

5. SQUARE ROOTS AND CUBE ROOTS

IMPORTANT FACTS AND FORMULAE

Square Root : If $x^2 = y$, we say that the square root of y is x and we write, $\sqrt{y} = x$.

Thus, $\sqrt{4} = 2$, $\sqrt{9} = 3$, $\sqrt{196} = 14$.

Cube Root : The cube root of a given number x is the number whose cube is x . We denote the cube root of x by $\sqrt[3]{x}$.

Thus, $\sqrt[3]{8} = \sqrt[3]{2 \times 2 \times 2} = 2$, $\sqrt[3]{343} = \sqrt[3]{7 \times 7 \times 7} = 7$ etc.

Note :

$$1. \sqrt{xy} = \sqrt{x} \times \sqrt{y} \quad 2. \sqrt{\frac{x}{y}} = \frac{\sqrt{x}}{\sqrt{y}} = \frac{\sqrt{x}}{\sqrt{y}} \times \frac{\sqrt{y}}{\sqrt{y}} = \frac{\sqrt{xy}}{y}$$

SOLVED EXAMPLES

Ex. 1. Evaluate $\sqrt{6084}$ by factorization method.

Sol. **Method :** Express the given number as the product of prime factors.

Now, take the product of these prime factors choosing one out of every pair of the same primes. This product gives the square root of the given number.

Thus, resolving 6084 into prime factors, we get :

$$6084 = 2^2 \times 3^2 \times 13^2$$

$$\therefore \sqrt{6084} = (2 \times 3 \times 13) = 78.$$

2	6084
2	3042
3	1521
3	507
13	169
	13

Ex. 2. Find the square root of 1471369.

Sol. **Explanation :** In the given number, mark off the digits in pairs starting from the unit's digit. Each pair and the remaining one digit is called a period.

Now, $1^2 = 1$. On subtracting, we get 0 as remainder.

Now, bring down the next period i.e., 47.

Now, trial divisor is $1 \times 2 = 2$ and trial dividend is 47.

So, we take 22 as divisor and put 2 as quotient.

The remainder is 3.

Next, we bring down the next period which is 13.

Now, trial divisor is $12 \times 2 = 24$ and trial dividend is 313. So, we take 241 as dividend and 1 as quotient.

The remainder is 72.

Bring down the next period i.e., 69.

Now, the trial divisor is $121 \times 2 = 242$ and the trial dividend is 7269. So, we take 3 as quotient and 2423 as divisor. The remainder is then zero.

Hence, $\sqrt{1471369} = 1213$.

1	1471369	(1213
	1	
22	47	
	44	
241	313	
	241	
2423	7269	
	7269	
	x	

Ex. 3. Evaluate : $\sqrt{248 + \sqrt{51 + \sqrt{169}}}$.

Sol. Given expression = $\sqrt{248 + \sqrt{51 + 13}} = \sqrt{248 + \sqrt{64}} = \sqrt{248 + 8} = \sqrt{256} = 16$.

Ex. 4. If $a+b+c = \frac{\sqrt{(a+2)(b+3)}}{c+1}$, then find the value of $6*15*3$.

Sol. $6*15*3 = \frac{\sqrt{(6+2)(15+3)}}{3+1} = \frac{\sqrt{8*18}}{4} = \frac{\sqrt{144}}{4} = \frac{12}{4} = 3$.

Ex. 5. Find the value of $\sqrt{1\frac{9}{16}}$.

Sol. $\sqrt{1\frac{9}{16}} = \sqrt{\frac{25}{16}} = \frac{\sqrt{25}}{\sqrt{16}} = \frac{5}{4} = 1\frac{1}{4}$.

Ex. 6. What is the square root of 0.0009?

Sol. $\sqrt{0.0009} = \sqrt{\frac{9}{10000}} = \frac{\sqrt{9}}{\sqrt{10000}} = \frac{3}{100} = 0.03$.

