

**Topic : Mathematical Tools**

**Type of Questions**

Single choice Objective ('-1' negative marking) Q.1 to Q.4

(3 marks, 3 min.)

**M.M., Min.**

**[12, 12]**

Subjective Questions ('-1' negative marking) Q.5 to Q. 6

(4 marks, 5 min.)

**[8, 10]**

Comprehension ('-1' negative marking) Q.7 to Q.9

(3 marks, 3 min.)

**[9, 9]**

1. Maximum value of  $f(x) = \sin x + \cos x$  is :  
(A) 1 (B) 2 (C)  $\frac{1}{\sqrt{2}}$  (D)  $\sqrt{2}$
2. The displacement of a body at any time  $t$  after starting is given by  $s = 15t - 0.4t^2$ . The velocity of the body will be  $7 \text{ ms}^{-1}$  after time :  
(A) 20 s (B) 15 s (C) 10 s (D) 5 s
3. For the previous question, the acceleration of the particle at any time  $t$  is :  
(A)  $-0.8 \text{ m/s}^2$  (B)  $0.8 \text{ m/s}^2$  (C)  $-0.6 \text{ m/s}^2$  (D)  $0.5 \text{ m/s}^2$
4. A particle is moving in a straight line. Its displacement at time  $t$  is given by  $s$  (in m)  $= -4t^2 + 2t$ , then its velocity and acceleration at time  $t = \frac{1}{2}$  second are  
(A)  $-2 \text{ m/s}, -8 \text{ m/s}^2$  (B)  $2 \text{ m/s}, 6 \text{ m/s}^2$  (C)  $-2 \text{ m/s}, 8 \text{ m/s}^2$  (D)  $2 \text{ m/s}, 8 \text{ m/s}^2$
5. A stone thrown upwards from ground level, has its equation of height  $h = 490t - 4.9t^2$  where 'h' is in metres and  $t$  is in seconds respectively. What is the maximum height reached by it ?
6. If  $\int (x+1)dy$

**COMPREHENSION**

If a man has a velocity varying with time given as  $v = 3t^2$ ,  $v$  is in m/s and  $t$  in sec then :



7. Find out the velocity of the man after 3 sec.  
(A) 18 m/s (B) 9 m/s (C) 27 m/s (D) 36 m/s
8. Find out his displacement after 2 seconds of his start :  
(A) 10 m (B) 6 m (C) 12 m (D) 8 m
9. Find out his acceleration after 3 seconds :  
(A)  $9 \text{ m/s}^2$  (B)  $18 \text{ m/s}^2$  (C)  $12 \text{ m/s}^2$  (D)  $6 \text{ m/s}^2$

# Answers Key

## DPP NO. - 5

1. (D)    2. (C)    3. (A)    4. (A)  
5. 12250 m    6.  $4x^3 + 6x^2 + C$   
7. (C)    8. (D)    9. (B)

# Hint & Solutions

## DPP NO. - 5

1.  $y = f(x) = \sin x + \cos x$

$$\frac{dy}{dx} = \cos x - \sin x$$

$$\frac{dy}{dx} = 0, \sin x = \cos x, \tan x = 1$$

$$x = 45^\circ$$

$$y = \sin 45^\circ + \cos 45^\circ$$

$$= \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}$$

$$= \frac{2}{\sqrt{2}} = \sqrt{2}$$

**Alter :**  $f(x) = \sqrt{2} \sin(x + \frac{\pi}{4})$

$$f(x)_{\max} = \sqrt{2}$$

2. (C\*) 10 s

3.  $\frac{ds}{dt} = 15 - 0.8t = 7 = v$

;  $8 = 0.8t$ ;  $t = 10$  second.

$$a = \frac{d^2s}{dt^2} = -0.8 \text{ m/s}^2$$

4. (A\*)  $-2 \text{ m/s}, -8 \text{ m/s}^2$

$$5. \quad \frac{ds}{dt} = 490 - 9.8t = 0 \quad t = \frac{490}{9.8} = 50 \text{ second.}$$

$$S_{\max} = 490 \times 50 - 4.9 \times 2500 = 12250 \text{ m}$$

$$6. \quad dy = 12x dx \quad \int (x+1)(12x) dx = 4x^3 + 6x^2 + C$$

$$7. \quad v = 3t^2$$

$$v = 3(3)^2 = 27 \text{ m/s}$$

$$8. \quad \int_0^s dS = \int_0^2 3t^2 dt$$

$$S = \left[ t^3 \right]_0^2 = 8$$

$$9. \quad f = \frac{dv}{dt} = 6t$$

$$f = 6 \times 3 = 18 \text{ m/s}^2$$