



Assignment

Value of Function

Basic Level

If $f(x) = \frac{1-x}{1+x}$, then $f[f(\cos 2\theta)]$ equal to [MP PET 1994, 2001]

- (a) $\tan 2\theta$ (b) $\sec 2\theta$ (c) $\cos 2\theta$ (d) $\cot 2\theta$

If $f(x) = \frac{\cos^2 x + \sin^4 x}{\sin^2 x + \cos^4 x}$ for $x \in R$, then $f(2002) =$ [EAMCET 2002]

- (a) 1 (b) 2 (c) 3 (d) 4

If $\phi(x) = a^x$, then $\{\phi(p)\}^3$ is equal to [MP PET 1999]

- (a) $\phi(3p)$ (b) $3\phi(p)$ (c) $6\phi(p)$ (d) $2\phi(p)$

If $f(x) = \cos(\log x)$, then $f(x)f(y) - \frac{1}{2}[f(\frac{x}{y}) + f(xy)] =$ [IIT 1983; Rajasthan PET 1995; MP PET 1995; KCET 1999; UPSEAT 2001]

- (a) $\frac{1}{2}$ (b) 2 (c) 0 (d) 1

If $f(\theta) = \tan \theta$, then $\frac{f(\theta) - f(\phi)}{1 + f(\theta)f(\phi)}$ is equal to [Rajasthan PET 1996]

- (a) $f(\theta - \phi)$ (b) $f(\phi - \theta)$ (c) $f(\theta + \phi)$ (d) None of these

If $f(x) = 2x\sqrt{1-x^2}$, then $f\left(\sin \frac{x}{2}\right)$ equals [Rajasthan PET 1989]

- (a) $\sin 2x$ (b) $\sin x$ (c) $2 \sin x$ (d) $2 \sin \frac{x}{2}$

If $f(x) = \frac{x}{x-1}$, then $\frac{f(a)}{f(a+1)}$ is equal to [MP PET 1996]

- (a) $f(-a)$ (b) $f\left(\frac{1}{a}\right)$ (c) $f(a^2)$ (d) $f\left(\frac{-a}{a-1}\right)$

If $f(x) = \begin{cases} 2x-3 & , x \geq 2 \\ x & , x < 2 \end{cases}$, then $f(1)$ is equal to [Karnataka CET 1989]

- (a) $2f(2)$ (b) $f(2)$ (c) $-f(2)$ (d) $\frac{1}{2}f(2)$

If $f(x) = x^2 - x^{-2}$, then $f\left(\frac{1}{x}\right)$ is equal to [SCRA 1999]

- (a) $f(x)$ (b) $-f(x)$ (c) $\frac{1}{f(x)}$ (d) $[f(x)]^2$

If $f(x) = 4x^3 + 3x^2 + 3x + 4$, then $x^3 f\left(\frac{1}{x}\right)$ is

[SCRA 1996]

- (a) $f(-x)$ (b) $\frac{1}{f(x)}$ (c) $\left[f\left(\frac{1}{x}\right)\right]^2$ (d) $f(x)$

The equivalent function of $\log x^2$ is

[MP PET 1997]

- (a) $2 \log x$ (b) $2 \log |x|$ (c) $|\log x^2|$ (d) $(\log x)^2$

Advance

If $f(x) = \cos[\pi]x + \cos[\pi x]$, where $[y]$ is the greatest integer function of y then $f\left(\frac{\pi}{2}\right)$ is equal to

- (a) $\cos 3$ (b) 0 (c) $\cos 4$ (d) None of these

Let $f(x) = \begin{cases} 1+|x| & , x < -1 \\ [x] & , x \geq -1 \end{cases}$, where $[.]$ denotes the greatest integer function. Then $f\{f(-2.3)\}$ is equal to

- (a) 4 (b) 2 (c) -3 (d) 3

If $f(x_1) + f(x_2) = f\left(\frac{x_1 + x_2}{1 + x_1 x_2}\right)$, $x_1 x_2 \in (-1, 1)$, then $f(x)$ is equal to

[Roorkee 1998]

