11. Algebraic Expressions

EXERCISE 11(A)

Question 1.

Separate the constants and variables from the following :

$$-7,7+x,7x+yz,\sqrt{5},\sqrt{xy},\frac{3yz}{8},4.5y-3x,$$

$$8-5$$
, $8-5x$, $8x-5y \times p$ and $3y^2z \div 4x$

Solution:

Clearly constants are : -7, $\sqrt{5}$, 8 – 5

Variable are : 7 + x, 7x + yz, \sqrt{xy} , $\frac{3yz}{8}$, 4.5y

-3x

$$8 - 5x$$
, $8x - 5y \times p$ and $3y^2 z \div 4x$

Question 2.

Write the number of terms in each of the following polynomials. (i) $5x^2 + 3x$ ax (ii) ax $\div 4 - 7$ (iii) ax - by + y x z(iv) $23 + a \times b \div 2$. Solution: (i) $5x^2 + 3 \times ax = 5x^2 + 3ax$... The number of terms in this polynomial = 2 (*ii*) $ax \div 4 - 7 = \frac{ax}{4} - 7$... The number of terms in this polynomial = 2 (iii) $ax - by + y \times z = ax - by + yz$ The number of terms in this polynomial = 3 $(iv) 23 + a \times b \div 2 = 23 + \frac{ab}{2}$... The number of terms in this Polynomial = 2

Question 3.

Separate monomials, binomials, trinomials and polynomials from the following algebraic expressions :

 $8 - 3x, xy^{2}, 3y^{2} - 5y + 8, 9x - 3x^{2} + 15x^{3} - 7,$ $3x \times 5y, 3x \div 5y, 2y \div 7 + 3x - 7 \text{ and } 4 - ax^{2} +$ bx + y

Solution:

Monomials are : xy^2 , $3x \times 5y$, $3x \div 5y$;

Bionomials are : 8 - 3x

Trinomials are : $3y^2 - 5y + 8$, $2y \div 7 + 3x - 7$ Polynomials are : 8 - 3x, $3y^2 - 5y + 8$, $9x - 3x^2 + 15x^3 - 7$, $2y \div 7 + 3x - 7$, $4 - ax^2 + bx + y$

Question 4.

Write the degree of each polynomial given below :

(i) xy + 7z (ii) $x^2 - 6x^3 + 8$ (iii) $y - 6y^2 + 5y^8$ (iv) xyz - 3(v) $xy + yz^2 - zx^3$ (vi) $x^5y^7 - 8x^3y^8 + 10x^4y^4z^4$ Solution: (i) degree = 2 (Polynomial is xy + 7z)

(ii) degree = 3 (Polynomial is $x^2 - 6x^3 + 8y$) (iii) degree = 8 (Polynomial is $y - 6y^2 + 5y^8$) (iv) degree = 3 (Polynomial is xyz - 3) (v) degree = 4 (Polynomial is $xy + yz^2 - xz^3$) (vi) degree = 12 (Polynomial is $x^5y^7 - 8x^3y^8 + 10x^4, y^4z^4$)

Question 5.

Write the coefficient of : (i) ab in 7abx , (ii) 7a in 7abx ; (iii) $5x^2$ in $5x^2 - 5x$; (iv) 8 in $a^2 - 8ax + a$; (v) 4xy in $x^2 - 4xy + y^2$. **Solution:** (i) The coefficient of ab in 7abx = 7x

(ii) The coefficient of 7a in 7abx = bx

- (iii) The coefficient of $5x^2$ in $5x^2 5x = 1$
- (iv) The coefficient of 8 in $a^2 8ax + a = -ax$
- (v) The coefficient of 4xy in $x^2 4xy + y^2 = -1$

Question 6.

 $\ln \frac{5}{7} xy^2 z^3$, write the coefficient of

(i) 5	(ii) $\frac{5}{7}$	(iii) 5 <i>x</i>	
(iv) xy^2	(v) <i>z</i> ³	(vi) <i>xz</i> ³	
(vii) 5 <i>xy</i> ²	(viii) $\frac{1}{7} yz$	(ix) <i>z</i>	
(x) yz^2	(xi) 5 <i>xyz</i>		

Solution:

In
$$\frac{5}{7} xy^2z^3$$
, Co-efficient of
(i) 5 is $\frac{1}{7}xy^2z^3$ (ii) $\frac{5}{7}$ is xy^2z^3
(iii) 5x is $\frac{1}{7}y^2z^3$ (iv) xy^2 is $\frac{5}{7}z^3$
(v) z^3 is $\frac{5}{7}xy^2$ (vi) xz^3 is $\frac{5}{7}y^2$
(vii) $5xy^2$ is $\frac{1}{7}z^3$ (viii) $\frac{1}{7}yz$ is $5xyz^2$
(ix) z is $\frac{5}{7}xy^2z^2$ (x) yz^2 is $\frac{5}{7}xy-z$
(xi) $5xyz$ is $\frac{1}{7}yz^2$

Question 7.

In each polynomial, given below, separate the like terms :

(i) $3xy_{,} - 4yx^{2}$, $2xy^{2}$, $2.5x^{2}y_{,} -8yx_{,} -3.2y^{2}x$ and $x^{2}y$ (ii) $y^{2}z^{3}$, $xy^{2}z^{3}$, $-5x^{2}yz_{,} -4y^{2}z^{3}$, $-8xz^{3}y^{2}$, $3x^{2}yz$ and $2z^{3}y^{2}$

Solution:

(i) Like terms are $3xy, -8yx -4yx^2, 2.5x^2y$ and x^2y ; $2xy^2$ and $-3.2y^2x$ (ii) $y^2z^3, -y^2z^3$ and $2z^3y^2$; xy^2z^3 and $-8xz^3y^2$; $-5x^2yz$ and $2x^2yz$

EXERCISE 11(B)

Question 1. Evaluate: (i) $-7x^2 + 18x^2 + 3x^2 - 5x^2$ (ii) $b^2y - 9b^2y + 2b^2y - 5b^2y$ (iii) abx - 15abx - 10abx + 32abx. (iv) 7x - 9y + 3 - 3x - 5y + 8(v) $3x^2 + 5xy - 4y^2 + x^2 - 8xy - 5y^2$

Solution:

(i)
$$-7x^2 + 18x^2 + 3x^2 - 5x^2$$

 $= 21x^2 - 12x^2$
 $= 9x^2$
(ii) $b^2y - 9b^2y + 2b^2y - 5b^2y$
 $= 3b^2y - 14b^2y$
 $= -11b^2y$
(iii) $abx - 15abx - 10abx + 32abx$
 $= 33abx - 25abx$
 $= 8abx$
(iv) $7x - 9y + 3 - 3x - 5y + 8$
 $= 7x - 3x - 9y - 5y + 3 + 8$
 $= 4x - 14y + 11$
(v) $3x^2 + 5xy - 4y^2 - 8xy - 5y^2$
 $= 3x^2 + 5xy - 8xy - 4y^2 - 5y^2$
 $= 3x^2 - 3xy - 9y^2$

Question 2.

