

DIFFERENTIATION

SYNOPSIS

- If $y = f(x)$ is differentiable at any point 'x' then its derivative is $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ and it is called the first derivative of $f(x)$.
A function f is said to be derivable at $x=a$ if $\lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$ exists. The limit is called the derivative of f at $x=a$ and is denoted by $f'(a)$.
i.e., $\lim_{x \rightarrow a^+} \frac{f(x) - f(a)}{x - a} = \lim_{x \rightarrow a^-} \frac{f(x) - f(a)}{x - a}$ then the limit value denoted by $f'(a)$ is called derivative of $f(x)$ at $x=a$.
- Let f be a function defined on $[a, b]$. Then f is said to be differentiable on $[a, b]$, if
 - f is differentiable at 'c' i.e., $\lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c}$ where $c \in (a, b)$ exists
 - f is right differentiable at 'a' i.e., $\lim_{x \rightarrow a^+} \frac{f(x) - f(a)}{x - a}$ exists
 - f is left differentiable at 'b' i.e., $\lim_{x \rightarrow b^-} \frac{f(x) - f(b)}{x - b}$ exists.
- If $f(x), g(x)$ are two differentiable functions of 'x' then the linear combination of the two functions is also differentiable function of 'x'.
i.e., $\frac{d}{dx}(c_1 f(x) + c_2 g(x)) = c_1 \frac{d}{dx} f(x) + c_2 \frac{d}{dx} g(x)$ where c_1, c_2 are constants.
- PRODUCT RULE:** If $f(x), g(x)$ are two differentiable functions of 'x' then
 - $\frac{d}{dx}(f(x).g(x)) = g(x) \frac{d}{dx} f(x) + f(x) \frac{d}{dx} g(x)$
 - If $f(x), g(x), h(x)$ are three differentiable functions of 'x' then

$$\frac{d}{dx}(f(x).g(x).h(x)) = g(x).h(x) \frac{d}{dx} f(x) + f(x).h(x) \frac{d}{dx} g(x) + f(x).g(x) \frac{d}{dx} h(x)$$
- QUOTIENT RULE:** If $f(x), g(x)$ are two differentiable functions of 'x' then

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{g(x) \frac{d}{dx} f(x) - f(x) \frac{d}{dx} g(x)}{(g(x))^2}$$
- PARAMETRIC DIFFERENTIATION:** If $x=f(t)$ and $y=g(t)$ are the parametric equations of a curve then

$$\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = \frac{g'(t)}{f'(t)}$$

- $\frac{d}{dx}(x^n) = n.x^{n-1}$
- $\frac{d}{dx}(\sin x) = \cos x$
- $\frac{d}{dx}(\cos x) = -\sin x$
- $\frac{d}{dx}(\tan x) = \sec^2 x$
- $\frac{d}{dx}(\cot x) = -\operatorname{cosec}^2 x$
- $\frac{d}{dx}(\sec x) = \sec x \cdot \tan x$
- $\frac{d}{dx}(\operatorname{cosec} x) = -\operatorname{cosec} x \cdot \cot x$
- $\frac{d}{dx}(e^x) = e^x$
- $\frac{d}{dx}(a^x) = a^x \cdot \log a$
- $\frac{d}{dx}(\log x) = \frac{1}{x}$
- $\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}} \quad x \in (-1, 1)$
- $\frac{d}{dx}(\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}} \quad x \in (-1, 1)$
- $\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2} \quad x \in R$
- $\frac{d}{dx}(\cot^{-1} x) = \frac{-1}{1+x^2} \quad x \in R$
- $\frac{d}{dx}(\sec^{-1} x) = \frac{1}{|x| \cdot \sqrt{x^2 - 1}} \quad x < -1 \text{ or } x > 1$
- $\frac{d}{dx}(\operatorname{cosec}^{-1} x) = \frac{-1}{|x| \cdot \sqrt{x^2 - 1}} \quad x < -1 \text{ or } x > 1$
- $\frac{d}{dx}(\sinh x) = \cosh x$
- $\frac{d}{dx}(\cosh x) = \sinh x$
- $\frac{d}{dx}(\tanh x) = \operatorname{sech}^2 x$
- $\frac{d}{dx}(\coth x) = -\operatorname{cosech}^2 x$
- $\frac{d}{dx}(\sec hx) = -\sec hx \tanh x$

- $\frac{d}{dx}(\operatorname{cosech} x) = -\operatorname{cosech} x \cdot \coth x$
- $\frac{d}{dx}(\sinh^{-1} x) = \frac{1}{\sqrt{1+x^2}}$
- $\frac{d}{dx}(\cosh^{-1} x) = \frac{1}{\sqrt{x^2-1}}$
- $\frac{d}{dx}(\tanh^{-1} x) = \frac{1}{1-x^2}$ for $x \in (-1, 1)$
- $\frac{d}{dx}(\coth^{-1} x) = \frac{1}{1-x^2}$ for $x \in (-\infty, -1) \cup (1, \infty)$
- $\frac{d}{dx}(\operatorname{sech}^{-1} x) = \frac{-1}{x\sqrt{1-x^2}}$ for $x \in (0, 1)$
- $\frac{d}{dx}(\operatorname{cosec} h^{-1} x) = \frac{-1}{|x| \cdot \sqrt{1+x^2}}$
for $x \in (-\infty, 0) \cup (0, \infty)$
- If $f(x, y) = 0$ then $\frac{dy}{dx} = \frac{-f_x}{f_y}$
where f_x, f_y are the partial derivatives.
- If $y = \sqrt{f(x)} + \sqrt{f(x)} + \sqrt{f(x)} + \dots \dots \dots \text{to } \infty$ then
 $\frac{dy}{dx} = \frac{f^1(x)}{(2y-1)}$
- Let $f(x), g(x)$ be the two differentiable functions of 'x'
and if $y = f(x)^{g(x)}$ then
 $\frac{dy}{dx} = y \left(g^1(x) \log f(x) + g(x) \frac{f^1(x)}{f(x)} \right)$
- If $y = f(x) + \frac{1}{y}$ then $\frac{dy}{dx} = \frac{y^2 f^1(x)}{y^2 + 1}$
- If $f(x+y) = f(x) \cdot f(y) \quad \forall \quad x, y \in \mathbf{R}$ and $f(x) \neq 0$ then
 $f^1(x) = f^1(0) \cdot f(x)$.
- $\frac{d}{dx} \left(\frac{ax+b}{cx+d} \right) = \frac{ad-bc}{(cx+d)^2}$
- $\frac{d}{dx} \left(\frac{af(x)+b}{cf(x)+d} \right) = \frac{(ad-bc)f^1(x)}{\{cf(x)+d\}^2}$
- $\frac{d}{dx} \{ \log_e f(x) \} = \frac{f^1(x)}{f(x)}$
- $\frac{d}{dx} \{ \sqrt{f(x)} \} = \frac{f^1(x)}{2\sqrt{f(x)}}$

- $\frac{d}{dx} \left\{ \frac{1}{f(x)} \right\} = \frac{-f^1(x)}{(f(x))^2}$
- $\frac{d}{dx} \{ (f(x))^n \} = n \{ f(x) \}^{n-1} \cdot f^1(x)$
- If $y = \tan^{-1} \left(\frac{f(x) \pm g(x)}{1 \pm f(x) \cdot g(x)} \right)$ then
 $\frac{dy}{dx} = \frac{f^1(x)}{1 + \{f(x)\}^2} \pm \frac{g^1(x)}{1 + \{g(x)\}^2}$
- If $y = (g \circ f)(x)$ then $\frac{dy}{dx} = g^1(f(x)) \cdot f^1(x)$
- If $y = f(x)$ and $z = g(x)$ then $\frac{dy}{dz} = \frac{f^1(x)}{g^1(x)}$
- If $y = f(x)^y$ then $\frac{dy}{dx} = \frac{y^2 \cdot f^1(x)}{f(x) \{ 1 - y \log_e f(x) \}}$
- While differentiating the given function using trigonometric transformation, observe the following points.
- If the function involve the term $\sqrt{a^2 - x^2}$, then put $x = a \sin \theta$ or $x = a \cos \theta$
- If the function involve the term $\sqrt{a^2 + x^2}$, then put $x = a \tan \theta$ or $x = a \cot \theta$
- If the function involve the term $\sqrt{x^2 - a^2}$, then put $x = a \sec \theta$ or $x = a \operatorname{cosec} \theta$
- If the function involve the term
 $\sqrt{\frac{a-x}{a+x}}$ or $\sqrt{\frac{a+x}{a-x}}$, then put $x = a \cos \theta$ or $x = a \cos 2\theta$
- All the above substitutions are also true if $a = 1$
- If $f(x) = |x|$, then $f^1(0)$ does not exist.
 $\frac{d|x|}{dx} = \frac{|x|}{x}$, if $x \neq 0$
- If $f(x) = |x|$, $f(x)$ is continuous at $x = 0$ but not differentiable at $x = 0$.
- If $f(x) = x \sin \frac{1}{x}$, $f(x)$ is continuous at $x = 0$ but not differentiable at $x = 0$
- If $f(x) = x \cos \frac{1}{x}$, $f(x)$ is continuous at $x = 0$ but not differentiable at $x = 0$.

