Discriminant  $D = B^2 - 4AC$   $= (5)^2 - 4.1. - (a^2 + a - 6)$   $= 25 + 4a^2 + 4a - 24 = 4a^2 + 4a + 1$  $= (2a + 1)^2 > 0$  Using  $a^2 + 2ab + b^2 = (a + b)^2$ 

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{(2a + 1)^2}$$
  
= (2a + 1)

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-5 + (2a + 1)}{2 \times 1} = \frac{2a - 4}{2} = a - 2$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-5 - (2a + 1)}{2 \times 1} = \frac{-2a - 6}{2} = -a - 3 = -(a + 3)$$
$$x = (a - 2) \text{ or } x = -(a + 3)$$

Hence the roots of equation are (a - 2) or x = -(a + 3)

### **Question: 30**

Find the roots of

#### Solution:

Given:  $x^2 - 4ax - b^2 + 4a^2 = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 1, B = -4a, C = -b^2 + 4a^2$$

Discriminant D =  $B^2 - 4AC$ 

$$= (-4a)^2 - 4.1. (-b^2 + 4a^2)$$

$$= 16a^2 + 4b^2 - 16a^2 = 4b^2 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{4b^2} = 2b$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-(-4a) + 2b}{2 \times 1} = \frac{4a + 2b}{2} = 2a + b$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-(-4a) - 2b}{2 \times 1} = \frac{4a - 2b}{2} = 2a - b$$
$$x = (2a - b) \text{ or } x = (2a + b)$$

Hence the roots of equation are (2a - b) or (2a + b)

# **Question: 31**

Given:  $4x^2 - 4a^2x + (a^4 - b^4) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 4, B = -4a^2, C = (a^4 - b^4)$$

Discriminant D =  $B^2 - 4AC$ 

$$= (-4a^2)^2 - 4.4. (a^4 - b^4)$$

$$= 16a^4 + 16b^4 - 16a^4 = 16b^4 > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{16b^4} = 4b^2$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-(-4a^2) + 4b^2}{2 \times 4} = \frac{4(a^2 + b^2)}{8} = \frac{a^2 + b^2}{2}$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-(-4a^2) - 4b^2}{2 \times 4} = \frac{4(a^2 - b^2)}{8} = \frac{a^2 - b^2}{2}$$
$$x = \frac{a^2 + b^2}{2} \text{ or } x = \frac{a^2 - b^2}{2}$$

Hence the roots of equation are  $\frac{a^2 + b^2}{2}$ ,  $\frac{a^2 - b^2}{2}$ 

### **Question: 32**

Find the roots of

# Solution:

Given:  $4x^2 + 4bx - (a^2 - b^2) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 4, B = 4b, C = -(a^2 - b^2)$$

Discriminant D =  $B^2 - 4AC$ 

$$= (4b)^{2} - 4.4. - (a^{2} - b^{2})$$
$$= 16b^{2} + 16a^{2} - 16b^{2} = 16 a^{2} > 0$$

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{16a^2} = 4a$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-(4b) + 4a}{2 \times 4} = \frac{4(a - b)}{8} = \frac{a - b}{2}$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-(4b) - 4a}{2 \times 4} = \frac{-4(a + b)}{8} = \frac{-(a + b)}{2}$$
$$x = \frac{-(a + b)}{2} \text{ or } x = \frac{a - b}{2}$$

Hence the roots of equation are  $\frac{-(a+b)}{2}$  or  $\frac{a-b}{2}$ 

### **Question: 33**

Given:  $x^2 - (2b - 1)x + (b^2 - b - 20) = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 1, B = -(2b - 1), C = (b^2 - b - 20)$$

Discriminant D =  $B^2 - 4AC$ 

= 
$$[-(2b-1)^2] - 4.1$$
.  $(b^2 - b - 20)$  Using  $a^2 - 2ab + b^2 = (a - b)^2$ 

 $= 4b^2 - 4b + 1 - 4b^2 + 4b + 80 = 81 > 0$ 

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{81} = 9$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-[-(2b-1)] + 9}{2 \times 1} = \frac{2b + 8}{2} = b + 4$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-[-(2b-1] - 9}{2 \times 1} = \frac{2b - 10}{2} = b - 5$$
$$x = (b + 4) \text{ or } x = (b - 5)$$

Hence the roots of equation are (b + 4) or (b - 5)

### **Question: 34**

Find the roots of

### Solution:

Given:  $3a^2x^2 + 8abx + 4b^2 = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 3a^2$$
,  $B = 8ab$ ,  $C = 4b^2$ 

Discriminant D =  $B^2 - 4AC$ 

$$= (8ab)^2 - 4.3a^2 \cdot 4b^2$$

 $= 64 a^2b^2 - 48a^2b^2 = 16a^2b^2 > 0$ 

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{16a^2b^2}$$
$$= 4ab$$

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-8ab + 4ab}{2 \times 3a^2} = \frac{-4ab}{6a^2} = \frac{-2b}{3a}$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-8ab - 4ab}{2 \times 3a^2} = \frac{-12ab}{6a^2} = \frac{-2b}{a}$$
$$x = \frac{-2b}{3a} \text{ or } x = \frac{-2b}{a}$$

Hence the roots of equation are  $\frac{-2b}{3a}$  or  $x = \frac{-2b}{a}$ 

### **Question: 35**

Given: 
$$a^{2}b^{2}x^{2} - (4b^{4} - 3a^{4})x - 12a^{2}b^{2} = 0$$
  
Comparing with standard quadratic equation  $Ax^{2} + Bx + C =$   
 $A = a^{2}b^{2}, B = -(4b^{4} - 3a^{4}), C = -12a^{2}b^{2}$   
Discriminant  $D = B^{2} - 4AC$   
 $= [-(4b^{4} - 3a^{4})]^{2} - 4a^{2}b^{2}. - 12a^{2}b^{2}$   
 $= 16b^{8} - 24a^{4}b^{4} + 9a^{8} + 48a^{4}b^{4}$   
 $= 16b^{8} + 24a^{4}b^{4} + 9a^{8}$   
 $= (4b^{4} + 3a^{4})^{2} > 0$  Using  $a^{2} + 2ab + b^{2} = (a + b)^{2}$   
Hence the roots of equation are real.

0

$$\sqrt{D} = \sqrt{(4b^4 + 3a^4)^2}$$
  
= 4b<sup>4</sup> + 3a<sup>4</sup>

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-[-(4b^4 - 3a^4)] + (4b^4 + 3a^4)}{2 \times a^2 b^2} = \frac{8b^4}{2a^2 b^2} = \frac{4b^2}{a^2}$$
$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-[-(4b^4 - 3a^4)] - (4b^4 + 3a^4)}{2 \times a^2 b^2} = \frac{-6a^4}{2a^2 b^2} = \frac{-3a^2}{b^2}$$
$$x = \frac{4b^2}{a^2} \text{ or } x = \frac{-3a^2}{b^2}$$

Hence the roots of equation are  $\frac{4b^2}{a^2}$  or  $\frac{-3a^2}{b^2}$ 

# **Question: 36**

Find the roots of

#### Solution:

Given:  $12abx^2 - (9a^2 - 8b^2)x - 6ab = 0$ 

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

$$A = 12ab, B = -(9a^2 - 8b^2), C = -6ab$$

Discriminant D = 
$$B^2 - 4AC$$

$$= [-(9a^2 - 8b^2)]^2 - 4.12ab. - 6ab$$

$$= 81a^4 - 144a^2b^2 + 64b^4 + 288a^2b^2$$

$$= 81a^4 + 144a^2b^2 + 64b^4$$

$$= (9a^{2} + 8b^{2})^{2} > 0$$
 Using  $a^{2} + 2ab + b^{2} = (a + b)^{2}$ 

Hence the roots of equation are real.

$$\sqrt{D} = \sqrt{(9a^2 + 8b^2)^2}$$
  
= 9a<sup>2</sup> + 8b<sup>2</sup>

Roots  $\alpha$  and  $\beta$  are given by

$$\alpha = \frac{-B + \sqrt{D}}{2A} = \frac{-[-(9a^2 - 8b^2)] + (9a^2 + 8b^2)}{2 \times 12ab} = \frac{18a^2}{24ab} = \frac{3a}{4b}$$

$$\beta = \frac{-B - \sqrt{D}}{2A} = \frac{-[-(9a^2 - 8b^2)] - (9a^2 + 8b^2)}{2 \times 12ab} = \frac{-16a^2}{24ab} = \frac{-2b}{3a}$$
$$x = \frac{3a}{4b} \text{ or } x = \frac{-2b}{3a}$$

Hence the roots of equation are  $\frac{3a}{4b}$  or  $\frac{-2b}{3a}$ 

# **Exercise : 10D**

### **Question: 1** A

Find the nature o

### Solution:

Given:  $2x^2 - 8x + 5 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (-8)^2 - 4.2.5$$

= 64 - 40 = 24 > 0

Hence the roots of equation are real and unequal.

### **Question: 1 B**

Find the nature o

#### Solution:

Given:  $3x^2 - 2\sqrt{6}x + 2 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

 $a = 3b = -2\sqrt{6}c = 2$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (-2\sqrt{6})^2 - 4.3.2$$

= 24 - 24 = 0

Hence the roots of equation are real and equal.

#### **Question: 1 C**

Find the nature o

# Solution:

Given:  $5x^2 - 4x + 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 5, b = -4, c = 1$$

Discriminant D =  $b^2 - 4ac$ 

$$= (-4)^2 - 4.5.1$$

$$= 16 - 20 = -4 < 0$$

Hence the equation has no real roots.

#### **Question: 1 D**

Find the nature o

#### Solution:

Given: 5x(x-2) + 6 = 0

 $5x^2 - 10x + 6 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

Discriminant D =  $b^2 - 4ac$ 

$$= (-10)^2 - 4.5.6$$

= 100 - 120 = -20 < 0

Hence the equation has no real roots.

#### **Question: 1 E**

Find the nature o

#### Solution:

Given:  $12x^2 - 4\sqrt{15}x + 5 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 12, b = -4\sqrt{15}, c = 5$$

Discriminant D =  $b^2 - 4ac$ 

$$= (-4\sqrt{15})^2 - 4.12.5$$

$$= 240 - 240 = 0$$

Hence the equation has real and equal roots.

# **Question: 1 F**

Find the nature o

#### Solution:

Given:  $x^2 - x + 2 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 1, b = - 1, c = 2

Discriminant D =  $b^2 - 4ac$ 

 $= (-1)^2 - 4.1.2$ 

= 1 - 8 = - 7 < 0

Hence the equation has no real roots.

#### **Question: 2**

If a and b are di

### Solution:

Given:  $2(a^2 + b^2)x^2 + 2(a + b)x + 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

 $a = 2 (a^2 + b^2), b = 2(a + b), c = 1$ 

$$= [2(a + b)]^{2} - 4 \cdot 2 (a^{2} + b^{2}) \cdot 1$$
  
= 4(a<sup>2</sup> + b<sup>2</sup> + 2ab) - 8 a<sup>2</sup> - 8b<sup>2</sup>  
= 4a<sup>2</sup> + 4b<sup>2</sup> + 8ab - 8a<sup>2</sup> - 8b<sup>2</sup>  
= - 4a<sup>2</sup> - 4b<sup>2</sup> + 8ab  
= - 4(a<sup>2</sup> + b<sup>2</sup> - 2ab)  
= - 4(a - b)<sup>2</sup> < 0

Hence the equation has no real roots.

#### **Question: 3**

Show that the roo

### Solution:

Given equation  $x^2 + px - q^2 = 0$ 

$$a = 1 b = p x = -q^2$$

Discriminant D =  $b^2 - 4ac$ 

$$= (p)^{2} - 4.1. - q^{2}$$
$$= (p^{2} + 4q^{2}) > 0$$

Thus the roots of equation are real.

### **Question: 4**

For what values o

#### Solution:

Given:  $3x^2 + 2kx + 27 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 3 b = 2k c = 27

Given that the roots of equation are real and equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

 $(2k)^2 - 4.3.27 = 0$ 

 $4k^2 - 324 = 0$ 

$$4k^2 = 324$$

 $k^2 = 81$  taking square root on both sides

k = 9 or k = -9

The values of k are 9, – 9 for which roots of the quadratic equation are real and equal.

#### **Question: 5**

For what value of

### Solution:

Given equation is  $kx(x - 2\sqrt{5}) + 10 = 0$ 

$$kx^2 - 2\sqrt{5}kx + 10 = 0$$

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

 $a = kb = -2\sqrt{5}kc = 10$ 

Given that the roots of equation are real and equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

$$(-k2\sqrt{5})^2 - 4.k.10 = 0$$

 $20k^2 - 40k = 0$ 

20k(k-2) = 0

20k = 0 or (k - 2) = 0

k = 0 or k = 2

The values of k are 0, 2 for which roots of the quadratic equation are real and equal.

# **Question:** 6

For what values o

# Solution:

Given equation is  $4x^2 + px + 3 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 4 b = p c = 3$$

Given that the roots of equation are real and equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

 $(p)^2 - 4.4.3 = 0$ 

$$p^2 = 48$$

$$p = \pm 4\sqrt{3}$$

$$\mathbf{p} = 4\sqrt{3} \, \mathrm{or} \, \mathbf{p} = \mathbf{p} = -4\sqrt{3}$$

The values of p are  $4\sqrt{3}$ ,  $-4\sqrt{3}$  for which roots of the quadratic equation are real and equal.

# **Question:** 7

Find the nonzero

# Solution:

Given equation is  $9x^2 - 3kx + k = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 9 b = -3k c = k$$

Given that the roots of equation are real and equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

 $(-3k)^2 - 4.9.k = 0$ 

 $9 k^2 - 36k = 0$ 

9k(k-4)=0

9k = 0 or(k - 4) = 0

k = 0 or k = 4

But given k is non zero hence k = 4 for which roots of the quadratic equation are real and equal.

### **Question: 8**

Find the values o

#### Solution:

Given equation is  $(3k + 1) x^2 + 2(k + 1)x + 1 = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = (3k + 1) b = 2(k + 1) c = 1

Given that the roots of equation are real and equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

 $(2k + 2)^2 - 4.(3k + 1).1 = 0$  using  $(a + b)^2 = a^2 + 2ab + b^2$ 

 $4k^2 + 8k + 4 - 12k - 4 = 0$ 

 $4\mathbf{k}^2 - 4\mathbf{k} = 0$ 

4k(k-1)=0

k = 0 (k - 1) = 0

$$k = 0 k = 1$$

The values of k are 0, 1 for which roots of the quadratic equation are real and equal.

#### **Question: 9**

Find the values o

#### Solution:

Given equation is  $(2p + 1)x^2 - (7p + 2)x + (7p - 3) = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = (2p + 1) b = -(7p + 2) c = (7p - 3)

Given that the roots of equation are real and equal

Thus D = 0

Discriminant D = b<sup>2</sup> - 4ac = 0  $[-(7p + 2)]^{2} - 4.(2p + 1).(7p - 3) = 0 \text{ using } (a + b)^{2} = a^{2} + 2ab + b^{2}$   $(49p^{2} + 28p + 4) - 4(14p^{2} + p - 3) = 0$   $49p^{2} + 28p + 4 - 56p^{2} - 4p + 12 = 0$   $- 7p^{2} + 24p + 16 = 0$   $7p^{2} - 24p - 16 = 0$   $7p^{2} - 28p + 4p - 16 = 0$  7p(p - 4) + 4(p - 4) = 0 (7p + 4)(p - 4) = 0 (7p + 4) = 0 or (p - 4) = 0  $p = \frac{-4}{7} \text{ or } p = 4$  The values of p are  $\frac{-4}{7}$  or 4 for which roots of the quadratic equation are real and equal.

#### **Question: 10**

Find the values o

#### Solution:

Given equation is  $(p + 1)x^2 - 6 (p + 1) x + 3 (p + 9) = 0$ Comparing with standard quadratic equation  $ax^2 + bx + c = 0$  a = (p + 1) b = -6(p + 1) c = 3(p + 9)Given that the roots of equation are equal Thus D = 0Discriminant  $D = b^2 - 4ac = 0$   $[-6(p + 1)]^2 - 4.(p + 1).3(p + 9) = 0$  36(p + 1)(p + 1) - 12(p + 1)(p + 9) = 0 12(p + 1)[3(p + 1) - (p + 9)] = 0 12(p + 1)[3p + 3 - p - 9] = 0 12(p + 1)[2p - 6] = 0 (p + 1) = 0 or [2p - 6] = 0p = -1 or p = 3

The values of p are – 1, 3 for which roots of the quadratic equation are real and equal.

#### **Question: 11**

If - 5 is a root

#### Solution:

Given that – 5 is a root of the quadratic equation  $2x^2 + px - 15 = 0$ 

 $2(-5)^2 - 5p - 15 = 0$  5p = 35 p = 7Given equation is  $p(x^2 + x) + k = 0$ 

 $px^2 + px + k = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = p b = p c = k$$

Given that the roots of equation are equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

$$[p]^2 - 4.p.k = 0$$

 $7^2 - 28k = 0$ 

49 - 28k = 0

$$k = \frac{49}{28} = \frac{7}{4}$$

The value of k is  $\frac{7}{4}$  for which roots of the quadratic equation are equal.