Add:
(i)
$$5a + 3b, a - 2b, 3a + 5b$$

(ii) $8x - 3y + 7z, -4x + 5y - 4z, -x - y - 2z$
(iii) $3b - 7c + 10, 5c - 2b - 15, 15 + 12c + b$
(iv) $a - 3b + 3; 2a + 5 - 3c; 6c - 15 + 6b$
(v) $13ab - 9cd - xy; 5xy; 15cd - 7ab;$
 $6xy - 3cd$
(vi) $x^3 - x^2y + 5xy^2 + y^3; -x^3 - 9xy^2 + y^3; 3x^2y + 9xy^2$
(vii) $a^6 - 4a^4 + 6a; 5a^6 + 5a^4 + 6a;$
 $12a^6 - 10a$

(viii) 2ax - 6by + 4cz, 4by - 14ax, 9cz - 4ax - 6bySolution:

(i)
$$5a + 3b$$

 $a - 2b$
 $3a + 5b$
 $9a + 6b$
(ii) $8x - 3y + 7z$
 $-4x + 5y - 4z$
 $-x - y - 2z$
 $3x + y + z$
(iii) $3b - 7c + 10$
 $-2b + 5c - 15$
 $+b + 12c + 15$
 $2b + 10c + 10$
 $a - 3b + 3$
 $2a - 3c + 5$
 $+ 6b + 6c - 15$
 $3a + 3b + 3c - 7$
(v) $13ab - 9cd + xy$
 $+ 5xy$
 $-7ab + 15cd$
 $- 3cd + 6xy$
 $(vi) x^3 - x^2y + 5xy^2 + y^3$
 $-x^3 - 9xy^2 + y^3$
 $+ 3x^2y + 9xy^2$
 $2x^2y + 5xy^2 + 2y^3$

Question 3.

Find the total savings of a boy who saves \mathbf{R} (4x - 6y); \mathbf{R} (6x + 2y); \mathbf{R} (4y - x) and \mathbf{R} (y - 2x) for four consecutive weeks.

Solution:

$$4x-6y$$

$$6x+2y$$

$$-x+4y$$

$$-2x+y$$

$$7x+y$$

 \therefore Total savings = $\not\in (7x + y)$

Question 4.

(i)
$$4xy^2$$
 from $3xy^2$;
(ii) $-2x^2y + 3xy^2$ from $8x^2y$;
(iii) $3a-5b+c+2d$ from $7a-3b+c-2d$
(iv) $x^3 - 4x - 1$ from $3x^3 - x^2 + 6$
(v) $6a+3$ from a^3-3a^2+4a+1
(vi) $cab - 4cad - cbd$ from $3abc + 5bcd - cda$
(vii) $a^2 + ab + b^2$ from $4a^2 - 3ab + 2b^2$.

Solution:

(i)
$$3xy^2 - 4xy^2 = -xy^2$$

(ii) $8x^2y$
 $-2x^2y + 3xy^2$
 $+$ -
(iii) $7a - 3b + c - 2d$
 $3a - 5b + c + 2d$
 $- + - -$
(iv) $3x^3 - x^2 + 6$
 $x^3 - 4x - 1$
 $- + + +$
 $2x^3 - x^2 + 4x + 7$
(v) $a^3 - 3a^2 + 4a + 1$
 $+ 6a + 3$
 $- -$
(vi) $3abc + 5bcd - cda$
 $+ cab - cbd - 4cad$
 $- + +$
(vii) $4a^2 - 3ab + 2b^2$
 $+ a^2 + ab + b^2$
 $- - -$
 $3a^2 - 4ab + b^2$

Question 5.

(i) Take away $-3x^3 + 4x^2 - 5x + 6$ from $3x^3 - 4x^2 + 5x - 6$

(ii) Take $m^2 + m + 4$ from $-m^2 + 3m + 6$ and the result from $m^2 + m + 1$.

Solution:

Question 6.

Subtract the sum of $5y^2 + y - 3$ and $y^2 - 3y + 7$ from $6y^2 + y - 2$. Solution:

$$5y^{2} + y - 3$$

$$\frac{y^{2} - 3y + 7}{6y^{2} - 2y + 4}$$

$$6y^{2} + y - 2$$

$$6y^{2} - 2y + 4$$

$$- + -$$

$$3y - 6$$

Question 7.

What must be added to $x^4 - x^3 + x^2 + x + 3$ to obtain $x^4 + x^2 - 1$? **Solution:**

Question 8.

- (i) How much more than $2x^2 + 4xy + 2y^2$ is $5x^2 + 10xy y^2$?
- (ii) How much less $2a^2 + 1$ is than $3a^2 6$?

Solution:

Question 9.

If x = 6a + 86 + 9c; y = 2b - 3a - 6c and z = c - b + 3a; find (i) x + y + z(ii) x - y + z(iii) 2x - y - 3z(iv) 3y - 2z - 5xSolution: x = 6a + 8b + 9c*(i)* y = -3a + 2b - 6cz = +3a - b + cAdding x+y+z = 6a + 9b + 4c(*ii*) x-y+z = (6a+8b+9c)-(2b-3a-6c)+(c-b+3a)= 6a+8b+9c-2b+3a+6c+c-b+3a= 6a+3a+3a+8b-2b-b+9c+6c+c= 12a + 5b + 16c(iii)2x-y-3z = 2(6a+8b+9c)-(2b-3a-6c)-3(c-b+3a)=12a+16b+18c-2b+3a+6c-3c+3b-9a=12a+3a-9a+16b+3b-2b+18c+6c-3c= 6a + 17b + 21c(iv)3y-2z-5x = 3(2b-3a-6c)-2(c-b+3a)-5(6a+8b+9c)=6b-9a-18c-2c+2b-6a-30a-40b-45c=-9a-6a-30a+6b+2b-40b-18c-2c-45c= -45a - 32b - 65c

Question 10.