**MULTIPLE CHOICE QUESTIONS
LEVEL - I**

1. $\lim_{h \rightarrow 0} \frac{\sqrt{x+h} - \sqrt{x}}{h} =$
 1. $\sqrt{x}$ 2. $\frac{1}{2\sqrt{x}}$ 3. $2\sqrt{x}$ 4. $\frac{1}{\sqrt{x}}$
2. $\frac{d}{dx} \left\{ x + \frac{1}{x} \right\} =$
 1. $1 - \frac{1}{x^2}$ 2. $1 + \frac{1}{x^2}$ 3. $\frac{1}{x^2} - 1$ 4. $1 - \frac{1}{x}$
3. $\frac{d}{dx} \left\{ \frac{3x-5}{2x+3} \right\} =$
 1. $\frac{19}{(2x+3)^2}$ 2. $\frac{14}{(2x+3)^2}$
 3. $\frac{-19}{(2x+3)^2}$ 4. $\frac{-1}{(2x+3)^2}$
4. If $y = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$ to ∞ then $\frac{dy}{dx} =$
 1. x 2. 0 3. y 4. $\frac{1}{y}$
5. If $ax^2 + 2hxy + by^2 = 0$ then $\frac{dy}{dx} =$
 1. $-\left(\frac{ax+hy}{hx+by}\right)$ 2. $\left(\frac{ax+hy}{hx+by}\right)$
 3. $-(ax+hy)(hx+by)$ 4. $(ax+hy)(hx+by)$
6. If $x^2 + y^2 + 2gx + 2fy + c = 0$ then $\frac{dy}{dx} =$
 1. $-\left(\frac{g+x}{f+y}\right)$ 2. $\frac{f+y}{g+x}$ 3. $\frac{xy+g}{f+x^2}$ 4. $\frac{x+g}{y+g}$
7. If $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$ then $\frac{dy}{dx} =$
 1. $\frac{-(ax+hy+g)}{(hx+by+f)}$ 2. $\frac{-(hx+by+f)}{(ax+hy+g)}$
 3. $\frac{(ax+hy+g)}{(hx+by+f)}$ 4. $\frac{(hx+by+f)}{(ax+hy+g)}$
8. If $\sin^2 mx + \cos^2 ny = a^2$ then $\frac{dy}{dx} =$
 1. $\frac{m \cdot \sin 2mx}{n \cdot \sin 2ny}$ 2. $\frac{m \cdot \sin mx}{n \cdot \sin nx}$
 3. $\frac{-m \cdot \cos 2mx}{n \cdot \cos 2nx}$ 4. $\frac{n \cdot \sin 2mx}{m \cdot \sin 2nx}$

9. $\lim_{h \rightarrow 0} \frac{\sin(3x+3h) - \sin 3x}{h} =$
 1. $3\cos 3x$ 2. $\frac{3}{2} \cos 3x$ 3. $-3\cos 3x$ 4. 0
10. $\lim_{h \rightarrow 0} \frac{\tan \sqrt{x+h} - \tan \sqrt{x}}{h} =$
 1. $\sec^2 \sqrt{x}$ 2. $\frac{\sec^2 \sqrt{x}}{2\sqrt{x}}$ 3. $\frac{-\tan \sqrt{x}}{2\sqrt{x}}$ 4. $\frac{\tan \sqrt{x}}{2\sqrt{x}}$
11. $\frac{d}{dx} \left\{ \frac{a-b \cos x}{a+b \cos x} \right\} =$
 1. $\frac{2ab \cos x}{(a+b \cos x)^2}$ 2. $\frac{2ab \sin x}{(a+b \cos x)^2}$
 3. $\frac{-2ab \cos x}{(a+b \cos x)^2}$ 4. $\frac{-2ab \sin x}{(a+b \cos x)^2}$
12. $\frac{d}{dx} (3 \sin x^0) =$
 1. $3 \cos x^0$ 2. $\frac{3\pi}{180} \sin x^0$
 3. $3\pi \sin x^0$ 4. $\frac{\pi}{60} \cos x^0$
13. If $y = \sec(x^0 + 30^0)$ then $\frac{dy}{dx} =$
 1. $\frac{\pi}{60} \sec(x^0 + 30^0) \cdot \tan(x^0 + 30^0)$
 2. $\frac{\pi}{180} \sec(x^0 + 30^0) \tan(x^0 + 30^0)$
 3. $\frac{-\pi}{60} \sec^2(x^0 + 30^0) \cdot \tan(x^0 + 30^0)$
 4. $\frac{-\pi}{180} \sec(x^0 + 30^0) \tan(x^0 + 30^0)$
14. If $x+y = \sin(x+y)$ then $\frac{dy}{dx} =$
 1. $\frac{1}{2}$ 2. 0 3. -1 4. $\frac{1}{3}$
15. $\frac{d}{dx} \left\{ \sin^{-1} \frac{x}{a} \right\} =$
 1. $\frac{1}{\sqrt{a^2 - x^2}}$ 2. $\frac{1}{\sqrt{a^2 - x^2}}$
 3. $\frac{x}{\sqrt{a^2 - x^2}}$ 4. $\frac{-1}{\sqrt{a^2 - x^2}}$

16. If $y = \tan^{-1}\left(\cot\left(\frac{\pi}{2} - x\right)\right)$ then $\frac{dy}{dx} =$

1. 1 2. -1 3. 0 4. $\frac{1}{2}$

17. $\frac{d}{dx} [\log(\cosh x)] =$

1. $\sinh x$ 2. $\coth x$ 3. $\tanh x$ 4. $-\coth x$

18. $\frac{d}{dx} [\sinh^{-1} 3x] =$

1. $\frac{3}{\sqrt{1+9x^2}}$ 2. $\frac{3}{\sqrt{1-9x^2}}$ 3. $\frac{1}{\sqrt{1+9x^2}}$ 4. $\frac{1}{\sqrt{1-9x^2}}$

19. $\frac{d}{dx} \left(\cosh^{-1} \frac{x}{2} \right) =$

1. $\frac{1}{\sqrt{x^2+4}}$ 2. $\frac{1}{\sqrt{x^2-4}}$ 3. $\frac{-1}{\sqrt{x^2+4}}$ 4. $\frac{-1}{\sqrt{x^2-4}}$

20. If $f(x) = \frac{a^x}{x^a}$ then $f'(a) =$

- 1) $\log a - 1$ 2) $\log a - a$
3) $a \log a - a$ 4) $a \log a + a$

21. $\lim_{h \rightarrow 0} \frac{e^{2x+2h} - e^{2x}}{h} =$

1. e^{2x} 2. $-e^{2x}$ 3. $2e^{2x}$ 4. $\frac{-1}{2} e^{2x}$

22. $\frac{d}{dx} \left\{ e^{\log \sqrt{1+\cot^2 x}} \right\} =$

1. $\operatorname{cosec} x \cot x$ 2. $-\operatorname{cosec} x \cdot \cot x$
3. $\operatorname{cosec}^2 x \cdot \cot x$ 4. 0

23. If $y = 3^{2 \log x + 7}$ then $\frac{dy}{dx} =$

1. $\frac{2}{x} \log 3$ 2. $\frac{2y \cdot \log 3}{x}$
3. $2xy$ 4. $\frac{-2 \log 3}{x}$

24. If $y = a^x \cdot e^x$ then $\frac{dy}{dx} =$

1. $y(1+\log a)$ 2. $y^2(1+\log a)$
3. $-y(1+\log a)$ 4. $y(1-\log a)$

25. $\frac{d}{dx} \left\{ e^{ax} \cdot \sin(bx+c) \right\} =$

1. $e^{ax} \{ a \sin(bx+c) + b \cos(bx+c) \}$
2. $e^{ax} \{ a \cos(bx+c) + b \sin(bx+c) \}$
3. $e^{ax} \{ a \sin(bx+c) - b \cos(bx+c) \}$
4. $e^{ax} \{ a \cos(bx+c) - b \sin(bx+c) \}$

26. If $x = at^2$, $y = 2at$ then $\frac{dy}{dx} =$

1. $\frac{1}{t}$ 2. t 3. t^2 4. 1

27. If $x = \tan t$, $y = \cos t$, $0 < t < \frac{\pi}{2}$ then $\frac{dy}{dx} =$

1. xy^2 2. $-x^2y$ 3. xy 4. $-xy^3$

28. If $|x| < 1$, then

$$\frac{d}{dx} \left[1 + \frac{p}{q}x + \frac{p(p+q)}{2} \left(\frac{x}{q} \right)^2 + \frac{p(p+q)(p+2q)}{3} \left(\frac{x}{q} \right)^3 + \dots \infty \right] =$$

1. $\frac{p}{q} \frac{1}{(1-x)^{\frac{p}{q}+1}}$ 2. $\frac{p}{q} \frac{1}{(1-x)^{\frac{p}{q}}}$
3. $(1-x)^{-pq-1}$ 4. $(1-x)^{pq+1}$

29. The derivative of $\tan^{-1} \left(\frac{\sqrt{1+x^2}-1}{x} \right)$ w.r.t

$$\tan^{-1} \left(\frac{2x\sqrt{1-x^2}}{1-2x^2} \right) \text{ at } x = 0 \text{ is}$$

1. $1/4$ 2. $1/8$ 3. $1/2$ 4. 1

30. If $[x]$ denotes the greatest integer contained in x

then for $4 < x < 5$, $\frac{d}{dx} \{ [x] \} =$

1. $[x-4, 5]$ 2. $[x]$
3. 0 4. 1

31. If $f(x) = ax^2 + bx + c$ then $\lim_{x \rightarrow 5} \frac{f(x) - f(5)}{x - 5} =$

1. $5a + 5$ 2. $10a + 5$
3. $25a + 5b + b$ 4. $10a + b$

32. A differentiable function f is defined for all $x > 0$ as

$f(x) = 6x + 5$ then $f'(16)$ is equal to

1. 64 2. 16 3. 32 4. 6

33. If $\left(\frac{x}{a} \right)^n + \left(\frac{y}{b} \right)^n = 2$ then $\frac{dy}{dx}$ at (a, b) is

1. a/b 2. $-a/b$ 3. b/a 4. $-b/a$

34. If $f(x)$ is an odd differentiable function defined

on $(-\infty, \infty)$ such that $f'(3) = 2$ then $f'(-3) =$

1. 0 2. 1 3. 2 4. 4

KEY

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|-------|-------|-------|-------|-------|
| 1. 2 | 2. 1 | 3. 1 | 4. 3 | 5. 1 |
| 6. 1 | 7. 1 | 8. 1 | 9. 1 | 10. 2 |
| 11. 2 | 12. 4 | 13. 2 | 14. 3 | 15. 2 |
| 16. 1 | 17. 3 | 18. 1 | 19. 2 | 20. 1 |
| 21. 3 | 22. 2 | 23. 2 | 24. 1 | 25. 1 |
| 26. 1 | 27. 4 | 28. 1 | 29. 1 | 30. 3 |
| 31. 4 | 32. 4 | 33. 4 | 34. 3 | |

LEVEL - II

1. $\frac{d}{dx} \left\{ \frac{x^2 - x + 1}{x^2 + x + 1} \right\} =$

1. $\frac{2(x^2 - 1)}{(x^2 + x + 1)^2}$

2. $\frac{2(x^2 + 1)}{(x^2 + x + 1)^2}$

3. $\frac{2(1 - x^2)}{(x^2 + x + 1)^2}$

4. $\frac{-2(1 + x^2)}{(x^2 + x + 1)^2}$

2. If $y = \left(x + \sqrt{x^2 - a^2} \right)^n$ then $\left(x^2 - a^2 \right) \left(\frac{dy}{dx} \right)^2 =$

1. $n^2 y$

2. $-n^2 y$

3. ny^2

4. $n^2 y^2$

3. If $y = \frac{1}{\sqrt{x^2 + 4} + \sqrt{x^2 + 2}}$ then $\frac{dy}{dx} =$

1. $\frac{x}{2} \left[\frac{1}{\sqrt{x^2 + 4}} - \frac{1}{\sqrt{x^2 + 2}} \right]$