#### **Question: 12**

If 3 is a root of  $% \left[ {{\left[ {{\left[ {{\left[ {\left( {1 \right) }} \right]_{{\rm{T}}}}} \right]_{{\rm{T}}}}} \right]_{{\rm{T}}}} \right]} \right]$ 

### Solution:

Given 3 is a root of the quadratic equation  $x^2 - x + k = 0$ 

 $(3)^2 - 3 + k = 0$ 

k + 6 = 0

k = - 6

Given equation is  $x^2 + k(2x + k + 2) + p = 0$ 

 $x^2 + 2kx + (k^2 + 2k + p) = 0$ 

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 1 b = 2k c = k^2 + 2k + p$$

Given that the roots of equation are equal

Thus D = 0

Discriminant D =  $b^2 - 4ac = 0$ 

 $(2k)^2 - 4.1.(k^2 + 2k + p) = 0$ 

 $4k^2 - 4k^2 - 8k - 4p = 0$ 

-8k - 4p = 0

4p = -8k

p = - 2k

p = -2. - 6 = 12

p = 12

The value of  $p\ is$  – 12 for which roots of the quadratic equation are equal.

### **Question: 13**

If - 4 is a root

# Solution:

Given - 4 is a root of the equation  $x^2 + 2x + 4p = 0$ 

 $(-4)^2 + 2(-4) + 4p = 0$ 

8 + 4p = 0

The quadratic equation  $x^2 + px (1 + 3k) + 7(3 + 2k) = 0$  has equal roots

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = 1 b = p(1 + 3k) c = 7(3 + 2k)$$
  
Thus D = 0  
Discriminant D = b<sup>2</sup> - 4ac = 0  

$$[p(1 + 3k)]^{2} - 4.1.7(3 + 2k) = 0$$
  

$$[ - 2(1 + 3k)]^{2} - 4.1.7(3 + 2k) = 0$$
  

$$4(1 + 6k + 9k^{2}) - 4.7(3 + 2k) = 0 \text{ using } (a + b)^{2} = a^{2} + 2ab + b^{2}$$
  

$$4(1 + 6k + 9k^{2} - 21 - 14k) = 0$$

 $9k^{2} - 8k - 20 = 0$   $9k^{2} - 18k - 10k - 20 = 0$  9k(k - 2) + 10(k - 2) = 0 (9k + 10)(k - 2) = 0 $k = \frac{-10}{9} \text{ or } k = 2$ 

The value of k is  $\frac{-10}{9}$  or 2 for which roots of the quadratic equation are equal.

#### **Question: 14**

If the quadratic

#### Solution:

The quadratic equation  $(1 + m^2) x^2 + 2mcx + c^2 - a^2 = 0$  has equal roots Comparing with standard quadratic equation  $ax^2 + bx + c = 0$   $a = (1 + m^2) b = 2mc c = c^2 - a^2$ Thus D = 0 Discriminant D = b<sup>2</sup> - 4ac = 0  $(2mc)^2 - 4.(1 + m^2)(c^2 - a^2) = 0$   $4 m^2c^2 - 4c^2 + 4a^2 - 4 m^2c^2 + 4 m^2a^2 = 0$   $- 4c^2 + 4a^2 + 4m^2a^2 = 0$   $a^2 + m^2a^2 = c^2$   $c^2 = a^2 (1 + m^2)$ Hence proved Question: 15

# If the roots of t

#### Solution:

Given that the roots of the equation  $(c^2 - ab)x^2 - 2(a^2 - bc)x + (b^2 - ac) = 0$  are real and equal Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

 $a = (c^{2} - ab) b = -2(a^{2} - bc) c = (b^{2} - ac)$ Thus D = 0 Discriminant D = b<sup>2</sup> - 4ac = 0  $[-2(a^{2} - bc)]^{2} - 4(c^{2} - ab) (b^{2} - ac) = 0$   $4(a^{4} - 2a^{2}bc + b^{2}c^{2}) - 4(b^{2}c^{2} - ac^{3} - ab^{3} + a^{2}bc) = 0$ using (a - b)<sup>2</sup> = a<sup>2</sup> - 2ab + b<sup>2</sup> a<sup>4</sup> - 2a^{2}bc + b^{2}c^{2} - b^{2}c^{2} + ac^{3} + ab^{3} - a^{2}bc = 0  $a^{4} - 3a^{2}bc + ac^{3} + ab^{3} = 0$   $a (a^{3} - 3abc + c^{3} + b^{3}) = 0$ Hence proved a = 0 or a<sup>3</sup> + c<sup>3</sup> + b<sup>3</sup> = 3abc

#### **Question: 16**

Find the values o

#### Solution:

Given that the quadratic equation  $2x^2 + px + 8 = 0$  has real roots

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 2 b = p c = 8 Thus D = 0 Discriminant D = b<sup>2</sup> - 4ac  $\geq 0$ (p)<sup>2</sup> - 4.2.8 $\geq 0$ (p)<sup>2</sup> - 64 $\geq 0$ p<sup>2</sup>  $\geq$  64 taking square root on both sides p $\geq 8$  or p $\leq -8$ The roots of equation are real for p $\geq 8$  or p $\leq -8$ **Question: 17** 

Find the value of

#### Solution:

Given that the quadratic equation  $(a - 12)x^2 + 2(a - 12)x + 2 = 0$  has equal roots

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ 

A = (a - 12) B = 2(a - 12) C = 2Thus D = 0 Discriminant D = B<sup>2</sup> - 4AC  $\ge 0$   $[2(a - 12)]^{2} - 4(a - 12)2 \ge 0$   $4(a^{2} + 144 - 24a) - 8a + 96 = 0 \text{ using } (a - b)^{2} = a^{2} - 2ab + b^{2}$   $4a^{2} + 576 - 96a - 8a + 96 = 0$   $4a^{2} - 104a + 672 = 0$   $a^{2} - 26a + 168 = 0$   $a^{2} - 14a - 12a + 168 = 0$  a(a - 14) - 12(a - 14) = 0 (a - 14)(a - 12) = 0 a = 14 or a = 12for a = 12 the equation will become non quadratic - - (a - 12)x^{2} + 2(a - 12)x + 2 = 0

A, B will become zero

Thus value of a = 14 for which the equation has equal roots.

# **Question: 18**

Find the value of

# Solution:

Given that the quadratic equation  $9x^2 + 8kx + 16 = 0$  roots are real and equal.

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

a = 9 b = 8k c = 16Thus D = 0Discriminant D =  $b^2 - 4ac = 0$  $(8k)^2 - 4.9.16 = 0$  $64k^2 - 576 = 0$  $k^2 = 9$  taking square root both sides k = +3Thus k = 3 or k = -3 for which the roots are real and equal. **Ouestion: 19** Find the values o Solution: (i) Given:  $kx^2 + 6x + 1 = 0$ Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ a = k b = 6 c = 1For real and distinct roots: D > 0Discriminant D =  $b^2 - 4ac > 0$  $6^2 - 4k > 0$ 36 - 4k > 04k < 36 **k** < 9 (ii) Given:  $x^2 - kx + 9 = 0$ Comparing with standard guadratic equation  $ax^2 + bx + c = 0$ a = 1 b = -k c = 9For real and distinct roots: D > 0Discriminant D =  $b^2 - 4ac > 0$  $(-k)^2 - 4.1.9 = k^2 - 36 > 0$  $k^2 > 36$ k > 6 or k < -6 taking square root both sides (iii)  $9x^2 + 3kx + 4 = 0$ Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ a = 9 b = 3k c = 4For real and distinct roots: D > 0Discriminant D =  $b^2 - 4ac > 0$  $(3k)^2 - 4.4.9 = 9k^2 - 144 > 0$  $9k^2 > 144$  $k^2 > 16$ 

k > 4ork < -4 taking square root both sides

(iv)  $5x^2 - kx + 1 = 0$ 

Comparing with standard guadratic equation  $ax^2 + bx + c = 0$ 

a = 5 b = -k c = 1

For real and distinct roots: D > 0

Discriminant D =  $b^2 - 4ac > 0$ 

 $(-k)^2 - 4.5.1 = k^2 - 20 > 0$ 

 $k^2 > 20$ 

 $k>2\sqrt{5}$  or  $k<-2\sqrt{5}$  taking square root both sides

### **Question: 20**

If a and b are re

#### Solution:

Comparing with standard quadratic equation  $ax^2 + bx + c = 0$ 

$$a = (a - b) b = 5(a + b) c = -2(a - b)$$

Discriminant D =  $b^2 - 4ac$ 

 $= [5(a + b)]^2 - 4(a - b)(-2(a - b))$ 

$$= 25(a + b)^2 + 8(a - b)^2$$

Since a and b are real and  $a \neq b$  then  $(a + b)^2 > 0$   $(a - b)^2 > 0$ 

 $8(a - b)^2 > 0 - - - - (1)$  product of two positive numbers is always positive

 $25(a + b)^2 > 0 - - - (2)$  product of two positive numbers is always positive

Adding (1) and (2) we get

 $8(a - b)^2 + 25(a + b)^2 > 0$  (sum of two positive numbers is always positive)

#### D > 0

Hence the roots of given equation are real and unequal.

### **Question: 21**

If the roots of t

### Solution:

Given the roots of the equation are equation  $(a^2 + b^2)x^2 - 2(ac + bd)x + (c^2 + d^2) = 0$  are equal. Comparing with standard quadratic equation  $ax^2 + bx + c = 0$  $a = (a^2 + b^2)b = -2(ac + bd)c = (c^2 + d^2)$ 

For real and distinct roots: 
$$D = 0$$

Discriminant D =  $b^2 - 4ac = 0$ 

$$[-2(ac + bd)]^2 - 4(a^2 + b^2)(c^2 + d^2) = 0$$

 $4(a^{2}c^{2} + b^{2}d^{2} + 2abcd) - 4(a^{2}c^{2} + a^{2}d^{2} + b^{2}c^{2} + b^{2}d^{2}) = 0$ 

using  $(a + b)^2 = a^2 + 2ab + b^2$ 

$$4(a^2c^2 + b^2d^2 + 2abcd - a^2c^2 - a^2d^2 - b^2c^2 - b^2d^2) = 0$$

$$2abcd - a^2d^2 - b^2c^2 = 0$$

 $-(2abcd + a^2d^2 + b^2c^2) = 0$ 

 $(ad - bc)^2 = 0$ ad = bc

 $\frac{a}{b} = \frac{c}{d}$ 

Hence proved.

### **Question: 22**

If the roots of t

### Solution:

Given the roots of the equations  $ax^2 + 2bx + c = 0$  are real.

Comparing with standard quadratic equation  $Ax^2 + Bx + C = 0$ A = a B = 2b C = cDiscriminant D<sub>1</sub> = B<sup>2</sup> – 4AC  $\ge 0$  $= (2b)^2 - 4.a.c \ge 0$  $= 4(b^2 - ac) \ge 0$  $= (b^2 - ac) \ge 0 - - - - - (1)$ For the equation  $bx^2 - 2\sqrt{acx} + b = 0$ Discriminant  $D_2 = b^2 - 4ac \ge 0$  $= (-2\sqrt{ac})^2 - 4. b. b \ge 0$  $= 4(ac - b^2) \ge 0$  $= -4(b^2 - ac) \ge 0$  $= (b^2 - ac) \ge 0 - - - - - (2)$ The roots of the are simultaneously real if (1) and (2) are true together  $b^2 - ac = 0$  $b^2 = ac$ 

Hence proved.

# **Exercise : 10E**

# **Question: 1**

The sum of a natu

### Solution:

Let the required number be x

According to given condition,

$$\mathbf{x} + \mathbf{x}^2 = 156$$

$$x^2 + x - 156 = 0$$

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 1 c = -156

= 1. - 156 = -156

And either of their sum or difference = b = 1 Thus the two terms are 13 and - 12 Sum = 13 - 12 = 1 Product = 13. - 12 = - 156  $x^{2} + x - 156 = 0$  $x^{2} + 13x - 12x - 156 = 0$ x(x + 13) - 12 (x + 13) = 0(x - 12) (x + 13) = 0x = 12 or x = -13x cannot be negative Hence the required natural number is 12

### **Question: 2**

The sum of a natu

### Solution:

Let the required number be x

According to given condition,

 $x + \sqrt{x} = 132$ 

putting  $\sqrt{x} = y \text{ or } x = y^2$  we get

 $y^2 + y = 132$ 

 $y^2 + y - 132 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1 b = 1 c = -132= 1. - 132 = -132 And either of their sum or difference = b = 1 Thus the two terms are 12 and - 11 Difference = 12 - 11 = 1 Product = 12. - 11 = -132  $y^2 + y - 132 = 0$   $y'^2 + 12y - 11y - 132 = 0$  y(y + 12) - 11(y + 12) = 0 (y + 12) (y - 11) = 0 (y + 12) = 0 or (y - 11) = 0 y = -12 or y = 11 but y cannot be negative Thus y = 11 Now  $\sqrt{x} = y$ 

x = y squaring both sides

 $x = (11)^2 = 121$ 

Hence the required number is 121

# **Question: 3**

The sum of two na

# Solution:

Let the required number be  $x \mbox{ and } 28$  – x

According to given condition,

x(28 - x) = 192

 $x^2 - 28x + 192 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -28 c = 192

= 1.192 = 192

And either of their sum or difference = b

= - 28

Thus the two terms are – 16 and – 12  $\,$ 

Sum = -16 - 12 = -28

Product = -16. - 12 = 192

 $x^2 - 28x + 192 = 0$ 

 $x^2 - 16x - 12x + 192 = 0$ 

x(x - 16) - 12(x - 16) = 0

(x - 16) (x - 12) = 0

(x - 16) = 0 or (x - 12) = 0

x = 16 or x = 12

Hence the required numbers are 16, 12

# **Question: 4**

The sum of the sq

# Solution:

Let the required two consecutive positive integers be  $x \mbox{ and } x+1$ 

According to given condition,

$$x^{2} + (x + 1)^{2} = 365$$
  

$$x^{2} + x^{2} + 2x + 1 = 365 \text{ using } (a + b)^{2} = a^{2} + 2ab + b^{2}$$
  

$$2x^{2} + 2x - 364 = 0$$
  

$$x^{2} + x - 182 = 0$$

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1 b = 1 c = -182= 1. - 182 = -182And either of their sum or difference = b = 1 Thus the two terms are 14 and - 13 Difference = 14 - 13 = 1Product = 14. - 13 = -182 $x^2 + x - 182 = 0$  $x^2 + 14x - 13x - 182 = 0$ x(x + 14) - 13(x + 14) = 0(x + 14) (x - 13) = 0(x + 14) = 0 or (x - 13) = 0x = -14 or x = 13x = 13 (x is a positive integer) x + 1 = 13 + 1 = 14

Thus the required two consecutive positive integers are 13, 14

# **Question:** 5

The sum of the sq

### Solution:

Let the two consecutive positive odd numbers be x and x + 2

According to given condition,

 $x^2 + (x+2)^2 = 514$ 

 $x^{2} + x^{2} + 4x + 4 = 514$  using  $(a + b)^{2} = a^{2} + 2ab + b^{2}$ 

 $2x^2 + 4x - 510 = 0$ 

 $x^2 + 2x - 255 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 2 c = -255

= 1. - 255 = - 255

And either of their sum or difference = b

= 2

Thus the two terms are 17 and – 15  $\,$ 

Difference = 17 - 15 = 2

Product = 17. - 15 = -255

 $x^2 + 2x - 255 = 0$ 

 $x^2 + 17x - 15x - 255 = 0$ 

x(x + 17) - 15(x + 17) = 0

(x + 17) (x - 15) = 0(x + 17) = 0 or (x - 15) = 0x = -17 or x = 15x = 15 (x is positive odd number)

$$x + 2 = 15 + 2 = 17$$

Thus the two consecutive positive odd numbers are 15 and 17

### **Question: 6**

The sum of the sq

### Solution:

Let the two consecutive positive even numbers be x and (x + 2)

According to given condition,

 $x^{2} + (x + 2)^{2} = 452$  $x^{2} + x^{2} + 4x + 4 = 452$  using  $(a + b)^{2} = a^{2} + 2ab + b^{2}$  $2x^{2} + 4x - 448 = 0$ 

 $x^2 + 2x - 224 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 2 c = -224

= 1. - 224 = -224

And either of their sum or difference = b

= 2

Thus the two terms are 16 and –  $14\,$ 

Difference = 16 - 14 = 2

Product = 16. - 14 = -224

 $x^2 + 2x - 224 = 0$ 

 $x^2 + 16x - 14x - 224 = 0$ 

x(x + 16) - 14(x + 16) = 0

(x + 16) (x - 14) = 0

(x + 16) = 0 or (x - 14) = 0

x = -16 or x = 14

x = 14 (x is positive odd number)

$$x + 2 = 14 + 2 = 16$$

Thus the two consecutive positive even numbers are 14 and 16

# **Question:** 7

The product of tw

# Solution:

Let the two consecutive positive integers be x and (x + 1)

According to given condition,

 $\mathbf{x}(\mathbf{x}+1) = 306$ 

 $x^2 + x - 306 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1 b = 1 c = -306= 1. - 306 = -306And either of their sum or difference = b = 1 Thus the two terms are 18 and - 17 Difference = 18 - 17 = 1Product = 18. - 17 = -306 $x^2 + x - 306 = 0$  $x^2 + 18x - 17x - 306 = 0$ x(x + 18) - 17(x + 18) = 0(x + 18) (x - 17) = 0(x + 18) = 0 or (x - 17) = 0x = -18 or x = 17but x = 17 ( x is a positive integers) x + 1 = 17 + 1 = 18

Thus the two consecutive positive integers are  $17 \ \text{and} \ 18$ 

# **Question: 8**

Two natural numbe

# Solution:

Let the two natural numbers be x and (x + 3)

