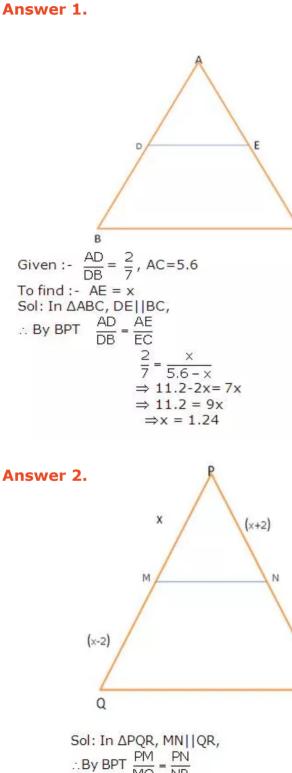
Ex 15.1

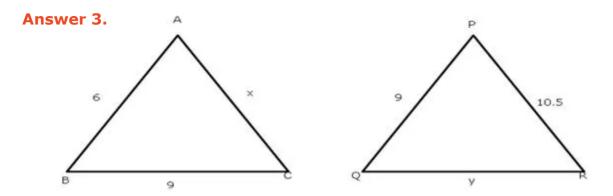


By BPT
$$\frac{111}{MQ} = \frac{111}{NR}$$

 $\frac{x}{x-2} = \frac{x+2}{x-2}$
 $\Rightarrow x^2 - x = x^2 - 4$
 $\Rightarrow -x = -4$
 $\Rightarrow x = 4$

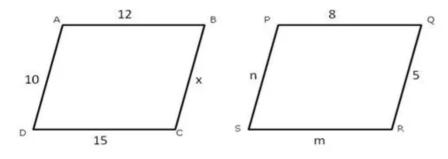
(x-1)

R



Given: - $\triangle ABC \sim \triangle PQR$ To find: - AC and QR Sol: $\triangle ABC \sim \triangle PQR$ $\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$ (Similar sides of similar triangles) $\frac{6}{9} = \frac{9}{y} = \frac{x}{10.5}$ $\frac{6}{9} = \frac{9}{y}$, $\frac{6}{9} = \frac{x}{10.5}$ $\Rightarrow 6y = 81$ $\Rightarrow 63 = 9x$ $\Rightarrow y = \frac{81}{6}$ $\Rightarrow x = 7$ $\Rightarrow y = \frac{27}{2}$ $\Rightarrow AC = 7cm$ $\Rightarrow QR = 13.5cm$

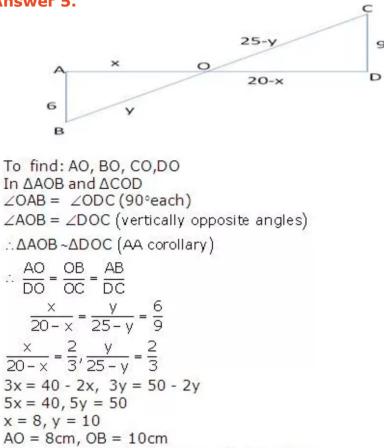




Given: quadrilateral ABCD~quadrilateral PORS To find: x, m and n Sol: quadrilateral ABCD~quadrilateral PORS $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{DC}{SR} = \frac{AD}{SR}$

 $\frac{12}{8} = \frac{x}{5} = \frac{15}{m} = \frac{10}{n}$ $\frac{12}{8} = \frac{x}{5}, \frac{12}{8} = \frac{15}{m}, \frac{12}{8} = \frac{10}{n}$ 60 = 8x, 4m = 40, 3n = 20 $x = \frac{60}{8}, m = 10 \text{ cm}, n = \frac{20}{3}$ $x = \frac{15}{2}, m = 10 \text{ cm}, n = 6.66 \text{ ...}$ x = 7.5 cm, m = 10 cm, n = 6.67 cm