2. $\frac{x}{2} \left[\frac{1}{\sqrt{x^2 + 4}} + \frac{1}{\sqrt{x^2 + 2}} \right]$

3. $\frac{-x}{2} \left[\frac{1}{\sqrt{x^2 + 4}} + \frac{1}{\sqrt{x^2 + 2}} \right]$

4. $\frac{1}{2} \left[\frac{1}{\sqrt{x^2 + 4}} + \frac{1}{\sqrt{x^2 + 2}} \right]$

4. If $y^2 - 2x^2 = y$ then $\left(\frac{dy}{dx} \right)_{(1,-1)} =$

1. $-\frac{4}{3}$

2. $\frac{4}{3}$

3. $\frac{3}{4}$

4. $-\frac{3}{4}$

5. If $3x^2 + 4xy + 2y^2 + x - 8 = 0$ then $\left(\frac{dy}{dx} \right)_{(-1,3)} =$

1. $\frac{3}{8}$

2. $-\frac{7}{8}$

3. $\frac{5}{8}$

4. $-\frac{5}{8}$

6. If $(x+y)^2 = ax^2 + by^2$ then $\frac{dy}{dx} =$

1. $\frac{x(a+1)-y}{x+y(1-b)}$

2. $\frac{x(a-1)-y}{x+y(1-b)}$

3. $\frac{x(a+1)+y}{x+y(1-b)}$

4. $\frac{x(a+1)+y}{x+y(1+b)}$

7. If $xy = x + y$, then $\frac{dy}{dx} =$

1. $\frac{xy}{1-x}$

2. $\frac{y+1}{1-x}$

3. $\frac{y}{1-xy}$

4. $\frac{-1}{(x-1)^2}$

8. If $x^2 - y^2 = a(x - y)$ and $x \neq y$, then $\frac{dy}{dx} =$

1. 1

2. $\frac{1}{2}$

3. $\frac{1}{3}$

4. -1

9. $\frac{d}{dx} (4\cos^3 x^0 - 3\cos x^0) =$

1. $-\frac{\pi}{60} \sin 3x^0$

2. $\cos 3x^0$

3. $\tan 3x^0$

4. $\frac{\pi}{60} \sin 3x^0$

10. $\frac{d}{dx} \left(\sqrt{\sin \sqrt{x}} \right) =$

1. $\frac{\cos \sqrt{x}}{4\sqrt{x} \sin \sqrt{x}}$

2. $\frac{\sin \sqrt{x}}{4\sqrt{x} \cos \sqrt{x}}$

3. $\frac{-\cos \sqrt{x}}{4\sqrt{x} \sin \sqrt{x}}$

4. $\frac{-\tan \sqrt{x}}{4\sqrt{x} \cos \sqrt{x}}$

11. If $y = \sqrt{\frac{1 - \cos x}{1 + \cos x}}$ then $\frac{dy}{dx} =$

1. $\sec^2 \frac{x}{2}$

2. $x \sec \frac{x}{2}$

3. $x^2 \sec \frac{x}{2}$

4. $\frac{1}{2} \sec^2 \frac{x}{2}$

12. If $y = \sqrt{\frac{1 - \sin 2x}{1 + \sin 2x}}$ then $\left(\frac{dy}{dx} \right)_{x=0} =$

1. $\frac{1}{2}$

2. 1

3. -2

4. 2

13. If $y = \cos(1 - x^2)^2$ then $\frac{dy}{dx} =$

1. $4x(1 - x^2)\sin(1 - x^2)^2$

2. $4x(1 - x^2)\sin(1 - x^2)$

3. $-4x(1 - x^2)\sin(1 - x^2)^2$

4. $4x(1 + x^2)\sin(1 + x^2)$

14. If $y = \sin^5(3x + 1)$ then $\frac{dy}{dx} =$

1. $\sin^4(3x + 1)\cos^2(3x + 1)$

2. $15\sin^4(3x + 1)\cos(3x + 1)$

3. $15\sin^5(3x + 1)\cos(3x + 1)$

4. $-\sin^4(3x + 1)\cos 2(3x + 1)$

15. $\frac{d}{dx} (\sin^5 x \cdot \sin 5x) =$

1. $\sin^4 x \cdot \sin 5x$

2. $5\sin^4 x \cdot \sin 6x$

3. $5\sin^4 x \cdot \sin 5x$

4. $-5\sin^4 x \cdot \sin 6x$

16. If $y = \log_2 \log_3 \log_5 x$ then $\left(\frac{dy}{dx} \right)_{x=125} =$

1. $\frac{1}{125 \log_2 \log_3 \log_5}$

2. $\frac{1}{250 \log_2 \log_3 \log_5}$

3. $\frac{1}{375 \log_2 \log_3 \log_5}$

4. $\frac{1}{500 \log_2 \log_3 \log_5}$

17. $\frac{d}{dx} \{\sin^3 x \cdot \cos 3x\} =$
 1. $-3\sin^2 x \cdot \cos 4x$ 2. $3\sin^2 x \cdot \cos 4x$
 3. $-3\sin^3 x \cdot \cos 3x$ 4. $3\sin^3 x \cdot \cos 3x$
18. If $y = \sin^3 2x \cdot \cos^2 3x$ then $\frac{dy}{dx} =$
 1. $6\sin^2 2x \cdot \cos 3x$ 2. $6\sin^2 2x \cdot \cos 3x \cdot \cos 5x$
 3. $\sin^2 2x \cdot \cos 3x \cdot \cos 5x$ 4. $-6\sin^2 2x \cdot \cos 3x \cdot \cos 5x$
19. $\frac{d}{dx} (\sin \sqrt{2x-3}) =$
 1. $\frac{\cos \sqrt{2x-3}}{\sqrt{2x-3}}$ 2. $\frac{-\cos \sqrt{2x-3}}{2\sqrt{2x-3}}$
 3. $\sqrt{2x-3} \cos \sqrt{2x-3}$ 4. $\cos \sqrt{2x-3}$
20. If $\tan(x+y) + \tan(x-y) = 1$ then $\frac{dy}{dx} =$
 1. $\frac{\sec^2(x+y) + \sec^2(x-y)}{\sec^2(x+y) - \sec^2(x-y)}$
 2. $-\left[\frac{\sec^2(x+y) + \sec^2(x-y)}{\sec^2(x+y) - \sec^2(x-y)} \right]$
 3. $\frac{\sec^2(x+y) - \sec^2(x-y)}{\sec^2(x+y) + \sec^2(x-y)}$
 4. $\frac{1}{2(x^2 + y^2)}$
21. If $y \sin x = x + y$ then $\frac{dy}{dx}$ at $x=0$ is
 1. 1 2. -1 3. 0 4. 2
22. If $y = x \sin y$, then $\frac{dy}{dx} =$
 1. $\frac{1 - x \sin y}{\sin y}$ 2. $\frac{1 - x \sin y}{x \cos y}$
 3. $\frac{1 - \sin y}{x \cos y}$ 4. $\frac{\sin^2 y}{\sin y - y \cos y}$
23. If $\cos y = x \cdot \cos(a+y)$ then $\frac{dy}{dx} =$
 1. $\frac{\cos^2(a+y)}{\sin a}$ 2. $\frac{\cos^2(a+y)}{\cos a}$
 3. $\frac{\cos a}{\sin^2(a+y)}$ 4. $\frac{\cos(a+y)}{\sin a}$
24. If $y = \sqrt{\sec^2 x + \operatorname{cosec}^2 x}$ then $\frac{dy}{dx} =$
 1. $-4 \operatorname{cosec} 2x \cdot \cot 2x$ 2. $\sec 2x$
 3. $2 \operatorname{cosec} 2x \cdot \cot 2x$ 4. $2 \sec 2x$

25. If $y = \sqrt{\frac{\sec x - 1}{\sec x + 1}}$ then $\frac{dy}{dx} =$
 1. $\frac{1}{2} \sec^2 \frac{x}{2}$ 2. $\sec^2 \frac{x}{2}$ 3. $\frac{1}{2} \tan \frac{x}{2}$ 4. $\tan \frac{x}{2}$
26. $\frac{d}{dx} \left\{ \sin^{-1} x + \cos^{-1} \sqrt{1-x^2} \right\} =$
 1. $\frac{1}{\sqrt{1-x^2}}$ 2. $\frac{x}{\sqrt{1-x^2}}$ 3. $\frac{2}{\sqrt{1-x^2}}$ 4. $\frac{4}{\sqrt{1-x^2}}$
27. If $y = \sin^{-1} \sqrt{\frac{1-x}{2}}$ then $\frac{dy}{dx} =$
 1. $\frac{-1}{2\sqrt{1-x^2}}$ 2. $\frac{1}{2\sqrt{1-x^2}}$
 3. $\frac{1}{\sqrt{1-x^2}}$ 4. $\frac{-x}{\sqrt{1-x^2}}$
28. $\frac{d}{dx} \left\{ \sin^{-1} x + \sin^{-1} \sqrt{1-x^2} \right\} =$
 1. $\frac{1}{2}$ 2. $\frac{2}{\sqrt{1-x^2}}$ 3. $2\sqrt{1-x^2}$ 4. 0
29. If $y = \tan^{-1} \sqrt{\frac{1-\cos x}{1+\cos x}}$ then $\frac{dy}{dx} =$
 1. 1 2. -1 3. $\frac{-1}{2}$ 4. $\frac{1}{2}$
30. If $y = \tan^{-1} \left(\frac{\cos x}{1 + \sin x} \right)$ then $\frac{dy}{dx} =$
 1. 1 2. -1 3. $\frac{-1}{2}$ 4. $\frac{1}{3}$
31. If $y = \tan^{-1}(\sec x + \tan x)$ then $\frac{dy}{dx} =$
 1. 1 2. $\frac{1}{2}$ 3. -1 4. 0
32. If $y = \cot^{-1}(\operatorname{cosec} x - \cot x)$ then $\frac{dy}{dx} =$
 1. 1 2. $\frac{-1}{2}$ 3. -1 4. 0
33. If $y = \sin^{-1}(\cos x)$ then $\frac{dy}{dx} =$
 1. 1 2. -1 3. 0 4. 2
34. If $y = \cos^{-1} \sqrt{\frac{1+x}{2}}$ then $\frac{dy}{dx} =$
 1. $\frac{-1}{2\sqrt{1-x^2}}$ 2. $\frac{1}{2\sqrt{1-x^2}}$ 3. $\frac{1}{\sqrt{1-x^2}}$ 4. $\frac{-1}{\sqrt{1-x^2}}$