According to given condition,

 $\mathbf{x}(\mathbf{x}+3) = 504$ 

 $x^2 + 3x - 504 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1 b = 3 c = -504= 1. - 504 = - 504 And either of their sum or difference = b = 3 Thus the two terms are 24 and - 21 Difference = 24 - 21 = 3 Product = 24. - 21 = - 504  $x^2 + 3x - 504 = 0$   $x^{2} + 24x - 21x - 504 = 0$  x (x + 24) - 21(x + 24) = 0 (x + 24) (x - 21) = 0 (x + 24) = 0 or (x - 21) = 0 x = -24 or x = 21Case I: x = 21 x + 3 = 21 + 3 = 24The numbers are (21, 24) Case I: x = -24 x + 3 = -24 + 3 = -21The numbers are (-24, -21)

### **Question: 9**

Find two consecut

#### Solution:

Let the required consecutive multiples of 3 be 3x and 3(x + 1)

According to given condition,

3x.3(x + 1) = 648  $9(x^{2} + x) = 648$   $x^{2} + x = 72$  $x^{2} + x - 72 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 1 c = -72

= 1. - 72 = - 72

And either of their sum or difference = b

= 1

Thus the two terms are 9 and - 8

Difference = 9 - 8 = 1

Product = 9. - 8 = -72

 $x^2 + 9x - 8x - 72 = 0$ 

x (x + 9) - 8(x + 9) = 0

(x + 9) (x - 8) = 0

(x + 9) = 0 or (x - 8) = 0

x = -9 or x = 8

x = 8 (rejecting the negative values)

$$3x = 3.8 = 24$$

3(x + 1) = 3(8 + 9) = 3.9 = 27

Hence, the required numbers are 24 and 27

#### **Question: 10**

Find two consecut

### Solution:

Let the required consecutive positive odd integers be x and (x + 2)

According to given condition,

x(x + 2) = 483

 $x^2 + 2x - 483 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 2 c = -483

= 1. - 483 = - 483

And either of their sum or difference = b

= 2

Thus the two terms are 23 and – 21  $\,$ 

Difference = 23 - 21 = 2

Product = 23. - 21 = - 483

 $x^2 + 2x - 483 = 0$ 

 $x^2 + 23x - 21x - 483 = 0$ 

x (x + 23) - 21(x + 23) = 0

(x + 23) (x - 21) = 0

(x + 23) = 0 or (x - 21) = 0

x = -23 or x = 21

x = 21 (x is a positive odd integer)

$$x + 2 = 21 + 2 = 23$$

Hence, the required integers are 21 and 23

### **Question: 11**

Find two consecut

# Solution:

Let the two consecutive positive even integers be x and (x + 2)

According to given condition,

x(x + 2) = 288

 $x^2 + 2x - 288 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 2 c = -288

= 1. - 288 = - 288

And either of their sum or difference = b

= 2

Thus the two terms are 18 and – 16  $\,$ 

Difference = 18 - 16 = 2

Product = 18. - 16 = - 288

 $x^2 + 18x - 16x - 288 = 0$ 

x (x + 18) - 16(x + 18) = 0

(x + 18) (x - 16) = 0

(x + 18) = 0 or (x - 16) = 0

x = -18 or x = 16

x = 16 (x is a positive odd integer)

x + 2 = 16 + 2 = 18

Hence, the required integers are 16 and 18

# **Question: 12**

The sum of two na

### Solution:

Let the required natural numbers x and (9 - x)

According to given condition,

 $\frac{1}{x} + \frac{1}{9-x} = \frac{1}{2}$   $\frac{9-x+x}{x(9-x)} = \frac{1}{2} \text{ taking LCM}$   $\frac{9}{9x-x^2} = \frac{1}{2}$   $9x - x^2 = 18 \text{ cross multiplying}$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

 $x^2 - 9x + 18 = 0$ 

For the given equation a = 1 b = -9 c = 18

= 1.18 = 18

And either of their sum or difference = b

Thus the two terms are –  $6 \mbox{ and }$  –  $3 \mbox{ }$ 

Sum = -6 - 3 = -9

Product = -6. - 3 = 18

 $x^2 - 9x + 18 = 0$ 

 $x^{2} - 6x - 3x + 18 = 0$ x(x - 6) - 3(x - 6) = 0

(x - 6) (x - 3) = 0

(x - 6) = 0 or (x - 3) = 0

x = 6 or x = 3Case I: when x = 69 - x = 9 - 6 = 3Case II: when x = 39 - x = 9 - 3 = 6

Hence required numbers are 3 and 6.

### **Question: 13**

The sum of two na

### Solution:

Let the required natural numbers x and (15 - x)

According to given condition,

 $\frac{1}{x} + \frac{1}{15 - x} = \frac{3}{10}$ 

taking LCM

 $\frac{15 - x + x}{x(15 - x)} = \frac{3}{10}$ 

cross multiplying

 $\frac{15}{15x - x^2} = \frac{3}{10}$  $15x - x^2 = 50$  $x^2 - 15x + 50 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -15 c = 50

= 1.50 = 50

And either of their sum or difference = b

= - 15

Thus the two terms are – 10 and – 5

Sum = - 10 - 5 = - 15

Product = -10. - 5 = 50  $x^2 - 10x - 5x + 50 = 0$  x(x - 10) - 5(x - 10) = 0 (x - 5) (x - 10) = 0 (x - 5) = 0 or (x - 10) = 0 x = 5 or x = 10Case I: when x = 5

Case I: when x = 3

15 - x = 15 - 5 = 10

Case II: when x = 10

15 - x = 15 - 10 = 5

Hence required numbers are 5 and 10.

### **Question: 14**

The difference of

### Solution:

Let the required natural numbers x and (x + 3)

x < x + 3

Thus  $\frac{1}{x} > \frac{1}{x+3}$ 

According to given condition,

 $\frac{1}{x} - \frac{1}{x+3} = \frac{3}{28}$ 

taking LCM

 $\frac{x+3-x}{x(x+3)} = \frac{3}{28}$ 

$$\frac{3}{x^2 + 3x} = \frac{3}{28}$$

cross multiplying

 $x^{2} + 3x = 28$  $x^{2} + 3x - 28 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 3 c = -28

= 1. - 28 = - 28

And either of their sum or difference = b

= 3

Thus the two terms are 7 and –  $4\,$ 

Difference = 7 - 4 = 3

Product = 7. - 4 = -28

$$x^2 + 3x - 28 = 0$$

 $x^2 + 7x - 4x - 28 = 0$ 

x(x + 7) - 4(x + 7) = 0

(x - 4) (x + 7) = 0

(x - 4) = 0 or (x + 7) = 0

x = 4 or x = -7

x = 4 (x < x + 3)

$$x + 3 = 4 + 3 = 7$$

Hence required numbers are 4 and 7.

# **Question: 15**

The difference of

#### Solution:

Let the required natural numbers x and (x + 5)

x < x + 5

Thus  $\frac{1}{x} > \frac{1}{x+5}$ 

According to given condition,

$$\frac{1}{x} - \frac{1}{x+5} = \frac{5}{14}$$

taking LCM

$$\frac{x+5-x}{x(x+5)} = \frac{5}{14}$$
$$\frac{5}{x^2+5x} = \frac{5}{14}$$

cross multiplying

$$x^2 + 5x = 14$$

 $x^2 + 5x - 14 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 5 c = -14

= 1. - 14 = - 14

And either of their sum or difference = b

= 5

Thus the two terms are 7 and – 2  $\,$ 

Difference = 7 - 2 = 5

Product = 7. - 2 = -14

 $x^2 + 7x - 2x - 14 = 0$ 

x (x + 7) - 2(x + 7) = 0

(x - 2) (x + 7) = 0

(x - 2) = 0 or (x + 7) = 0

x = 2 or x = -7

x = 2 (x < x + 3)

x + 5 = 2 + 5 = 7

Hence required natural numbers are 2 and 7.

### **Question: 16**

The sum of the sq

### Solution:

Let the required consecutive multiples of 7 be 7x and 7(x + 1)

According to given condition,

 $(7x)^2 + [7(x + 1)]^2 = 1225$ 

 $49 x^{2} + 49(x^{2} + 2x + 1) = 1225 \text{ using } (a + b)^{2} = a^{2} + 2ab + b^{2}$  $49 x^{2} + 49x^{2} + 98x + 49 = 1225$  $98x^{2} + 98x - 1176 = 0$ 

 $x^2 + x - 12 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 1 c = -12

= 1. - 12 = -12

And either of their sum or difference = b

```
= 1
```

Thus the two terms are  $4 \mbox{ and } - 3$ 

Difference = 4 - 3 = 1

Product = 4. - 3 = -12

 $x^2 + 4x - 3x - 12 = 0$ 

x(x + 4) - 3(x + 4) = 0

(x - 3) (x + 4) = 0

(x - 3) = 0 or (x + 4) = 0

x = 3 or x = -4

when x = 3,

7x = 7.3 = 21

7(x + 1) = 7(3 + 1) = 7.4 = 28

Hence required multiples are 21, 28.

# **Question: 17**

The sum of a natu

### Solution:

Let the required natural numbers  $\boldsymbol{x}$ 

According to given condition,

$$x + \frac{1}{x} = \frac{65}{8}$$
$$\frac{x^2 + 1}{x} = \frac{65}{8}$$
$$8x^2 + 8 = 65x$$

 $8x^2 - 65x + 8 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 8 b = -65 c = 8

= 8.8 = 64

And either of their sum or difference = b

= - 65 Thus the two terms are - 64 and - 1 Difference = - 64 - 1 = - 65 Product = - 64. - 1 = 64  $8x^2 - 64x - x + 8 = 0$  8x (x - 8) - 1(x - 8) = 0 (x - 8) (8x - 1) = 0 (x - 8) = 0 or (8x - 1) = 0x = 8 or x = 1/8

x = 8 (x is a natural number)

Hence the required number is 8.

#### **Question: 18**

Divide 57 into tw

### Solution:

Let the two consecutive positive even integers be x and (57 - x)

According to given condition,

x(57 - x) = 680

 $57x - x^2 = 680$ 

Product = a.c

 $x^2 - 57x - 680 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

For the given equation a = 1 b = -57 c = -680= 1. - 680 = - 680And either of their sum or difference = b = - 57 Thus the two terms are - 40 and - 17 Sum = - 40 - 17 = - 57 Product = -40. - 17 = -680 $x^2 - 57x - 680 = 0$  $x^2 - 40x - 17x - 680 = 0$ x (x - 40) - 17(x - 40) = 0(x - 40) (x - 17) = 0(x - 40) = 0 or (x - 17) = 0x = 40 or x = 17When x = 4057 - x = 57 - 40 = 17When x = 1757 - x = 57 - 17 = 40

Hence the required parts are 17 and 40.

#### **Question: 19**

Divide 27 into tw

#### Solution:

Let the two parts be x and (27 - x)

According to given condition,

$$\frac{1}{x} + \frac{1}{27 - x} = \frac{3}{20}$$
$$\frac{27 - x + x}{x(27 - x)} = \frac{3}{20}$$

On taking the LCM

$$\frac{27}{27x - x^2} = \frac{3}{20}$$

 $27x - x^2 = 180$ 

Product = a.c

On Cross multiplying

 $x^2 - 27x + 180 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

For the given equation a = 1 b = -27 c = 180= 1. - 180 = -180And either of their sum or difference = b= - 27 Thus the two terms are - 15 and - 12 Sum = - 15 - 12 = - 27 Product = -15. - 12 = 180 $x^2 - 15x - 12x + 180 = 0$ x (x - 15) - 12(x - 15) = 0(x - 15) (x - 12) = 0(x - 15) = 0 or (x - 12) = 0x = 15 or x = 12Case I: when x = 1227 - x = 27 - 12 = 15Case II: when x = 1527 - x = 27 - 15 = 12Hence required numbers are 12 and 15. **Ouestion: 20** Divide 16 into tw

#### Solution:

Let the larger and the smaller parts be x and y respectively.

According to the question

x + y = 16 - - - - (1)  $2x^{2} = y^{2} + 164 - - - (2)$ From (1) x = 16 - y - - - (3) From (2) and (3) we get  $2(16 - y)^{2} = y^{2} + 164$   $2(256 - 32y + y^{2}) = y^{2} + 164 \text{ using } (a + b)^{2} = a^{2} + 2ab + b^{2}$   $512 - 64y + 2y^{2} = y^{2} + 164$  $y^{2} - 64y + 348 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

```
Product = a.c
For the given equation a = 1 b = -64 c = 348
= 1.348 = 348
And either of their sum or difference = b
= - 64
Thus the two terms are - 58 and - 6
Sum = -58 - 6 = -64
Product = -58. - 6 = 348
v^2 - 64v + 348 = 0
y^2 - 58y - 6y + 348 = 0
y(y - 58) - 6(y - 58) = 0
(y - 58) (y - 6) = 0
(y - 58) = 0 or (y - 6) = 0
y = 6 (y < 16)
putting the value of y in (3), we get
x = 16 - 6
= 10
Hence the two natural numbers are 6 and 10.
Question: 21
Find two natural
Solution:
Let the two natural numbers be x and y.
According to the question
```

$$x^{2} + y^{2} = 25(x + y) - - - - (1)$$
  

$$x^{2} + y^{2} = 50(x - y) - - - (2)$$
  
From (1) and (2) we get  

$$25(x + y) = 50(x - y)$$

 $\mathbf{x} + \mathbf{y} = 2(\mathbf{x} - \mathbf{y})$ 

x + y = 2x - 2y y + 2y = 2x - x 3y = x - - - - (3)From (2) and (3) we get  $(3y)^{2} + y^{2} = 50(3y - y)$   $9y^{2} + y^{2} = 50(3y - y)$   $10 y^{2} = 100y$  y = 10From (3) we have, x = 3y = 3.10 = 30

Hence the two natural numbers are 30 and 10.

### **Question: 22**

The difference of

#### Solution:

Let the larger number be x and smaller number be y.

According to the question

$$x^{2} - y^{2} = 45 - - - - (1)$$
  
 $y^{2} = 4x - - - - - (2)$ 

From (1) and (2) we get

$$\mathbf{x}^2 - 4\mathbf{x} = 45$$

 $x^2 - 4x - 45 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -4 c = -45

= 1. - 45 = - 45

And either of their sum or difference = b

= - 4

Thus the two terms are – 9 and 5

Sum = -9 + 5 = -4

Product = -9.5 = -45

 $x^2 - 9x + 5x - 45 = 0$ 

x(x - 9) + 5(x - 9) = 0

(x + 5) (x - 9) = 0

(x + 5) = 0 or (x - 9) = 0

$$x = -5 \text{ or } x = 9$$

putting the value of x in equation (2), we get

 $y^2 = 4.9 = 36$ 

taking square root

y = 6

Hence the two numbers are  $9 \ \text{and} \ 6$ 

# **Question: 23**

Three consecutive

### Solution:

Let the three consecutive positive integers be x, x + 1, x + 2

According to the given condition,

 $x^{2} + (x + 1)(x + 2) = 46$  $x^{2} + x^{2} + 3x + 2 = 46$ 

 $2x^2 + 3x - 44 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 2 b = 3 c = -44

= 2. - 44 = - 88

And either of their sum or difference = b

```
= 3
```

Thus the two terms are 11 and – 8

Sum = 11 - 8 = 3

Product = 11. - 8 = -88

 $2x^2 + 3x - 44 = 0$ 

 $2x^2 + 11x - 8x - 44 = 0$ 

x(2x + 11) - 4(2x + 11) = 0

(2x + 11)(x - 4) = 0

x = 4 or - 11/2

x = 4 (x is a positive integers)

When x = 4

x + 1 = 4 + 1 = 5

$$x + 2 = 4 + 2 = 6$$

Hence the required integers are 4, 5, 6

# **Question: 24**

A two - digit num

# Solution:

Let the digits at units and tens places be x and y respectively.