Ex. 7. Evaluate $\sqrt{175.2976}$.

Sol. Method : We make even number of decimal places by affixing a zero, if necessary. Now, we mark off periods and extract the square root as shown.

$$\therefore \sqrt{175.2976} = 13.24.$$

1	175.2976 (13.24
	1
23	75
	69
262	629
	524
2644	10576
	10576
	X

Ex. 8. What will come in place of question mark in each of the following questions?

$$(i) \sqrt{\frac{32.4}{?}} = 2 \quad (ii) \sqrt{86.49} + \sqrt{5 + (?)^2} = 12.3. \quad (\text{R.R.B. 2002})$$

Sol. (i) Let $\sqrt{\frac{32.4}{x}} = 2$. Then, $\frac{32.4}{x} = 4 \Leftrightarrow 4x = 32.4 \Leftrightarrow x = 8.1$.

$$(ii) \text{Let } \sqrt{86.49} + \sqrt{5 + x^2} = 12.3.$$

$$\text{Then, } 9.3 + \sqrt{5 + x^2} = 12.3 \Leftrightarrow \sqrt{5 + x^2} = 12.3 - 9.3 = 3$$

$$\Leftrightarrow 5 + x^2 = 9 \Leftrightarrow x^2 = 9 - 5 = 4 \Leftrightarrow x = \sqrt{4} = 2.$$

Ex. 9. Find the value of $\sqrt{\frac{0.289}{0.00121}}$. (IGNOU, 2003)

$$\text{Sol. } \sqrt{\frac{0.289}{0.00121}} = \sqrt{\frac{0.28900}{0.00121}} = \sqrt{\frac{28900}{121}} = \frac{170}{11}.$$

Ex. 10. If $\sqrt{1 + \frac{x}{144}} = \frac{13}{12}$, then find the value of x .

Sol. $\sqrt{1 + \frac{x}{144}} = \frac{13}{12} \Rightarrow \left(1 + \frac{x}{144}\right) = \left(\frac{13}{12}\right)^2 = \frac{169}{144} \Rightarrow \frac{x}{144} = \frac{169}{144} - 1$
 $\Rightarrow \frac{x}{144} = \frac{25}{144} \Rightarrow x = 25.$

Ex. 11. Find the value of $\sqrt{3}$ upto three places of decimal.

Sol. 1
$$\begin{array}{r} 3.000000 \\ | \\ 1 \\ \hline 27 \\ | \\ 200 \\ | \\ 189 \\ \hline 343 \\ | \\ 1100 \\ | \\ 1029 \\ \hline 7100 \\ | \\ 6924 \\ \hline \end{array}$$

∴ $\sqrt{3} = 1.732.$

Ex. 12. If $\sqrt{3} = 1.732$, find the value of $\sqrt{192} - \frac{1}{2}\sqrt{48} - \sqrt{75}$ correct to 3 places of decimal. (S.S.C. 2004)

Sol. $\sqrt{192} - \frac{1}{2}\sqrt{48} - \sqrt{75} = \sqrt{64 \times 3} - \frac{1}{2}\sqrt{16 \times 3} - \sqrt{25 \times 3} = 8\sqrt{3} - \frac{1}{2} \times 4\sqrt{3} - 5\sqrt{3}$
 $= 3\sqrt{3} - 2\sqrt{3} = \sqrt{3} = 1.732$

Ex. 13. Evaluate : $\frac{9.5 \times .0085 \times 18.9}{.0017 \times 1.9 \times 0.021}$.

Sol. Given exp. = $\frac{9.5 \times .0085 \times 18.900}{.0017 \times 1.9 \times 0.021}$.

Now, since the sum of decimal places in the numerator and denominator under the radical sign is the same, we remove the decimal.

