

# 1.

## INTRODUCTION

### IDEAL FLUID AND REAL FLUID

- **Ideal fluid:** A fluid is said to be ideal if it is assumed to be both incompressible and non-viscous. Its bulk modulus is infinite.
- **Real fluid:** Real fluid have viscosity, finite compressibility and surface tension.



Remember

- Ideal fluid has no surface tension.
- Ideal fluid are imaginary and do not exist in nature.

### SPECIFIC WEIGHT, SPECIFIC VOLUME, SPECIFIC GRAVITY

$$\text{Specific weight } (\omega) \text{ or weight density} = \frac{\text{Weight}}{\text{Volume}} = \frac{mg}{V} = \rho g$$

Here,  $\rho$  = Density

$g$  = Acceleration due to gravity

Specific weight of water = 9810 N/m<sup>3</sup>

$$\text{Specific Volume} = \frac{1}{\text{Density}}$$

- **Specific gravity (S) or Relative density**

$$\begin{aligned} \text{Specific gravity} &= \frac{\text{Density of fluid}}{\text{Density of standard fluid}} \\ &= \frac{\text{Specific weight of fluid}}{\text{Specific weight of standard fluid}} \end{aligned}$$



Remember

- Specific gravity for water is 1.0 at 4°C and for mercury it is 13.6
- Specific gravity varies with temperature therefore it should be determined at specified temperature (4°C or 27°C).

### NEWTON'S LAW OF VISCOSITY

$$\tau = \mu \cdot \frac{du}{dy} = \mu \frac{d\theta}{dt}$$

$\tau$  = shear stress

$\mu$  = coefficient of viscosity or absolute viscosity or dynamic viscosity

Here,  $\frac{du}{dy}$  = Velocity gradient

$\frac{d\theta}{dt}$  = Rate of angular deformation or Rate of shear strain

- For newtonian fluid, coefficient of viscosity remains constant.

### VISCOSITY/KINEMATIC VISCOSITY

Due to viscosity a fluid offer resistance to flow

- (i) **Dynamic Viscosity ( $\mu$ )**

- Its SI unit is pascal-second or **N-sec/m<sup>2</sup>**
- Its CGS unit is Poise = Dyne-sec/cm<sup>2</sup>
- 1 poise = 0.1 N-s/m<sup>2</sup>

- (ii) **Kinematic Viscosity**

$$v = \frac{\text{Dynamic viscosity } (\mu)}{\text{Mass density } (\rho)}$$

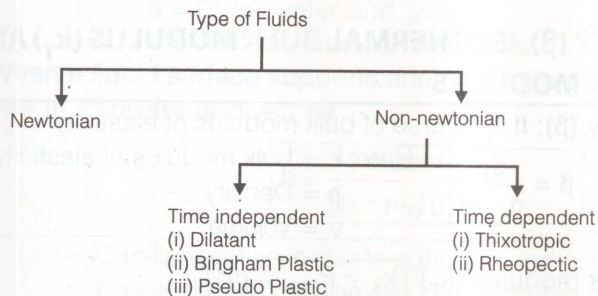
- Its SI unit is m<sup>2</sup>/s.
- Its CGS unit is cm<sup>2</sup>/s or stoke.
- 1 stoke = 10<sup>-4</sup> m<sup>2</sup>/s



Remember

- Viscosity of **liquids** decreases with temperature whereas viscosity of **gases** increases with increase in temperature.
- Liquids with increasing order of viscosity are gasoline, water, crude oil, castor oil.
- Viscosity of **water** at 1°C is 1 centipoise.
- Viscosity of liquids is due to **cohesion** and for gases it is due to **molecular momentum transfer**.