- (a) $\log\left(\frac{1-x}{1+x}\right)$ (b) $\tan^{-1}\left(\frac{1-x}{1+x}\right)$ (c) $\log\left(\frac{2x}{1-x^2}\right)$ (d) $\tan^{-1}\left(\frac{1+x}{1-x}\right)$

If $f(x) = \frac{|x|}{x}$, $x \neq 0$, then the value of function

[BIT Mesra 1999]

- (a) 1 (b) 0 (c) -1 (d) Does not exist

If a function $g(x)$ is defined in $[-1, 1]$ and two vertices of an equilateral triangle are $(0, 0)$ and $(x, g(x))$ and its area is $\frac{\sqrt{3}}{4}$, then $g(x)$ equals [IIT 1989]

- (a) $\sqrt{1+x^2}$ (b) $-\sqrt{1+x^2}$ (c) $\sqrt{1-x^2}$ (d) None of these

If $f(x) = \frac{2^x + 2^{-x}}{2}$, then $f(x+y) \cdot f(x-y)$ is equal to

[Rajasthan PET 1998]

- (a) $\frac{1}{2}[f(x+y) + f(x-y)]$ (b) $\frac{1}{2}[f(2x) + f(2y)]$ (c) $\frac{1}{2}[f(x+y) \cdot f(x-y)]$ (d) None of these

$f(1) = 1$ and $f(n+1) = 2f(n) + 1$ if $n \geq 1$, then $f(n)$ is

[Karnataka CET 1994; IIT 1995]

- (a) 2^{n+1} (b) 2^n (c) $2^n - 1$ (d) $2^{n-1} - 1$

If $2f(x) - 3f(1/x) = x^2$, $x \neq 0$, then $f(2)$ is equal to

[IIT 1991]

- (a) $5/2$ (b) $-7/4$ (c) -1 (d) None of these

If $f(x) \neq x-1$, then correct statement is

[IIT 1983]

- (a) $f(x^2) = [f(x)]^2$ (b) $f(|x|) \neq f(x)$ (c) $f(x+y) = f(x) + f(y)$ (d) None of these

Domain of Function

Basic Level

The domain of the function $f(x) = \sqrt{\log_{0.5} x}$ is

[Roorkee 1990]

- (a) $(0, 1]$ (b) $(0, \infty)$ (c) $(0.5, \infty)$ (d) $[1, \infty)$

The domain of definition of the real function $f(x) = \sqrt{\log_{12} x^2}$ of the real variable x is

- (a) $x > 0$ (b) $|x| \geq 1$ (c) $|x| \geq 4$ (d) $x \geq 4$

The natural domain of the real valued function defined by $f(x) = \sqrt{x^2 - 1} + \sqrt{x^2 + 1}$ [SCRA 1996]

- (a) $1 < x < \infty$ (b) $-\infty < x < \infty$ (c) $-\infty < x < -1$ (d) $(-\infty, \infty) - (-1, 1)$

The domain of the function $y = \sqrt{\frac{1}{x} - 1}$ is, [AMU 2000]

- (a) $x \leq 1$ (b) $0 \leq x \leq 1$ (c) $0 \leq x < 1$ (d) $0 < x \leq 1$

Domain of $f(x) = \log |\log x|$ is [Pb. CET 1998; DCE 2002]

- (a) $(0, \infty)$ (b) $(1, \infty)$ (c) $(0, 1) \cup (1, \infty)$ (d) $(-\infty, 1)$

Domain of function $f(x) = \left[\log_{10} \left(\frac{5x - x^2}{4} \right) \right]^{1/2}$ is [UPSEAT 2001]

- (a) $-\infty < x < \infty$ (b) $1 \leq x \leq 4$ (c) $4 \leq x \leq 16$ (d) $-1 \leq x \leq 1$

Domain of the function $\sin^{-1} \left[\log_2 \left(\frac{x^2}{2} \right) \right]$ is [MP PET 1998]

- (a) $[1, 2]$ (b) $[-1, 2]$ (c) $[-2, 2] - (-1, 1)$ (d) $[-2, 2] - \{ \}$

The domain of the function $f(x) = \frac{\sqrt{4 - x^2}}{\sin^{-1}(2 - x)}$ is

- (a) $[0, 2]$ (b) $[0, 2)$ (c) $[1, 2)$ (d) $[1, 2]$

The domain of the function $f(x) = \log(\sqrt{x - 4} + \sqrt{6 - x})$ is [Rajasthan PET 2001]