Given exp. = $\sqrt{\frac{95 \times 85 \times 18900}{17 \times 19 \times 21}} = \sqrt{5 \times 5 \times 900} = 5 \times 30 = 150.$

Ex. 14. Simplify : $\sqrt{[(12.1)^2 - (8.1)^2] + [(0.25)^2 + (0.25)(19.95)]}$. (C.B.I. 2003)

Sol. Given exp. = $\sqrt{\frac{(12.1 + 8.1)(12.1 - 8.1)}{(0.25)(0.25 + 19.95)}} = \sqrt{\frac{20.2 \times 4}{0.25 \times 20.2}}$
 $= \sqrt{\frac{4}{0.25}} = \sqrt{\frac{400}{25}} = \sqrt{16} = 4.$

Ex. 15. If $x = 1 + \sqrt{2}$ and $y = 1 - \sqrt{2}$, find the value of $(x^2 + y^2)$.

Sol. $x^2 + y^2 = (1 + \sqrt{2})^2 + (1 - \sqrt{2})^2 = 2[(1)^2 + (\sqrt{2})^2] = 2 \times 3 = 6.$

Ex. 16. Evaluate $\sqrt{0.9}$ upto 3 places of decimal. (R.R.B. 2003)

Sol. 9
$$\begin{array}{r} 0.900000 (.948) \\ | \\ 81 \\ | \\ 900 \\ | \\ 736 \\ \hline 16400 \\ | \\ 15104 \\ \hline \end{array}$$

∴ $\sqrt{0.9} = 0.948.$

Ex. 17. If $\sqrt{15} = 3.88$, find the value of $\sqrt{\frac{5}{3}}$.

(S.S.C. 2003)

$$\text{Sol. } \sqrt{\frac{5}{3}} = \sqrt{\frac{5 \times 3}{3 \times 3}} = \frac{\sqrt{15}}{3} = \frac{3.88}{3} = 1.2933, \dots = 1.29\bar{3}.$$

Ex. 18. Find the least square number which is exactly divisible by 10, 12, 15 and 18.

Sol. L.C.M. of 10, 12, 15, 18 = 180. Now, $180 = 2 \times 2 \times 3 \times 3 \times 5 = 2^2 \times 3^2 \times 5$.

To make it a perfect square, it must be multiplied by 5.

$$\therefore \text{Required number} = (2^2 \times 3^2 \times 5^2) = 900.$$

Ex. 19. Find the greatest number of five digits which is a perfect square.

(R.R.B. 1998)

Sol. Greatest number of 5 digits is 99999.

$$\begin{array}{r|rr} 3 & \overline{99999} & (316 \\ & 9 & \\ \hline 61 & 99 & \\ & 61 & \\ \hline 626 & 3899 & \\ & 3756 & \\ \hline & 143 & \end{array}$$

$$\therefore \text{Required number} = (99999 - 143) = 99856.$$

Ex. 20. Find the smallest number that must be added to 1780 to make it a perfect square.

$$\begin{array}{r|rr} 4 & \overline{1780} & (42 \\ & 16 & \\ \hline 82 & 180 & \\ & 164 & \\ \hline & 16 & \end{array}$$

$$\therefore \text{Number to be added} = (43)^2 - 1780 = 1849 - 1780 = 69.$$

Ex. 21. If $\sqrt{2} = 1.4142$, find the value of $\frac{\sqrt{2}}{(2 + \sqrt{2})}$.

$$\text{Sol. } \frac{\sqrt{2}}{(2 + \sqrt{2})} = \frac{\sqrt{2}}{(2 + \sqrt{2})} \times \frac{(2 - \sqrt{2})}{(2 - \sqrt{2})} = \frac{2\sqrt{2} - 2}{(4 - 2)} = \frac{2(\sqrt{2} - 1)}{2} = (\sqrt{2} - 1) = (1.4142 - 1) = 0.4142.$$

Ex. 22. If $x = \left(\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} \right)$ and $y = \left(\frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} \right)$, find the value of $(x^2 + y^2)$.