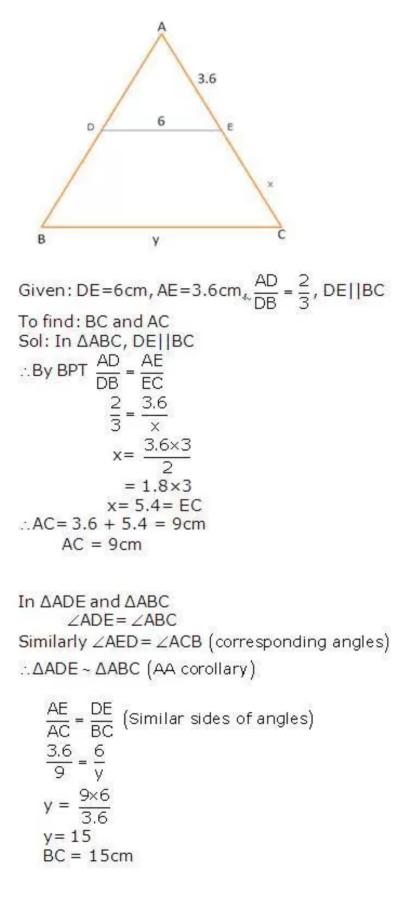
Answer 5.



9

OD = 20 - 8 = 12 cm , OC = 25-10 = 15 cm

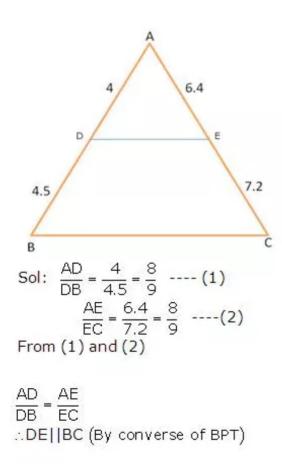
Answer 6.

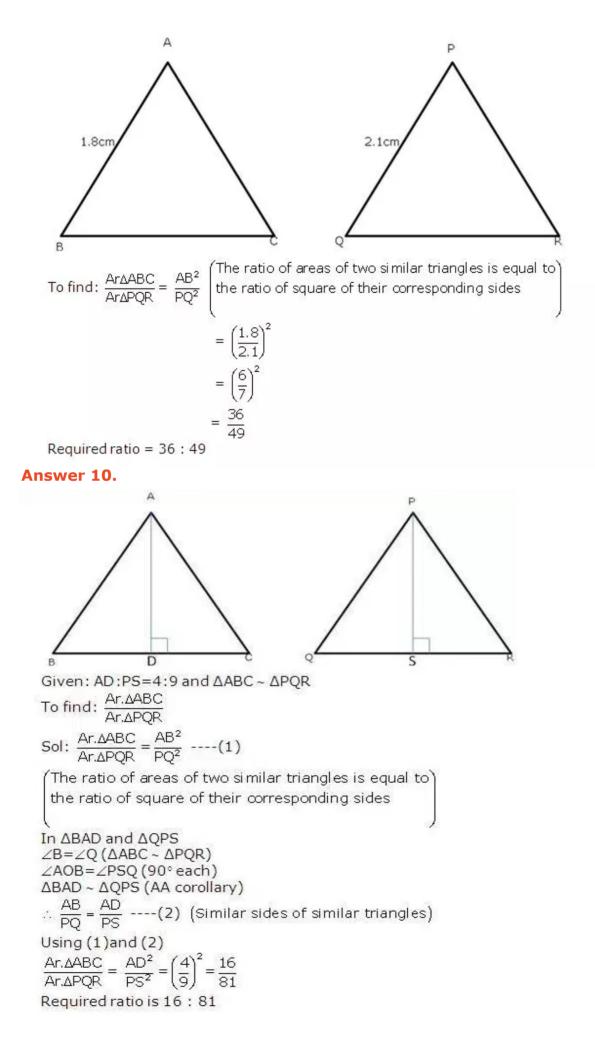


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Answer 7.