35. $\frac{d}{dx} \left\{ \frac{1}{2} \cot h \frac{x}{2} - \frac{1}{6} \cot h^3 \frac{x}{2} \right\} =$
 1. $-\frac{1}{4} \operatorname{cosec} h \frac{4x}{2}$ 2. $-1/4 \cot h^4 x/2$
 3. $1/4 \operatorname{cosec} h^4 x/2$ 4. $1/4 \cot h^4 x/2$

36. $\frac{d}{dx} \left\{ \cos^{-1} \left(\frac{1-x^2}{1+x^2} \right) \right\}$
 1. $\frac{2}{\sqrt{1-x^2}}$ 2. $\frac{-2}{\sqrt{1-x^2}}$ 3. $\frac{1}{\sqrt{1-x^2}}$ 4. $\frac{2}{1+x^2}$

37. $\frac{d}{dx} \left\{ \operatorname{cosec}^{-1} \frac{1}{2x\sqrt{1-x^2}} \right\} =$
 1. $\frac{1}{\sqrt{1-x^2}}$ 2. $\frac{2}{\sqrt{1-x^2}}$

38. $\frac{d}{dx} \left\{ \operatorname{Tan}^{-1} \frac{x}{1+x^2} + \operatorname{Tan}^{-1} \frac{1+x^2}{x} \right\} =$
 1. 0 2. 1 3. $\frac{1}{2}$ 4. 2

39. $\frac{d}{dx} \left\{ \operatorname{Tan}^{-1} \frac{\sqrt{x} + \sqrt{a}}{1 - \sqrt{ax}} \right\} =$
 1. $\frac{1}{2\sqrt{x}(1+x)}$ 2. $\frac{-1}{2\sqrt{x}(1+x)}$
 3. $\frac{2}{\sqrt{x}(1+x)}$ 4. $\frac{-2}{\sqrt{x}(1+x)}$

40. $\frac{d}{dx} \left\{ \sec^{-1} \frac{\sqrt{x}+1}{\sqrt{x}-1} + \sin^{-1} \frac{\sqrt{x}-1}{\sqrt{x}+1} \right\} =$
 1. -1 2. 0 3. 1 4. 2

41. If $y = \operatorname{Sin}^{-1} \sqrt{\frac{x-a}{b-a}}$, $a < x < b$ then $\frac{dy}{dx} =$
 1. $\frac{1}{\sqrt{(x-a)(b-x)}}$ 2. $\frac{1}{2\sqrt{(x-a)(b-x)}}$
 3. $\frac{-1}{2\sqrt{(x-a)(b-x)}}$ 4. $\frac{-1}{\sqrt{(x-a)(b-x)}}$

42. If $y = \operatorname{Tan}^{-1} \sqrt{\frac{x-a}{b-x}}$, $a < x < b$ then $\frac{dy}{dx} =$
 1. $\frac{1}{2\sqrt{(x-a)(b-x)}}$ 2. $\frac{1}{\sqrt{(x-a)(b-x)}}$
 3. $\sqrt{\frac{x-a}{b-x}}$ 4. $\sqrt{\frac{b-x}{x-a}}$

43. If $y = \sin(2\sin^{-1}x)$ then $\frac{dy}{dx} =$

1. $\sqrt{\frac{1-y^2}{1-x^2}}$ 2. $\sqrt{\frac{1-x^2}{1-y^2}}$
 3. $2\sqrt{\frac{1-y^2}{1-x^2}}$ 4. $2\sqrt{\frac{1-x^2}{1-y^2}}$

44. If $y = \operatorname{Sin}^{-1}(4x^3-3x)$ then $\frac{dy}{dx} =$

1. $\frac{3}{\sqrt{1-x^2}}$ 2. $\frac{-3}{\sqrt{1-x^2}}$ 3. $\frac{1}{\sqrt{1-x^2}}$ 4. $\frac{-1}{\sqrt{1-x^2}}$

45. If $y = \operatorname{Tan}^{-1} \left(\frac{(3-x)\sqrt{x}}{1-3x} \right)$ then $\frac{dy}{dx} =$

1. $\frac{3}{(1+x)\sqrt{x}}$ 2. $\frac{3}{2(1+x)\sqrt{x}}$
 3. $\frac{-3}{2(1+x)\sqrt{x}}$ 4. 0

46. If $y = \operatorname{Tan}^{-1} \left(\frac{x^{\frac{1}{3}} + a^{\frac{1}{3}}}{1 - x^{\frac{1}{3}}a^{\frac{1}{3}}} \right)$ then $\frac{dy}{dx} =$

1. $\frac{1}{3x^{\frac{2}{3}} \left(1 + x^{\frac{2}{3}} \right)}$ 2. $\frac{-1}{3x^{\frac{2}{3}} \left(1 + x^{\frac{2}{3}} \right)}$
 3. $\frac{1}{x^{\frac{2}{3}} \left(1 + x^{\frac{2}{3}} \right)}$ 4. $\frac{-1}{x^{\frac{2}{3}} \left(1 + x^{\frac{2}{3}} \right)}$

47. If $y = \operatorname{Tan}^{-1} \left(\frac{3a^2x-x^3}{a^3-3ax^2} \right)$ then $\frac{dy}{dx} =$

1. $\frac{3a}{a^2+x^2}$ 2. $\frac{1}{a^2+x^2}$
 3. $\frac{-3a^2}{a^2+x^2}$ 4. $\frac{-3a}{a^2+x^2}$

48. If $y = \operatorname{Tan}^{-1} \frac{\sqrt{1+x^2}-1}{x}$ then $\frac{dy}{dx} =$

1. $\frac{1}{1+x^2}$ 2. $\frac{-1}{1+x^2}$ 3. $\frac{1}{2(1+x^2)}$ 4. $\frac{2}{1+x^2}$

49. If $y = \tan^{-1}\left(\frac{6x-8x^3}{1-12x^2}\right)$ then $\frac{dy}{dx} =$
1. $\frac{-6}{1+4x^2}$
 2. $\frac{6}{1+4x^2}$
 3. $\frac{1}{1+4x^2}$
 4. $\frac{1}{1+x^2}$
50. If $y = \tan^{-1}\left(\frac{\sqrt{1+a^2x^2}-1}{ax}\right)$ then $\frac{dy}{dx} =$
1. $\frac{a}{2(1+a^2x^2)}$
 2. $\frac{-a}{2(1+a^2x^2)}$
 3. $\frac{1}{2(1+a^2x^2)}$
 4. $\frac{a^2}{2(1+a^2x^2)}$
51. If $y = \tan^{-1}\left(\frac{3x-4}{1+12x}\right)$ then $\frac{dy}{dx} =$
1. $\frac{1}{1+9x^2}$
 2. $\frac{-1}{1+9x^2}$
 3. $\frac{3}{1+9x^2}$
 4. $\frac{-3}{1+9x^2}$
52. If $y = \sin^{-1}(3x-4x^3) + \cos^{-1}(4x^3-3x)$ then $\frac{dy}{dx} =$
1. -1
 2. $\frac{1}{2}$
 3. 0
 4. 2
53. If $y = \cos^{-1}\left(\frac{1-x^{2p}}{1+x^{2p}}\right)$ then $\frac{dy}{dx} =$
1. $\frac{2px^{p-1}}{1+x^{2p}}$
 2. $\frac{px^{p-1}}{1+x^{2p}}$
 3. $\frac{x^{p-1}}{1+x^{2p}}$
 4. $\frac{2px^{p-1}}{1+x^p}$
54. If $y = \tan^{-1}\left(\frac{4\sqrt{x}}{1-4x}\right)$ then $\frac{dy}{dx} =$
1. $\frac{2}{\sqrt{x}(1+4x)}$
 2. $\frac{1}{\sqrt{x}(1+4x)}$
 3. $\frac{-2}{1+4x}$
 4. $\frac{2}{1+4x^2}$
55. If $y = \tan^{-1}\left(\sqrt{1+x^2}-x\right)$ then $\frac{dy}{dx} =$
1. $\frac{1}{1+x^2}$
 2. $\frac{-1}{2(1+x^2)}$
 3. $\frac{1}{2(1+x^2)}$
 4. $\frac{-1}{1+x^2}$
56. $\frac{d}{dx} \cot^{-1}\left(\frac{1+x}{1-x}\right) =$
1. $\frac{1}{1+x^2}$
 2. $\frac{-1}{1+x^2}$
 3. $\frac{1}{\sqrt{1-x^2}}$
 4. $\frac{-1}{\sqrt{1-x^2}}$
57. $\frac{d}{dx} \{\sin^{-1}(6x-32x^3)\} =$
1. $\frac{6}{\sqrt{1-4x^2}}$
 2. $\frac{1}{\sqrt{1-4x^2}}$
 3. $\frac{-1}{\sqrt{1-4x^2}}$
 4. $\frac{-6}{\sqrt{1-4x^2}}$

