DPP No. 28

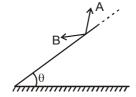
Total Marks: 24

Max. Time: 25 min.

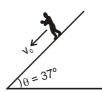
Topics: Relative Motion, Newtons's Law of Motion

Type of Questions		M.M., Min.
Single choice Objective ('-1' negative marking) Q.1 to Q.4	(3 marks, 3 min.)	[12, 12]
Multiple choice objective ('-1' negative marking) Q.5 to Q.6	(4 marks, 4 min.)	[8, 8]
Subjective Questions ('–1' negative marking) Q.7	(4 marks, 5 min.)	[4, 5]

1. Two stones A and B are projected from an inclined plane such that A has range up the incline and B has range down the incline. For range of both stones on the incline to be equal in magnitude, pick up the correct condition. (Neglect air friction)



- (A) Component of initial velocity of both stones along the incline should be equal and also component of initial velocity of both stones perpendicular to the incline should be equal.
- (B) Horizontal component of initial velocity of both stones should be equal and also vertical component of initial velocity of both stones should be equal.
- (C) Component of initial velocity of both stones perpendicular to the incline should be equal and also horizontal component of initial velocity of both stones should be equal in magnitude.
- (D) None of these.
- 2. A man is moving downward on an inclined plane ($\theta = 37^{\circ}$) with velocity v_0 and rain drops appear to him moving in horizontal direction with velocity $2v_0$ towards him. If man increases his velocity to $2v_0$ him velocity of rain drops as observed by man is:



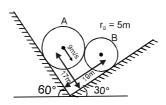
(A)
$$\sqrt{\frac{41}{5}} \ v_0$$

(B) $\sqrt{39} \ v_0$

$$(C)7v_0$$

 $(D) 6 v_0$

3. System is shown in the figure. Velocity of sphere A is 9 m/s. Then speed of sphere B will be:



(A) 9 m/s

(B) 12 m/s

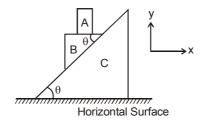
(C)
$$9 \times \frac{5}{4}$$
 m/s

(D) none of these

4. Objects A and B each of mass m are connected by light inextensible cord. They are constrained to move on a frictionless ring in a vertical plane as shown in figure. The objects are released from rest at the positions shown. The tension in the cord just after release will be



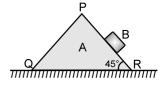
- (A) mg $\sqrt{2}$
- (B) $\frac{\text{mg}}{\sqrt{2}}$
- (C) $\frac{\text{mg}}{2}$
- (D) $\frac{\text{mg}}{4}$
- 5. In the figure shown all the surface are smooth. All the blocks A, B and C are movable X-axis is horizontal and y-axis vertical as shown. Just after the system is relased from the position as shown.



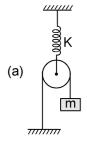
- (A) Acceleration of 'A' relative to ground is in negative y-direction
- (B) Acceleration of 'A' relative to B is in positive x-direction
- (C) The horizontal acceleration of 'B' relative to ground is in negative x-direction.
- (D) The acceleration of 'B' relative to ground directed along the inclined surface of 'C' is greater than $g \sin \theta$.
- 6. A block B of mass 0.6 kg slides down the smooth face PR of a wedge A of mass 1.7 kg which can move freely on a smooth horizontal surface.

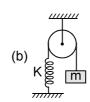
The inclination of the face PR to the horizontal is 45°. Then:

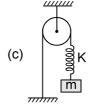
- (A) the acceleration of A is 3 g/20
- (B) the vertical component of the acceleration of B is 23 g/40
- (C) the horizontal component of the acceleration of B is 17 g/40
- (D) none of these

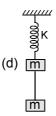


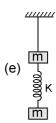
7. Find the tension in the string and the extension in the spring at equilibrium. Where pulley, strings and springs are ideal.