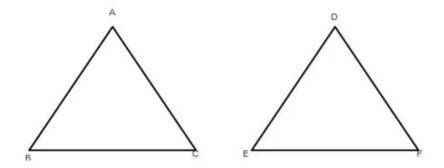
Answer 7.
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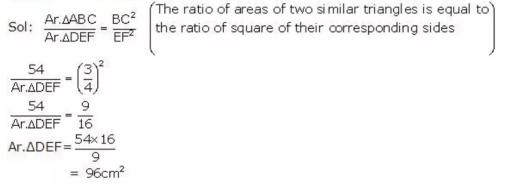




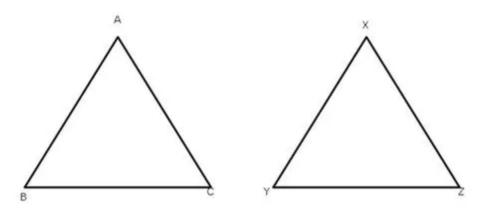
Answer 11.



Given: ΔABC ~ΔDEF To find: Ar. of ΔDEF

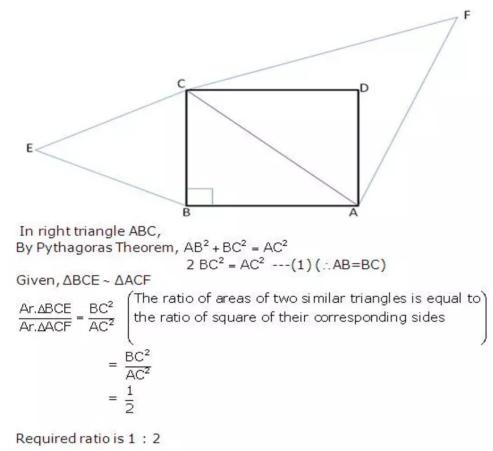


Answer 12.



Given: ΔABC ~ ΔXYZ To find: YZ

Sol: $\frac{Ar.\Delta ABC}{Ar.\Delta XYZ} = \frac{BC^2}{YZ^2}$ (The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides) $\frac{9}{16} = \frac{(2.1)^2}{YZ^2}$ Taking square root both sides, $\frac{3}{4} = \frac{2.1}{YZ}$ $YZ = \frac{2.1 \times 4}{3}$ YZ = 2.8 cm



Answer 14.

(a) If AN : AC = 5 : 8, find ar(Δ AMN) : ar(Δ ABC)

Given : $\frac{AN}{AC} = \frac{5}{8}$

To Find : Ar.AAMN

In AAMN and AABC

 $\angle AMN = \angle ACB$ (corresponding angles))

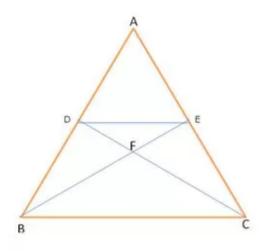
∠ABC =∠ACB

: AAMN ~ AABC (AA corollary)

 $\therefore \frac{Ar. \triangle AMN}{Ar. \triangle ABC} = \frac{AN^2}{AC^2} \left(\begin{array}{c} \text{The ratio of areas of two similar triangles is equal to} \\ \text{the ratio of square of their corresponding sides.} \end{array} \right)$

 $= \left(\frac{5}{8}\right)^{2}$ $\frac{Ar.\Delta AMN}{Ar.\Delta ABC} = \frac{25}{64}$ Required ratio is 25 : 64
(b) If $\frac{AB}{AM} = \frac{9}{4}$, find $\frac{Ar.(trapeziumMBCN)}{Ar.(\Delta ABC)}$ $\Delta AMN \sim \Delta ABC \text{ (proved above)}$ $\therefore \frac{Ar.\Delta AMN}{Ar.\Delta ABC} = \frac{AM^{2}}{AB^{2}} = \left(\frac{4}{9}\right)^{2} = \frac{16}{81}$

Answer 15.