The sides of a triangle are $x^2 - 3xy + 8$, $4x^2 + 5xy - 3$ and $6 - 3x^2 + 4xy$. Find its perimeter.

Solution:

Required perimeter = Sum of three sides = $x^2 - 3xy + 8 + 4x^2 + 5xy - 3 + 6 - 3x^2 + 4xy$ = $x^2 + 4x^2 - 3x^2 - 3xy + 5xy + 4xy + 8 - 3 + 6$ = $2x^2 + 6xy + 11$

Question 11.

The perimeter of a triangle is $8y^2 - 9y + 4$ and its two sides are $3y^2 - 5y$ and $4y^2 + 12$. Find its third side.

Solution:

Perimeter of the triangle = Sum of three sides $= 8y^{2} - 9y + 4$ Sum of two sides = $3y^{2} - 5y + 4y^{2} + 12$ $= 7y^{2} - 5y + 12$ $\therefore (8y^{2} - 9y + 4) - (7y^{2} - 5y + 12)$ $= 8y^{2} - 9y + 4 - 7y^{2} + 5y - 12$ $= y^{2} - 4y - 8$ Hence third side = $y^{2} - 4y - 8$

Question 12.

The two adjacent sides of a rectangle are $2x^2 - 5xy + 3z^2$ and $4xy - x^2 - z^2$. Find its perimeter.

Solution:

Adjacent sides of a rectangle are $2x^2 - 5xy + 3z^2$ and $4xy - x^2 - z^2$ \therefore Perimeter = $2(2x^2 - 5xy + 3z^2 + 4xy - x^2 - z^2)$ = $4x^2 - 10xy + 6z^2 + 8xy - 2x^2 - 2z^2$ = $2x^2 - 2xy + 4z^2$

Question 13.

What must be subtracted from $19x^4 + 2x^3 + 30x - 37$ to get $8x^4 + 22x^3 - 7x - 60$? **Solution:**

The required result will be $(19x^4 + 2x^3 + 30x - 37) - (8x^4 + 22x^3 - 7x - 60)$ $= 19x^4 + 2x^3 + 30x - 37 - 8x^4 - 22x^3 + 7x + 60$ $= 11x^4 - 20x^3 + 37x + 23$

Question 14.

How much smaller is 15x - 18y + 19z than 22x - 20y - 13z + 26? Solution: The required result is (22x - 20y - 13z + 26) - (15x - 18y + 19z)= 22x - 20y - 13z + 26 - 15x + 18y - 19z= 7x - 2y - 32z + 26

Question 15.

How much bigger is $15x^2y^2 - 18xy^2 - 10x^2y$ than $-5x^2 + 6x^2y - 7xy$? **Solution:**

The required result,

 $(5x^2y^2 - 18xy^2 - 10x^2y) - (-5x^2 + 6x^2y - 7xy)$ = $5x^2y^2 - 18xy^2 - 10x^2y + 5x^2 - 6x^2y + 7xy$ = $5x^2y^2 - 18xy^2 - 16x^2y + 5x^2 + 7xy$

EXERCISE 11(C)

Question 1. Multiply : (i) $8ab^2$ by $4a^3b^4$

(i)
$$8ab^{2}$$
 by $-4a^{3}b^{4}$
(ii) $\frac{2}{3}ab$ by $-\frac{1}{4}a^{2}b$
(iii) $-5cd^{2}$ by $-5cd^{2}$.
(iv) $4a$ and $(6a + 7)$
(v) $-8x$ and $(4 - 2x - x^{2})$
(vi) $2a^{2} - 5a - 4$ and $-3a$.
(vii) $x + 4$ by $x - 5$
(viii) $5a - 1$ by $7a - 3$
(ix) $12a + 5b$ by $7a - b$
(x) $x^{2} + x + 1$ by $1 - x$
(xi) $2m^{2} - 3m - 1$ and $4m^{2} - m - 1$
(xii) a^{2} , ab and b^{2}
(xiii) abx , $-3a^{2}x$ and $7b^{2}x^{3}$
(xiv) $-3bx$, $-5xy$ and $-7b^{3}y^{2}$
(xv) $\left(-\frac{3}{2}x^{5}y^{3}\right)$ and $\left(\frac{4}{9}a^{2}x^{3}y\right)$
(xvi) $\left(-\frac{2}{3}a^{7}b^{2}\right)$ and $\left(-\frac{9}{4}ab^{5}\right)$
(xvii) $(2a^{3} - 3a^{2}b)$ and $\left(-\frac{1}{2}ab^{2}\right)$
(xviii) $\left(2x + \frac{1}{2}y\right)$ and $\left(2x - \frac{1}{2}y\right)$

Solution:

(i)
$$8ab^2 \times -4a^3b^4 = (8 \times -4)(ab^2 \times a^3b^4)$$

 $= -32a^{1+3} \cdot b^{2+4}$
 $= -32a^4b^6$
(ii) $\frac{2}{3}ab \times -\frac{1}{4}a^2b = (\frac{2}{3} \times \frac{-1}{4})(ab \times a^2b)$
 $= -\frac{1}{6}a^{1+2} \cdot b^{1+1}$
 $= -\frac{1}{6}a^3b^2$
(iii) $-5cd^2 \times -5cd^2 = (-5 \times -5)(cd^2 \times cd^2)$
 $= 25c^{1+1}d^{2+2}$
 $= 25c^2d^4$
(iv) $4a (6a + 7)$
 $= 4a \times 6a + 4a \times 7$
 $= 24a^2 + 28a$
(v) $-8x (4 - 2x - x^2)$
 $= -8x \times 4 - 8x \times -2x - 8x \times -x^2$
 $= -32x + 16x^2 + 8x^3$
(vi) $-3a (2a^2 - 5a - 4)$
 $= -3a \times 2a^2 - 5a \times -3a - 4$
 $\times -3a$
 $= -6a^3 + 15a^2 + 12a$
(vii) $(x+4)(x-5) = x(x-5) + 4(x-5)$
 $= x^2 - 5x + 4x - 20$
 $= x^2 - x - 20$
(viii) $(5a - 1)(7a - 3)$
 $= 5a (7a - 3) - 1 (7a - 3)$
 $= 35a^2 - 15a - 7a + 3$
 $= 35a^2 - 22a + 3$
(ix) $(12a + 5b) (7a - b) = 12a (7a - b) + 5b$
 $(7a - b)$
 $= 84a^2 - 12ab + 35ab - 5b^2$
 $= 84a^2 + 23ab - 5b^2$
(x) $(x^2 + x + 1) (1-x) = 1(x^2 + x + 1) - x(x^2 + x + 1)$
 $= x^2 + x + 1 - x^3 - x^2 - x$.
 $= 1 - x^3$