Original number = 10y + x

According to the question

10y + x = 4(x + y)

10y + x = 4x + 4y

3x - 6y = 0 x = 2y - - - (1)also, 10y + x = 2xyUsing (1) 10y + 2y = 2.2y.y  $12y = 4y^2$  y = 3From (1) we get x = 2.3 = 6Original number = 10y + x= (10.3) + 6 = 36

### **Question: 25**

A two - digit num

#### Solution:

Let the digits at units and tens place be x and y respectively

$$xy = 14$$
  
 $y = \frac{14}{x} - - - - (1)$ 

According to the question

(10y + x) + 45 = 10x + y 9y - 9x = -45 y - x = -5 - - - - (2)From (1) and (2) we get  $\frac{14}{x} - x = -5$   $\frac{14 - x^2}{x} = -5$  $14 - x^2 = -5x$ 

 $x^2 - 5x - 14 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -5 c = -14

= 1. - 14 = - 14

And either of their sum or difference = b

= - 5

Thus the two terms are –  $7 \mbox{ and } 2$ 

Difference = -7 + 2 = -5

Product = -7.2 = -14

 $x^{2} - 5x - 14 = 0$   $x^{2} - 7x + 2x - 14 = 0$  x(x - 7) + 2(x - 7) = 0 (x + 2)(x - 7) = 0 x = 7 or x = -2 x = 7 (neglecting the negative part)Putting x = 7 in equation (1) we get y = 2

Required number = 10.2 + 7 = 27

#### **Question: 26**

The denominator o

#### Solution:

Let the numerator be  $\boldsymbol{x}$ 

Denominator = x + 3

Original number =  $\frac{x}{x+3}$ 

$$\frac{x}{x+3} + \frac{1}{\frac{x}{x+3}} = 2\frac{9}{10}$$

On taking the LCM

 $\frac{x}{x+3} + \frac{x+3}{x} = \frac{29}{10}$   $\frac{x^2 + (x+3)^2}{x(x+3)} = \frac{29}{10}$   $\frac{x^2 + x^2 + 6x + 9}{x^2 + 3x} = \frac{29}{10} \{ \text{ using } (a+b)^2 = a^2 + 2ab + b^2 \}$   $\frac{2x^2 + 6x + 9}{x^2 + 3x} = \frac{29}{10}$   $29x^2 + 87x = 20x^2 + 60x + 90$   $9x^2 + 27x - 90 = 0$   $9(x^2 + 3x - 10) = 0$   $x^2 + 3x - 10 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 3 c = -10

= 1. - 10 = -10

And either of their sum or difference = b

= 3

Thus the two terms are 5 and – 2  $\,$ 

Difference = 5 - 2 = 3

Product = 5. - 2 = -10

 $x^{2} + 5x - 2x - 10 = 0$  x(x + 5) - 2(x + 5) = 0 (x + 5)(x - 2) = 0 (x + 5) = 0 or (x - 2) = 0 x = 2 or x = -5 x = 2 (rejecting the negative value) So numerator is 2 Denominator = x + 3 = 2 + 3 = 5So required fraction is 2/5

### **Question: 27**

The numerator of

### Solution:

Let the denominator of required fraction be x

Numerator of required fraction be = x - 3

Original number =  $\frac{x-3}{x}$ 

If 1 is added to the denominator, then the new fraction will become  $\frac{x-3}{x+1}$ 

According to the given condition,

$$\frac{x-3}{x+1} = \frac{x-3}{x} - \frac{1}{15}$$

$$\frac{x-3}{x+1} - \frac{x-3}{x} = \frac{1}{15}$$

$$\frac{(x-3)(x+1) - x(x-3)}{x(x+1)} = \frac{1}{15}$$

$$\frac{x^2 - 2x - 3 - x^2 + 3x}{x^2 + x} = \frac{1}{15}$$

$$\frac{x-3}{x^2 + x} = \frac{1}{15}$$

$$x^2 + x = 15x - 45$$

$$x^2 - 14x + 45 = 0$$
Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:  
Product = a.c

For the given equation a = 1 b = -14 c = 45

= 1.45 = 45

And either of their sum or difference = b

= - 14

Thus the two terms are – 9 and – 5  $\,$ 

Sum = -9 - 5 = -14

Product = -9. - 5 = -45

 $x^2 - 14x + 45 = 0$ 

 $x^{2} - 9x - 5x + 45 = 0$  x(x - 9) - 5(x - 9) = 0 (x - 9)(x - 5) = 0 x = 9 or x = 5Case I: x = 5

 $\frac{x-3}{x} = \frac{5-3}{5} = \frac{2}{5}$ 

Case II: x = 9

 $\frac{x-3}{x} = \frac{9-3}{9} = \frac{6}{9} = \frac{2}{3}$  (Rejected because this does not satisfy the condition given)

Hence the required fraction is  $\frac{2}{5}$ 

# **Question: 28**

The sum of a numb

# Solution:

Let the required number be x.

According to the given condition,

 $x + \frac{1}{x} = 2\frac{1}{30}$  $\frac{x^2 + 1}{x} = \frac{61}{30}$ 

 $30x^2 + 30 = 61x$ 

 $30x^2 - 61x + 30 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 30 b = -61 c = 30 = 30.30 = 900 And either of their sum or difference = b = -61 Thus the two terms are - 36 and - 25 Sum = -36 - 25 = -61 Product = -36. - 25 = 900  $30x^2 - 36x - 25x + 30 = 0$  6x(5x - 6) - 5(5x - 6) = 0 (5x - 6) (6x - 5) = 0 (5x - 6) = 0 or (6x - 5) = 0  $x = \frac{5}{6}$  or  $x = \frac{6}{5}$ Hence the required number is  $\frac{5}{6}$  or  $\frac{6}{5}$ 

### **Question: 29**

#### A teacher on atte

#### Solution:

Let there be x rows

Then the number of students in each row will also be x

Total number of students  $x^2 + 24$ 

According to the question,

 $(x + 1)^2 - 25 = x^2 + 24$  using  $(a + b)^2 = a^2 + 2ab + b^2$ 

 $x^2 + 2x + 1 - 25 - x^2 - 24 = 0$ 

$$2\mathbf{x} - 4\mathbf{8} = \mathbf{0}$$

Total number of students =  $24^2 + 24 = 576 + 24 = 600$ 

#### **Question: 30**

300 apples are di

#### Solution:

Let the total number of students be x

According to the question

$$\frac{300}{x} - \frac{300}{x + 10} = 1$$
  
$$\frac{300(x + 10) - 300x}{x(x + 10)} = 1 \text{ taking LCM}$$
  
$$\frac{300x + 3000 - 300x}{x^2 + 10x} = 1$$
  
$$3000 = x^2 + 10x \text{ cross multiplying}$$

$$x^2 + 10x - 3000 = 0$$

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1 b = 10 c = -3000= 1. -3000 = -3000And either of their sum or difference = b = 10 Thus the two terms are 60 and -50Difference = 60 -50 = 10Product = 60. -50 = -3000  $x^{2} + 60x - 50x - 3000 = 0$  x(x + 60) - 50(x + 60) = 0 (x + 60) (x - 50) = 0 (x - 50) = 0 or (x + 60) = 0x = 50 or x = -60

 $\boldsymbol{x}$  cannot be negative thus total number of students = 50

#### **Question: 31**

In a class test,

#### Solution:

Let Kamal's marks in mathematics and English be x and y, respectively

According to the question

x + y = 40 - - - - - - (1)Also (x + 3)(y - 4) = 360(x + 3)(40 - x - 4) = 360 from (1) (x + 3)(36 - x) = 360 $36x - x^2 + 108 - 3x = 360$  $33x - x^2 - 252 = 0$  $x^2 - 33x + 252 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -33 c = 252

= 1. - 252 = 252

And either of their sum or difference = b

```
= - 33
```

Thus the two terms are - 21 and - 12

Sum = -21 - 12 = -33

Product = -21. - 12 = 252

 $x^2 - 33x + 252 = 0$ 

 $x^2 - 21x - 12x + 252 = 0$ 

x(x - 21) - 12(x - 21) = 0

(x - 21) (x - 12) = 0

(x - 21) = 0 or (x - 12) = 0

x = 21 or x = 12

if x = 21

```
y = 40 - 21 = 19
```

Kamal's marks in mathematics and English are 21 and 19

if x = 12

y = 40 - 12 = 28

Kamal's marks in mathematics and English are 12 and 28

# **Question: 32**

Some students pla

### Solution:

Let x be the number of students who planned picnic

Original cost of food for each member = Rs.  $\frac{2000}{3}$ 

5 students failed to attend the picnic, so (x - 5) students attended the picnic

New cost of food for each member = Rs.  $\frac{2000}{x-5}$ 

According to the question

 $\frac{2000}{x-5} - \frac{2000}{x} = 20$   $\frac{2000x - 2000x + 10000}{x(x-5)} = 20 \text{ taking LCM}$   $\frac{10000}{x^2 - 5x} = 20$   $x^2 - 5x = 500 \text{ cross multiplying}$   $x^2 - 5x - 500 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1 b = -5 c = -500= 1. - 500 = -500And either of their sum or difference = b = -5Thus the two terms are - 25 and 20 Sum = -25 + 20 = -5Product = -25.20 = -500 $x^2 - 5x - 500 = 0$  $x^2 - 25x + 20x - 500 = 0$ x(x - 25) + 20(x - 25) = 0(x + 20) (x - 25) = 0(x + 20) = 0 or (x - 25) = 0x = -20 or x = 25x cannot be negative thus x = 25The number of students who planned picnic = x - 5 = 25 - 5 = 20Cost of food for each member = Rs.  $\frac{2000}{25-5}$  = Rs.  $\frac{2000}{20}$  = Rs. 100 **Question: 33** If the price of a Solution: Let the original price of the book be Rs x Number of books bought at original price for  $600 = \frac{600}{100}$ If the price of a book is reduced by Rs. 5, then new price of book is Rs (x - 5)Number of books bought at reduced price =  $\frac{600}{v-5}$ 

According to the question - -

 $\frac{600}{x-5} - \frac{600}{x} = 4$   $\frac{600x - 600x + 3000}{x(x-5)} = 4$   $\frac{3000}{x^2 - 5x} = 4$   $x^2 - 5x = 750$   $x^2 - 5x - 750 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -5 c = -750

= 1. - 750 = - 750

And either of their sum or difference = b

= - 5

Thus the two terms are – 30 and 25

Difference = -30 + 25 = -5

Product = -30.25 = -750

 $x^2 - 5x - 750 = 0$ 

 $x^2 - 30x + 25x - 750 = 0$ 

x(x - 30) + 25(x - 30) = 0

(x + 25) (x - 30) = 0

(x + 25) = 0 or (x - 30) = 0

```
x=-\,25 , x=\,30
```

x = 30 (Price cannot be negative)

Hence the original price of the book is Rs 30.

### **Question: 34**

A person on tour

### Solution:

Let the original duration of the tour be x days

Original daily expenses = Rs.  $\frac{10800}{x}$ 

If he extends his tour by 4 days his daily expenses = Rs.  $\frac{10800}{x+4}$ 

According to the question – –

```
\frac{10800}{x} - \frac{1080}{x+4} = 90
\frac{10800x + 43200 - 10800x}{x(x+4)} = 90 \text{ taking LCM}
\frac{43200}{x^2 + 4x} = 90
```

 $x^2 + 4x = 480$  cross multiplying

 $x^2 + 4x - 480 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1 b = 4 c = -480= 1. - 480 = - 480 And either of their sum or difference = b = 4 Thus the two terms are 24 and - 20 Difference = 24 - 20 = 4 Product = 24. - 20 = - 480  $x^2 + 24x - 20x - 480 = 0$  x(x + 24) - 20(x + 24) = 0 (x + 24) (x - 20) = 0 (x + 24) = 0 or (x - 20) = 0 x = -24, x = 20 x = 20 (number of days cannot be negative) Hence the original price of tour is 20 days

#### **Question: 35**

In a class test,

### Solution:

Let the marks obtained by P in mathematics and science be x and (28 - x) respectively

According to the given condition,

(x + 3)(28 - x - 4) = 180(x + 3)(24 - x) = 180- x<sup>2</sup> + 21x + 72 = 180x<sup>2</sup> - 21x + 108 = 0

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -21 c = 108

= 1.108 = 108

And either of their sum or difference = b

= - 21

Thus the two terms are – 12 and – 9  $\,$ 

Difference = -12 - 9 = -21

Product = -12. - 9 = 108

 $x^2 - 12x - 9x + 108 = 0$ 

x (x - 12) - 9 (x - 12) = 0

(x - 12) (x - 9) = 0 (x - 12) = 0 or (x - 9) = 0 x = 12, x = 9When x = 12, 28 - x = 28 - 12 = 16When x = 9, 28 - x = 28 - 9 = 19

Hence he obtained 12 marks in mathematics and 16 science or

He obtained 9 marks in mathematics and 19 science.

# **Question: 36**

A man buys a numb

### Solution:

Let the total number of pens be  $\boldsymbol{x}$ 

According to the question - -

$$\frac{180}{x} - \frac{180}{x+3} = 3$$

$$\frac{180(x+3) - 180x}{x(x+3)} = 3 \text{ taking LCM}$$

$$180x + 540 - 180x$$

 $\frac{180x + 540 - 180x}{x^2 + 3x} = 3$ 

 $540 = 3x^2 + 9x$  cross multiplying

 $3x^2 + 9x - 540 = 0$ 

 $x^2 + 3x - 180 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 3 c = -180

= 1. - 108 = - 180

And either of their sum or difference = b

= 3

Thus the two terms are 15 and – 12  $\,$ 

Difference = 15 - 12 = 3

Product = 15. - 12 = -180

 $x^2 + 15x - 12x - 180 = 0$ 

x(x + 15) - 12(x + 15) = 0

(x + 15)(x - 12) = 0

(x + 15) = 0 or (x - 12) = 0

$$x = -15, x = 12$$

x = 12 (Total number of pens cannot be negative)

Hence the Total number of pens is 12

## **Question: 37**

A dealer sells an

# Solution:

Let the cost price of the article be  $\boldsymbol{x}$ 

Gain percent x%

According to the given condition,

 $x + \frac{x}{100}x = 75$  (cost price + gain = selling price)

 $\frac{100x + x^2}{100} = 75 \text{ taking LCM}$ 

by cross multiplying

 $x^2 + 100x = 7500$ 

 $x^2 + 100x - 7500 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 100 c = -7500

= 1. - 7500 = - 7500

And either of their sum or difference = b

= 100

Thus the two terms are 150 and – 50

Difference = 150 - 50 = 100

Product = 150. - 50 = -7500

 $x^2 + 150x - 50x - 7500 = 0$ 

x(x + 150) - 50(x + 150) = 0

(x + 150) (x - 50) = 0

(x + 150) = 0 or (x - 50) = 0

 $x = 50 (x \neq -150 as price cannot be negative)$ 

Hence the cost price of the article is  $\mbox{Rs}\ 50$ 

# **Question: 38**

One year ago, a m

# Solution:

Let the present age of son be x years

The present age of man =  $x^2$  years

One year ago age of son = (x - 1)years

age of man =  $(x^2 - 1)$ years

According to given question, One year ago, a man was 8 times as old as his son

$$x^{2} - 1 = 8(x - 1)$$
  
 $x^{2} - 1 = 8x - 8$   
 $x^{2} - 8x + 7 = 0$ 

 $x^{2} - 7x - x + 7 = 0$  x(x - 7) - 1(x - 7) = 0 (x - 7) (x - 1) = 0 x = 1 or x = 7Man's age cannot be 1 year Thus x = 7Thus the present age of son is 7 years

The present age of man is  $7^2 = 49$  years

## **Question: 39**

The sum of the re

# Solution:

Let the present age of Meena be x years Meena's age three years ago = (x - 3) years Meena's age five years hence = (x + 5) years According to given question

 $\frac{1}{x-3} + \frac{1}{x+5} = \frac{1}{3}$  $\frac{x+5+x-3}{(x-3)(x+5)} = \frac{1}{3}$  $\frac{2x+2}{(x^2+2x-15)} = \frac{1}{3}$  $x^2 + 2x - 15 = 6x + 6$  $x^2 - 4x - 21 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -4 c = -21

= 1. - 21 = - 21

And either of their sum or difference = b

= - 4

Thus the two terms are – 7 and 3  $\,$ 

Sum = -7 + 3 = -4

Product = -7.3 = -21

 $x^2 - 7x + 3x - 21 = 0$ 

x (x - 7) + 3(x - 7) = 0

(x - 7) (x + 3) = 0

x = -3 or x = 7

x = 7 age cannot be negative

Hence the present age of Meena is 7 years

# **Question: 40**

The sum of the ag

# Solution:

Let the present age of boy and his brother be x years and (25 - x) years

According to given question

x(25 - x) = 126 $25x - x^2 = 126$ 

 $x^2 - 25x + 126 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -25 c = 126

= 1.126 = 126

And either of their sum or difference = b

= - 25

Thus the two terms are – 18 and – 7

Sum = - 18 - 7 = - 25

Product = -18. - 7 = 126

 $x^2 - 18x - 7x + 126 = 0$ 

x (x - 18) - 7(x - 18) = 0

(x - 18) (x - 7) = 0

x = 18 or x = 7

x = 18 (Present age of boy cannot be less than his brother)

if x = 18

The present age of boy is 18 years and his brother is (25 - 18) = 7 years

# **Question: 41**

The product of Ta

# Solution:

Let the present age of Tanvy be x years

Tanvy's age five years ago = (x - 5) years

Tanvy's age eight years from now = (x + 8) years

(x - 5)(x + 8) = 30

 $x^2 + 3x - 40 = 30$ 

 $x^2 + 3x - 70 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 3 c = -70

= 1. - 70 = - 70

And either of their sum or difference = b

= 3

Thus the two terms are 10 and - 7 Difference = 10 - 7 = 3Product = 10 - 7 = -70  $x^{2} + 10x - 7x - 70 = 0$  x (x + 10) - 7(x + 10) = 0 (x + 10) (x - 7) = 0 x = -10 or x = 7 (age cannot be negative) x = 7The present age of Tanvy is 7 years

#### **Question: 42**

Two years ago, a

#### Solution:

Let son's age 2 years ago be x years, Then

man's age 2 years ago be  $3x^2$  years

son's present age = (x + 2) years

man's present age =  $(3x^2 + 2)years$ 

In three years' time :

son's age = (x + 2 + 3) = (x + 5) years

man's age =  $(3x^2 + 2 + 3)$ years =  $(3x^2 + 5)$  years

According to question

Man's age = 4 son's age

 $3x^2 + 5 = 4(x + 5)$ 

 $3x^2 + 5 = 4x + 20$ 

 $3x^2 - 4x - 15 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 3 b = -4 c = -15

= 3. - 15 = - 45

And either of their sum or difference = b

```
= - 4
```

Thus the two terms are -9 and 5 Difference = -9 + 5 = -4

Product = -9.5 = -45

 $3x^2 - 9x + 5x - 15 = 0$ 

3x(x - 3) + 5(x - 3) = 0

(x - 3) (3x + 5) = 0

(x - 3) = 0 or (3x + 5) = 0

x = 3 or x = -5/3 (age cannot be negative)

x = 3

son's present age = (3 + 2) = 5years

man's present age =  $(3.3^2 + 2) = 29$ years

# **Question: 43**

A truck covers a

# Solution:

Let the first speed of the truck be x km/h

Time taken to cover 150 km =  $\frac{150}{r}$  h

New speed of truck = x + 20 km/h

Time taken to cover 200 km =  $\frac{200}{x+20}$  h

According to given question

$$\frac{150}{x} + \frac{200}{x+20} = 5$$

$$\frac{150x + 3000 + 200x}{x(x+20)} = 5$$

$$\frac{350x + 3000}{x(x+20)} = 5$$

$$350x + 3000 = 5(x^2 + 20x)$$

$$350x + 3000 = 5x^2 + 100x$$

$$5x^2 - 250x - 3000 = 0$$

$$x^2 - 50x - 600 = 0$$

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -50 c = -600

= 1. - 600 = - 600

And either of their sum or difference = b

= - 50

Thus the two terms are –  $60 \mbox{ and } 10$ 

Difference = -60 + 10 = -50

Product = -60.10 = -600

 $x^2 - 60x + 10x - 600 = 0$ 

x (x - 60) + 10(x - 60) = 0

(x - 60) (x + 10) = 0

$$x = 60 \text{ or } x = -10$$

x = 60 (speed cannot be negative)