- (a) $[4, \infty)$ (b) $(-\infty, 6]$ (c) $[4, 6]$ (d) None of these

Advance

The largest set of real values of x for which $f(x) = \sqrt{(x+2)(5-x)} - \frac{1}{\sqrt{x^2 - 4}}$ is a real function

- (a) $[1, 2] \cup (2, 5]$ (b) $(2, 5]$ (c) $[3, 4]$ (d) None of these

The domain of the function $f(x) = \frac{1}{\log_{10}(1-x)} + \sqrt{x+2}$ is [DCE 2000]

- (a) $] -3, -2.5[\cup] -2.5, -2[$ (b) $[-2, 0[\cup] 0, 1[$
(c) $] 0, 1[$ (d) None of these

The domain of the function $f(x) = \log_e(x - [x])$, where $[.]$ denotes the greatest integer function, is

- (a) R (b) $R - Z$ (c) $(0, +\infty)$ (d) None of these

The domain of the function $f(x) = \frac{\sin^{-1}(3-x)}{\ln(|x| - 2)}$ is [Orissa JEE 2002]

- (a) $[2, 4]$ (b) $(2, 3) \cup (3, 4]$ (c) $[2, \infty)$ (d) $(-\infty, -3) \cup [2, \infty)$

Domain of the function $f(x) = \sin^{-1}(1 + 3x + 2x^2)$ is [Roorkee 2000]

- (a) $(-\infty, \infty)$ (b) $(-1, 1)$ (c) $\left[-\frac{3}{2}, 0 \right]$ (d) $\left(-\infty, -\frac{1}{2} \right) \cup (2, \infty)$

Domain of the function $\sin \ln \left(\frac{\sqrt{4-x^2}}{1-x} \right)$ [IIT 1985; Rajasthan PET 2003]

- (a) $[-2, 1]$ (b) $(-2, 1)$ (c) $[-2, 1)$ (d) $(-2, 1]$

Domain of the function $f(x) = \sqrt{\log_{0.5}(3x-8) - \log_{0.5}(x^2+4)}$ is [AMU 1999]

- (a) $\left(\frac{8}{3}, \infty\right)$ (b) $\left(-\infty, \frac{8}{3}\right)$ (c) $(-\infty, \infty)$ (d) $(0, \infty)$

The domain of $f(x) = \frac{1}{\sqrt{|\cos x| + \cos x}}$ is

- (a) $[-2n\pi, 2n\pi]$ (b) $(2n\pi, 2n+1\pi)$ (c) $\left(\frac{(4n+1)\pi}{2}, \frac{(4n+3)\pi}{2}\right)$ (d) $\left(\frac{(4n-1)\pi}{2}, \frac{(4n+1)\pi}{2}\right)$

The domain of $f(x) = \sin^{-1}\left(\frac{1+x^2}{2x}\right) + \sqrt{1-x^2}$ is

- (a) $\{1\}$ (b) $(-1, 1)$ (c) $\{1, -1\}$ (d) None of these

The domain of the function $f(x) = \sqrt{\log\left(\frac{1}{|\sin x|}\right)}$ is

[Rajasthan PET 2001]

- (a) $R - \{-\pi, \pi\}$ (b) $R - \{n\pi | n \in \mathbb{Z}\}$ (c) $R - \{2n\pi | n \in \mathbb{Z}\}$ (d) $(-\infty, \infty)$

The domain of the function $f(x) = {}^{16-x}C_{2x-1} + {}^{20-3x}P_{4x-5}$, where the symbols have their usual meanings, is the set

[AMU 2002]

- (a) $\{2, 3\}$ (b) $\{2, 3, 4\}$ (c) $\{1, 2, 3, 4\}$ (d) $\{1, 2, 3, 4, 5\}$

Domain of the function $f(x) = \sin^{-1}\{1 + e^x\}^{-1}$ is

[AMU 1999]