$$(xi) \quad (2m^2 - 3m - 1) \quad (4m^2 - m - 1) \\ = 2m^2 \quad (4m^2 - m - 1) - 3m(4m^2 - m - 1) - 1(4m^2 - m - 1) \\ = 8m^4 \cdot 2m^3 - 2m^2 - 12m^3 + 3m^2 + 3m - 4m^2 + m + 1 \\ = 8m^4 - 14m^3 - 6m^2 + 3m^2 + 4m + 1 \\ (xii) \quad a^2 \times ab \times b^2 \qquad = a^{2+1} \cdot b^{1+2} \\ = a^3b^3 \\ (xiii) \quad abx \times -3a^2x \times 7b^2x^3 \\ = (-3 \times 7) \quad (a \times a^2) \quad (b \times b^2) \quad (x \times x \times x^3) \\ = -21a^3b^3x^5 \\ (xiv) \quad -3bx \times -5xy \times -7b^3y^2 \\ = (-3 \times -5 \times -7)(b \times b^3)(x \times x)(y \times y^2) \\ = -105 \quad b^4x^2y^3 \\ (xv) \quad \left(-\frac{3}{2}x^5y^3\right)\left(\frac{4}{9}a^2x^3y\right) \\ = \left(-\frac{3}{2} \times \frac{4}{9}\right) \quad (a^2)(x^5 \times x^3)(y^3 \times y) \\ (xvi) \quad \left(-\frac{2}{3}a^7b^2\right)\left(-\frac{9}{4}ab^5\right) \\ = \left(-\frac{2}{3} \times \frac{-9}{4}\right) \quad (a^7 \times a)(b^2 \times b^5) \\ = \frac{3}{2}a^8b^7 \\ (xvii) \quad (2a^3 - 3a^2b) \quad \left(-\frac{1}{2}ab^2\right) \\ = -a^4b^2 + \frac{3}{2}a^3b^3 \\ (xviii) \quad \left(2x + \frac{1}{2}y\right)\left(2x - \frac{1}{2}y\right) \\ = 2x \quad \left(2x - \frac{1}{2}y\right) + \frac{1}{2}y\left(2x - \frac{1}{2}y\right) \\ = 4x^2 - xy + xy - \frac{1}{4}y^2 \\ = 4x^2 - \frac{1}{4}y^2$$

Question 2.

Multiply:
(i)
$$5x^2 - 8xy + 6y^2 - 3$$
 by $- 3xy$
(ii) $3 - \frac{2}{3}xy + \frac{5}{7}xy^2 - \frac{16}{21}x^2 y$ by $- 21x^2 y^2$
(iii) $6x^3 - 5x + 10$ by $4 - 3x^2$
(iv) $2y - 4y^3 + 6y^5$ by $y^2 + y - 3$
(v) $5p^2 + 25pq + 4q^2$ by $2p^2 - 2pq + 3q^2$
Solution:
(i) $5x^2 - 8xy + 6y^2 - 3 \times -3xy$
 $= 15x^3y^3 + 24x^2y^2 - 18xy^3 + 9xy$
(ii) $3 - \frac{2}{3}xy + \frac{5}{7}xy^2 - \frac{16}{21}x^2 y$
 $\times -21x^2y^2$
 $-63x^2y^2 + 14x^3y^3 - 15x^3y^4 + 16x^4y^3$
(iii) $6x^3 - 5x + 10$
 $\frac{\times 4 - 3x^2}{24x^3 - 20x + 40}$
 $\frac{-18x^5 + 15x^3 - 30x^2}{-18x^5 + 39x^3 - 30x^2 - 20x + 40}$
(iv) $2y - 4y^3 + 6y^5$
 $\frac{\times y^2 + y - 3}{2y^3 - 4y^5 + 6y^7}$
 $+ 2y^2 - 4y^4 + 6y^6$
 $\frac{-6y + 12y^3 - 18y^5}{6y^7 + 6y^6 - (4 + 18)y^5 - 4y^4 + (2 + 12)y^3 + 2y^2 - 6y}$
(v) $5p^2 + 25pq + 4q^2$
 $\frac{\times 2p^2 - 2pq + 3q^2}{10p^4 + 50p^3 q + 8p^2q^2}$
 $- 10p^3q - 50p^2q^2 - 8pq^3$
 $\frac{+15p^2q^2 + 75pq^3 + 12q^4}{10p^4 + 40p^3q - 27p^2q^2 + 67pq^3 + 12q^4}$

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Question 3.

Simplify : (i) (7x - 8) (3x + 2)(ii) (px - q) (px + q)(iii) (5a + 5b - c) (2b - 3c)(iv) (4x - 5y) (5x - 4y)(v) (3y + 4z) (3y - 4z) + (2y + 7z) (y + z)

Solution:

(i)
$$(7x - 8) (3x + 2) = 7x(3x + 2) - 8 (3x + 2)$$

= $21x^2 + 14x - 24x - 16 = 21x^2 - 10x - 16$
(ii) $(px - q) (px + q) = px (px + q) - q (px + q)$
= $p^2x^2 + pxq - pqx - q^2 = p^2x^2 - q^2$
(iii) $(5a + 5b - c) (2b - 3c)$
= $5a (2b - 3c) + 5b (2b - 3c) - c (2b - 3c)$
= $10ab - 15ac + 10b^2 - 15bc - 2bc + 3c^2$
= $10ab + 10b^2 - 17bc - 15ac + 3c^2$
(iv) $(4x - 5y) (5x - 4y)$
= $4x (5x - 4y) - 5y (5x - 4y)$
= $20x^2 - 16xy - 25xy + 20y^2$
= $20x^2 - 41xy + 20y^2$
(v) $(3y + 4z) (3y - 4z) + (2y + 7z) (y + z)$
= $3y (3y - 4z) + 4z (3y - 4z) + 2y (y + z) + 7z (y + z)$
= $9y^2 - 12yz + 12yz - 16z^2 + 2y^2 + 2yz + 7yz + 7z^2$
= $(9 + 2)y^2 + (-12 + 12 + 2 + 7)yz + (-16 + 7)z^2$
= $11y^2 + 9yz - 9z^2$

Question 4.