Hence the first speed of the truck is 60 km/hr

# **Question: 44**

While boarding an

#### Solution:

Let the original speed of the plane be x km/h

Actual speed of the plane = (x + 100) km/h

Distance of journey = 1500km

Time taken to reach destination at original speed =  $\frac{1500}{h}$ 

Time taken to reach destination at actual speed =  $\frac{1500}{x+100}$  h

According to given question

30 mins = 1/2 hr  $\frac{1500}{x} = \frac{1500}{x+100} + \frac{1}{2}$   $\frac{1500}{x} - \frac{1500}{x+100} = \frac{1}{2}$   $\frac{1500x + 150000 - 1500x}{x(x+100)} = \frac{1}{2}$   $\frac{150000}{x(x+100)} = \frac{1}{2}$   $x^{2} + 100x = 300000$   $x^{2} + 100x - 300000 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 100 c = -300000

= 1. - 300000 = - 300000

And either of their sum or difference = b

= 100

Thus the two terms are 600 and - 500

Difference = 600 - 500 = 100

Product = 600. - 500 = -300000

 $x^2 + 600x - 500x + 300000 = 0$ 

x (x + 600) - 500(x + 600) = 0

(x + 600)(x - 500) = 0

x = -600 or x = 500

x = 500 (speed cannot be negative)

Hence the original speed of the plane is 500 km/hr

# **Question: 45**

A train covers a

#### Solution:

Let the usual speed of the train be x km/h

Reduced speed of the train = (x - 8) km/h

Distance of journey = 480km

Time taken to reach destination at usual speed =  $\frac{480}{x}$  h

Time taken to reach destination at reduced speed =  $\frac{480}{x-8}$  h

According to given question

$$\frac{480}{x-8} = \frac{480}{x} + 3$$
  

$$\Rightarrow \frac{480}{x-8} - \frac{480}{x} = 3$$
  

$$\Rightarrow \frac{480x - 480x + 3840}{x(x-8)} = 3$$
  

$$\Rightarrow \frac{3840}{x(x-8)} = 3$$
  

$$\Rightarrow x^2 - 8x = 1280$$
  

$$\Rightarrow x^2 - 8x - 1280 = 0$$
  

$$\Rightarrow x^2 - 40x + 32x - 1280 = 0$$
  

$$\Rightarrow x(x - 40) + 32(x - 40) = 0$$
  

$$\Rightarrow (x - 40)(x + 32) = 0$$
  

$$\Rightarrow x = 40 \text{ or } x = -32$$
  

$$\Rightarrow x = 40 \text{ (speed cannot be negative)}$$

Hence the usual speed of the train is 40 km/h

#### **Question: 46**

A train travels a

#### Solution:

Let the first speed of the train be x km/h

Time taken to cover 54 km =  $\frac{54}{x}$  h

New speed of train = x + 6 km/h

Time taken to cover 63 km =  $\frac{63}{x+6}$  h

According to given question

$$\Rightarrow \frac{54}{x} + \frac{63}{x+6} = 3$$
  

$$\Rightarrow \frac{54x+324+63x}{x(x+6)} = 3$$
Taking LCM  

$$\Rightarrow 117x + 324 = 3(x^{2} + 6x)$$
  

$$\Rightarrow 117x + 324 = 3x^{2} + 18x$$
  

$$\Rightarrow 3x^{2} - 99x - 324 = 0$$
  

$$\Rightarrow x^{2} - 33x - 108 = 0$$
  

$$\Rightarrow x^{2} - 36x + 3x - 108 = 0$$
  

$$\Rightarrow x (x - 36) + 3(x - 36) = 0$$

 $\Rightarrow (x - 36) (x + 3) = 0$ 

 $\Rightarrow$  x = 36 or x = -3

 $\Rightarrow$  x = 36 (speed cannot be negative)

Hence the first speed of the train is 36 km/hr

# **Question: 47**

A train travels 1

# Solution:

Let the usual speed of the train be  $x\ km/h$ 

Time taken to cover 180 km =  $\frac{180}{x}$  h

New speed of train = x + 9 km/h

Time taken to cover 180 km =  $\frac{180}{x+9}$  h

According to the question

$$\frac{180}{x} - \frac{180}{x+9} = 1$$

$$\frac{180(x+9-x)}{x(x+9)} = 1$$

$$\frac{180.9}{x(x+9)} = 1$$

$$\frac{1620}{x(x+9)} = 1$$

$$1620 = x^2 + 9x$$

$$x^2 + 9x - 1620 = 0$$
Using the splitting m

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

```
Product = a.c

For the given equation a = 1 b = 9 c = -1620

= 1. - 1620 = - 1620

And either of their sum or difference = b

= 9

Thus the two terms are 45 and - 36

Difference = - 36 + 45 = 9

Product = - 36.45 = - 1620

x^2 + 45x - 36x + 1620 = 0

x(x + 45) - 36(x + 45) = 0

(x + 45) (x - 36) = 0

x = -45 or x = 36 (but x cannot be negative)

x = 36

Hence the usual speed of the train is 36 km/h

Question: 48
```

A train covers a

# Solution:

Let the original speed of the train be x km/h

Time taken to cover 90 km =  $\frac{90}{x}$  h New speed of train = x + 15 km/h Time taken to cover 90 km =  $\frac{90}{x+15}$  h According to the question  $\frac{90}{x} - \frac{90}{x+15} = \frac{1}{2}$   $\frac{90(x+15)-90x}{x(x+15)} = \frac{1}{2}$   $\frac{90x+1350-90x}{x(x+15)} = \frac{1}{2}$  $\frac{1350}{x(x+15)} = \frac{1}{2}$ 

 $2700 = x^2 + 15x$ 

 $x^2 + 15x - 2700 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 15 c = -2700

= 1. - 2700 = - 2700

And either of their sum or difference = b

= 15

Thus the two terms are –  $45 \ \text{and} \ 60$ 

Difference = 60 - 45 = 15

Product = 60. - 45 = -2700

 $x^2 + 60x - 45x - 2700 = 0$ 

x(x + 60) - 45(x + 60) = 0

(x + 60) (x - 45) = 0

x = -60 or x = 45 (but x cannot be negative)

Hence the original speed of the train is 45 km/h  $\,$ 

# **Question: 49**

A passenger train

# Solution:

Let the usual speed of the train be  $x\ km/h$ 

Time taken to cover 300 km =  $\frac{300}{x}$  h

New speed of train = x + 5 km/h

Time taken to cover 90 km =  $\frac{300}{x+5}$  h

According to the question

$$\frac{300}{x} - \frac{300}{x+5} = 2$$

$$\frac{300(x+5) - 300x}{x(x+5)} = 2$$

$$\frac{300x + 1550 - 300x}{x(x+5)} = 2$$

$$\frac{1550}{x(x+5)} = 2$$

$$750 = x^2 + 5x$$

$$x^2 + 5x - 750 = 0$$

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 5 c = -750

= 1. - 750 = - 750

And either of their sum or difference = b

```
= 5
```

Thus the two terms are – 25 and 30

Difference = 30 - 25 = 5

Product = 30. - 25 = -750

 $x^2 + 30x - 25x - 750 = 0$ 

x(x + 30) - 25(x + 30) = 0

(x + 30) (x - 25) = 0

x = -30 or x = 25 (but x cannot be negative)

x = 25

Hence the usual speed of the train is 25 km/h  $\,$ 

## **Question: 50**

The distance betw

# Solution:

Let the speed of Deccan Queen be  $x\ km/h$ 

Speed of another train = (x - 20)km/h

According to the question

$$\frac{192}{x-20} - \frac{192}{x} = \frac{48}{60}$$
$$\frac{4}{x-20} - \frac{4}{x} = \frac{1}{60}$$
$$\frac{4x-4(x-20)}{x(x-20)} = \frac{1}{60}$$
 taking LCM

 $\frac{4x - 4x + 80}{x(x - 20)} = \frac{1}{60}$  $\frac{80}{x(x - 20)} = \frac{1}{60}$ 

 $4800 = x^2 - 20x$  cross multiplying

 $x^2 - 20x - 4800 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -20 c = -4800

= 1. - 4800 = -4800

And either of their sum or difference = b

= - 20

Thus the two terms are – 80 and 60

Difference = -80 + 60 = -20

Product = -80.60 = -4800

 $x^2 - 80x + 60x - 4800 = 0$ 

x(x - 80) + 60(x - 80) = 0

(x - 80) (x + 60) = 0

x = 80 or x = -60 (but x cannot be negative)

Hence the speed of Deccan Queen is 80 km/hr

## **Question: 51**

A motor boat whos

#### Solution:

Let the speed of stream be  $x\ km/h$ 

Speed of boat is 18 km/hr

 $\Rightarrow$  Speed of boat in downstream = (18 + x)km/h

 $\Rightarrow$  Speed of boat in upstream = (18 - x)km/h

As, distance = spped × time  $\Rightarrow$  time =  $\frac{\text{distance}}{\text{speed}}$   $\Rightarrow$  Time taken by boat in downstream to travel

$$24 \text{ Km} = \frac{24}{18 + x} \text{ hours}$$

 $\Rightarrow \text{ Time taken by boat in upstream to travel 24 Km} = \frac{24}{18 - x} \quad \text{hours} \Rightarrow \frac{24}{18 - x} - \frac{24}{18 + x} = 1$ 

$$\Rightarrow \frac{1}{18 - x} - \frac{1}{18 + x} = \frac{1}{24}$$
  
$$\Rightarrow \frac{18 + x - (18 - x)}{(18 + x)(18 - x)} = \frac{1}{24}$$
  
$$\Rightarrow \frac{2x}{18^2 - x^2} = \frac{1}{24} \quad [\text{using } (a + b)(a - b) = a^2 - b^2]$$
  
$$\Rightarrow 324 - x^2 = 48x$$
  
$$\Rightarrow x^2 + 48x - 324 = 0$$

 $\Rightarrow x^{2} + 54x - 6x - 324 = 0$  $\Rightarrow x(x + 54) - 6(x + 54) = 0$  $\Rightarrow (x + 54)(x - 6) = 0$  $\Rightarrow x = -54 \text{ or } x = 6$ (but speed cannot be negative)

 $\Rightarrow x = 6$ 

Hence the speed of stream is 6 km/h  $\,$ 

#### **Question: 52**

The speed of a bo

# Solution:

Let the speed of stream be x km/h

Speed of boat is 8 km/hr

Speed downstream = (8 + x)km/h

Speed upstream = (8 - x)km/h

$$\frac{22}{8+x} + \frac{15}{8-x} = 5$$

$$\frac{22(8-x) + 15(8+x)}{(8-x)(8+x)} = 5$$

$$\frac{176 - 22x + 120 + 15x}{(8+x)(8-x)} = 5$$

$$\frac{296 - 7x}{8^2 - x^2} = 5$$

$$296 - 7x = 320 - 5x^2$$

$$5x^2 - 7x - 24 = 0$$

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 5 b = -7 c = -24

= 5. - 24 = - 120

And either of their sum or difference = b

Thus the two terms are 8 and –  $15\,$ 

Difference = 8 - 15 = -7Product = 8 - 15 = -120  $5x^2 - 7x - 24 = 0$   $5x^2 - 15x + 8x - 24 = 0$  5x(x - 3) + 8(x - 3) = 0 (5x + 8)(x - 3) = 0x = 3 or x = -8/5

(but x cannot be negative)

x = 3

Hence the speed of stream is 3 km/hr

# **Question: 53**

A motorboat whose

# Solution:

Let the speed of stream be  $x\ km/h$ 

Speed of boat is 9km/hr

Speed downstream = (9 + x)km/h

Speed upstream = (9 - x)km/h

Distance covered downstream = Distance covered upstream = 15km

Total time taken = 3 hours 45 minutes =  $3 + \frac{45}{60} = \frac{225}{60} = \frac{15}{4}$  hrs

$$\frac{15}{9+x} + \frac{15}{9-x} = \frac{15}{4}$$
$$\frac{1}{9+x} + \frac{1}{9-x} = \frac{1}{4}$$
$$\frac{9-x+9+x}{(9+x)(9-x)} = \frac{1}{4}$$
taking LCM
$$\frac{18}{(9+x)(9-x)} = \frac{1}{4}$$

 $81 - x^2 = 72$  cross multiplying

$$x^2 = 81 - 72$$

 $x^2 = 9$  taking square root

x = 3 or - 3 (rejecting negative value)

Hence the speed of stream is 3 km/hr

# **Question: 54**

A takes 10 days l

# Solution:

Let B take x days to complete the work

Work one by B in one day  $\frac{1}{2}$ 

A will take (x - 10) days to complete the work

Work one by B in one day  $\frac{1}{x-10}$ 

According to the question

$$\frac{1}{x} + \frac{1}{x - 10} = \frac{1}{12}$$
$$\frac{x - 10 + x}{(x)(x - 10)} = \frac{1}{12}$$
$$\frac{2x - 10}{(x^2 - 10x)} = \frac{1}{12}$$
$$x^2 - 10x = 12 (2x - 10)$$
$$x^2 - 10x = 24x - 120$$

 $x^2 - 34x + 120 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.cFor the given equation a = 1 b = -34 c = 120= 1.120 = 120And either of their sum or difference = b = -34Thus the two terms are - 30 and - 4 Sum = -30 - 4 = -34Product = -30. - 4 = 120 $x^2 - 30x - 4x + 120 = 0$ x(x - 30) - 4(x - 30) = 0(x - 30) (x - 4) = 0x = 30 or x = 4x = 30 (number of days to complete the work by B cannot be less than A) B completes the work in 30 days **Question: 55** Two pipes running Solution:

Let one pipe fills a cistern in x mins.

Other pipe fills the cistern in (x + 3) mins.

Running together can fill a cistern in  $3\frac{1}{12}$  minutes = 40/13 mins

Part filled by one pipe in  $1 \min = \frac{1}{2}$ 

Part filled by other pipe in  $1 \min = \frac{1}{x+3}$ 

Part filled by both pipes Running together in  $1\min = \frac{1}{x} + \frac{1}{x+3}$ 

$$\frac{1}{x} + \frac{1}{x+3} = \frac{13}{40}$$
$$\frac{x+3+x}{x(x+3)} = \frac{13}{40}$$
$$\frac{2x+3}{x(x+3)} = \frac{13}{40}$$
$$13x^2 + 39x = 80x + 120$$
$$13x^2 - 41x - 120 = 0$$

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 13 b = -41 c = -120

= 13. - 120 = -1560

And either of their sum or difference = b = - 41 Thus the two terms are - 65 and 24 Difference = - 65 + 24 = - 41 Product = - 65.24 = - 1560  $13x^2 - 65x + 24x - 120 = 0$  13x(x - 5) + 24(x - 5) = 0 (x - 5) (13x + 24) = 0 (x - 5) = 0 (13x + 24) = 0 x = 5 or x = -24/13x = 5 (speed cannot be negative fraction)

Hence one pipe fills a cistern in 5 minutes and other pipe fills the cistern in (5 + 3) = 8 minutes.