58. $\frac{d}{dx} \left(\tan^{-1} \frac{x}{\sqrt{a^2-x^2}} \right) =$
1. $\frac{1}{\sqrt{a^2+x^2}}$
 2. $\frac{-1}{\sqrt{a^2+x^2}}$
 3. $\frac{x}{\sqrt{a^2-x^2}}$
 4. $\frac{1}{\sqrt{a^2-x^2}}$
59. $\frac{d}{dx} \left(\cot^{-1} \left(\frac{1+\cos x}{\sin x} \right) \right) =$
1. 1
 2. $\frac{1}{2}$
 3. $\frac{1}{3}$
 4. -1
60. $\frac{d}{dx} \left(\cot^{-1} \left(\frac{3-2\tan x}{2+3\tan x} \right) \right) =$
1. $\frac{-1}{1+x^2}$
 2. $\frac{1}{1+x^2}$
 3. 0
 4. 1
61. If $y = a\cos\theta - b\sin\theta$ then $y^2 + \left(\frac{dy}{d\theta}\right)^2 =$
1. $\frac{a^2}{b^2}$
 2. $\frac{b^2}{a^2}$
 3. $a^2 - b^2$
 4. $a^2 + b^2$
62. The derivative of $\cos^{-1} \frac{1-x^2}{1+x^2}$ w.r.t. $\tan^{-1} \frac{2x}{1-x^2}$ is
1. 0
 2. 1
 3. 2
 4. $\frac{1}{2}$
63. The derivative of $\tan^{-1} \frac{\sqrt{1+x^2}-1}{x}$ w.r.t. $\tan^{-1}x$ is
1. 0
 2. 1
 3. 2
 4. $\frac{1}{2}$
64. If $f(x) = x \cdot \sin \frac{1}{x}$ for $x \neq 0$, $f(0) = 0$ then
1. f is continuous at $x=0$
 2. f is differentiable at $x=0$
 3. $f'(0^-)$ exists but $f'(0^+)$ does not exist
 4. f is discontinuous at $x=0$
65. If $f(x) = \frac{1+\tan x}{1-\tan x}$, then $f'(x) =$
- 1) $\sec^2\left(\frac{\pi}{4} + x\right)$
 - 2) $\sec^2\left(\frac{\pi}{4} - x\right)$
 - 3) $-\sec^2\left(\frac{\pi}{4} - x\right)$
 - 4) $-\sec^2\left(\frac{\pi}{4} + x\right)$
66. $\frac{d}{dx} \left[\frac{\tan x - \cot x}{\tan x + \cot x} \right] =$
- 1) $2 \sin 2x$
 - 2) $-2 \sin 2x$
 - 3) $2 \cos 2x$
 - 4) $-2 \cos 2x$

67. $\frac{d}{dx} \left[\tan^{-1} \frac{\sqrt{2ax-x^2}}{a-x} \right] =$

- 1) $\frac{1}{\sqrt{a^2-x^2}}$ 2) $\frac{1}{\sqrt{2ax-x^2}}$
 3) $\frac{-1}{\sqrt{2ax-x^2}}$ 4) $\frac{-1}{\sqrt{a^2-x^2}}$

68. If $x \sin y = 3 \sin y + 4 \cos y$, then $\frac{dy}{dx} =$

- 1) $\frac{-\sin^2 y}{4}$ 2) $\frac{\sin^2 y}{4}$
 3) $\frac{-\cos^2 y}{4}$ 4) $\frac{\cos^2 y}{4}$

69. If $y = c \cosh \frac{x}{c}$ then $\sqrt{1 + \left(\frac{dy}{dx} \right)^2} =$

- 1) $\sinh x/c$ 2) $c \sinh x/c$
 3) $1/c \sinh x/c$ 4) y/c

70. If a function satisfies $f^{-1}(x) = f(x)$, then $f(x) =$
 1) e^{2x} 2) $\log x$ 3) ce^x 4) $\tan x$

71. If $y = 2e^{\sqrt{x}}(\sqrt{x}-1)$ then $\frac{dy}{dx} =$

- 1) $2e^{\sqrt{x}}$ 2) $1/2e^{\sqrt{x}}$ 3) $e^{-\sqrt{x}}$ 4) $e^{\sqrt{x}}$

72. $\frac{d}{dx} \left\{ 3^{\frac{-5}{3} \log_3(2x+1)} \right\} =$

1. $\frac{-10}{3(2x+1)^{8/3}}$ 2. $\frac{10}{3(2x+1)^{8/3}}$
 3. $\frac{1}{(2x+1)^{8/3}}$ 4. $\frac{-1}{(2x+1)^{8/3}}$

73. $\frac{d}{dx} \left\{ e^{n(\log(a+x) - \log(a-x))} \right\} =$

1. $2an \left(\frac{a+x}{a-x} \right)^{n-1}$ 2. $\frac{-2an(a+x)^{n-1}}{(a-x)^{n+1}}$
 3. $\frac{2an(a+x)^{n-1}}{(a-x)^{n+1}}$ 4. $2an \left(\frac{a+x}{a-x} \right)^n$

74. If $y = 5^{2\{\log_5(x+1) - \log_5(3x+1)\}}$ then $\frac{dy}{dx}$ at $x=0$ is

1. 0 2. $\frac{1}{3}$ 3. $\frac{3}{5}$ 4. -4

75. $\frac{d}{dx} \{ 5^{\log x} \} =$

1. $5^{\log x}$ 2. $5^{\log x} \cdot \log 5$
 3. $x \cdot 5^{\log x} \cdot \log 5$ 4. $\frac{5^{\log x} \cdot \log 5}{x}$

76. If $y = a^{a^x}$ then $\frac{dy}{dx} =$

1. $y \cdot a^x (\log a)^2$ 2. $y \cdot a^x \cdot \log a$
 3. $(y \cdot a^x)^2$ 4. $(y \cdot a^x)$

77. $\frac{d}{dx} \left[e^{3 \log x + x^2} \right] =$

1. $e^{3 \log x + x^2} \left(2x + \frac{3}{x} \right)$ 2. $e^{3 \log x + x^2} \left(2x - \frac{3}{x} \right)$
 3. $e^{3 \log x + x^2}$ 4. $e^{3 \log x}$

78. $\frac{d}{dx} \left[a^{\log(\sin x)} \right] =$

1. $a^{\log(\sin x)} \cdot \tan x \cdot \log a$ 2. $a^{\log(\sin x)} \cdot \cot x \cdot \log a$
 3. $a^{\log(\sin x)}$ 4. $-a^{\log(\sin x)}$

79. If $e^{x+y} = xy$ then $\frac{dy}{dx} =$

1. $\frac{y(1-x)}{x(y-1)}$ 2. $\frac{-y(1-x)}{x(y-1)}$
 3. $\frac{x(y-1)}{y(1+x)}$ 4. $\frac{-x(y-1)}{y(1+x)}$

80. $\frac{d}{dx} \left(\frac{e^{4x} + e^{-4x}}{e^{4x} - e^{-4x}} \right) =$

1. $\frac{16}{(e^{4x} - e^{-4x})^2}$ 2. $\frac{-16}{(e^{4x} - e^{-4x})^2}$
 3. $\frac{(e^{4x} + e^{-4x})}{(e^{4x} - e^{-4x})^2}$ 4. $\frac{-(e^{4x} + e^{-4x})}{(e^{4x} - e^{-4x})^2}$

81. $\frac{d}{dx} \left(\frac{3^x - 3^{-x}}{3^x + 3^{-x}} \right) =$

1. $\frac{4 \log 3}{(3^x + 3^{-x})^2}$ 2. $\frac{-4 \log 3}{(3^x + 3^{-x})^2}$
 3. $\frac{1}{(3^x + 3^{-x})^2}$ 4. $\frac{-1}{(3^x + 3^{-x})^2}$

82. The derivation of $a^{\sin x}$ w.r.t. $\cos x$ is

1. $\cot x \cdot a^{\sin x} \cdot \log a$ 2. $-\cot x \cdot a^{\sin x} \cdot \log a$
 3. $\tan x \cdot a^{\sin x} \cdot \log a$ 4. $-\tan x \cdot a^{\sin x} \cdot \log a$

83. The derivative of $\sec^{-1}\left(\frac{1}{2x^2-1}\right)$ w.r.t. $\sqrt{1-x^2}$ is

1. 0 2. x 3. $\frac{x}{2}$ 4. $\frac{2}{x}$

84. The derivative of a^x w.r.t. $\sin^{-1}x$ is

1. $a^x \cdot \log_e a \sqrt{1-x^2}$ 2. $\frac{a^x \cdot \log_e a}{\sqrt{1-x^2}}$
3. $\frac{a^x}{\sqrt{1-x^2}}$ 4. $\frac{-a^x}{\sqrt{1-x^2}}$

85. The derivative of $e^{\sin^{-1}x}$ w.r.t. $\log x$ is

1. $\frac{-xe^{\sin^{-1}x}}{\sqrt{1-x^2}}$ 2. $\frac{xe^{\sin^{-1}x}}{\sqrt{1-x^2}}$
3. $\frac{e^{\sin^{-1}x}}{\sqrt{1-x^2}}$ 4. $e^{\sin^{-1}x} \cdot \sqrt{1-x^2}$

86. The derivative of $\tan^2x$ w.r.t. $\cos^2x$ is

1. $\sec^4x$ 2. $-\sec^4x$ 3. $\cos^4x$ 4. $-\cos^4x$

87. The derivative of $\sin^{-1}\left(2x\sqrt{1-x^2}\right)$ w.r.t.

$\tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$ is

1. $\frac{2(1+x^2)}{3\sqrt{1-x^2}}$ 2. $\frac{3\sqrt{1-x^2}}{2(1+x^2)}$
3. $\frac{1+x^2}{\sqrt{1-x^2}}$ 4. 0

88. The derivative of $\sin^{-1}(3x-4x^3)$ w.r.t. $\tan^{-1}\left(\frac{x}{\sqrt{1-x^2}}\right)$

is

1. 1 2. 2 3. 3 4. 0

89. The derivative of $\sin^{-1}\left(\frac{1-x}{1+x}\right)$ w.r.t. $\sqrt{x}$ is

1. $\frac{1}{1+x}$ 2. $\frac{-2}{1+x}$ 3. $\frac{-1}{1+x}$ 4. $\frac{2}{1+x}$

90. If $x = a\cos^3t$, $y = a\sin^3t$ then $\frac{dy}{dx}$ at $t = \frac{\pi}{3}$ is

1. $\sqrt{3}$ 2. $\frac{1}{\sqrt{3}}$ 3. $-\sqrt{3}$ 4. $-\frac{1}{\sqrt{3}}$

91. If $x = a(1 - \cos \theta)$, $y = a(\theta + \sin \theta)$ then $\frac{dy}{dx}$ at $\theta = \frac{\pi}{2}$ is

1. 1 2. $\frac{1}{2}$ 3. 0 4. $-\frac{1}{2}$

92. If $x = a(\cos t + \log(\tan \frac{t}{2}))$, $y = a \sin t$ then $\frac{dy}{dx} =$

1. $\sin t$ 2. $\cot t$ 3. $\tan t$ 4. $\tan^2 t$

93. If $x = 3\cos t - \cos^3t$, $y = 3\sin t - \sin^3t$ then $\frac{dy}{dx} =$

1. $\cot^3t$ 2. $-\cot^3t$ 3. $\tan^3t$ 4. $-\tan^3t$

94. If $\sqrt{a^2 - x^2} + \sqrt{a^2 - y^2} = k(x - y)$ then $\frac{dy}{dx} =$

1. $\sqrt{\frac{a^2 - y^2}{a^2 - x^2}}$ 2. $-\sqrt{\frac{a^2 + y^2}{a^2 + x^2}}$
3. $\sqrt{\frac{a^2 + x^2}{a^2 + y^2}}$ 4. $\frac{1}{2}\sqrt{\frac{a^2 + y^2}{a^2 + x^2}}$