- (a) $(-\infty, \infty)$ (b) $[-1, 0]$ (c) $[0, 1]$ (d) $[-1, 1]$

If n is an integer then domain of the function $\sqrt{\sin 2x}$ is

[MP PET 2003]

- (a) $[n\pi - \frac{\pi}{2}, n\pi]$ (b) $\left[n\pi, n\pi + \frac{\pi}{2}\right]$ (c) $[(2n-1)\pi, 2n\pi]$ (d) $[2n\pi, (2n+1)\pi]$

Range of Function

Basic Level

If $A = \{-2, -1, 0, 1, 2\}$ and $f: A \rightarrow \mathbb{Z}, f(x) = x^2 + 1$, then the range of f is

[Rajasthan PET 1995]

- (a) $\{0, 1, 2, 5\}$ (b) $\{1, 2, 5\}$ (c) $\{-5, -2, 1, 2, 3\}$ (d) A

The range of the function $f: [0, 1] \rightarrow \mathbb{R}, f(x) = x^3 - x^2 + 4x + 2 \sin^{-1} x$ is

- (a) $[-\pi - 2, 0]$ (b) $[2, 3]$ (c) $[0, 4 + \pi]$ (d) $[0, 2 + \pi]$

The range of $f(x) = \cos(x/3)$ is

[Rajasthan PET 2002]

- (a) $[-1/3, 1/3]$ (b) $[-3, 3]$ (c) $[1/3, -1/3]$ (d) $[-1, 1]$

Range of $f(x) = \frac{x^2 + 34x - 71}{x^2 + 2x - 7}$ is

[Roorkee 1983]

- (a) $[5, 9]$ (b) $(-\infty, 5] \cup [9, \infty)$ (c) $(5, 9)$ (d) None of these

Range of the function $f(x) = \frac{x^2 - x + 1}{x^2 + x + 1}$

[Karnataka CET 1993]

- (a) $\mathbb{R}$ (b) $[3, \infty)$ (c) $\left[\frac{1}{3}, 3\right]$ (d) None of these

Advance

The range of the function $f(x) = \cos[x]$, where $-\frac{\pi}{2} < x < \frac{\pi}{2}$ is

[Karnataka CET 1994]

- (a) $\{-1, 1, 0\}$ (b) $\{\cos 1, 1, \cos 2\}$ (c) $\{\cos 1, -\cos 1, 1\}$ (d) None of these

The range of the function $f(x) = |x-1| + |x-2|$, $-1 \leq x \leq 3$ is

- (a) [1, 3] (b) [1, 5] (c) [3, 5] (d) None of these

Let $f(x) = (1+b^2)x^2 + 2bx + 1$ and $m(b)$ the minimum value of $f(x)$ for a given b . As b varies, the range of $m(b)$ is

[IIT Screening 2001]

- (a) [0, 1] (b) $\left[0, \frac{1}{2}\right]$ (c) $\left[\frac{1}{2}, 1\right]$ (d) (0, 1]

Kind of Functions

Basic Level

Which of the following functions defined from R to R is onto

[Rajasthan PET 1985, 86]

- (a) $f(x) = |x|$ (b) $f(x) = e^{-x}$ (c) $f(x) = x^3$ (d) $f(x) = \sin x$

The number of bijective function from set A to itself when A contains 106 elements is

[EAMCET 1994]

- (a) 106 (b) $(106)^2$ (c) $106!$ (d) 2^{106}

If A contains 3 elements and B contains 4 elements, then the number of all one – one functions defined from A to B is

[EAMCET 1992; UPSEAT 2001]

- (a) 144 (b) 12 (c) 24 (d) 64

If $A = \{a, b\}$, then total number of functions which can be defined from A to A is

- (a) 2 (b) 3 (c) 4 (d) 1

Function $f: R \rightarrow R$, $f(x) = x^3 + 7$ is

[Rajasthan PET 1984]

- (a) One – one onto (b) One – one into (c) Many – one onto (d) Many – one into

Which of the following functions from R to R is into

[Rajasthan PET 1984]

- (a) x^5 (b) $3x - 7$ (c) x^3 (d) $\sin x$

Function $f: R \rightarrow R$, $f(x) = x^2$ is

[IIT 1970; MP PET 1997]