# **Question: 56**

Two pipes running

# Solution:

Let the time taken by one pipe to fill the tank be x minutes

The time taken by other pipe to fill the tank = x + 5 minutes

Volume of tank be V

Volume of tank filled by one pipe in x minutes = V

Volume of tank filled by one pipe in 1 minutes = V/x

Volume of tank filled by one pipe in  $11\frac{1}{9}$  minutes  $=\frac{V}{x} \cdot 11\frac{1}{9} = \frac{V}{x} \cdot \frac{100}{9}$ 

Volume of tank filled by other pipe in  $11\frac{1}{9}$  minutes  $=\frac{V}{x+5}$ .  $11\frac{1}{9} = \frac{V}{x+5}$ .  $\frac{100}{9}$ 

Volume of tank filled by one pipe in  $11\frac{1}{9}$  minutes + Volume of tank filled by other pipe in  $11\frac{1}{9}$  minutes = V

 $\frac{100}{9} V \left(\frac{1}{x} + \frac{1}{x+5}\right) = V$  $\frac{1}{x} + \frac{1}{x+5} = \frac{9}{100}$  $\frac{x+5+x}{x(x+5)} = \frac{9}{100}$  $\frac{5+2x}{x(x+5)} = \frac{9}{100}$  $200x + 500 = 9x^2 + 45x$  $9x^2 - 155x - 500 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 9 b = -155 c = -500

= 9. - 500 = - 4500

And either of their sum or difference = b

= - 155 Thus the two terms are - 180 and 25 Difference = - 180 + 25 = - 155 Product = - 180.25 = - 4500  $9x^2 - 180x + 25x - 500 = 0$  9x(x - 20) + 25(x - 20) = 0 (x - 20) (9x + 25) = 0 (x - 20) = 0 (9x + 25) = 0 x = 20 or x = - 25/9x = 20 (time cannot be negative fraction)

Hence one pipe fills the tank in 20 mins. and other pipe fills the cistern in (20 + 5) = 25 mins

#### **Question: 57**

Two water taps to

#### Solution:

Let the time taken by tap of smaller diameter to fill the tank be x hours

The time taken by tap of larger diameter to fill the tank = x - 9 hours

Let the volume of the tank be  $\boldsymbol{V}$ 

Volume of tank filled by tap of smaller diameter in x hours = V

 $\Rightarrow$  Volume of tank filled by tap of smaller diameter in 1 hour = V/x

 $\Rightarrow$  Volume of tank filled by tap of smaller diameter in 6 hours =  $\frac{V}{V}$ .6 =  $\frac{6V}{V}$ 

Similarly, Volume of tank filled by tap of larger diameter in 6 hours =  $\frac{V}{v=0}$ . 6

Volume of tank filled by tap of smaller diameter in 6 hours + Volume of tank filled by tap of larger diameter in 6 hours = V

 $6V\left(\frac{1}{x} + \frac{1}{x+9}\right) = V$   $\Rightarrow \frac{1}{x} + \frac{1}{x-9} = \frac{1}{6}$   $\Rightarrow \frac{x-9+x}{x(x-9)} = \frac{1}{6}$   $\Rightarrow \frac{2x-9}{x(x-9)} = \frac{1}{6}$   $\Rightarrow 12x - 54 = x^2 - 9x$   $\Rightarrow x^2 - 21x + 54 = 0$   $\Rightarrow x^2 - 18x - 3x + 54 = 0$   $\Rightarrow x(x - 18) - 3(x - 18) = 0$   $\Rightarrow (x - 18)(x - 3) = 0 \Rightarrow (x - 18) = 0 \text{ and } (x - 3) = 0$   $\Rightarrow x = 18 \text{ or } x = 3$ For x = 3, time taken by tap of larger diameter is negative which is not possible Hence the time taken by tap of smaller diameter to fill the tank be  $18\ hours$ 

The time taken by tap of larger diameter to fill the tank = 18 - 9 = 9 hours

## **Question: 58**

The length of a r

# Solution:

Let the length and breadth of a rectangle be 2x and x respectively

According to the question;

Area =  $288 \text{ cm}^2$ 

Area = length.breadth

 $x(2x) = 288 \text{ cm}^2$ 

 $2x^2 = 288$ 

 $x^2 = 144$ 

x = 12 or x = -12

x = 12 ( x cannot be negative)

length = 2.12 = 24 cm, breadth = 12 cm

# **Question: 59**

The length of a r

# Solution:

Let the length and breadth of a rectangle be 3x and x respectively

According to the question;

Area =  $147 \text{cm}^2$ 

Area = length.breadth

$$x(3x) = 147 \text{cm}^2$$

 $3x^2 = 147$ 

 $x^2 = 49$ 

x = 7 or x = -7 taking square root both sides

x = 7 (x cannot be negative)

length = 3.7 = 21cm, breadth = 7cm

# **Question: 60**

The length of a h

# Solution:

Let the breadth of hall be x m

The length of hall will be (x + 3) m

According to the question;

Area = 238cm<sup>2</sup>

Area = length .breadth

 $x^2 + 3x - 238 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1 b = 3 c = - 238 = 1. - 238 = - 238 And either of their sum or difference = b = 3 Thus the two terms are 17 and - 14 Difference = 17 - 14 = 3Product = 17 - 14 = -238  $x^{2} + 17x - 14x - 238 = 0$  x(x + 17) - 14(x + 17) = 0 (x + 17) (x - 14) = 0 x = -17 or x = 14x = 14 ( x cannot be negative)

Hence the breadth of hall is 14 m and the length of hall is (14 + 3) = 17 m

# **Question: 61**

The perimeter of

#### Solution:

Let the length and breadth of rectangular plot be  $\boldsymbol{x}$  and  $\boldsymbol{y}$  respectively.

Perimeter = 2(x + y) = 62 - - - - (1)

Area = xy = 228

y = 228/x

Putting the value of y in 1

$$2\left(x + \frac{228}{x}\right) = 62$$
$$x + \frac{228}{x} = 31$$
$$\frac{x^2 + 228}{x} = 31 \text{ taking LCM}$$
$$x^2 + 228 = 31x \text{ cross multiplying}$$

$$x^2 - 31x + 288 = 0$$

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -31 c = 288

= 1.288 = 288

And either of their sum or difference = b

= - 31

Thus the two terms are – 19 and – 12  $\,$ 

Difference = -19 - 12 = -31

Product = -19. - 12 = 288

 $x^{2} - 19x - 12x + 288 = 0$  x(x - 19) - 12(x - 19) = 0 (x - 19) (x - 12) = 0 x = 19 or x = 12if x = 19  $y = \frac{228}{19} = 12$ if x = 12 $y = \frac{228}{12} = 19$ 

length is 19m and breadth is  $12\ensuremath{m}$ 

length is 12m and breadth is 19m

#### **Question: 62**

A rectangular fie

#### Solution:

Let the width of the path be x m

Length of the field including the path = 16 + x + x = 16 + 2x

Breadth of the field including the path = 10 + x + x = 10 + 2x

Area of field including the path - Area of field excluding the path = Area of path

(16 + 2x) (10 + 2x) - (16.10) = 120

 $160 + 32x + 20x + 4x^2 - 160 = 120$ 

 $4x^2 + 52x - 120 = 0$ 

 $x^2 + 13x - 30 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 13 c = -30

= 1. - 30 = - 30

And either of their sum or difference = b

= 13

Thus the two terms are 15 and – 2  $\,$ 

Difference = 15 - 2 = 13

Product = 15. - 2 = -30

 $x^2 + 15x - 2x - 30 = 0$ 

x(x + 15) - 2(x + 15) = 0

(x + 15) (x - 2) = 0

$$x = 2 \text{ or } x = -15$$

x = 2 (width cannot be negative)

Thus the width of the path is 2 m

# **Question: 63**

The sum of the ar

#### Solution:

Let the length of first and second square be x and y respectively

According to the question;

$$x^{2} + y^{2} = 640 - - - (1)$$
  
Also  $4x - 4y = 64$   
 $x - y = 16$   
 $x = 16 + y$   
Putting the value of x in(1) we get  
 $(16 + y)^{2} + y^{2} = 640$  using  $(a + b)^{2} = a^{2} + 2ab + b^{2}$   
 $256 + 32y + y^{2} + y^{2} = 640$   
 $2y^{2} + 32y - 384 = 0$   
 $y^{2} + 16y - 192 = 0$   
Using the splitting middle term - the middle term of the generic divided in two such values that:

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 16 c = -192

= 1. - 192 = - 192

And either of their sum or difference = b

= 16

Thus the two terms are 24 and -8

Difference = 24 - 8 = 16

Product = 24. - 8 = 192

 $y^2 + 24y - 8y - 192 = 0$ 

y(y + 24) - 8(y + 24) = 0

(y + 24) (y - 8) = 0

(y + 24) = 0 (y - 8) = 0

y = 8 or y = -24

y = 8 (y cannot be negative)

x = 16 + 8 = 24m

Hence the length of first square is 24m and second square is 8m.

## **Question: 64**

The length of a r

#### Solution:

Let the breadth of a rectangle be x cm According to the question; Side of square = (x + 4) cm Length of a rectangle = [3(x + 4)] cm Area of rectangle and square are equal - -  $3(x + 4)x = (x + 4)^{2}$   $3x^{2} + 12x = (x + 4)^{2}$   $3x^{2} + 12x = x^{2} + 8x + 16 \{ using (a + b)^{2} = a^{2} + 2ab + b^{2} \}$   $2x^{2} + 4x - 16 = 0$  $x^{2} + 2x - 8 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 2 c = -8

= 1. - 8 = - 8

And either of their sum or difference = b

```
= 2
```

Thus the two terms are 4 and – 2  $\,$ 

Difference = 4 - 2 = 2

Product = 4. - 2 = -8

 $x^2 + 4x - 2x - 8 = 0$ 

x(x + 4) - 2(x + 4) = 0

(x + 4) (x - 2) = 0

 $\Rightarrow$  x = -4 or x = 2

x = 2 (width cannot be negative)

Thus the breadth of a rectangle = 2 cm

Length of a rectangle = [3(x + 4)] = 3(2 + 4) = 18 cm

Side of square = (x + 4) = 2 + 4 = 6cm

# **Question: 65**

A farmer prepares

## Solution:

Let the length and breadth of rectangular plot be x and y respectively.

Area = 
$$xy = 180 \text{ sq m} - - - - (1)$$
  
 $2(x + y) - x = 39$   
 $2x + 2y - x = 39$   
 $2y + x = 39$   
 $x = 39 - 2y$   
Putting the value of x in (1) we get  
 $(39 - 2y)y = 180$   
 $39y - 2y^2 = 180$ 

 $2y^2 - 39y + 180 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

For the given equation a = 2 b = -39 c = 180= 2.180 = 360 And either of their sum or difference = b = - 39 Thus the two terms are - 24 and - 15 Difference = - 24 - 15 = - 39 Product = - 24. - 15 = 360  $2y^2 - 24y - 15y + 180 = 0$ 2y(y - 12) - 15(y - 12) = 0(y - 12)(2y - 15) = 0y = 12 or y = 15/2 = 7.5if y = 12 x = 39 - 2y = 39 - (2.12) = 39 - 24 = 15if y = 7.5 x = 39 - 2y = 39 - [(2)(7.5)] = 39 - 15 = 24Hence either l = 24 m, b = 7.5 m or l = 15 m, b = 12 m

#### **Question: 66**

The area of a rig

#### Solution:

Let the altitude of the given triangle  $x \ cm$ 

Thus the base of the triangle will be (x + 10)cm

Area of triangle =  $\frac{1}{2}x(x + 10) = 600$ 

x(x + 10) = 1200

 $x^2 + 10x - 1200 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 10 c = -1200

= 1. - 1200 = - 1200

And either of their sum or difference = b

= 10

Thus the two terms are 40 and – 30  $\,$ 

Difference = 40 - 30 = 10

Product = 40. - 30 = -1200

 $x^2 + 40x - 30x - 1200 = 0$ 

x(x + 40) - 30(x + 40) = 0

(x + 40)(x - 30) = 0

$$x = -40, 30$$

x = 30 (altitude cannot be negative)

Thus the altitude of the given triangle is 30cm and base of the triangle = 30 + 10 = 40cm

 $Hypotenuse^2 = altitude^2 + base^2$ 

 $Hypotenuse^2 = (30)^2 + (40)^2$ = 900 + 1600 = 2500Hypotenuse = 50 cmAltitude = 30cm Base = 40cm**Question: 67** The area of a rig Solution: Let the altitude of the triangle be x m The base will be 3x m Area of triangle = 1/2. Base. altitude 1/2.3x.x = 96 $\frac{x^2}{2} = 32$  $x^2 = 64$ x = 8 or - 8 taking square rootValue of x cannot be negative Thus the altitude of the triangle be 8 m The base will be 3.8 = 24m **Ouestion: 68** 

The area of a rig

#### Solution:

Let the base be x m

The altitude will be x + 7 m

Area of triangle = 1/2 base. altitude

= 1/2 x (x + 7) = 165

 $\mathbf{x}^2 + 7\mathbf{x} = 330$ 

 $x^2 + 7x - 330 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c For the given equation a = 1 b = 7 c = -330= 1. - 330 = - 330 And either of their sum or difference = b = 7 Thus the two terms are 22 and - 15 Difference = 22 - 15 = 7 Product = 22. - 15 = - 330  $x^2 + 22x - 15x - 330 = 0$  x(x + 22) - 15(x + 22) = 0

(x + 22) (x - 15) = 0

x = -22 or x = 15

Value of x cannot be negative

Thus the base be 15m and altitude = 15 + 7 = 22m

# **Question: 69**

The hypotenuse of

# Solution:

Let one side of right – angled triangle be  $x\ m$  and other side be  $x\ +\ 4\ m$ 

On applying the Pythagoras theorem -

$$20^{2} = (x + 4)^{2} + x^{2}$$
  

$$400 = x^{2} + 8x + 16 + x^{2}$$
  

$$400 = 2x^{2} + 8x + 16$$
  

$$2x^{2} + 8x - 384 = 0$$
  

$$x^{2} + 4x - 192 = 0$$

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = 4 c = -192

= 1. - 192 = - 192

And either of their sum or difference = b

= 4

Thus the two terms are 16 and –  $12\,$ 

Difference = 16 - 12 = 4

Product = 16. - 12 = -192

 $x^2 + 16x - 12x - 192 = 0$ 

x(x + 16) - 12(x + 16) = 0

(x + 16) (x - 12) = 0

```
x = 16 \text{ or } x = 12
```

x cannot be negative

Base is 12m and other side is 12 + 4 = 16m

# **Question: 70**

The length of the

# Solution:

Let the base and altitude of the right angled triangle be  $\boldsymbol{x}$  and  $\boldsymbol{y}$  respectively.

Thus the hypotenuse of triangle will be x + 2 cm

 $(x + 2)^2 = y^2 + x^2 - - - (1)$ 

Also the hypotenuse exceeds twice the length of the altitude by 1 cm

h = 2y + 1 x + 2 = 2y + 1 x = 2y - 1Putting the value of x in (1) we get  $(2y - 1 + 2)^{2} = y^{2} + (2y - 1)^{2}$   $(2y + 1)^{2} = y^{2} + 4y^{2} - 4y + 1$   $4y^{2} + 4y + 1 = 5y^{2} - 4y + 1 \text{ using } (a + b)^{2} = a^{2} + 2ab + b^{2}$   $-y^{2} + 8y = 0$  y(y - 8) = 0 y = 8 x = 16 - 1 = 15 cmh = 16 + 1 = 17 cm

Thus the base, altitude, hypotenuse of triangle are 15cm, 8cm, 17cm respectively.

#### **Question: 71**

The hypotenuse of

#### Solution:

Let the shortest side of triangle be xm

According to the question ;

Hypotenuse = 2x - 1 m

Third side = x + 1 m

Applying Pythagoras theorem

 $(2x - 1)^2 = (x + 1)^2 + x^2$ 

 $4x^2 - 4x + 1 = x^2 + 2x + 1 + x^2$  using  $(a - b)^2 = a^2 - 2ab + b^2$ 

 $2 x^2 - 6x = 0$ 

2x(x-3)=0

x = 0 or x = 3

Length of side cannot be 0 thus the shortest side is 3m

Hypotenuse = 2x - 1 = 6 - 1 = 5m

Third side = x + 1 = 3 + 1 = 4m

Thus the dimensions of triangle are 3m, 4m and 5m.

# **Exercise : 10F**

#### **Question: 1**

Which of the foll

#### Solution:

A quadratic equation is of the form  $ax^2 + bx + c = 0$  i.e. of degree 2 (a  $\neq$  0, a, b, c are real numbers)

A.  $x^2 - 3\sqrt{x} + 2 = 0$  this is not of the form  $ax^2 + bx + c = 0$  hence it is not quadratic equation. B.  $x + \frac{1}{x} = x^2$   $x^2 + 1 = x^3 x^3 - x^2 - 1 = 0$ 

This is not of the form  $ax^2 + bx + c = 0$  hence it is not quadratic equation.

C. 
$$x^{2} + \frac{1}{x^{2}} = 5$$
  
 $x^{4} + 1 = 5x^{2}$   
 $5x^{2} - x^{4} - 1 = 0$ 

This is not of the form  $ax^2 + bx + c = 0$  hence it is not quadratic equation.

D. 
$$2x^2 - 5x = (x - 1)^2$$
 using  $(a - b)^2 = a^2 + b^2 - 2ab$   
 $2x^2 - 5x = x^2 - 2x + 1$   
 $2x^2 - 5x - x^2 + 2x - 1 = 0$   
 $x^2 - 3x - 1 = 0$   
 $a = 1b = -3c = -1$ 

This is of the form  $ax^2 + bx + c = 0$  i.e. of degree 2 (a  $\neq 0$ , a, b, c are real numbers) Hence this is a quadratic equation.

#### **Question: 2**

Which of the foll

# Solution:

A.  $(x^{2} + 1) = (2 - x)^{2} + 3$  using  $(a - b)^{2} = a^{2} + b^{2} - 2ab$   $x^{2} + 1 = 4 + x^{2} - 4x + 3$   $x^{2} + 1 - 4 - x^{2} + 4x - 3 = 0$ 4x - 6 = 0

This is not of the form  $ax^2 + bx + c = 0$  hence it is not quadratic equation.

B.  $x^{3} - x^{2} = (x - 1)^{3}$  using  $(a - b)^{3} = a^{3} - b^{3} - 3a^{2}b + 3ab^{2}$   $x^{3} - x^{2} = x^{3} - 1 - 3x^{2} + 3x$   $x^{3} - x^{2} - x^{3} + 1 + 3x^{2} - 3x = 0$   $2x^{2} - 3x + 1 = 0$ a = 2b = -3c = 1

This is of the form  $ax^2 + bx + c = 0$  i.e. of degree 2 (a  $\neq 0$ , a, b, c are real numbers) Hence this is a quadratic equation.

#### **Question: 3**

Which of the foll

#### Solution:

A. 
$$3x - x^2 = x^2 + 5$$
  
 $3x - x^2 - x^2 - 5 = 0$   
 $-2x^2 + 3x - 5 = 0$ 

This is a quadratic equation of the form  $ax^2 + bx + c = 0$  hence i.e. of degree 2 (a  $\neq$  0, a, b, c are real numbers).

