

INERTIA OF REST

The property of a body due to which it cannot change its state of rest by itself.

INERTIA OF DIRECTION

The property due to which a body cannot change its direction of motion by itself.

INERTIA OF MOTION

The tendency of a body to remain in a state of uniform motion in a straight line.


FORCES

(i) Normal Contact force

(1) always acts along the common Normal of two Surface in contact.

(2) Always directed towards the System.

(3) It is an electromagnetic type of force. Normal force on block is N . $N = mg$



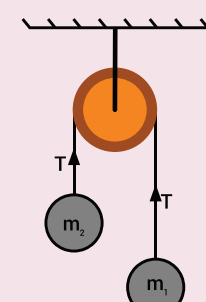
(ii) Tension force

(1) Acts along the string and away from the system on which it acts.

(2) Tension in a massless string remains constant throughout the string if no tangential force acts along the string.

(3) This is force applied by a string on an object or force applied by one part of string on the remaining part of string.

(4) It is an electromagnetic type of force.



(iii) Friction Force

(1) Rolling friction:- The force of friction which comes into play when one body rolls or tends to roll on the surface of another body.

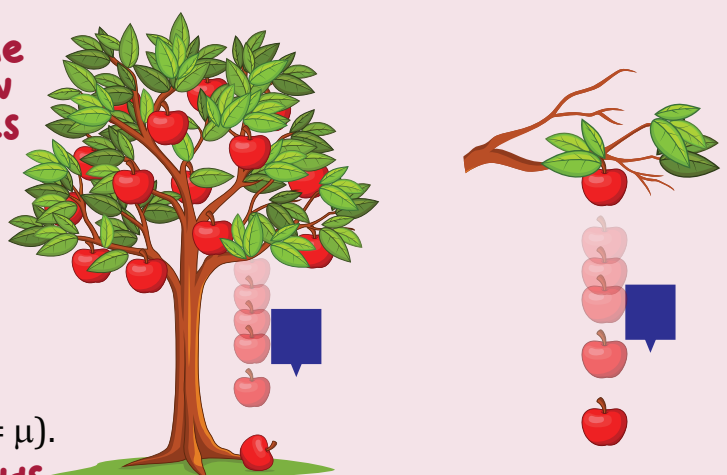
(iv) Sliding friction

Resistance offered to the relative motion between the surface of two bodies in contact.

The frictional force f is directly proportional to the Normal force N exerted by the surface on the body.

$(F \propto N \text{ or } f/N = \text{Constant} = \mu)$.

The friction force depends upon the nature of surfaces in contact and independent of the area of contact.



Types of friction

Static friction

acts when a body is at rest on application of a force

$f_s = \mu_s N$.

Limiting friction

acts when a body is just at the verge of movement

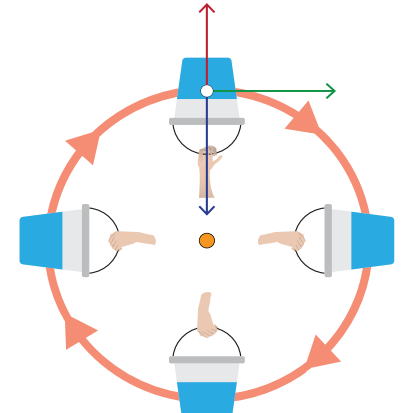
$F_l = \mu_s N$.

Kinetic friction

acts when a body is actually sliding

$f_k = \mu_k N$

Circular motion



Kinematics of Uniform Circular motion

- A particle moves in a circle at a constant speed
- Angular displacement (θ) SI Unit: rad or degree.
- Angular velocity (ω):

$$\omega_{avg} = \frac{\Delta\theta}{\Delta t} [\text{Unit: rad / sec}] \quad \omega_{ins} = \frac{d\theta}{dt}$$

Centripetal Force

$$F_c = ma_c = \frac{mv^2}{r} = mr\omega^2$$

$$\Delta S = r\Delta\theta \quad v = r\omega$$

$$\vec{V} = \vec{\omega} \times \vec{r}$$

\vec{V} is linear velocity (tangential vector)
 $\vec{\omega}$ (axial vector)
 \vec{r} = radius vector

NEWTON'S LAWS OF MOTION

Newton's 3rd law

To every action there is always an equal and opposite reaction.

$$\vec{F}_{AB} = -\vec{F}_{BA}$$

Action & Reaction act on different bodies and not on the same body. - action - reaction forces are of same type.

We cannot produce a single isolated force in nature. Forces are always produced in action - reaction pairs.

Due to no time gap, any one force can be action, and the other reaction.

Applicable for all the interactive forces e.g. Gravitational, electrostatic, electromagnetic, Tension, friction, viscous forces, etc.

Newton's 1st law

A body continues its state of rest or motion until unless an external force is acted on it.