- (a) One – one but not onto (b) Onto but not one- one (c) Neither one-one nor onto (d) One- one onto

If $A = R - \{3\}$, $B = R - \{1\}$ and $f: A \rightarrow B$, $f(x) = \frac{x-2}{x-3}$, then f is

- (a) One-one (b) Onto (c) One-one onto (d) Many-one into

Advance

Let $f(x) = \frac{x^2 - 4}{x^2 + 4}$ for $|x| > 2$, then the function $f: (-\infty, -2] \cup [2, \infty) \rightarrow (-1, 1)$ is

[Orissa JEE 2002]

- (a) One-one into (b) One-one onto (c) Many one into (d) Many one onto

Let the function $f: R \rightarrow R$ be defined by $f(x) = 2x + \sin x$, $x \in R$. Then f is

[IIT Screening 2002]

- (a) One-to-one and onto (b) One-to-one but not onto
(c) Onto but not one-to-one (d) Neither one-to-one nor onto

function $f: R \rightarrow R$, $f(x) = x|x|$ is

[Rajasthan PET 1991, 98]

- (a) One – one but not onto (b) Onto but not one – one
(c) One – one onto (d) Neither one – one nor onto

If for two function f and g ; gof is a bijection, then correct statement is

[Haryana CEE 1998]

- (a) Both g and f must be bijections (b) g must be a bijection

(c) f must be a bijection

(d) Neither of them may be a bijection

If $f: [0, \infty) \rightarrow [0, \infty)$ and $f(x) = \frac{x}{1+x}$, then f is

[IIT Screening 2003]

(a) One - one and onto

(b) One - one but not onto

(c) Onto but not one - one

(d) Neither one - one nor onto

The number of all onto functions which can be defined from $A = \{1, 2, 3, \dots, n\}$, $n \geq 2$ to $B = \{a, b\}$ is

[IIT Screening 1992]

(a) ${}^n P_2$

(b) $2^n - 2$

(c) $2^n - 1$

(d) None of these

If $1+2x$ is a function having $\left(\frac{-\pi}{2}, \frac{\pi}{2}\right)$ as domain and $(-\infty, \infty)$ as co-domain, then it is

[IIT 1992]

(a) Onto but not one - one

(b) One - one but not onto

(c) One - one and onto

(d) Neither one - one nor onto

If $A = \{x \mid -1 \leq x \leq 1\} = B$ and $f: A \rightarrow B$, $f(x) = \sin \pi x$, then f is

(a) One - one

(b) Onto

(c) One - one onto

(d) Many one into

If the real-valued function $f(x) = px + \sin x$ is a bijective function then the set of possible values of $p \in \mathbb{R}$ is

(a) $\mathbb{R} - \{0\}$

(b) $\mathbb{R}$

(c) $(0, +\infty)$

(d) None of these

Even/Odd Functions

Basic Level

The function $f(x) = x \cos x$ is

(a) Even function

(b) Odd function

(c) Neither even nor odd

(d) Periodic function

A function whose graph is symmetrical about the y-axis is given by

(a) $f(x) = \log_e(x + \sqrt{x^2 + 1})$

(b) $f(x+y) = f(x) + f(y)$ for all $x, y \in \mathbb{R}$

(c) $f(x) = \cos x + \sin x$

(d) None of these

Let $f(x+y) = f(x) + f(y)$ for all $x, y \in \mathbb{R}$. Then

(a) $f(x)$ is an even function

(b) $f(x)$ is an odd function

(c) $f(0) = 0$

(d) $f(n) = nf(1), n \in \mathbb{N}$

If $f(x)$ is an odd function then

(a) $\frac{f(-x) + f(x)}{2}$ is an even function

(b) $[|f(x)| + 1]$ is even, where $[x]$ = the greatest integer $\leq x$

(c) $\frac{f(x) - f(-x)}{2}$ is neither even nor odd

(d) None of these

Advance

If $f(x)$ and $g(x)$ are two functions of x such that $f(x) + g(x) = e^x$ and $f(x) - g(x) = e^{-x}$ then