95. If $x = a(t + \sin t)$, $y = a(1 - \cos t)$ if $\frac{dx}{dy} = \cot p$ then $p =$

1. t 2. $2t$ 3. $\frac{t}{2}$ 4. $-t^2$

96. If $x = e^t(\cos t + \sin t)$, $y = e^t(\cos t - \sin t)$ then $\frac{dy}{dx} =$

1. $\tan t$ 2. $-\tan t$ 3. $\cot t$ 4. $\cot^2t$

97. If $x = 2\cos t - \cos 2t$, $y = 2\sin t - \sin 2t$ then $\frac{dy}{dx}$ at $t = \frac{\pi}{4}$ is

1. $\sqrt{2} - 1$ 2. $2\sqrt{2}$ 3. $\sqrt{2} + 1$ 4. 0

98. If $x = \sin \theta + \theta \cos \theta$, $y = \cos \theta - \theta \sin \theta$ then $\frac{dy}{dx}$ at

$\theta = \frac{\pi}{2}$ is

1. $-\frac{\pi}{2}$ 2. $\frac{2}{\pi}$ 3. $\frac{\pi}{4}$ 4. $\frac{4}{\pi}$

99. If $x = a\cos^2 2t$, $y = b\sin^2 2t$, then $\frac{dy}{dx}$ at $t = \frac{18\pi}{5}$ is

1. $\frac{a}{b}$ 2. $-\frac{b}{a}$ 3. $\frac{b}{a}$ 4. $-\frac{a}{b}$

100. If $x = a\cos^4t$, $y = b\sin^4t$ then $\frac{dy}{dx}$ at $t = \frac{3\pi}{4}$ is

1. $-\frac{b}{a}$ 2. $\frac{b}{a}$ 3. $\frac{a}{b}$ 4. $-\frac{a}{b}$

101. If $x = \sin^{-1}t$, $y = \log(1-t^2)$ then $\left(\frac{dy}{dx}\right)$ at $t = \frac{1}{2}$ is

1. $\frac{2}{\sqrt{3}}$ 2. $\frac{\sqrt{3}}{2}$ 3. $-\frac{2}{\sqrt{3}}$ 4. $-\frac{\sqrt{3}}{2}$

102. $y = e^{|\sin^2 x + \sin^4 x + \sin^6 x + \dots + \infty|}$, then $\frac{dy}{dx} =$

- 1) $e^{\tan^2 x}$ 2) $e^{\tan^2 x} \sec^2 x$
3) $2e^{\tan^2 x} \tan x \sec^2 x$ 4) 1

103. If $y = \sin^{-1} \left[\frac{e^x - e^{-x}}{e^x + e^{-x}} \right]$, then $\frac{dy}{dx} =$

- 1) $e \operatorname{sech} x$ 2) $\operatorname{sech} x$ 3) $\operatorname{sech}^2 x$ 4) $e^2 \operatorname{sech}^2 x$

104. If $y = \sqrt{a^{3x+1} + \sqrt{a^{3x+1} + \sqrt{a^{3x+1} + \dots \text{to } \infty}}}$ then $\frac{dy}{dx} =$

1. $\frac{a^{3x+1} \cdot \log a}{(2y-1)}$ 2. $\frac{3a^{3x+1} \cdot \log a}{(2y-1)}$
3. $\frac{3a^{3x+1} \cdot \log a}{(2y+1)}$ 4. $\frac{a^{3x+1} \cdot \log a}{(2y+1)}$

105. If $y = \sqrt{\sin \sqrt{x} + y}$ then $\frac{dy}{dx} =$

1. $\frac{\cos \sqrt{x}}{2\sqrt{x}(2y-1)}$ 2. $\frac{\cos \sqrt{x}}{2\sqrt{x}(2y+1)}$
3. $\frac{\sin \sqrt{x}}{2\sqrt{x}(2y-1)}$ 4. $\frac{\sin \sqrt{x}}{2\sqrt{x}(2y+1)}$

106. If $y = \sqrt{\log(\cos 2x) + y}$ then $\frac{dy}{dx} =$

1. $\frac{2 \tan 2x}{(2y-1)}$ 2. $\frac{\tan 2x}{(2y-1)}$
3. $\frac{-2 \tan 2x}{(2y-1)}$ 4. $\frac{1}{(2y-1)}$

107. If $y = \sqrt[3]{x + \sqrt[3]{x + \sqrt[3]{x + \dots \text{to } \infty}}}$ then $\frac{dy}{dx} =$

1. $\frac{1}{(3y^2-1)}$ 2. $\frac{1}{(3y^2+1)}$
3. $\frac{1}{(2y-1)}$ 4. $\frac{1}{(2y+1)}$

108. If $y = \sqrt[3]{\sin x + y}$ then $\frac{dy}{dx} =$

1. $\frac{\sin x}{(3y^2-1)}$ 2. $\frac{\cos x}{(3y^2-1)}$
3. $\frac{-\cos x}{(3y^2+1)}$ 4. $\frac{\sin x}{(3y^2+1)}$

109. If $y = x^{x^{x^{\dots \infty}}}$ then $\frac{dy}{dx} =$

1. $\frac{y^2}{x(1+y \log x)}$ 2. $\frac{y^2}{x(1-\log x)}$
3. $\frac{y^2}{x(1-y \log x)}$ 4. $\frac{y^2}{x(1+\log x)}$

110. If $y = (e^x)^{(e^x)^{(e^x)^{\dots \text{to } \infty}}}$, then $\frac{dy}{dx} =$

1. $\frac{y^2}{1-xy}$ 2. $\frac{y^2}{1+xy}$ 3. $y^2(1-xy)$ 4. $y^2(1+xy)$

111. If $y = (\sin x)^{(\sin x)^{(\sin x)^{(\sin x)^{\dots \text{to } \infty}}}}$ then $\frac{dy}{dx} =$

1. $\frac{y^2}{1-y \log(\sin x)}$ 2. $\frac{y^2 \cot x}{1-y \log(\sin x)}$
3. $\frac{y^2 \cot x}{1+y \log(\sin x)}$ 4. $\frac{y^2}{1+y \log(\sin x)}$

112. If $y = x^x + 2^x$ then $\frac{dy}{dx} =$

1. $x^x \cdot \log(e^x) + 2^x$ 2. $x^x + 2^x \log 2$
3. $x^x \cdot \log(ex) + 2^x \cdot \log 2$ 4. $x^x - 2^x \log 2$

113. $\frac{d}{dx} \left\{ \cos^{-1} \left(\frac{2 \cos x + 3 \sin x}{\sqrt{13}} \right) \right\} =$

1. $-\frac{1}{2}$ 2. 1 3. $\frac{1}{2}$ 4. 0

114. $\frac{d}{dx} \left\{ \sin^{-1} \left(\frac{5x + 12\sqrt{1-x^2}}{13} \right) \right\} =$

1. $\frac{1}{\sqrt{1-x^2}}$ 2. $-\frac{1}{\sqrt{1-x^2}}$ 3. $\frac{2}{\sqrt{1-x^2}}$ 4. 0

115. The set of all points where the function $f(x) = \frac{x}{1+|x|}$ is differentiable is

1. $(-\infty, \infty)$ 2. $(0, \infty)$
3. $(-\infty, 0) \cup (0, \infty)$ 4. $(-\infty, 0)$

116. If $f(a)=2, f'(a)=1, g(a)=-1, g'(a)=2$ then

$$\lim_{x \rightarrow a} \frac{g(x)f(a) - g(a)f(x)}{x - a} =$$

1. -5 2. $\frac{1}{5}$ 3. 5 4. 1

117. Let $f(x)$ be an odd function. Then $f^{-1}(x)$ is

1. is an even function 2. is an odd function
3. may be even or odd 4. neither even nor odd

118. The function $f(x) = |x - 3|, x \geq 1$

$$= \frac{x^2}{4} - \frac{3x}{2} + \frac{13}{4}, x < 1$$

1. not continuous at $x=1$
2. not derivable at $x=1$
3. continuous and derivable at $x=1$
4. continuous at $x=1$ but not derivable at $x=1$

119. If f is an even function and $f'(x)$ exists then $f'(0)=$

1. 0 2. 1 3. -1 4. $f(0)$

120. If $f(x) = |x|$ then $f'(0)=$

1. 0 2. 1 3. -1 4. doesn't exist

121. $\frac{d}{dx} \left\{ \log_a(x^2 + 1) \right\} =$

1. $\frac{\log_e^e . 2x}{(x^2 + 1)}$ 2. $\frac{\log_e^a . 2x}{(x^2 + 1)}$
3. $\frac{2x}{(x^2 + 1)}$ 4. $\frac{-2x}{(x^2 + 1)}$

122. $\frac{d}{dx} \left\{ \log(x + \sqrt{a^2 + x^2}) \right\} =$

1. $\frac{1}{(x + \sqrt{a^2 + x^2})}$ 2. $\frac{x}{\sqrt{a^2 + x^2}}$
3. $\frac{1}{x(x + \sqrt{a^2 + x^2})}$ 4. $\frac{1}{\sqrt{a^2 + x^2}}$

123. $\frac{d}{dx} \{ \log(\operatorname{Cosec} x + \cot x) \} =$

1. $\operatorname{Cosec} x$ 2. $-\operatorname{Cosec} x$
3. $\operatorname{Cosec} x . \cot x$ 4. $\cot x$

124. $\frac{d}{dx} \{ \log(\sec x + \tan x) \} =$

1. $\sec x$ 2. $-\sec x$
3. $\sec^2 x$ 4. $\sec x . \tan x$

125. $\frac{d}{dx} [\log \{ \log(\log x) \}] =$

1. $\frac{1}{x \log x \log(\log x)}$ 2. $\frac{-1}{x \log x \log(\log x)}$
3. $\frac{x}{\log x \log(\log x)}$ 4. $\frac{1}{\log x \log(\log x)}$

126. $\frac{d}{dx} \left\{ \log(x + \sqrt{x^2 - 1}) \right\} =$

1. $\frac{1}{x^2 - 1}$ 2. $\sqrt{x^2 - 1}$ 3. $\frac{1}{\sqrt{x^2 - 1}}$ 4. $x^2 - 1$