Given: $\frac{DE}{BC} = \frac{2}{7}$ To find: (Similar sides of similar triangles) In Δ FDE and Δ FCB \angle FDE = \angle FCB \angle FED = \angle FBC (Alternate interior angles) Δ FDE ~ Δ FCB (AA corollary) Δ r Δ FDE DE^2 (2)² 4 (The ratio of areas of the second secon

$$\therefore \frac{\text{Ar}.\Delta\text{FDE}}{\text{Ar}.\Delta\text{FBC}} = \frac{\text{DE}^2}{\text{BC}^2} = \left(\frac{2}{7}\right)^2 = \frac{4}{49} \left(\frac{\text{The ratio of areas of two similar triangles is equal to}}{\text{the ratio of square of their corresponding sides}}\right)$$

Answer 16.

Given: $\frac{PT}{TR} = \frac{5}{3}$, To find : $\frac{Ar.(\Delta MTS)}{Ar.(\Delta MQR)}$ Sol: In ΔPST and ΔPRQ $\angle PST = \angle PQR$ $\angle PTS = \angle PRQ$ (Corresponding angles) $\therefore \Delta PST \sim \Delta PQR$ (AA corollary) $\therefore \frac{PT}{PR} = \frac{ST}{QR} = \frac{5}{8}$ (Similar sides of similar triangles) Now, In ΔMTS and ΔMQR $\angle MTS = \angle MQR$ (Alternate interior angles) $\angle MST = \angle MRQ$ $\therefore \Delta MTS \sim \Delta MQR$ (AA corollary) $\therefore \frac{Ar.(\Delta MTS)}{Ar.(\Delta MQR)} = \frac{TS^2}{QR^2} = \left(\frac{5}{8}\right)^2 = \frac{25}{64}$ i.e. 25 : 64 (The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides

Answer 17.

Given: $\frac{KL}{KT} = \frac{9}{5}$ To find: $\frac{Ar.\Delta KLM}{Ar.\Delta KTP}$ Sol: In ΔKLM and ΔKTP $\angle KLM = \angle KTP$ (Given) $\angle LKM = \angle TKP$ (Common) $\Delta KLM \sim \Delta KTP$ (AA corollary) $\therefore \frac{Ar.\Delta KLM}{Ar.\Delta KTP} = \left(\frac{KL}{KT}\right)^2 = \left(\frac{9}{5}\right)^2 = \frac{81}{25}$ (The ratio

i.e., 81:25 (The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides (the ratio of square of their corresponding sides (the ratio of square of the square of the

Answer 18.

In ΔDEF and ΔGHF , $\angle DEF = \angle GHF$ (90°each) $\angle DFE = \angle GFH$ (Common) $\Delta DEF \sim \Delta GHF$ (AA corollary) $\therefore \frac{Ar.(VDEF)}{Ar.(VGHF)} = \frac{EF^2}{HF^2} ----(1)$ (The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides) In right ΔDEF , (By Pythagoras theorem) $DE^2 + EF^2 = DF^2$ $EF^2 = 10^2 - 8^2$ $EF^2 = 36$ EF = 6From (1), $\frac{Ar.(VDEF)}{Ar.(VGHF)} = \left(\frac{6}{4}\right)^2 = \frac{9}{4}$ i.e., 9 : 4

Ex 15.2

Answer 1.

Scale = 1 : 500 1cm represents 500cm $\frac{500}{100} = 5m$ 1cm represents 5m Length of model = $\frac{50}{5} = 10cm$ Breadth of model = $\frac{40}{5} = 8cm$ Height of model = $\frac{70}{5} = 14cm$

Answer 2.

20cm represents 400m

1cm represents $\frac{400}{20}$ = 20cm

Width of model = $\frac{100}{20}$ = 5cm

Length of model = 20cm

Surface area of the deck of the model = $5 \text{cm} \times 20 \text{cm}$

 $= 100 \, \text{cm}^2$

Answer 3.