(a) $f(x)$ is an odd function

(b) $g(x)$ is an odd function

(c) $f(x)$ is an even function

(d) $g(x)$ is an even function

If $f(x) = \begin{cases} x^2 \sin \frac{\pi x}{2}, & |x| < 1 \\ |x| |x|, & |x| \geq 1 \end{cases}$ then $f(x)$ is

(a) An even function

(b) An odd function

(c) A periodic function

(d) None of these

Which of the following is an even function? Here $[.]$ denotes the greatest integer function and f is any function

(a) $[x] - x$

(b) $f(x) - f(-x)$

(c) $e^{3-2x} \cdot \tan^2 x$

(d) $f(x) + f(-x)$

Periodic Function

Basic Level

The period of $|\cos x|$ is

[Rajasthan PET 1998]

- (a) 2π (b) π (c) $\frac{\pi}{2}$ (d) $\frac{3\pi}{2}$

The period of the function $\sin\left(\frac{\pi x}{2}\right) + \cos\left(\frac{\pi x}{2}\right)$ is

[EAMCET 1990]

- (a) 4 (b) 6 (c) 12 (d) 24

If $f(x)$ is a periodic function of the period T , then $f(ax + b)$ where $a > 0$, is a periodic function of the period

[AMU 2000]

- (a) T/b (b) aT (c) bT (d) T/a

The period of the function $f(x) = \sin\left(\frac{2x+3}{6\pi}\right)$ is

- (a) 2π (b) 6π (c) $6\pi^2$ (d) None of these

The period of the function $f(x) = 3 \sin \frac{\pi x}{3} + 4 \cos \frac{\pi x}{4}$ is

- (a) 6 (b) 24 (c) 8 (d) 2π

The period of the function $f(x) = |\sin x| + |\cos x|$ is

- (a) π (b) $\pi/2$ (c) 2π (d) None of these

Advance

Let $f(x) = \cos 3x + \sin \sqrt{3}x$. Then $f(x)$ is

- (a) A periodic function of period 2π (b) A periodic function of period $\sqrt{3}\pi$
(c) Not a periodic function (d) None of these

$f(x) = \cos \sqrt{x}$, correct statement is

[Haryana CEE 1998]

- (a) $f(x)$ is periodic & its period $= \sqrt{2}\pi$ (b) $f(x)$ is periodic & its period $= 4\pi^2$
(c) $f(x)$ is periodic & its period $= \sqrt{\pi}$ (d) $f(x)$ is not periodic

Composite Functions

Basic Level

If $f: R \rightarrow R$, $f(x) = \sin x$; $g: R \rightarrow R$, $g(x) = x^2$, then $(fog)(x)$ equals to

[UPSEAT 1987, 2000]

- (a) $\sin x^2$ (b) $\sin^2 x$ (c) $\sin x + x^2$ (d) $\sin \frac{x}{x^2}$

If $f(x) = (a - x^n)^{1/n}$, where $a > 0$ and n is a positive integer, then $f[f(x)] =$

[IIT 1983; UPSET 2001]

- (a) x^3 (b) x^2 (c) x (d) None of these

If $f(x) = \frac{x}{\sqrt{1+x^2}}$, then $fofof(x)$ is equal to

[Rajasthan PET 2000]

- (a) $\frac{x}{\sqrt{1+3x^2}}$ (b) $\frac{x}{\sqrt{1+2x^2}}$ (c) $\frac{x}{\sqrt{1+x^2}}$ (d) None of these

Let f and g be functions defined by $f(x) = \frac{x}{x+1}$, $g(x) = \frac{x}{1-x}$, then $(fog)(x)$ is

- (a) $\frac{1}{x}$ (b) $\frac{1}{x-1}$ (c) $x-1$ (d) x

If $f(x) = ax + b$ and $g(x) = cx + d$, then $f(g(x)) = g(f(x))$ is equivalent to

[UPSEAT 2001]

- (a) $f(a) = g(c)$ (b) $f(b) = g(b)$ (c) $f(d) = g(b)$ (d) $f(c) = g(a)$

Advance

If $f(x) = \sqrt{x-1}$ and $g(x) = \sin x$, then $(fog)(x)$ is equal to

[Roorkee 1992]