If $\vec{F}_{ext} = 0$; $\vec{a} = 0$

Newton's 2nd Law

The rate of change of linear momentum of a body is directly proportional to the external force applied on the body in the direction of force.

$$\vec{F} = \frac{d\vec{p}}{dt} = m\vec{a}$$

S.I. Unit of force = Newton (N)

If $m = \text{const}$ $\vec{F} = \frac{m d\vec{v}}{dt} = m\vec{a} \Rightarrow \text{dimensional formula} = [M^1 L^1 T^{-2}]$

Conservation of linear momentum:- if there is no external force acting on it, total momentum of an isolated system of interacting particles is conserved

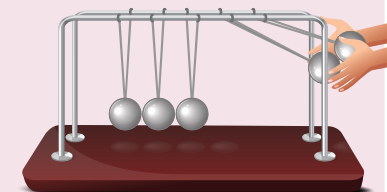
if $\vec{V} = \text{const} \Rightarrow \vec{F} = \vec{V} \frac{dm}{dt}$
conveyer belt & rocket propulsion

Impulse

$$\vec{I} = \vec{F}_{avg} \Delta t = \Delta \vec{P}$$

$$\Rightarrow I = \Delta P = \int F \cdot dt = \text{area under } f - t \text{ curve}$$

Horizontal Circular motion (Conical Pendulum):-



$$T_{\sin\theta} = \frac{mv^2}{r} \quad \text{and} \quad T_{\cos\theta} = mg$$


$$V = \sqrt{rg \tan\theta}$$

Angular Speed, ω $\omega = \frac{v}{r} = \sqrt{\frac{g \tan\theta}{r}}$

Time Period T $T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{r}{g \tan\theta}} = 2\pi \sqrt{\frac{L \cos\theta}{g}}$

Vertical Circular motion

- Particle oscillates in the lower half circle. Condition of oscillation ($0 < u \leq \sqrt{2gR}$)
- Particle moves to the upper half circle but not able to complete the loop. Condition of leaving the circle: ($\sqrt{2gR} < u < \sqrt{5gR}$)
- Particle completes the loop. Condition of looping the loop ($u \geq \sqrt{5gR}$)



Kinematics of Non-Uniform circular motion

Speed of the particle in a horizontal circular motion changes with respect to time.

Tangential acceleration:

$$\vec{a}_t = \vec{\alpha} \times \vec{r}$$

Centripetal force

$$F_c = ma_c = \frac{mv^2}{r} = mr\omega^2$$

Tangential force $F_t = ma_t$

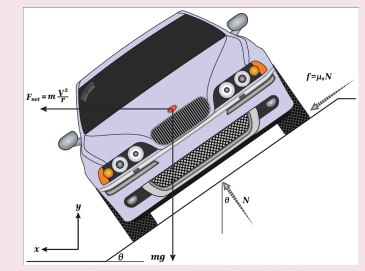
Net force $F_{net} = m\sqrt{a_c^2 + a_t^2}$

\vec{a}_c responsible for change in direction of movement of particle

MOTION OF A CAR ON LEVEL ROAD (by friction only):-

$$v_{max} \leq \sqrt{\mu_s Rg}$$

MOTION OF A CAR ON BANKED ROAD



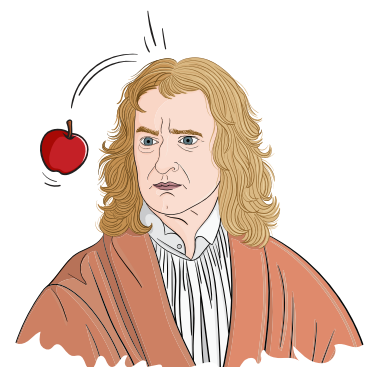
(i) Optimum speed of a vehicle on a banked road. $V = \sqrt{rg \tan\theta}$

Maximum safe speed on a banked frictional road. $V_{max} = \sqrt{\frac{rg(\mu + \tan\theta)}{1 - \mu \tan\theta}}$

Minimum safe speed on a banked frictional road $V_{min} = \sqrt{\frac{Rg(\tan\theta - \mu)}{1 + \mu \tan\theta}}$

For Non-inertial frame

$$\vec{F}_{ext} + \vec{F}_{pseudo} = m\vec{a}$$

$$\vec{F}_{pseudo} = -M\vec{a}_{frame}$$


SOLVING PROBLEMS IN MECHANICS

- Draw FBD of bodies in the system.
- Choose a convenient part of the assembly as one system.
- Identify the unknown force and accelerations.
- Resolve forces into their components.

- Apply $\sum \vec{F} = m\vec{a}$ in the direction of motion.
- Apply $\sum \vec{F} = 0$ in the direction of equilibrium
- Write constraint relation if exists.
- Solve the equation $\sum \vec{F} = m\vec{a}$ & $\sum \vec{F} = 0$.