Scale:- 1 : 500 1cm represents 500cm $= \frac{500}{100} = 5m$ 1cm represents 5m (i) Actual length of ship= 60 × 5m = 300m (ii) 1 cm² represents 5m × 5m= 25m²

Deck area of the ship = $1500000m^2$

Deck area of the model = $\frac{1500000}{25}$ cm² = 60000cm² (iii) 1 cm³ represents 5m × 5m × 5m = 125 m³ Volume of the model = 200 cm³ Volume of the ship = 200 × 125 m³

 $= 25000 \text{ m}^3$

Answer 4.

15cm represents = 30m

1cm represents $\frac{30}{15} = 2m$

 1 cm^2 represents $2\text{m} \times 2\text{m} = 4 \text{m}^2$

Surface area of the model = $150 \, \text{cm}^2$

Actual surface area of aeroplane = $150 \times 2 \times 2 \text{ m}^2$

 $= 600 \text{ m}^2$

 50 m^2 is left out for windows Area to be painted = 600 - 50= 50 m^2 Cost of painting per m² = Rs. 120 Cost of painting 550 m² = 120×550 = Rs. 66000

Answer 5.

1cm on map represents 12500m on land

1 cm represents 12.5km on land

Length of river on map = 54cm

Actual length of the river = 54×12.5

= 675.000km

=675km

Answer 6.

(i) Scale: -1: 200000

: 1cm represents 200000cm

$$=\frac{200000}{1000\times100}=2$$
km

1cm represents 2km

(ii) 1cm represents 2 km

 $112^2 + 16^2$ represents $2 \times 2 = 4$ km²

(iii)4km² is represented by km² 1km² is represented by $\frac{1}{4}$ cm² 20km² is represented by $\frac{1}{4}$ ×20cm² = 5cm² Area on map that represents the plot of land= 5cm²

Answer 7.

Actual area= 1872km²

Area on map represents $117\,{\rm cm}^2$

- Let 1cm represents \times km
- $\therefore\,1\,\text{cm}^2$ represents $\times\times\times\,k\,\text{m}^2$

Actual area = $\times \times \times \times$ 117 km^2

$$1872 = x^{2} \times 117$$
$$x^{2} = \frac{1872}{117}$$
$$x^{2} = 16$$
$$x = 4$$

:: 1cm represents 4 km

Length of coastline on map = 44cm

Actual length of coastline = 44×4 km

= 176 km

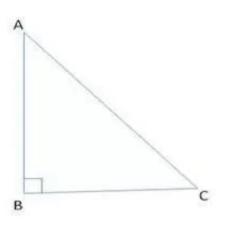
Answer 8.

Scale:- 1:25000

:1 cm represents 25000cm

$$=\frac{25000}{1000\times100}=2.5$$
km

∴1cm represents 0.25km



Actual length of $AB = 6 \times 0.25$

= 1.50 km

Area of
$$\triangle ABC = \frac{1}{2} \times BC \times AB$$
$$= \frac{1}{2} \times 8 \times 6 = 24 \text{ cm}^2$$

1 cm represents 0.25 km

 $1\,\text{cm}^2$ represents $0.25 \times 0.25 \text{km}^2$

The area of plot = $0.25 \times 0.25 \times 24$ km²

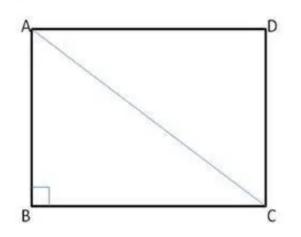
Answer 9.

Scale :- 1 : 25000

1 cm represents 25000 cm

$$=\frac{25000}{1000\times100}=0.25$$
km

1 cm represents 0.25km



$$AC^{2} = AB^{2} + BC^{2}$$

= $12^{2} + 16^{2}$
= $144 + 256$
 $AC^{2} = 400$
 $AC = 20 \text{ cm}$

Actual length of diagonal = 20 ×0.25

1 cm represents 0.25km

1cm² represents 0.25 × 0.25km²

The area of the rectangle ABCD = AB \times BC

 $= 16 \times 12 = 192 \, \text{cm}^2$

The area of the plot = $0.25 \times 0.25 \times 192$ km²

= 12km²