- (a) $\sin \sqrt{x-1}$ (b) $|\sin x/2 - \cos x/2|$ (c) $|\sin x - \cos x|$ (d) None of these

If f and g are two real valued function defined by $f(x) = e^x$ and $g(x) = 3x - 2$, then $(fog)^{-1}(x)$ is equal to

[Roorkee 1998]

- (a) $\log(3x - 2)$ (b) $\frac{2 + \log x}{3}$ (c) $\log\left(\frac{x+2}{3}\right)$ (d) None of these

If $f(x) = \frac{1}{1-x}$, $x \neq 0, 1$, then the graph of the function $y = f\{f(f(x))\}$, $x > 1$, is

- (a) A circle (b) An ellipse (c) A straight line (d) A pair of straight lines

If $f(x)$ is defined on $[0, 1]$ by the rule $f(x) = \begin{cases} x, & \text{if } x \text{ is rational} \\ 1-x, & \text{if } x \text{ is irrational} \end{cases}$. Then for all $x \in [0, 1]$, $f(f(x))$ is

- (a) Constant (b) $1+x$ (c) x (d) None of these

Inverse Function

Basic Level

$f: R \rightarrow R$ is a function defined by $f(x) = 10x - 7$. If $g = f^{-1}$, then $g(x) =$

[EAMCET 1993]

- (a) $\frac{1}{10x-7}$ (b) $\frac{1}{10x+7}$ (c) $\frac{x+7}{10}$ (d) $\frac{x-7}{10}$

If $y = f(x) = \frac{x+2}{x-1}$, then $x =$

[IIT 1984]

- (a) $f(y)$ (b) $2f(y)$ (c) $\frac{1}{f(y)}$ (d) None of these

Inverse of the function $y = 2x - 3$ is

[UPSEAT 2002]

- (a) $\frac{x+3}{2}$ (b) $\frac{x-3}{2}$ (c) $\frac{1}{2x-3}$ (d) None of these

Advance

The value of α for which the function $f(x) = 1 + \alpha x$, $\alpha \neq 0$ is inverse of itself will be

[IIT 1992]

- (a) -2 (b) -1 (c) 1 (d) 2

If $f: [1, +\infty) \rightarrow [2, +\infty)$ is given by $f(x) = x + \frac{1}{x}$ then f^{-1} equals

[IIT Screening 2001]

- (a) $\frac{x + \sqrt{x^2 - 4}}{2}$ (b) $\frac{x}{1+x^2}$ (c) $\frac{x - \sqrt{x^2 - 4}}{2}$ (d) $1 + \sqrt{x^2 - 4}$

The inverse of the function $f(x) = \frac{10^x - 10^{-x}}{10^x + 10^{-x}}$ is

[Rajasthan PET 2001]

- (a) $\log_{10}(2-x)$ (b) $\frac{1}{2} \log_{10}\left(\frac{1+x}{1-x}\right)$ (c) $\frac{1}{2} \log_{10}(2x-1)$ (d) $\frac{1}{4} \log\left(\frac{2x}{2-x}\right)$

The inverse of the function $f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} + 2$ is given by

[Haryana CEE 1996]

- (a) $\log_e\left(\frac{x-2}{x-1}\right)^{\frac{1}{2}}$ (b) $\log_e\left(\frac{x-1}{3-x}\right)^{\frac{1}{2}}$ (c) $\log_e\left(\frac{x}{2-x}\right)^{\frac{1}{2}}$ (d) $\log_e\left(\frac{x-1}{x+1}\right)^{-2}$

Answer Sheet

Assignment (Basic & Advance Level)

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
c	a	a	c	a	b	c	b	b	d	b	c	d	a	d	c	b	c	b	d
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
a	b	d	d	c	b	c	c	c	b	b	b	b	c	b	a	d	c	b	a
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
a	b	b	c	d	b	c	b	b	d	c	c	c	c	a	d	c	c	c	a
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
c	a	b	b	b	b	d	b	d	b,c,d	a,b	b,c	b	d	b	a	d	c	b	b
81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98		
c	d	a	c	a	d	c	b	b	c	c	c	a	a	b	a	b	b		