The adjacent sides of a rectangle are $x^2 - 4xy + 7y^2$ and $x^3 - 5xy^2$. Find its area. **Solution:**

Reqd. area =
$$(x^2 - 4xy + 7y^2) (x^3 - 5xy^2)$$

= $x^2 (x^3 - 5xy^2) - 4xy (x^3 - 5xy^2) + 7y^2 (x^3 - 5xy^2)$
= $x^5 - 5x^3y^2 - 4x^4y + 20x^2y^3 + 7x^3y^2 - 35xy^4$
= $x^5 + (7 - 5)x^3y^2 - 4x^4y + 20x^2y^3 - 35xy^4$
= $x^5 + 2x^3y^2 - 4x^4y + 20x^2y^3 - 35xy^4$
= $(x^5 - 4x^4y + 2x^3y^2 + 20x^2y^3 - 35xy^4)$ sq. unit.

Question 5.

The base and the altitude of a triangle are (3x - 4y) and (6x + 5y) respectively. Find its area. **Solution:**

Reqd. Area = $\frac{1}{2}$ (base) x (altitude) = $\frac{1}{2}$ (3x - 4y) (6x + 5y) = $\frac{1}{2}$ (18x² + 15xy - 24xy - 20y²) = $\frac{1}{2}$ (18x² - 9xy - 20y²) sq. unit.

Question 6.

...

Multiply $-4xy^3$ and $6x^2y$ and verify your result for x = 2 and y = 1. Solution:

$$(-4xy^{3}) \times (6x^{2}y) = (-4 \times 6) (x \times x^{2}) (y^{3} \times y)$$

= $-24x^{3}y^{4}$
For $x = 2$ and $y = 1$
 $(-4xy^{3}) \times (6x^{2}y) = (-4 \times 2 \times 1^{3}) \times (6 \times 2^{2} \times 1)$
= $(-8) \times 24 = -192$
And, $-24x^{3}y^{4} = -24 \times 2^{3} \times 1^{4}$
= $-24 \times 8 \times 1 = -192$
For $x = 2$ and $y = 1$, it is verified that
 $(-4xy^{3}) \times (6x^{2}y) = -24x^{3}y^{4}$

Question 7.

Find the value of $(3x^3) \times (-5xy^2) \times (2x^2yz^3)$ for x = 1, y = 2 and z = 3. Solution:

For
$$x = 1$$
, $y = 2$ and $z = 3$
 $(3x^3) \times (-5xy^2) \times (2x^2yz^3)$
 $(3 \times 1^3) \times (-5 \times 1 \times 2^2) \times (2 \times 1^2 \times 2 \times 3^3)$
 $3 \times (-5 \times 4) \times (2 \times 1 \times 2 \times 27)$
 $3 \times (-20) \times 108 = -6480$

Question 8.

Evaluate $(3x^4y^2) (2x^2y^3)$ for x = 1 and y = 2.

Solution:

 $(3x^{4}y^{2}) (2x^{2}y^{3})$ $(3 \times 1^{4} \times 2^{2}) \times (2 \times 1^{2} \times 2^{3})$ $(3 \times 1 \times 4) \times (2 \times 1 \times 8) \quad *$ $= 12 \times 16 = 192$

Question 9.

Evaluate (x⁵) x (3x²) x (-2x) for x = 1. Solution: For x = 1(x⁵) × (3x²) × (-2x) (1⁵) × (3 × 1²) × (-2 × 1) 1 × 3 × (-2) = -6

Question 10.

If x = 2 and y = 1; find the value of $(-4x^2y^3) \times (-5x^2y^5)$. Solution: For x = 2 and y = 1 $(-4x^2y^3) \times (-5x^2y^5)$ $(-4 \times 2^2 \times 1^3) \times (-5 \times 2^2 \times 1^5)$ $(-4 \times 4 \times 1) \times (-5 \times 4 \times 1)$ $-16 \times -20 = 320$

Question 11.

Evaluate: (i) (3x - 2)(x + 5) for x = 2. (ii) (2x - 5y)(2x + 3y) for x = 2 and y = 3. (iii) $xz (x^2 + y^2)$ for x = 2, y = 1 and z = 1.

Solution:

(i) For
$$x = 2$$

($3x - 2$) ($x + 5$)
($3 \times 2 - 2$) ($2 + 5$)
($6 - 2$) × 7
 $4 \times 7 = 28$
(ii) For $x = 2$ and $y = 1$
 $xy^2(x - 5y) + 1$
 $2 \times 1^2(2 - 5 \times 1) + 1$
 $2 \times (2 - 5) + 1$
 $2 \times (-3) + 1$
 $-6 + 1 = -5$
(iii) For $x = 2$, $y = 1$ and $z = 1$
 $xz(x^2 + y^2)$
 $2 \times 1(2^2 + 1^2)$
 $2(2 + 1)$
 $= 2 \times 3 = 6$
Question 12.
Evaluate:
(i) $x(x - 5) + 2$ for $x = 1$.
(ii) $xy^2(x - 5y) + 1$ for $x = 2$ and $y = 1$.
(iii) $2x(3x - 5) - 5(x - 2) - 18$ for $x = 2$.
Solution:
(i) For $x = 1$
 $x(x - 5) + 2$
 $1(1 - 5) + 2$
 $-4 + 2 = -2$
(ii) For $x = 2$ and $y = 1$
 $xy^2(x - 5y)$
 $2 \times 1^2(2 - 5 \times 1)$
 $2 \times (2 - 5)$
 $2 \times (-3) = -6$
(iii) For $x = 2$
 $2x(3x - 5) - 5(x - 2) - 18$
 $2 \times 2(3 \times 2 - 5) - 5(2 - 2) - 18$
 $4(6 - 5) - 5 \times 0 - 18$
 $4 - 18 = -14$

Question 13.

Multiply and then verify : $-3x^2y^2$ and (x - 2y) for x = 1 and y = 2. **Solution:** $(-3x^2y^2) \times (x - 2y)$ $= (-3x^2y^2) \times (x) = (-3x^2y^2)(2y)$

$$= (-3x^{2}y^{2}) \times (x) - (-3x^{2}y^{2})(2y)$$

$$= -3x^{3}y^{2} + 6x^{2}y^{3}$$

$$= 6x^{2}y^{3} - 3x^{3}y^{2}$$

For $x = 1$ and $y = 2$
 $(-3x^{2}y^{2}) \times (x - 2y)$

$$= (-3 \times 1^{2} \times 2^{2}) \times (1 - 2 \times 2)$$

$$= (6 \times 1 \times 8) - (3 \times 1 \times 4)$$

$$= 48 - 12 = 36$$

 $\therefore \text{ For } x = 1 \text{ and } y = 2, \text{ it is verified that,}$ $(-3x^2y^2) \times (x - 2y) = 6x^2y^3 - 3x^3y^2$

Question 14.