B. 
$$(x + 2)^2 = 2(x^2 - 5)$$
  
 $x^2 + 4 + 4x = 2x^2 - 10$  using  $(a + b)^2 = a^2 + b^2 + 2ab$   
 $x^2 + 4 + 4x - 2x^2 + 10 = 0$   
 $-x^2 + 4x + 14 = 0$ 

This is a quadratic equation of the form  $ax^2 + bx + c = 0$  i.e. of degree 2 (a  $\neq$  0, a, b, c are real numbers).

C. 
$$(\sqrt{2}x + 3)^2 = 2x^2 + 6$$
 using  $(a + b)^2 = a^2 + b^2 + 2ab$   
 $2x^2 + 9 + 6\sqrt{2}x = 2x^2 + 6$   
 $6\sqrt{2}x + 3 = 0$ 

This is not quadratic since it is not of the form  $ax^2 + bx + c = 0$  i.e. of degree 2 (a  $\neq 0$ , a, b, c are real numbers).

D. 
$$(x-1)^2 = 3x^2 + x - 2$$
  
 $x^2 - 2x + 1 = 3x^2 + x - 2$  using  $(a - b)^2 = a^2 + b^2 - 2ab$   
 $x^2 - 2x + 1 - 3x^2 - x + 2 = 0$   
 $-2x^2 - 3x + 3 = 0$ 

This is a quadratic equation of the form  $ax^2 + bx + c = 0$  i.e. of degree 2 (a  $\neq 0$ , a, b, c are real numbers).

## **Question: 4**

If x = 3 is a sol

# Solution:

 $3x^2 + (k-1)x + 9 = 0$ 

x = 3 is a solution of the equation means it satisfies the equation

```
3(3)^{2} + (k-1)3 + 9 = 0
```

27 + 3k - 3 + 9 = 0

27 + 3k + 6 = 0

3k = -33

k = -11

## **Question: 5**

If one root of th

# Solution:

One root of the equation  $2x^2 + ax + 6 = 0$  is 2 i.e. it satisfies the equation

$$2(2)^{2} + 2a + 6 = 0$$
  
 $8 + 2a + 6 = 0$   
 $2a = -14$   
 $a = -7$ 

# **Question: 6**

The sum of the ro

#### Solution:

For the equation  $x^2 - 6x + 2 = 0$ 

a = 1b = -6c = 2 comparing with general equation  $ax^2 + bx + c = 0$ 

$$\alpha + \beta = \frac{-b}{a}$$
$$= \frac{-(-6)}{1} = 6$$

Where  $\alpha$  and  $\beta$  are the roots of the equation.

#### **Question:** 7

If the product of

#### Solution:

Given that the product of the roots of the equation is - 2

$$x^{2} - 3x + k = 10$$
  

$$x^{2} - 3x + (k - 10) = 0$$
  

$$x^{2} - 3x + (k - 10) = 0$$
  

$$a = 1 b = -3 c = k - 10 \text{ comparing with general equation } ax^{2} + bx + c = 0$$
  
Product of the roots  $= \frac{c}{a}$   
 $= \frac{k - 10}{1} = k - 10$   
 $k - 10 = -2$   
 $k = -2 + 10$ 

$$k = 8$$

# **Question: 8**

The ratio of the

## Solution:

For the given equation  $7x^2 - 12x + 18 = 0$ 

a = 7 b = -12 c = 18 comparing with  $ax^2 + bx + c = 0$ Sum of the roots  $\frac{-b}{a} = \frac{-(-12)}{7}$ Product of the roots  $\frac{c}{a} = \frac{18}{7}$ Ratio of sum: product =  $\frac{12}{7}$ :  $\frac{18}{7}$ = 12:18 = 2:3 Question: 9 If one root of th

#### Solution:

For the given equation  $3x^2 - 10x + 3 = 0$ 

a = 3 b = -10 c = 3 comparing with  $ax^2 + bx + c = 0$ 

Product of the roots  $\frac{c}{a} = \frac{3}{3} = 1$ 

One root of the equation is  $\frac{1}{3}$ 

Let other root be  ${\boldsymbol{\alpha}}$ 

$$\alpha \frac{1}{3} = 1$$

 $\alpha = 3$ 

# **Question: 10**

If one root of 5x

## Solution:

Let the roots of equation be  $\alpha$  than other root will be  $\frac{1}{\alpha}$ 

Product of two roots  $=\frac{1}{\alpha}\alpha = 1$ 

Product of the roots =  $\frac{c}{a}$ 

For the given equation  $5x^2 + 13x + k = 0$ 

a = 5 b = 13 c = k comparing with  $ax^2 + bx + c = 0$ 

Product of the roots 
$$=\frac{k}{5} = 1$$

# **Question: 11**

If the sum of the

#### Solution:

For the given equation  $kx^2 + 2x + 3k = 0$  a = k b = 2 c = 3k comparing with  $ax^2 + bx + c = 0$ Sum of the roots  $= \frac{-b}{a} = \frac{-2}{k}$ Product of the roots  $\frac{c}{a} = \frac{3k}{k} = 3$ Sum of roots is equal to their product:  $\frac{-2}{k} = 3$  $k = \frac{-2}{3}$ 

# Question: 12

The roots of a qu

# Solution:

The roots of a quadratic equation will satisfy the equation - start with option 1

A. 
$$x^2 - 3x + 10 = 0$$
  
For  $x = 5$   
 $5^2 - (3.5) + 10$   
 $25 - 15 + 10 = 20 \neq 0$   
Hence this is not the equation  
B.  $x^2 - 3x - 10 = 0$ 

For x = 5

 $5^{2} - (3.5) - 10 = 25 - 15 - 10$ = 25 - 25 = 0For x = - 2 $= (-2)^{2} - (3. - 2) - 10$ = 4 + 6 - 10 = 10 - 10 = 0

This equation is satisfied for both the roots.

# **Question: 13**

If the sum of the

# Solution:

Sum = 6 and Product = 6

Quadratic equation =  $x^2$  -Sum x + Product = 0

 $= x^2 - 6x + 6 = 0$ 

# **Question: 14**

If  $\alpha$  and  $\beta$  are th

# Solution:

Given  $\alpha$  and  $\beta$  are the roots of the equation  $3x^2 + 8x + 2 = 0$ 

For the equation a = 3 b = 8 c = 2 comparing with  $ax^2 + bx + c = 0$ 

Sum of roots =  $\alpha + \beta = \frac{-b}{a} = \frac{-(8)}{3}$ 

Product of roots =  $\alpha\beta = \frac{c}{a} = \frac{2}{3}$ 

$$\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta} = \frac{\frac{-(8)}{3}}{\frac{2}{3}} = -4$$

# **Question: 15**

The roots of the

# Solution:

Let the roots of equation be  $\alpha$  and  $\frac{1}{\alpha}$ 

- Product of roots  $=\frac{1}{\alpha}\alpha = 1$
- Product of the roots  $\frac{c}{a} = 1$

Hence c = a

# **Question: 16**

If the roots of t

# Solution:

If roots of the equation  $ax^2 + bx + c = 0$  are equal

Then D = b<sup>2</sup> - 4ac = 0  
b<sup>2</sup> = 4ac  
c = 
$$\frac{b^2}{4a}$$

## **Question: 17**

If the equation 9

# Solution:

The equation  $9x^2 + 6kx + 4 = 0$  has equal roots

a = 9 b = 6k c = 4

Then  $D = b^2 - 4ac = 0$ 

 $(6k)^2 - 4.9.4 = 0$ 

 $36k^2 = 144$ 

 $k^2 = 4$  taking square root both sides

k = 2 or k = -2

# **Question: 18**

If the equation  $\boldsymbol{x}$ 

# Solution:

Given that the equation  $x^2 + 2(k + 2)x + 9k = 0$  has equal roots.

$$a = 1 b = 2(k + 2) c = 9k$$
  

$$D = b^{2} - 4ac = 0$$
  

$$(2k + 4)^{2} - 4.1.9k = 0$$
  

$$4k^{2} + 16 + 16k - 36k = 0$$
  

$$4k^{2} - 20k + 16 = 0$$
  

$$k^{2} - 5k + 4 = 0$$

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -5 c = 4

= 1.4 = 4

And either of their sum or difference = b

= - 5

Thus the two terms are -  $4 \mbox{ and }$  -  $1 \mbox{ }$ 

```
Difference = -4 - 1 = -5
```

Product = -4. -1 = 4

 $k^2 - 4k - k + 4 = 0$ 

k(k - 4) - 1(k - 4) = 0

(k - 4) (k - 1) = 0

k = 4 or k = 1

# **Question: 19**

If the equation 4

# Solution:

Given the equation  $4x^2 - 3kx + 1 = 0$  has equal roots

For the given equation a = 4 b = -3k c = 1

$$D = b^{2} - 4ac = 0$$
  
(-3k)<sup>2</sup> - 4.4.1 = 0  
9k<sup>2</sup> - 16 = 0  
9k<sup>2</sup> = 16

 $k^2 = 16/9$ 

 $k = \pm 4/3$ 

# **Question: 20**

The roots of ax

#### Solution:

The roots of equation are real and unequal, if  $(b^2 - 4ac) > 0$ 

#### **Question: 21**

In the equation a

## Solution:

If for the equation  $ax^2 + bx + c = 0$ , it is given that  $D = (b^2 - 4ac) > 0$  then the roots are real and unequal.

#### **Question: 22**

The roots of the

#### Solution:

For the given equation  $2x^2 - 6x + 7 = 0$ 

a = 2b = -6c = 7

 $D = b^2 - 4ac$ 

 $=(-6)^2 - 4.2.7$ 

= 36 - 56 = -20 < 0

Thus the roots of equation are imaginary.

#### **Question: 23**

The roots of the

# Solution:

For the given equation  $2x^2 - 6x + 3 = 0$ 

a = 2b = -6c = 3

 $D = b^2 - 4ac$ 

 $=(-6)^2 - 4.2.3$ 

= 36 - 24 = 12 > 0 this is not a perfect square hence the roots of the equation are real, unequal and irrational

#### **Question: 24**

If the roots of 5

## Solution:

Given that the roots of  $5x^2 - kx + 1 = 0$  are real and distinct

 $D = b^{2} - 4ac > 0$ = (-k)<sup>2</sup> - 4.5.1 = k<sup>2</sup> - 20 > 0 k<sup>2</sup> - 20

Roots are either  $k > 2\sqrt{5}$  or  $k < -2\sqrt{5}$ 

# **Question: 25**

If the equation **x** 

# Solution:

Given the equation  $x^2 + 5kx + 16 = 0$  has no real

a = 1 b = 5k c = 16Thus D = b<sup>2</sup>-4ac < 0 = (5k)<sup>2</sup>-4.1.16 < 0 = 25k<sup>2</sup>-64 < 0

 $\frac{25k^2}{5k^2} = 64$ 

$$k^{2} < \frac{64}{25}$$
  
 $\frac{-8}{5} < k < \frac{8}{5}$ 

# **Question: 26**

If the equation x

# Solution:

Given the equation  $x^2 - kx + 1 = 0$  has no real roots

a = 1 b = -kc = 1

Thus D =  $b^2 - 4ac < 0$ 

 $(-k)^2 - 4.1.1 < 0$ 

 $k^2 - 4 < 0$ 

 $k^2 - 4$ 

- 2 < k < 2

# **Question: 27**

For what values o

# Solution:

Given the equation  $kx^2 - 6x - 2 = 0$  has real roots a = k b = -6 c = -2

Thus  $D = b^2 - 4ac \ge 0$ 

 $(-6)^2 - 4.k. - 2 \ge 0$ 

<del>36 + 8k ≥0</del>

<del>8k≥ - 36</del>

 $k \ge \frac{-9}{2}$ 

#### **Question: 28**

The sum of a numb

# Solution:

Let the required number be x

According to the question

$$\frac{x + \frac{1}{x} = \frac{41}{20}}{\frac{x^2 + 1}{x} = \frac{41}{20}}$$

 $20x^2 - 41x + 20 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.c

For the given equation a = 20 b = -41 c = 20

= 20.20 = 400

And either of their sum or difference = b

```
---41
```

```
Thus the two terms are - 25 and - 16
```

```
Difference = -25 - 16 = -41
```

```
Product = -25. -16 = 400
```

```
20x^2 - 25x - 16x + 20 = 0
```

```
\frac{5x(4x-5)-4(4x-5)=0}{5x(4x-5)=0}
```

```
(5x - 4) (4x - 5) = 0
```

$$x = \frac{5}{4} \text{ or } \frac{4}{5}$$

# **Question: 29**

The perimeter of

# Solution:

Let the length and breadth of the rectangle be l and b respectively

Perimeter of a rectangle is 82 m 2(1 + b) = 82

1 + b = 41

l = 41 - b - (1)

Area is 400 m<sup>2</sup>

lb = 400

```
(41 - b) b = 400 using (1)
```

 $41b - b^2 = 400$ 

 $b^2 - 41b + 400 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.cFor the given equation a = 1 b = -41 c = 400= 1.400 = 400And either of their sum or difference = b = -41 Thus the two terms are - 25 and - 16 Difference = -25 - 16 = -41Product = -25. -16 = 400 $b^2 - 25b - 16b + 400 = 0$ b(b - 25) - 16(b - 25) = 0(b - 25)(b - 16) = 0b = 25 or b = 16If b = 25l = 41 - 25 = 16 but l cannot be less than b Thus b = 16mThe breadth of the rectangle = 16m**Ouestion: 30** The length of a r Solution: Let the breadth of the rectangle be x m Thus the length of the rectangle is (x + 8) m Area of the field is  $240 \text{ m}^2 = \text{length}$ . breadth x(x + 8) = 240

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.c

 $x^2 + 8x - 240 = 0$ 

For the given equation a = 1 b = 8 c = -240

= 1. - 240 = -240

And either of their sum or difference = b

= 8

Thus the two terms are 20 and - 12

 $\frac{\text{Difference} = 20 - 12 = 8}{2}$ 

Product = 20. - 12 = -240

 $x^2 + 20x - 12x - 240 = 0$ 

 $\frac{x(x+20)-12(x+20)=0}{x(x+20)=0}$ 

(x + 20)(x - 12) = 0

x = 12 or x = -20 (but breadth cannot be negative)

The breadth of the rectangle = 12m

### **Question: 31**

The roots of the

### Solution:

 $2x^2 - x - 6 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.c

For the given equation a = 2b = -1c = -6

= 2. - 6 = -12

And either of their sum or difference = b

```
<del>-1</del>
```

Thus the two terms are - 4 and 3

```
\overline{\text{Difference}} = -4 + 3 = -1
```

Product = -4.3 = -12

 $2x^2 - 4x + 3x - 6 = 0$ 

 $\frac{2x(x-2) + 3(x-2) = 0}{2x(x-2) - 1}$ 

(x-2)(2x+3) = 0

x = 2 x = -3/2

## **Question: 32**

The sum of two na

## Solution:

Let the required natural number be x and (8 - x)

their product is 15

 $\mathbf{x(8-x)} = 15$ 

 $8x - x^2 = 15$ 

 $x^2 - 8x + 15 = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.c

For the given equation a = 1 b = -8 c = 15

= 1.15 = 15

And either of their sum or difference = b

<del>--8</del>

Thus the two terms are - 5 and - 3

Sum = - 5 - 3 = - 8

Product = -5. -3 = 15

 $x^2 - 5x - 3x + 15 = 0$ 

 $\frac{x(x-5) - 3(x-5) = 0}{2}$ 

(x-5)(x-3) = 0

x = 5 or x = 3

Hence the required natural numbers are 5 and 3

## **Question: 33**

Show that x = -3

## Solution:

If x = -3 is a solution then it must satisfy the equation

- $x^2 + 6x + 9 = 0$
- $LHS = x^2 + 6x + 9$
- $=(-3)^2+6.-3+9$
- = 9 18 + 9
- = 18 18
- = 0 = RHS

Thus x = -3 is a solution of the equation

## **Question: 34**

Show that x = -2

## Solution:

If x = -2 is a solution then it must satisfy the equation

$$3x^2 + 13x + 14 = 0$$

 $LHS = 3x^2 + 13x + 14$ 

 $= 3(-2)^2 + 13(-2) + 14$ 

= 12 - 26 + 14 = 26 - 26 = 0 = RHS

Thus x = -2 is a solution of the equation

# **Question: 35**

<del>If</del>-

## Solution:

Given  $x = \frac{-1}{2}$  is a solution of the quadratic equation  $3x^2 + 2kx - 3 = 0$ . Thus it must satisfy the equation.

$$3\left(\frac{-1}{2}\right)^2 + 2k\left(\frac{-1}{2}\right) - 3 = 0$$
$$\left(\frac{3}{4}\right) - k - 3 = 0$$
$$k = \frac{3 - 12}{4} = \left(\frac{-9}{4}\right)$$

Hence the value of k is  $\frac{-9}{4}$ 

## **Question: 36**

Find the roots of

## Solution:

Given:  $2x^2 - x - 6 = 0$ 

Using the splitting middle term – the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.c For the given equation a = 2 b = -1 c = -6= 2. -6 = -12 And either of their sum or difference = b = -1 Thus the two terms are -4 and 3 Sum = -4 + 3 = -1 Product = -4.3 = -12  $2x^2 - 4x + 3x - 6 = 0$  2x(x - 2) + 3(x - 2) = 0 (x - 2)(2x + 3) = 0x = 2 or x = -3/2

Hence the roots of the given equation x = 2 or  $x = \frac{-3}{2}$ 

### **Question: 37**

Find the solution

## Solution:

The given  $3\sqrt{3}x^2 + 10x + \sqrt{3} = 0$ 

 $3\sqrt{3}x^2 + 9x + x + \sqrt{3} = 0$ 

Using the splitting middle term - the middle term of the general equation  $ax^2 + bx + c = 0$ -is divided in two such values that:

Product = a.c

For the given equation  $a = 3\sqrt{3} b = 10 c = \sqrt{3}$ 

 $= 3\sqrt{3} \cdot \sqrt{3} = 3.3 = 9$ 

And either of their sum or difference = b

= 10

Thus the two terms are 9 and 1

```
Sum = 9 + 1 = 10
```

Product = 9.1 = 9

 $3\sqrt{3}x^{2} + 9x + x + \sqrt{3} = 0 \text{ using } 9 = 3\sqrt{3} \cdot \sqrt{3}$  $3\sqrt{3}x (x + \sqrt{3}) + 1(x + \sqrt{3}) = 0$  $(x + \sqrt{3}) (3\sqrt{3}x + 1) = 0$  $(x + \sqrt{3}) = 0 \text{ or } (3\sqrt{3}x + 1) = 0$  $x = -\sqrt{3} \text{ or } x = \frac{1}{3\sqrt{3}}$ 

**Question: 38** 

### If the roots of t

### Solution:

The roots of the quadratic equation  $2x^2 + 8x + k = 0$  are equal then D = 0

a = 2 b = 8 c = k  $D = b^{2} - 4ac = 0$   $= 8^{2} - 4.2.k = 0$  = 64 - 8k = 0 8k = 64k = 8

## **Question: 39**

If the quadratic

### Solution:

The quadratic equation  $px^2 - 2\sqrt{5}px + 15 = 0$  has two equal roots

a = p b = 
$$-2\sqrt{5}pc = 15$$
  
D =  $b^2 - 4ac = 0$   
=  $(-2\sqrt{5}p)^2 - 4.p.15 = 0$   
=  $20p^2 - 60p = 0$   
=  $20p(p-3) = 0$   
p = 0 or p = 3

For p = 0 in the equation 0 + 0 + 15 = 0 but this is not possible

Thus  $p \neq 0$ 

### **Question: 40**

If 1 is a root of

## Solution:

Given that y = 1 is a root of the equation  $ay^2 + ay + 3 = 0$ 

- $a.1^2 + a.1 + 3 = 0$
- a + a + 3 = 0

2a + 3 = 0

a = -3/2

Also y = 1 is a root of the equation  $y^2 + y + b = 0$ 

 $1^2 + 1 + b = 0$ 

2 + b = 0

b = -2

$$ab = -2.\frac{-3}{2} = 3$$

Thus the value of ab = 3

### **Question: 41**

If one zero of th

### Solution:

Given one zero of the polynomial  $x^2 - 4x + 1$  is  $(2 + \sqrt{3})^7$ 

$$a = 1 b = -4 c = 1$$

Than let the other zero of the polynomial be  $\alpha$ 

Sum of zeroes 
$$=$$
  $\frac{-b}{a} = \frac{-(-4)}{1} = 4$   
 $\alpha + (2 + \sqrt{3}) = 4$   
 $\alpha = 4 - 2 - \sqrt{3}$ 

 $\alpha = 2 - \sqrt{3}$ 

Hence the other zero of the polynomial is  $2 - \sqrt{3}$ 

## **Question: 42**

If one root of th

### Solution:

Let  $\alpha$  and  $\beta$  be roots of the quadratic equation  $3x^2 - 10x + k = 0$ 

$$a = 3 b = -10 c = k$$
  
Then  $\alpha = \frac{1}{\beta}$   
 $\alpha\beta = 1$ 

For any general quadratic equation in the form  $ax^2 + bx + c = 0$ , we have Product of roots  $= \frac{c}{2} = \frac{k}{2}$ 

$$\frac{k}{3} = 1$$

## **Question: 43**

If the roots of t

## Solution:

Given that the roots of the quadratic equation px(x-2) + 6 = 0 are equal

$$px^2 - 2px + 6 = 0$$

Comparing with general equation $ax^2 + bx + c = 0$ , for the given equation

$$a = p b = -2p c = 6$$
  
Hence D = b<sup>2</sup> - 4ac = 0  
(-2p)<sup>2</sup> - 4. p. 6 = 0  
4p<sup>2</sup> - 24p = 0  
4p(p 6) = 0  
4p = 0 or (p 6) = 0  
p = 0 or p = 6

Putting p = 0 in equation given we get 6 = 0 that is not possible

Hence value of p = 6 for which the equation has equal roots.

#### **Question: 44**

Find the values o

#### Solution:

Given that the quadratic equation  $x^2 - 4kx + k = 0$  has equal roots

Comparing with general equation  $ax^2 + bx + c = 0$ , for the given equation

- a = 1 b = -4k c = kHence D = b<sup>2</sup> - 4ac = 0
- $(-4k)^2 4.1.k = 0$
- $16k^2 4k = 0$
- 4k(4k-1) = 0
- 4k = 0 or (4k-1) = 0
- $k = 0 \text{ or } k = \frac{1}{4}$

Hence 0 and  $\frac{1}{4}$  are values of k for which the equation has equal roots.

### **Question: 45**

Find the values o

### Solution:

Given that the quadratic equation  $9x^2 - 3kx + k = 0$  has equal roots

Comparing with general equation $ax^2 + bx + c = 0$ , for the given equation

- a = 9b = -3kc = k
- Hence  $D = b^2 4ac = 0$
- $(-3k)^2 4.9.k = 0$
- $9k^2 36k = 0$
- 9k(k-4) = 0
- 9k = 0 or (k-4) = 0
- k = 0 or k = 4

Hence 0 and 4 are values of k for which the equation has equal roots.

#### **Question: 46**

Solve:

#### Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 1 b = -(\sqrt{3} + 1) c = \sqrt{3}$ 

- $= 1.\sqrt{3}$
- $=\sqrt{3}$

And either of their sum or difference = b

$$= -(\sqrt{3} + 1)$$
  
Thus the two terms are  $-\sqrt{3} \& -1$   
Difference =  $-\sqrt{3} - 1 = -(\sqrt{3} - 1)$   
Product =  $-\sqrt{3} . -1 = \sqrt{3}$   
 $x^{2} - (\sqrt{3} + 1)x + \sqrt{3} = 0$   
 $x^{2} - \sqrt{3}x - x + \sqrt{3} = 0$   
 $x(x - \sqrt{3}) - 1(x - \sqrt{3}) = 0$   
 $(x - \sqrt{3})(x - 1) = 0$   
 $(x - \sqrt{3}) = 0 \text{ or } (x - 1) = 0$   
 $x = \sqrt{3} \text{ or } x = 1$ 

Hence the roots of given equation are  $x = \sqrt{3}$  or x = 1

# **Question: 47**

Solve: 2x

# Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 2b = ac = -a^2$ 

 $= 2.-a^2$ 

 $=-2a^{2}$ 

And either of their sum or difference = b

<del>-</del>-a

Thus the two terms are 2a & - a

```
\frac{\text{Difference}}{2a-a} = a
```

 $\frac{Product = 2a}{a} = -2a^2$ 

$$2x^2 + ax - a^2 = 0$$

 $2x^2 + 2ax - ax - a^2 = 0$ 

$$2x(x + a) - a(x + a) = 0$$

 $(\mathbf{x} + \mathbf{a})(2\mathbf{x} - \mathbf{a}) = \mathbf{0}$ 

(x + a) = 0 or (2x - a) = 0

$$x = -a \text{ or } x = \frac{a}{2}$$

Hence roots of equation are  $x = -a \text{ or } x = \frac{a}{2}$ 

# **Question: 48**

Solve: 3x<sup>2</sup>

#### Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.e For the given equation  $a = 3 b = 5\sqrt{5} c = -10$ = 3.-10 =--30 And either of their sum or difference = b =-5 $\sqrt{5}$ Thus the two terms are  $6\sqrt{5} \& -\sqrt{5}$ Difference =  $6\sqrt{5} - \sqrt{5} = 5\sqrt{5}$ Product =  $6\sqrt{5} - \sqrt{5} = -30$ -using  $\sqrt{5} \cdot \sqrt{5} = 5$   $3x^2 + 5\sqrt{5}x - 10 = 0$   $3x^2 + 6\sqrt{5}x - \sqrt{5}x - 10 = 0$   $3x(x + 2\sqrt{5}) - \sqrt{5}(x + 2\sqrt{5}x) = 0$   $(x + 2\sqrt{5})(3x - \sqrt{5}) = 0$   $(x + 2\sqrt{5}) = 0 \text{ or } (3x - \sqrt{5}) = 0$  $x = -2\sqrt{5} \text{ or } x = \frac{\sqrt{5}}{3}$ 

Hence roots of equation are  $x = -2\sqrt{5}$  or  $x = \frac{\sqrt{5}}{3}$ 

### **Question: 49**

Solve: √3x<

#### Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = \sqrt{3} b = 10 c = -8\sqrt{3}$ 

$$=\sqrt{3}.-8\sqrt{3}-using\sqrt{3}\sqrt{3} = 3$$

<del>-</del>--24

And either of their sum or difference = b

-10

Thus the two terms are 12 & -2

 $\frac{\text{Difference}}{12-2} = 10$ 

Product = 12. -2 = -24

 $\sqrt{3}x^2 + 10x - 8\sqrt{3} = 0$ 

 $\sqrt{3}x^2 + 12x - 2x - 8\sqrt{3} = 0$ 

 $\frac{\sqrt{3} x(x + 4\sqrt{3}) \cdot 2(x + 4\sqrt{3}) = 0}{(\sqrt{3} x \cdot 2)(x + 4\sqrt{3}) = 0}$  $\left(\sqrt{3} x - 2\right) = 0 \text{ or } \left(x + 4\sqrt{3}\right) = 0$  $x = -4\sqrt{3} \text{ or } x = \frac{2}{\sqrt{3}}$ 

Hence roots of equation are  $x = -4\sqrt{3}$  or  $x = \frac{2}{\sqrt{3}}$ 

### **Question: 50**

Solve: √3x<

### Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = \sqrt{3} b = -2\sqrt{2} c = -2\sqrt{3}$ 

$$=\sqrt{3} \cdot -2\sqrt{3} \cdot \text{using}\sqrt{3}\sqrt{3} = 3$$

---6

And either of their sum or difference = b

$$-2\sqrt{2}$$

Thus the two terms are  $-3\sqrt{2} \& \sqrt{2}$ 

Difference =  $-3\sqrt{2} + \sqrt{2} = -2\sqrt{2}$ Product =  $-3\sqrt{2}, \sqrt{2} = -6$ 

$$\sqrt{3} x^2 - 2\sqrt{2} x - 2\sqrt{3} = 0$$

$$\sqrt{3} x^2 - 3\sqrt{2} x + \sqrt{2} x - 2\sqrt{3} = 0$$

 $\sqrt{3} x(x \sqrt{6}) + \sqrt{2}(x \sqrt{6}) = 0$ 

$$(\sqrt{3} x + \sqrt{2})(x \sqrt{6}) = 0$$

 $(\sqrt{3} x + \sqrt{2}) = 0 \text{ or } (x - \sqrt{6}) = 0$ 

$$x = \sqrt{6} \text{ or } x = \frac{-\sqrt{2}}{\sqrt{3}}$$

Hence roots of equation are  $x = \sqrt{6}$  or  $x = \frac{-\sqrt{2}}{\sqrt{3}}$ 

## **Question: 51**

Solve:  $4\sqrt{3x^2}$ 

## Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 4\sqrt{3} b = 5 c = -2\sqrt{3}$ 

$$= 4\sqrt{3} \cdot -2\sqrt{3}$$

And either of their sum or difference = b =-5 Thus the two terms are 8 & - 3 Difference = 8 - 3 = 5 Product = 8. -3 = -24  $4\sqrt{3} x^2 + 5x - 2\sqrt{3} = 0$   $4\sqrt{3} x^2 + 8x - 3x - 2\sqrt{3} = 0$   $4x(\sqrt{3}x + 2) - \sqrt{3}(\sqrt{3}x + 2) = 0$   $(4x - \sqrt{3})(\sqrt{3}x + 2) = 0$   $(4x - \sqrt{3}) = 0 \text{ or } (\sqrt{3}x + 2) = 0$  $x = \frac{\sqrt{3}}{4} \text{ or } x = \frac{-2}{\sqrt{3}}$ 

Hence roots of equation are  $x = \frac{\sqrt{3}}{4}$  or  $x = \frac{-2}{\sqrt{3}}$ 

#### **Question: 52**

Solve: 4x

### Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 4b = 4bc = -(a^2 - b^2)$ 

 $= -4(a^2 - b^2)$ 

And either of their sum or difference = b

=-4b Thus the two terms are 2(a + b) & - 2(a - b)Difference = 2[(a + b) - (a - b)]=-2[2b] =-4b Product =  $2(a + b) \times -2(a - b)$ =--4(a + b)(a - b) using (a + b)(a - b) = a<sup>2</sup> - b<sup>2</sup> =--4(a<sup>2</sup> - b<sup>2</sup>) 4x<sup>2</sup> + 4bx - (a<sup>2</sup> - b<sup>2</sup>) = 0 4x<sup>2</sup> + 2[(a + b) - (a - b)]x - (a + b)(a - b) = 0 - using (a + b)(a - b) = a<sup>2</sup> - b<sup>2</sup> 4x<sup>2</sup> + 2(a + b)x - 2(a - b)x - (a + b)(a - b) = 0 2x[2x + (a + b)] - (a - b)[2x + (a + b)] = 0 [2x - (a - b)][2x + (a + b)] = 0 [2x - (a - b)] = 0 or [2x + (a + b)] = 0

2x = (a - b) or 2x = -(a + b)

$$x = \frac{-(a + b)}{2}$$
 or  $x = \frac{a - b}{2}$ 

Hence roots of equation are  $x = \frac{-(a+b)}{2}$  or  $x = \frac{a-b}{2}$ 

### **Question: 53**

Solve: x

## Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 1 b = 5 c = -(a^2 + a - 6)$ 

 $= -1. -(a^2 + a - 6) = -(a^2 + a - 6)$ 

And either of their sum or difference = b

----5

Thus the two terms are (a + 3) & (a - 2)

 $\frac{\text{Difference}}{a} = (a + 3) - (a - 2)$ 

----5

 $\frac{Product}{a} = (a + 3)(a - 2)$ 

$$= a^{2} + a - 6$$

$$x^{2} + 5x - (a^{2} + a - 6) = 0$$

$$x^{2} + 5x - (a + 3)(a - 2) = 0$$

$$x^{2} + [(a + 3) - (a - 2)]x - (a + 3)(a - 2) = 0$$

$$x^{2} + (a + 3)x - (a - 2)x - (a + 3)(a - 2) = 0$$

$$x[x + (a + 3)] - (a - 2)[x + (a + 3)] = 0$$

$$[x - (a - 2)][x + (a + 3)] = 0$$

$$[x - (a - 2)] = 0 \text{ or } [x + (a + 3)] = 0$$

$$x = (a - 2) \text{ or } x = -(a + 3)$$

Hence roots of equation are x = (a - 2)or - (a + 3)

### **Question: 54**

 $\mathbf{x}^2$ 

### Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 1b = 6c = -(a^2 + 2a - 8) =$ 

 $= 1.(a^2 + 2a - 8) = (a^2 + 2a - 8)$ 

And either of their sum or difference = b

=-6 Thus the two terms are (a + 4) & (a - 2)Difference = (a + 4) (a - 2)=-6 Product = (a + 4)(a - 2)=-a<sup>2</sup> + 2a - 8 x<sup>2</sup> + 6x -  $(a^2 + 2a - 8) = 0$ x<sup>2</sup> + 6x - (a + 4)(a - 2) = 0x<sup>2</sup> + [(a + 4) - (a - 2)]x - (a + 4)(a - 2) = 0x<sup>2</sup> + (a + 4)x - (a - 2)x - (a + 4)(a - 2) = 0x<sup>2</sup> + (a + 4)x - (a - 2)x - (a + 4)(a - 2) = 0x[x + (a + 4)] (a - 2)[x + (a + 4)] = 0[x - (a - 2)][x + (a + 4)] = 0[x - (a - 2)][x + (a + 4)] = 0x = (a - 2) or x = -(a + 4)Hence roots of equation are x = (a - 2) or (a + 4)

## **Question: 55**

```
×2
```

# Solution:

Using splitting middle term, the middle term of the general equation  $ax^2 + bx + c = 0$  is divided in two such values that:

Product = a.c

For the given equation  $a = 1 b = -4a c = 4a^2 - b^2$ 

 $=-1.(4a^2-b^2)=-4a^2-b^2$ 

And either of their sum or difference = b

<del>-</del>--4a

```
Thus the two terms are -(2a + b) \& -(2a - b)
```

```
Sum = -(2a + b) - (2a - b)
```

= -2a - b - 2a + b

<del>-</del>--4a

 $\frac{Product = -(2a + b) - (2a - b) \cdot using (a + b)(a - b) = a^2 - b^2}{a^2 - b^2}$ 

$$= -(2a + b)(2a - b) = -4a^{2} - b^{2}$$

$$x^{2} - 4ax + 4a^{2} - b^{2} = 0$$

$$x^{2} - 4ax + (2a + b)(2a - b) = 0$$

$$x^{2} - [(2a + b) + (2a - b)]x + (2a + b)(2a - b) = 0$$

$$x^{2} - (2a + b)x - (2a - b)x + (2a + b)(2a - b) = 0$$

$$x[x - (2a + b)] - (2a - b)[x - (2a + b)] = 0$$

$$[x - (2a - b)][x - (2a + b)] = 0$$

[x-(2a-b)] = 0 or [x-(2a+b)] = 0

x = (2a-b) or x = (2a + b)

Hence roots of equation are x = (2a - b) or x = (2a + b)