$$\text{Sol. } x = \frac{(\sqrt{5} + \sqrt{3})}{(\sqrt{5} - \sqrt{3})} \times \frac{(\sqrt{5} + \sqrt{3})}{(\sqrt{5} + \sqrt{3})} = \frac{(\sqrt{5} + \sqrt{3})^2}{(5 - 3)} = \frac{5 + 3 + 2\sqrt{15}}{2} = 4 + \sqrt{15}.$$

$$y = \frac{(\sqrt{5} - \sqrt{3})}{(\sqrt{5} + \sqrt{3})} \times \frac{(\sqrt{5} - \sqrt{3})}{(\sqrt{5} - \sqrt{3})} = \frac{(\sqrt{5} - \sqrt{3})^2}{(5 - 3)} = \frac{5 + 3 - 2\sqrt{15}}{2} = 4 - \sqrt{15}.$$

$$\therefore x^2 + y^2 = (4 + \sqrt{15})^2 + (4 - \sqrt{15})^2 = 2[(4)^2 + (\sqrt{15})^2] = 2 \times 31 = 62.$$

Ex. 23. Find the cube root of 2744.

Sol. Method : Resolve the given number as the product of prime factors and take the product of prime factors, choosing one out of three of the same prime factors. Resolving 2744 as the product of prime factors, we get :

$$2744 = 2^3 \times 7^3.$$

$$\therefore \sqrt[3]{2744} = 2 \times 7 = 14.$$

Ex. 24. By what least number 4320 be multiplied to obtain a number which is a perfect cube ?

Sol. Clearly, $4320 = 2^3 \times 3^3 \times 2^2 \times 5$.

To make it a perfect cube, it must be multiplied by 2×5^2 i.e., 50.

2	2744
2	1372
2	686
7	343
7	49
	7

EXERCISE 5

(OBJECTIVE TYPE QUESTIONS)

Directions : Mark (✓) against the correct answer :

- $\sqrt{53824} = ?$ (Bank P.O. 2003)
 (a) 202 (b) 232 (c) 242 (d) 332
- The square root of 64009 is : (R.R.B. 2003)
 (a) 253 (b) 347 (c) 363 (d) 803
- The value of $\sqrt{10 + \sqrt{25 + \sqrt{108 + \sqrt{154 + \sqrt{225}}}}}$ is : (S.S.C. 1998)
 (a) 4 (b) 6 (c) 8 (d) 10
- Evaluate : $\sqrt{41 - \sqrt{21 + \sqrt{19 - \sqrt{9}}}}$. (C.B.I. 1997)
 (a) 3 (b) 5 (c) 6 (d) 6.4
- $\sqrt{176 + \sqrt{2401}}$ is equal to :
 (a) 14 (b) 15 (c) 18 (d) 24
- $\left(\frac{\sqrt{625}}{11} \times \frac{14}{\sqrt{25}} \times \frac{11}{\sqrt{196}} \right)$ is equal to : (S.S.C. 2000)
 (a) 5 (b) 6 (c) 8 (d) 11
- $\left(\sqrt{\frac{225}{729}} - \sqrt{\frac{25}{144}} \right) \times \sqrt{\frac{16}{81}} = ?$
 (a) $\frac{1}{48}$ (b) $\frac{5}{48}$ (c) $\frac{5}{16}$ (d) None of these
- The square root of $(272^2 - 128^2)$ is : (S.S.C. 2000)
 (a) 144 (b) 200 (c) 240 (d) 256
- If $x * y = x + y + \sqrt{xy}$, the value of $6 * 24$ is : (C.B.I. 1998)
 (a) 41 (b) 42 (c) 43 (d) 44
- If $y = 5$, then what is the value of $10y \sqrt{y^3 - y^2}$? (R.R.B. 1998)
 (a) $50\sqrt{2}$ (b) 100 (c) $200\sqrt{5}$ (d) 500