Answers Key

DPP NO. - 28

- **1._** (C)
- **2.**_ (A)
- **3.** (B)
- **4.** (B)

- **5.** (A) (B) (C) (D)
- **6.** (A) (B) (C)
- 7. (a) $T = mg, x = \frac{2mg}{K}$;

(b)
$$T_1 = mg$$
, $T_2 = 2mg$, $x = \frac{mg}{K}$;

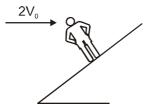
(c)
$$T_1 = mg$$
, $T_2 = 2mg$, $x = \frac{mg}{K}$;

(d) T = mg, x =
$$\frac{2mg}{K}$$
; (e) T = 2mg, x = $\frac{mg}{K}$

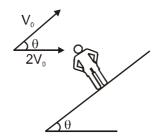
Hint & Solutions

DPP NO. - 28

- If component of velocity normal to incline are equal, time of flight is same. Also if horizontal components are equal, range on inclined plane will be equal for both.
- 2._ Velocity of rain with respect to man initially as shown



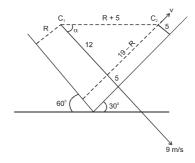
Velocity relative to man when it increase its speed to $2V_{_{0}}$



So resultant velocity of rain with respect to man

$$= \sqrt{(2V_0)^2 + (V_0)^2 + 4V_0^2 \cos 37^\circ} = \sqrt{\frac{41}{5}} V_0$$

3.

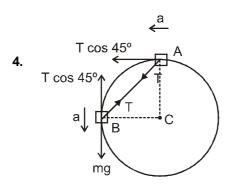


$$9\cos\alpha = v\sin\alpha \rightarrow (i)$$

$$\frac{19-R}{12} = \tan\alpha \longrightarrow (ii)$$

$$(R + 5)^2 = (12)^2 + (19 - R)^2$$
 [Pythagorean]
 $\Rightarrow R = 10$

Hence from (i) and (ii) v = 12 m/s



On block B:

$$mg - T \cos 45^{\circ} = ma$$
 ...(i)

on block A:

$$T \cos 45^{\circ} = ma$$
 ...(ii)

by equation (i) and (ii)

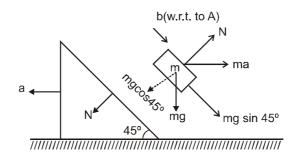
$$T = \frac{mg}{\sqrt{2}}$$

5. There is no horizontal force on block A, therefore it does not move in x-directing, whereas there is net downward force (mg – N) is acting on it, making its acceleration along negative y-direction. Block B moves downward as well as in negative x-direction. Downward acceleration of A and B will be equal due to constrain, thus w.r.t. B, A moves in positive x-direction.



Due to the component of normal exerted by C on B, it moves in negative x-direction.

6. F.B.D. of block B w.r.t. wedge



for block A

N
$$\cos 45^{\circ} = 1.7 a$$
(i)

for block B

$$0.6g \sin 45^{\circ} + 0.6a \cos 45^{\circ} = 0.6b$$
(ii)

$$N + 0.6 \text{ a} \cos 45^{\circ} = 0.6 \text{ g} \cos 45^{\circ}$$
(iii)

by solving (i), (ii) & (iii)

$$a = \frac{3g}{20}$$
 and $b = \frac{23g}{20\sqrt{2}}$

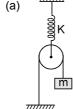
Now vertical component of acceleration of

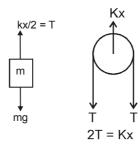
B = b cos 45° =
$$\frac{23g}{40}$$

and horizontal component of acceleration of

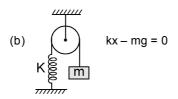
B = b sin
$$45^{\circ}$$
 - a = $\frac{17g}{40}$

. (a) F.B.D. of m FBD

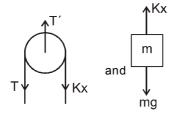




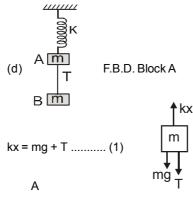
$$\frac{kx}{2}$$
 = mg $x = \frac{2mg}{k}$ T = mg



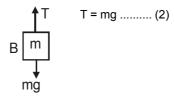
F.B.D of pulley



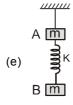
$$x = \frac{mg}{k}$$
 $T = mg$



F.B.D. Block B



$$\therefore kx = 2mg \quad x = \frac{2mg}{k}$$



F.B.D. of Upper Block A

A
$$T = mg + kx \dots (1)$$
 $mg kx$

F.B.D. of Lower Block (B)



$$kx = mg \dots (2) \therefore x = \frac{mg}{k}$$