Multiply: (i) $2x^2 - 4x + 5$ by $x^2 + 3x - 7$ (ii) (ab - 1)(3 - 2ab)

(i)
$$2x^2 - 4x + 5$$
 by $x^2 + 3x - 7$
 $(2x^2 - 4x + 5) \times (x^2 + 3x - 7)$
 $2x^2(x^2 + 3x - 7) - 4x(x^2 + 3x - 7) + 5(x^2 + 3x - 7)$
 $2x^4 + 6x^3 - 14x^2 - 4x^3 - 12x^2 + 28x + 5x^2 + 15x - 35$
 $2x^4 + 6x^3 - 4x^3 - 14x^2 - 12x^2 + 5x^2 + 28x + 15x - 35$
 $2x^4 + 2x^3 - 21x^2 + 43x - 35$
(ii) $(ab - 1) (3 - 2ab)$
 $ab(3 - 2ab) - 1(3 - 2ab)$
 $ab(3 - 2ab) - 1(3 - 2ab)$
 $3ab - 2a^2b^2 - 3 + 2ab$
 $-2a^2b^2 + 5ab - 3$
 $2a^2b^2 - 5ab + 3$

Question 15. Simplify : (5 - x)(6 - 5x)(2 - x). Solution: (5 - x) (6 - 5x) (2 - x) [(5 - x) (6 - 5x)] (2 - x) [5(6 - 5x) - x(6 - 5x)] (2 - x) $[30 - 25x - 6x + 5x^2] (2 - x)$ $(5x^2 - 31x + 30) (2 - x)$ $2(5x^2 - 31x + 30) - x (5x^2 - 31x + 30)$ $10x^2 - 62x + 60 - 5x^3 + 31x^2 - 30x$

$$-5x^3 + 10x^2 + 31x^2 - 62x - 30x + 60$$

$$-5x^3 + 41x^2 - 92x + 60$$

Question 1. Divide :

(i)
$$-70a^{3}$$
 by $14a^{2}$
(ii) $24x^{3}y^{3}$ by $-8y^{2}$
(iii) $15a^{4}b$ by $-5a^{3}b$
(iv) $-24x^{4}d^{3}$ by $-2x^{2}d^{5}$
(v) $63a^{4}b^{5}c^{6}$ by $-9a^{2}b^{4}c^{3}$
(vi) $8x - 10y + 6c$ by 2.
(vii) $15a^{3}b^{4} - 10a^{4}b^{3} - 25a^{3}b^{6}$ by $-5a^{3}b^{2}$
(viii) $-14x^{6}y^{3} - 21x^{4}y^{5} + 7x^{5}y^{4}$ by $7x^{2}y^{2}$
(ix) $a^{2} + 7a + 12$ by $a + 4$
(x) $x^{2} + 3x - 54$ by $x - 6$
(xi) $12x^{2} + 7xy - 12y^{2}$ by $3x + 4y$
(xii) $x^{6} - 8$ by $x^{2} - 2$
(xiii) $6x^{3} - 13x^{2} - 13x + 30$ by $2x^{2}-x-6$
(xiv) $4a^{2} + 12ab + 9b^{2} - 25c^{2}$ by $2a+3b+5c$.
(xv) $16+8x+x^{6}-8x^{3}-2x^{4}+x^{2}$ by $x + 4 - x^{3}$

Solution:

(i)
$$\frac{-70a^3}{14a^2} = \left(\frac{-70}{14}\right) \left(\frac{a^3}{a^2}\right)$$

= $-5a^{3-2}$
= $-5a$

$$(ii) \ \frac{24x^3y^3}{-8y^2} = \left(\frac{24}{-8}\right)(x^3)\left(\frac{y^3}{y^2}\right) \\ = -3x^3y^{3-2} \\ = -3x^3y \\ (iii) \ \frac{15a^4b}{-5a^3b} = \left(\frac{15}{-5}\right)\left(\frac{a^4}{a^3}\right)\left(\frac{b}{b}\right) \\ = -3a^{4-3}b^{1-1} \\ = -3a\ b^0 \\ = -3a \times 1 \quad (\because\ b^0 = 1) \\ = -3a \\ (iv) \ \frac{-24x^4d^3}{-2x^2d^5} = \left(\frac{-24}{-2}\right)\left(\frac{x^4}{x^2}\right)\left(\frac{d^3}{d^5}\right) \\ = 12x^{4-2}a^{3-5} = 12x^2a^{-2} \\ = \frac{12x^2}{d^2} \\ (v) \ \frac{63a^4b^5c^6}{-9a^2b^4c^3} = \left(\frac{63}{-9}\right)\left(\frac{a^4}{a^2}\right)\left(\frac{b^5}{b^4}\right)\left(\frac{c^6}{c^3}\right)$$

$$= -7a^{4-2} \cdot b^{5-4} \cdot c^{6-3}$$
$$= -7a^{2}bc^{3}$$

$$(vi) \ \frac{8x - 10y + 6c}{2} = \frac{8x}{2} - \frac{10y}{2} + \frac{6c}{2} = 4x - 5y + 3c$$

$$= 4x-5y+3c$$
(vii)
$$\frac{15a^3b^4 - 10a^4b^3 - 25a^3b^6}{-5a^3b^2}$$

$$= \frac{15a^{3}b^{4}}{-5a^{3}b^{2}} - \frac{10a^{4}b^{3}}{-5a^{3}b^{2}} - \frac{25a^{3}b^{6}}{-5a^{3}b^{2}}$$
$$= -3b^{4-2} + 2a^{4-3}b^{3-2} + 5b^{6-2}$$
$$= -3b^{2} + 2ab + 5b^{4}$$

$$\frac{-14x^6y^3 - 21x^4y^5 + 7x^5y^4}{7x^2y^2}$$

$$= \frac{-14x^{6}y^{3}}{7x^{2}y^{2}} - \frac{21x^{4}y^{5}}{7x^{2}y^{2}} + \frac{7x^{5}y^{4}}{7x^{2}y^{2}}$$
$$= -2x^{6-2}y^{3-2} - 3x^{4-2}y^{5-2} + x^{5-2}y^{4-2}$$
$$= -2x^{4}y - 3x^{2}y^{3} + x^{3}y^{2}$$