11. $\sqrt{110\frac{1}{4}} = ?$
- (a) 10.25 (b) 10.5 (c) 11.5 (d) 19.5
12. $\sqrt{\frac{25}{81} - \frac{1}{9}} = ?$
- (a) $\frac{2}{3}$ (b) $\frac{4}{9}$ (c) $\frac{16}{81}$ (d) $\frac{25}{81}$
13. The digit in the unit's place in the square root of 15876 is : (S.S.C. 2000)
- (a) 2 (b) 4 (c) 6 (d) 8
14. How many two-digit numbers satisfy this property : The last digit (unit's digit) of the square of the two-digit number is 8? (R.R.B. 2001)
- (a) 1 (b) 2 (c) 3 (d) None of these
15. What is the square root of 0.16? (P.C.S. 1998)
- (a) 0.004 (b) 0.04 (c) 0.4 (d) 4
16. The value of $\sqrt{0.000441}$ is : (S.S.C. 2002)
- (a) 0.00021 (b) 0.0021 (c) 0.021 (d) 0.21
17. $\sqrt{0.00004761}$ equals : (C.B.I. 2003)
- (a) 0.00069 (b) 0.0069 (c) 0.0609 (d) 0.069
18. $1.5^2 \times \sqrt{0.0225} = ?$ (Bank P.O. 2002)
- (a) 0.0375 (b) 0.3375 (c) 3.275 (d) 32.75
19. $\sqrt{0.01 + \sqrt{0.0064}} = ?$
- (a) 0.03 (b) 0.3 (c) 0.42 (d) None of these
20. The value of $\sqrt{0.01} + \sqrt{0.81} + \sqrt{1.21} + \sqrt{0.0009}$ is : (S.S.C. 2002)
- (a) 2.03 (b) 2.1 (c) 2.11 (d) 2.13
21. $\sqrt{.0025} \times \sqrt{2.25} \times \sqrt{.0001} = ?$ (Hotel Management, 1998)
- (a) .000075 (b) .0075 (c) .075 (d) None of these
22. $\sqrt{1.5625} = ?$ (S.B.I.P.O. 2003)
- (a) 1.05 (b) 1.25 (c) 1.45 (d) 1.55
23. If $\sqrt{0.0000676} = .0026$, the square root of 67,60,000 is :
- (a) $\frac{1}{26}$ (b) 26 (c) 260 (d) 2600
24. If $\sqrt{18225} = 135$, then the value of $(\sqrt{182.25} + \sqrt{1.8225} + \sqrt{0.018225} + \sqrt{0.00018225})$ is : (S.S.C. 2002)
- (a) 1.49985 (b) 14.9985 (c) 149.985 (d) 1499.85
25. Given that $\sqrt{13} = 3.605$ and $\sqrt{130} = 11.40$, find the value of $\sqrt{1.3} + \sqrt{1300} + \sqrt{0.013}$. (S.S.C. 1999)
- (a) 36.164 (b) 36.304 (c) 37.164 (d) 37.304
26. If $\frac{52}{x} = \sqrt{\frac{169}{289}}$, the value of x is : (C.B.I. 1998)
- (a) 52 (b) 58 (c) 62 (d) 68

27. For what value of * the statement $\left(\frac{*}{15}\right)\left(\frac{*}{135}\right) = 1$ is true? (S.S.C. 2002)

- (a) 15 (b) 25 (c) 35 (d) 45

28. Which number can replace both the question marks in the equation $\frac{4 \frac{1}{2}}{?} = \frac{?}{32}$.

- (a) 1 (b) 7 (c) $7\frac{1}{2}$ (d) None of these

(Hotel Management, 2000)

29. What should come in place of both the question marks in the equation $\frac{?}{\sqrt{128}} = \frac{\sqrt{162}}{?}$.

- (a) 12 (b) 14 (c) 144 (d) 196

(Bank P.O. 1999)