127. $\frac{d}{dx} \{ x^n . \log x \} =$

1. $x^n (1 + n \log x)$ 2. $x^{n-1} (1 + n \log x)$
3. $x^{n-1} (1 - n \log x)$ 4. $x^{n-1} (1 - n \log x)$

128. If $y = \log \left(\frac{1}{1+x} \right)$ then $\frac{dy}{dx} =$

1. 0 2. y 3. $-e^y$ 4. $\log y$

129. If $x^y = e^{x-y}$ then $\frac{dy}{dx} =$

1. $\frac{\log x}{1 + \log x}$ 2. $\frac{\log x}{(1 + \log x)^2}$
3. $\frac{-\log x}{(1 + \log x)^2}$ 4. $\frac{-\log x}{1 + \log x}$

130. If $y = (\cos ec hx)^{(\cos ec hx) \dots \dots \dots \infty}$, then $\frac{dy}{dx} =$

1. $\frac{-y^2 \coth x}{1 - y \log \operatorname{cosec} hx}$ 2. $\frac{-y^2 \tan hx}{1 - y \log \cos hx}$
3. $\frac{-y^2 \tan hx}{1 - y \log \operatorname{cosec} hx}$ 4. None

131. $\frac{d}{dx} \{ x^{\tan x} \} =$

1. $x^{\tan x} \left\{ \frac{\tan x}{x} + \sec^2 x . \log x \right\}$
2. $x^{\tan x} \left\{ \frac{\tan x}{x} - \sec^2 x . \log x \right\}$
3. $x^{\tan x} \left\{ \frac{x}{\tan x} + \sec^2 x . \log x \right\}$
4. $x^{\tan x} \left\{ \frac{x}{\tan x} - \sec^2 x . \log x \right\}$

132. $\frac{d}{dx} \{ (\log x)^{\log x} \} =$

1. $(\log x)^{\log x} \left\{ \frac{1 + \log(\log x)}{x} \right\}$
2. $(\log x)^{\log x} \left\{ \frac{1 - \log(\log x)}{x} \right\}$
3. $(\log x)^{\log x} \left\{ \frac{1 + \log x}{x} \right\}$
4. $(\log x)^{\log x} \left\{ \frac{1 - \log x}{x} \right\}$

133. $\frac{d}{dx} \{x^a + a^x + x^x + a^a\} =$
 1. $ax^{a-1} + a^x + x^x \cdot \log x$ 2. $ax^{a-1} + a^x \log a + x^x \cdot \log x$
 3. $ax^{a-1} + a^x \log a + x^x \cdot \log x$ 4. $x^a + a^x + x^x$

134. If $y = 2^{2^x}$ then $\frac{dy}{dx} =$
 1. $y(\log 2)^2 \cdot 2^x$ 2. $y(\log 2) \cdot 2^x$
 3. $y 2(\log 2)^2 \cdot 2^x$ 4. $-y(\log 2) \cdot 2^x$

135. If $y = (ax + b)^{(cx+d)}$ then $\frac{dy}{dx} =$

1. $y \left\{ \frac{a(cx+d)}{(ax+b)} + c \log(ax+b) \right\}$

2. $y \left\{ \frac{a(cx+d)}{(ax+b)} - c \log(ax+b) \right\}$

3. $y \left\{ \frac{(cx+d)}{(ax+b)} + \log(ax+b) \right\}$

4. $y \left\{ \frac{(cx+d)}{(ax+b)} - \log(ax+b) \right\}$

136. If $y = x^{\sin x}$ then $\frac{dy}{dx} =$

1. $y \left(\cos x \cdot \log x - \frac{\sin x}{x} \right)$

2. $y \left(\cos x \cdot \log x + \frac{\sin x}{x} \right)$

3. $y \left(\log x - \frac{\sin x}{x} \right)$ 4. $\frac{y}{x}$

137. If $y = (\sin x)^x$ then $\frac{dy}{dx} =$

1. $y\{\log(\sin x) + x \cot x\}$ 2. $y\{\log(\sin x) - x \cot x\}$
 3. $\{\log(\sin x) - x \cot x\}$ 4. $\{\log(\sin x) + x \cot x\}$

138. If $y = x^{2x}$ then $\frac{dy}{dx} =$

1. $y(1 + \log x)$ 2. $y(1 - \log x)$
 3. $2y(1 + \log x)$ 4. $y(1 + 2 \log x)$

139. $y = \tan^{-1} \sqrt{\frac{1-x}{1+x}}$ then $\frac{dy}{d(\cos^{-1} x)} = \dots$

1. -2 2. $-\frac{1}{2}$ 3. $\frac{1}{2}$ 4. 2

140. If $x < 1$, then

$\frac{1}{1+x} + \frac{2x}{1+x^2} + \frac{4x^3}{1+x^4} + \dots \infty =$

1. x 2. $\frac{1}{1+x}$ 3. $\frac{1}{1-x}$ 4. $\frac{1}{x}$

141. If $f(x) = \cos(x^2 - 2[x])$ for $0 < x < 1$ then

$f' \left(\frac{\sqrt{\pi}}{2} \right)$

1. $-\sqrt{\frac{\pi}{2}}$ 2. $-\sqrt{\pi}$ 3. $\sqrt{\frac{\pi}{2}}$ 4. $\sqrt{\pi}$

142. $\frac{d}{dx} \log[\tan\{\tan^{-1}(\sinh x)\}] =$

1. $\sinh 2x$ 2. $\cot hx$
 3. $\coth 2x$ 4. $-\sinh 2x$

143. Let $f'(1) = 2$ and $f(1) = 4$, then the derivative of $\log[f(e^x)]$ at the point $x = 0$ is equal to

1. 2 2. 1 3. $1/4$ 4. $1/2$

144. If $f(x) = (x-1)(x-2)(x-3)$ then $f'(0)$ is equal to

1. 0 2. 1 3. 6 4. 11

145. If $f(x) = |x^2 - 5x + 6|$ then $f'(2+)$ is

1. 0 2. 1 3. -1 4. 2

146. If $f(x) = \begin{cases} x \log \cos x & \text{for } x \neq 0 \\ 0 & \text{for } x = 0 \end{cases}$ then $f'(0)$

1. 0 2. $-1/2$ 3. $1/2$ 4. 1

147. If $\cos\left(\frac{x}{2}\right) \cos \frac{x}{2^2} \cos \frac{x}{2^3} \dots \infty = \frac{\sin x}{x}$ then

$\frac{1}{2} \tan\left(\frac{x}{2}\right) + \frac{1}{2^2} \tan\left(\frac{x}{2^2}\right) + \frac{1}{2^3} \tan\left(\frac{x}{2^3}\right) \dots \infty$

1. $\frac{x \cot x - 1}{x}$ 2. $\cot x$

3. $\frac{x \tan x - 1}{x}$ 4. $\tan x$

148. If $\sin \theta \sin(2\alpha + \theta) \sin(4\alpha + \theta) \dots$

$\sin(2(n-1)\alpha + \theta) = \sin n\theta / 2^{n-1}$, where

$2n\alpha = \pi$ then

$\cot(\theta) + \cot(2\alpha + \theta) + \cot(4\alpha + \theta) + \dots$

$+ \cot(2(n-1)\alpha + \theta) =$

1. $-n \cot n\theta$ 2. $n \cot n\theta$

3. $n \tan n\theta$ 4. $-n \tan n\theta$

149. It is given that

$f(x) = [\tan \pi/4 + \tan x][\tan \pi/4 + \tan(\pi/4 - x)]$ and $g(x) = x(x+1)$. then the value of $g^1[f(x)]$ is equal to

1. $\frac{1}{1+x^2}$ 2. 4

3. 0 4. $\frac{2x}{1+x^2}$

150. $\frac{d}{dx} [\log(x + \sqrt{x^2 - 1}) + \csc^{-1} x] =$

1. $\frac{1}{x\sqrt{x+1}}$ 2. $\frac{1}{x\sqrt{x-1}}$

3. $\frac{1}{x\sqrt{x^2+1}}$ 4. 0

151. If $f(x) = \begin{cases} \frac{1-\cos x}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}$ then $f^1(x) =$

1. $1/2$ 2. $1/4$
3. 3 4. Does not exist

152. If $f(x) = \begin{cases} \frac{x(e^{1/x} - 1)}{e^{1/x} + 1} & x \neq 0 \\ 0 & x = 0 \end{cases}$ then

$R f^1(0)$ (or) the right derivative of f at $x = 0$

1. 1 2. -1
3. 2 4. Does not exist

153. $f(x) = \begin{cases} \frac{x}{1+e^{1/x}} & x \neq 0 \\ 0 & x = 0 \end{cases}$ then the left derivative

of $f(x)$ at $x = 0$ is (or) $f^1(0-)$

1. 1 2. -1
3. 0 4. Does not exist

154. $f(x) = \begin{cases} x & x < 1 \\ 3-x & 1 \leq x \leq 3 \end{cases}$ then $f^1(x) =$

1. 2 2. 0
3. -1 4. Does not exist

155. $f(x) = |x-1| + |x-3|$ then $f^1(2) =$

1. -2 2. 2 3. 0 4. 1

156. If $f(x) = \begin{cases} x^n \cos \frac{1}{x} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$ and $n > 0$, then

$f(x)$ is differentiable at $x = 0$ if

1. $n \in (0, 1)$ 2. $n \in (0, 1]$
3. $n = 1$ 4. $n \in (1, \infty)$

157. If $f(x+y) = f(x)f(y) \forall x, y \in R$ and $f'(0) = 5, f(2) = 6$ then $f^1(2) =$

1. 10 2. 20 3. 30 4. 40

158. If $f(x) = |x| + |x-1|$ is not derivable at $x =$

1. -1 2. 1 3. 2 4. 3

159. If $\Delta_1 = \begin{vmatrix} x & a & a \\ b & x & a \\ b & b & x \end{vmatrix}$ and $\Delta_2 = \begin{vmatrix} x & a \\ b & x \end{vmatrix}$ then

1. $\frac{d}{dx}(\Delta_1) = \Delta_2$ 2. $\frac{d}{dx}(\Delta_1) = 3\Delta_2$

3. $\frac{d}{dx}(\Delta_1) = 2\Delta_2$ 4. 0

160. The function $y = \sin^{-1}(\cos x)$ is not differentiable at

1. $x = \pi$ 2. $x = -2\pi$
3. $x = 2\pi$ 4. All the above

161. The set of all points when the function $f(x) = \sqrt{1-e^{-x^2}}$ is differentiable is

1. $(0, \infty)$ 2. $(-\infty, \infty)$
3. $(-\infty, \infty) - \{0\}$ 4. $(-1, \infty)$