(ix)
$$a+4$$
) $a^2+7a+12$ (a+3)
 a^2+4a

:. Answer =
$$a + 3$$

(x) $x-6$) $x^2+3x-54$ (x+9)
 x^2-6x
- +
9x-54
+ 9x-54
- +
×

 \therefore Answer = x + 9

 \therefore Answer = 3x - 5

(xiv)

$2a+3b+5c) \overline{4a^2+}$	-12ab + 9b	b ² -250	c^2 (2a	+3b-5c
$4a^2 +$	6ab	+10 <i>ca</i>		
	-		-	_
$6ab+9b^2-25c^2-10ca$				
	$6ab + 9b^2$	2 +		+15bc
				-
		-100	a-250	$c^{2}-15bc$
		-100	a-250	c ² –15bc
		+	+	+
		×		

 \therefore Answer = 2a+3b-5c

(xv)

$$-x^{3}+x+4) + x^{6}-2x^{4}-8x^{3}+x^{2}+8x+16 (-x^{3}+x+4) + x^{6}-x^{4}-4x^{3} + x^{2}+8x+16 (-x^{3}+x+4) + x^{4}-4x^{3}+x^{2}+8x+16 (-x^{4}+x^{2}+4x) + x^{2}+4x + x^{2}+4x$$

Question 2.

Find the quotient and the remainder (if any) when :

(i) $a^3 - 5a^2 + 8a + 15$ is divided by a + 1.

(ii) $3x^4 + 6x^3 - 6x^2 + 2x - 7$ is divided by x - 3.

(iii) $6x^2 + x - 15$ is divided by 3x + 5. In each case, verify your answer.

(iv) $6y^5 + 30y^4 + 18y^3 + 6y^2 + 15y + 3$ is divided by $2y^3 + 1$. Solution:

 \therefore Quotient = $a^2 - 6a + 14$ and remainder = 1

(ii)

$$x - \overline{3})\overline{3x^4 + 6x^3 - 6x^2 + 2x - 7}(3x^3 + 15x^2 + 39x + 119)$$

$$3x^4 - 9x^3$$

$$- +$$

$$15x^3 - 6x^2 + 2x - 7$$

$$15x^3 - 45x^2$$

$$- +$$

$$\overline{39x^2 + 2x - 7}$$

$$39x^2 - 117x$$

$$- +$$

$$119x - 7$$

$$119x - 357$$

$$- +$$

$$350$$

:. Quotient = $3x^3 + 15x^2 + 39x + 119$ and remainder = 350

(iii)
$$3x + 5\overline{)6x^2 + x - 15(2x - 3)}$$

 $6x^2 + 10x$
 $-9x - 15$
 $-9x - 15$

 \therefore Quotient = $3y^2 + 15y + 9$ and remainder = $3y^2 - 6$

(i) Verification.

Dividend = Quotient × Divisor + Remainder = $(a^2 - 6a + 14) \times (a + 1) + 1$ = $a^3 - 6a^2 + 14a + a^2 - 6a + 14 + 1$ = $a^3 - 5a^2 + 8a + 15$ which is given

(ii) Verification:

Dividend = Quotient × Divisor + Remainder = $(3x^3 + 15x^2 + 39x + 119)(x - 3) + 350$ = $3x^4 + 15x^3 + 39x^2 + 119x - 9x^3 - 45x^2 - 117x - 357 + 350$ = $3x^4 + 6x^3 - 6x^2 + 2x - 7$ which is given

(iii) Verification:

Dividend = Quotient × Divisor + Remainder

$$= (2x-3)(3x+5)+0$$

$$= 6x^2 + 10x - 9x - 15 + 0$$

 $= 6x^2 - x - 15$ which is given

(iv) Verification:

Dividend = Quotient × Divisor + Remainder = $(3y^2 + 15y + 9) (2y^3 + 1) + 3y^2 - 6$ = $6y^5 + 30y^4 + 18y^3 + 3y^2 + 15y + 9 + 3y^2 - 6$ = $6y^5 + 30y^4 + 18y^3 + 6y^2 + 15y + 3$ which is given

Question 3.

The area of a rectangle is $x^3 - 8x^2 + 7$ and one of its sides is x - 1. Find the length of the adjacent side.

Solution:

Question 4.

The product of two numbers-is $16x^4 - 1$. If one number is 2x - 1, find the other.

Solution:

Product of two numbers = $16x^4 - 1$ One number = 2x - 1

Then second number = $\frac{16x^4 - 1}{2x - 1}$ = $8x^3 + 4x^2 + 2x + 1$

$$\frac{8x^{3} + 4x^{2} + 2x + 1}{2x - 1)16x^{4}} - 1(1) + 16x^{4} - 8x^{3} - 1(1) + 16x^{4} - 1(1) +$$

Question 5.

Divide $x^6 - y^6$ by the product of $x^2 + xy + y^2$ and x - y.

Solution:

Product of
$$(x^{2} + xy + y^{2})$$
 and $(x - y)$
= $(x - y) (x^{2} + xy + y^{2})$
= $x(x^{2} + xy + y^{2}) - y(x^{2} + xy + y^{2})$
= $x^{3} + x^{2}y + xy^{2} - x^{2}y - xy^{2} - y^{3}$
= $x^{3} - y^{3}$
Now, $(x^{6} - y^{6}) \div (x^{3} - y^{3})$
= $x^{3} + y^{3}$
 $x^{3} - y^{3})\overline{x^{6}} - y^{6}(x^{3} + y^{3})$
 $x^{6} - x^{3}y^{3}$
 $- +$

$$\begin{array}{r} x^3y^3 - y^6 \\ x^3y^3 - y^6 \\ - + \\ \hline \times \end{array}$$

Simplification (Using removal of brackets)

The signs for different types of brackets are :

- 1. ____; Vinculum or bar brackets,
- 2. (); Parenthesis or small brackets,
- 3. { }; Curly brackets or middle brackets,
- []; Square brackets or big brackets.
 In a combined operation, the brackets must be removed in the same order as written above:

EXERCISE 11(E)

Simplify :
Question 1.

$$a^2 - 2a + \{5a^2 - (3a - 4a^2)\}$$

Solution:
 $= a^2 - 2a + \{5a^2 - 3a + 4a^2\}$
 $= a^2 - 2a + \{9a - 3a\}$
 $= a^2 - 2a + 9a^2 - 3a = 10a^2 - 5a$

Question 2.

$$x - y - \{x - y - (x + y) - \overline{x - y}\}$$

Solution:
$$x - y - \{x - y - (x + y) - \overline{x - y}\}$$
$$= x - y - \{x - y - (x + y) - x + y\}$$
$$= x - y - \{x - y - x - y - x + y\}$$
$$= x - y - \{x - y - x - y - x + y\}$$
$$= x - y - x + y + x + y + x - y = 2x$$

Question 3.
-3
$$(1 - x^2) - 2 \{x^2 - (3 - 2x^2)\}$$

Solution:
-3 $(1 - x^2) - 2 \{x^2 - (3 - 2x^2)\}$
= -3 + 3x² - 2 $\{x^2 - 3 + 2x^2\}$
= -3 + 3x² - 2 $\{3x^2 - 3\}$
= -3 + 3x² - 6x² + 6 = 3 - 3x²

Question 4.