### TYPE OF FLUID

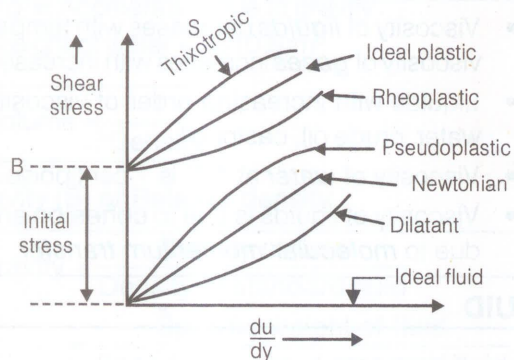


- **Non-Newtonian Fluids:** These do not follow Newton's law of viscosity. The relation between shear stress and velocity gradient is

$$\tau = A \left( \frac{du}{dy} \right)^n + B$$

where A and B are constants depending upon type of fluid and condition of flow.

- (i) For Dilatant Fluids:  $n > 1$  &  $B = 0$ ,  
Ex. Butter, Quick sand.
- (ii) For Bingham Plastic Fluids:  $n = 1$  &  $B \neq 0$   
Ex. Sewage sludge, Drilling mud, tooth paste and gel.  
These fluids always have certain minimum shear stress before they yield.
- (iii) For Pseudoplastic Fluids:  $n < 1$  &  $B = 0$   
Ex. Paper pulp, Rubber solution, Lipsticks, Paints, Blood, Polymetric solutions etc.
- (iv) For Thixotropic Fluids:  $n < 1$  &  $B \neq 0$   
Viscosity increases with time.  
Ex. Printers ink and Enamels.
- (v) For Rheopectic Fluids:  $n > 1$  &  $B \neq 0$   
Viscosity decreases with time.  
Ex. Gypsum solution in water & Bentonite solution.



## COMPRESSIBILITY ( $\beta$ ), ISOTHERMAL BULK MODULUS ( $k_T$ ) AND ADIABATIC BULK MODULUS

- Compressibility ( $\beta$ ): It is inverse of bulk modulus of elasticity.

$$\beta = \frac{1}{k} = \frac{-dv}{vdp}$$

$$\beta = \frac{dp}{\rho \cdot dP}$$

Here,  $k$  = bulk modulus of elasticity

$\rho$  = Density

$v$  = Volume

- Isothermal bulk modulus ( $k_T$ )  $k_T = P_{\text{final}} = \rho RT$

- Adiabatic bulk modulus  $k_a = \gamma \cdot P_{\text{final}}$

$$\gamma = \frac{C_p}{C_v}$$

Here,  $C_p$  = Specific heat at constant pressure  
 $C_v$  = Specific heat at constant volume

## SURFACE TENSION/PRESSURE INSIDE DROP, BUBBLE AND JET

Surface tension occurs at the interface of liquid and a gas **or** at the interface of two liquids. Surface tension is inversely proportional to temperature and it also acts when fluid is at rest.

- Pressure inside drop (Solid like sphere)  $P = \frac{4\sigma}{d}$
- Pressure inside bubble  $P = \frac{8\sigma}{d}$
- Pressure inside jet  $P = \frac{2\sigma}{d}$  Here,  $d$  = Diameter of drop  
 $P$  = Gauge pressure



Remember

- It is a **surface** phenomenon
- It is force per unit length (N/m)
- For **water-air** interface at 20°C its value is 0.0736 N/m
- At critical point, liquid-vapour state are same thus surface tension = 0
- It is due to **cohesion** only

## CAPILLARY ACTION

- Height of water in capillary tube

$$h = \frac{4 \sigma \cos \theta}{\rho g d}$$

Where,  $h$  = rise in capillary

$\sigma$  = surface tension of water & glass

$d$  = dia of tube

$\theta$  = angle of contact between the liquid and the material.

$\theta = 0^\circ$  for water and glass

$\theta = 128^\circ$  for mercury and glass

- When a liquid surface supports another liquid of density " $\rho_b$ ", then rise in capillary is given as

$$h = \frac{4 \sigma \cos \theta}{(\rho - \rho_b) g d}$$



Remember

- Capillary action is due to adhesion and cohesion, **both**.
- For capillary action diameter of tube should be **less** than 3 cm.