162. Let $f(x) = x - [x]$ then $f^1(x) = 1$

1. $\forall x \in R$ 2. $\forall x \in R - \{0\}$
3. $\forall x \in R - Z$ 4. $\forall x \in R$

163. The value of $3f(x) - 2f\left(\frac{1}{x}\right) = x$ then $f^1(2) =$

1. $\frac{2}{7}$ 2. $\frac{1}{2}$ 3. 2 4. $\frac{7}{2}$

164. If $x + 4|y| = 6y$ then y as a function of x is

1. Continuous at $x = 0$
2. Derivable at $x = 0$
3. $\frac{dy}{dx} = \frac{1}{2}$ for all x 4. $y = 2x$

KEY

1. 1	2. 4	3. 1	4. 1
5. 2	6. 2	7. 4	8. 4
9. 1	10. 1	11. 4	12. 3
13. 1	14. 2	15. 2	16. 3
17. 2	18. 2	19. 1	20. 2
21. 2	22. 4	23. 1	24. 1
25. 1	26. 3	27. 1	28. 4
29. 4	30. 3	31. 2	32. 2
33. 2	34. 1	35. 3	36. 4
37. 2	38. 1	39. 1	40. 2
41. 2	42. 1	43. 3	44. 2
45. 2	46. 1	47. 1	48. 3
49. 2	50. 1	51. 3	52. 3
53. 1	54. 1	55. 2	56. 2
57. 1	58. 4	59. 2	60. 4
61. 4	62. 2	63. 4	64. 1
65. 1	66. 1	67. 2	68. 1
69. 4	70. 3	71. 4	72. 1
73. 3	74. 4	75. 4	76. 1
77. 1	78. 2	79. 1	80. 2
81. 1	82. 2	83. 4	84. 1
85. 2	86. 2	87. 1	88. 3
89. 2	90. 3	91. 1	92. 3
93. 2	94. 1	95. 3	96. 2
97. 3	98. 4	99. 2	100. 1
101. 3	102. 3	103. 2	104. 2
105. 1	106. 3	107. 1	108. 2
109. 3	110. 1	111. 2	112. 3
113. 2	114. 1	115. 1	116. 3
117. 1	118. 3	119. 1	120. 4
121. 1	122. 4	123. 2	124. 1
125. 1	126. 3	127. 2	128. 3
129. 2	130. 1	131. 1	132. 1
133. 3	134. 1	135. 1	136. 2
137. 1	138. 3	139. 3	140. 3
141. 1	142. 2	143. 4	144. 4
145. 2	146. 1	147. 1	148. 2
149. 3	150. 1	151. 1	152. 1
153. 1	154. 4	155. 3	156. 4
157. 3	158. 2	159. 2	160. 4
161. 3	162. 3	163. 2	164. 1

HINTS

Note : F_k stands for k^{th} formula in the synopsis

2. Use F_{45}
4. Use F_{34}
9. Change degrees in terms of radians and use F_9
10. Use F_{43}
13. Use F_{47}
16. $x = 5^{3^{2^y}} \Rightarrow \frac{dy}{dx} = \frac{1}{375 \log_2 \log_3 \log_5} \quad x = 125$
19. Use F_{47}

21. Use F_{34}
23. Express 'x' as a function of 'y' and use F_5 . Finally consider its reciprocal.
24. Express $\sqrt{\sec^2 x + \cos^2 x} = \frac{2}{\sin 2x}$ and use F_{44}
26. Substitute $x = \sin \theta$ and use F_{17}
27. Substitute $x = \cos \theta$ and use F_{18}
29. Express $\tan^{-1} \sqrt{\frac{1 - \cos x}{1 + \cos x}}$ as $\frac{x}{2}$ and simplify
30. Express $\tan^{-1} \left(\frac{\cos x}{1 + \sin x} \right)$ as $\left(\frac{\pi}{4} - \frac{x}{2} \right)$ and simplify
34. Substitute $x = \cos \theta$ which converts $\cos^{-1} \sqrt{\frac{1+x}{2}}$ as $\frac{1}{2} \cos^{-1} x$ and simplify
35. $-\frac{1}{4} \operatorname{cosech}^2 \frac{x}{2} \left(1 - \coth^2 \frac{x}{2} \right)$
38. Use $\tan^{-1} f(x) + \tan^{-1} \frac{1}{f(x)} = \frac{\pi}{2}$
39. Use F_{46}
40. Use $\sin^{-1} x + \sec^{-1} \frac{1}{x} = \frac{\pi}{2}$
42. Use F_{47}
43. Express the function as $\sin^{-1} y = 2 \sin^{-1} x$ and use F_{17}
45. Using $\tan^{-1} \left\{ \frac{3\alpha - \alpha^3}{1 - 3\alpha^2} \right\} = 3 \tan^{-1} \alpha$. The function reduces to $3 \tan^{-1} \sqrt{x}$ and use F_{19} .
47. Substitute $x = a \tan \theta$
51. Use F_{46}
52. Use $\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}$
53. Substitute $x^p = \tan \theta$ and use F_{19}
54. Express $\tan^{-1} \left(\frac{4\sqrt{x}}{1 - 4x} \right) = 2 \tan^{-1} (2\sqrt{x})$ and use F_{47}
63. Express $\tan^{-1} \left(\frac{\sqrt{1+x^2} - 1}{x} \right)$ as $\frac{1}{2} \tan^{-1} x$ and differentiate w.r.t. $\tan^{-1} x$.

66. Express $\frac{\tan x - \cot x}{\tan x + \cot x}$ as $-\cos 2x$ and use F_9

74. Use F_7

76. Use F_{38}

79. Use F_{34}

82. Use F_{48}

87. Substitute $x = \tan \theta$ which reduces

$$\sin^{-1}\left(2x\sqrt{1-x^2}\right), \tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right) \text{ as}$$

$2\tan^{-1}x, 3\tan^{-1}x$ respectively and use F_{52} .

94. Let $x = a \sin \alpha, y = a \sin \beta$

96. Use F_6 .

103. Substitute $\frac{e^x - e^{-x}}{e^x + e^{-x}} = \tanh x$ and use F_{17} .

104. Use F_{35} .

107. Cubing on both sides and differentiating w.r.t. 'x'.

111. Use F_{49}

114. Express

$$\sin^{-1}\left(\frac{a\cos x + b\sin x}{\sqrt{a^2 + b^2}}\right) \text{ as } x + \sin^{-1}\left(\frac{a}{\sqrt{a^2 + b^2}}\right)$$

and simplify

116. Use L'hospital's rule.

118. Evaluate $\lim_{x \rightarrow 1} f(x)$ and $\lim_{x \rightarrow 1} \frac{f(x) - f(1)}{x - 1}$

125. Use F_{42}

128. Express the function as $-\log(1+x)$ and use F_{42}

132. Use F_{36}

136. Use F_{39} .

137. Use F_{36}

139. Let $\cos^{-1} x = \theta \quad y = \frac{\theta}{2}; \frac{dy}{d\theta} = \frac{1}{2}$

140.

$$\frac{dy}{dx} \left[\int \frac{1}{1+x} + \frac{2x}{1+x^2} + \frac{4x^3}{1+x^4} + \dots \infty \right] = \frac{d}{dx} [-\log(1-x)]$$

141. $f(x) = \cos x^2$

142. $\tan^{-1}(\sinh x) = \cot^{-1}(\cosh x)$

145. $f(x) = -x^2 + 5x - 6$

146. $f'(0) = \lim_{x \rightarrow 0} \frac{f(x) - f(0)}{x}$

147. Apply logarithms and differentiate

149. $f(x) = 2$

154. $f'(1^-) \neq f'(1^+)$

156. $f'(x) = \lim_{x \rightarrow 0} x^{n-1} \cos \frac{1}{x}$

LEVEL - III

1. If $y = \frac{\sqrt{x^2+1} + \sqrt{x^2-1}}{\sqrt{x^2+1} - \sqrt{x^2-1}}$ then $\frac{dy}{dx} - 2x =$

1. $\frac{x^3}{\sqrt{x^4-1}}$ 2. $\frac{2x^3}{\sqrt{x^4+1}}$ 3. $\frac{2x^3}{\sqrt{x^4-1}}$ 4. $\frac{2x^2}{\sqrt{x^4-1}}$

2. If $x^m \cdot y^n = (x+y)^{m+n}$ then $\frac{dy}{dx} =$

1. $\frac{x}{y}$ 2. xy 3. $\frac{-x}{y}$ 4. $\frac{y}{x}$

3. If $x\sqrt{1+y} + y\sqrt{1+x} = 0$ and $x \neq y$ then $\frac{dy}{dx} =$

1. $\frac{x+1}{(1-x)^2}$ 2. $\frac{1}{(1-x)^2}$ 3. $\frac{-1}{(1+x)^2}$ 4. $\frac{1}{(1+x)^2}$

4. If $\sqrt{1-x^2} + \sqrt{1-y^2} = a(x-y)$ then $\frac{dy}{dx} =$

1. $\sqrt{\frac{1-x^2}{1-y^2}}$ 2. $\sqrt{(1-x^2)(1-y^2)}$

3. $\sqrt{\frac{1-y^2}{1-x^2}}$ 4. $\frac{1}{\sqrt{(1-x^2)(1-y^2)}}$

5. If $y\sqrt{1-x^2} + x\sqrt{1-y^2} = 1$ then $\frac{dy}{dx} + \sqrt{\frac{1-y^2}{1-x^2}} =$

1. 1 2. $\frac{-1}{2}$ 3. 0 4. -1

6. $\frac{d}{dx} \left[\sqrt{\tan \sqrt{1+x^2}} \right] =$

1. $\frac{x \sec^2 \sqrt{1+x^2}}{2\sqrt{(1+x^2) \tan \sqrt{1+x^2}}}$

2. $\frac{x \sec^2 \sqrt{1+x^2}}{2(1+x^2)\sqrt{\tan \sqrt{1+x^2}}}$

3. $\frac{x \sec^2 \sqrt{1+x^2}}{2\sqrt{(1+x^2) \tan(1+x^2)}}$ 4. $\frac{x \sec^2 \sqrt{1+x^2}}{\sqrt{\tan(1+x^2)}}$