 $2\{m-3 (n + \overline{m-2n})\}$ Solution: $2\{m-3 (n + \overline{m-2n})\}$ $= 2\{m-3 (n + m - 2n)\} = 2\{m-3 (m - n)\}$ $= 2\{m-3m+3n\} = 2\{3n-2m\} = 6n - 4m$

Question 5.

 $3x - [3x - \{3x - (3x - \overline{3x - y})\}]$ Solution: $3x - [3x - \{3x - (3x - \overline{3x - y})\}]$ $= 3x - [3x - \{3x - (3x - 3x + y)\}]$ $= 3x - [3x - \{3x - y\}] = 3x - [3x - 3x + y]$ = 3x - y **Question 6.**

$$p^{2}x - 2\{px - 3x (x^{2} - \overline{3a - x^{2}})\}$$

Solution:
$$p^{2}x - 2\{px - 3x (x^{2} - \overline{3a - x^{2}})\}$$
$$= p^{2}x - 2\{px - 3x (x^{2} - 3a + x^{2})\}$$
$$= p^{2}x - 2\{px - 3x (2x^{2} - 3a)\}$$
$$= p^{2}x - 2\{px - 6x^{3} + 9ax\}$$
$$= p^{2}x - 2px + 12x^{3} - 18ax$$

Question 7.

 $2[6 + 4\{m - 6(7 - n + p) + q\}]$ Solution: $2[6 + 4\{m - 6(7 - n + p) + q\}]$ $= 2[6 + 4\{m - 6(7 - n - p) + q\}]$ $= 2[6 + 4\{m - 42 + 6n + 6p + q\}]$ = 2[6 + 4m - 168 + 24n + 24p + 4q] = 2[4m + 24n + 24p + 4q - 162] = 8m + 48n + 48p + 8q - 324

Question 8.

$$a - [a - b + a - \{a - (a - b - a)\}]$$

Solution:
$$a - [a - \overline{b + a} - \{a - (a - \overline{b - a})\}]$$
$$= a - [a - b - a - \{a - (a - b + a)\}]$$
$$= a - [-b - \{a - a + b - a\}]$$
$$= a - [-b - b + a]$$
$$= a + b + b - a = 2b$$

Question 9.

$$3x - [4x - \overline{3x - 5y} - 3 \{2x - (3x - \overline{2x - 3y})\}]$$

Solution:

$$3x - [4x - 3x - 5y - 3 \{2x - (3x - 2x - 3y)\}]$$

= $3x - [4x - 3x + 5y - 3 \{2x - (3x - 2x + 3y)\}]$
= $3x - [4x - 3x + 5y - 3 \{2x - (x + 3y)\}]$
= $3x - [4x - 3x + 5y - 3 \{2x - (x + 3y)\}]$
= $3x - [4x - 3x + 5y - 3 \{2x - x - 3y\}]$
= $3x - [x + 5y - 6x + 3x + 9y]$
= $3x - [-2x + 14y]$
= $3x + 2x - 14y$
= $5x - 14y$

Question 10.

 $a^{5} \div a^{3} + 3a \times 2a$ Solution: $a^{5} \div a^{3} + 3a \times 2a = a^{5-3} + 3a \times 2a = a^{2} + 6a^{2} = 7a^{2}$

Question 11.

 $x^5 \div (x^2 \times y^2) \times y^3$ Solution:

$$x^{5} \div (x^{2} \times y^{2}) \times y^{3} = \frac{x^{5}}{x^{2}y^{2}} \times y^{3} = x^{5-2} - y^{3-2} = x^{3}y$$

Question 12.

 $(x^5 \div x^2) \times y^2 \times y^3$ Solution: $(x^5 \div x^2) \times y^2 \times y^3 = x^{5-2} \times y^{2+3} = x^3 y^5$

Question 13.

 $(y^3 - 5y^2) \div y \times (y - 1)$

Solution:

$$(y^3 - 5y^2) \div y \times (y - 1) = \frac{y^3 - 5y^2}{y} \times y - 1$$

= $(y^2 - 5y) \times (y - 1) = y^2 (y - 1) - 5y (y - 1) = y^3 - y^2 - 5y^2 + 5y = y^3 - 6y^2 + 5y$

Question 14.

 $3a \times [8b \div 4 - 6 \{a - (5a - \overline{3b - 2a})\}]$ Solution: $3a \times [8b \div 4 - 6 \{a - (5a - \overline{3b - 2a})\}]$ $= 3a \times [\frac{8b}{4} - 6\{a - (5a - 3b + 2a)\}] = 3a \times [2b - 6 \{a - 7a + 3b\}] = 3a \times [2b - 6 \{-6a + 3b\}]$ $= 3a \times [2b + 36a - 18b] = 3a \times [36a - 16b] = 108a^2 - 48ab$

Question 15.

$$7x + 4 \{x^{2} \div (5x \div 10)\} - 3\{2 - x^{3} \div (3x^{2} \div x)\}$$

Solution:
$$7x + 4\{x^{2} \div (5x \div 10)\} - 3\{2 - x^{3} \div (3x^{2} \div x)\}$$
$$= 7x + 4 \left\{x^{2} \div \left(\frac{5x}{10}\right)\right\} - 3 \left\{2 - x^{3} \div \left(\frac{3x^{2}}{x}\right)\right\}$$
$$= 7x + 4 \left\{x^{2} \div \frac{x}{2}\right\} - 3 \left\{2 - x^{3} \div 3x\right\} = 7x + 4 \left\{x^{2} \times \frac{2}{x}\right\} - 3 \left\{2 - \frac{x^{3}}{3x}\right\}$$
$$= 7x + 8x - 6 + x^{2} = x^{2} + 15x - 6$$