30. If $0.13 + p^2 = 13$, then p equals : (S.S.C. 2000)

- (a) 0.01 (b) 0.1 (c) 10 (d) 100

31. What number should be divided by $\sqrt{0.25}$ to give the result as 25?

- (a) 12.5 (b) 25 (c) 50 (d) 125

(C.B.I. 2003)

32. If $\sqrt{3^n} = 729$, then the value of n is : (Section Officers', 2003)

- (a) 6 (b) 8 (c) 10 (d) 12

33. If $\sqrt{18 \times 14 \times x} = 84$, then x equals :

- (a) 22 (b) 24 (c) 28 (d) 32

34. $28\sqrt{?} + 1426 = \frac{3}{4}$ of 2872 (B.S.R.B. 1998)

- (a) 576 (b) 676 (c) 1296 (d) 1444

35. $\sqrt{\frac{?}{169}} = \frac{54}{39}$

- (a) 108 (b) 324 (c) 2916 (d) 4800

36. If $\sqrt{x} + \sqrt{441} = 0.02$, then the value of x is : (S.S.C. 1999)

- (a) 0.1764 (b) 1.764 (c) 1.64 (d) 2.64

37. $\sqrt{\frac{0.196}{?}} = 0.2$ (Hotel Management, 1999)

- (a) 0.49 (b) 0.7 (c) 4.9 (d) None of these

38. $\sqrt{0.0169 \times ?} = 1.3$ (Hotel Management, 2001)

- (a) 10 (b) 100 (c) 1000 (d) None of these

39. If $\sqrt{1369} + \sqrt{.0615 + x} = 37.25$, then x is equal to : (Hotel Management, 1998)

- (a) 10^{-1} (b) 10^{-2} (c) 10^{-3} (d) None of these

40. If $\sqrt{(x-1)(y+2)} = 7$, x and y being positive whole numbers, then the values of x and y respectively are : (Hotel Management, 1998)

- (a) 8, 5 (b) 15, 12 (c) 22, 19 (d) None of these

41. If $\sqrt{.04 \times A \times a} = .004 \times A \times \sqrt{b}$, then $\frac{a}{b}$ is : (Hotel Management, 1998)

- (a) 16×10^{-3} (b) 16×10^{-4} (c) 16×10^{-5} (d) None of these

42. Three-fifth of the square of a certain number is 126.15. What is the number ?
 (a) 14.5 (b) 75.69 (c) 145 (d) 210.25
 (S.S.C. 2002)
43. $\sqrt{\frac{0.361}{0.00169}} = ?$
 (a) $\frac{1.9}{13}$ (b) $\frac{19}{13}$ (c) $\frac{1.9}{130}$ (d) $\frac{190}{13}$
44. $\sqrt{\frac{48.4}{0.289}}$ is equal to :
 (a) $1\frac{5}{17}$ (b) $12\frac{1}{17}$ (c) $12\frac{16}{17}$ (d) $129\frac{7}{17}$
 (S.S.C. 2004)
45. If $\sqrt{1 + \frac{x}{169}} = \frac{14}{13}$, then x is equal to :
 (a) 1 (b) 13 (c) 27 (d) None of these
46. If $\sqrt{1 + \frac{55}{729}} = 1 + \frac{x}{27}$, then the value of x is :
 (a) 1 (b) 3 (c) 5 (d) 7
 (C.D.S. 2003)
47. The value of $\sqrt{2}$ upto three places of decimal is :
 (a) 1.410 (b) 1.412 (c) 1.413 (d) 1.414
48. $(2\sqrt{27} - \sqrt{75} + \sqrt{12})$ is equal to :
 (a) $\sqrt{3}$ (b) $2\sqrt{3}$ (c) $3\sqrt{3}$ (d) $4\sqrt{3}$
49. By how much does $\sqrt{12} + \sqrt{18}$ exceed $\sqrt{3} + \sqrt{2}$?
 (a) $\sqrt{2} - 4\sqrt{3}$ (b) $\sqrt{3} + 2\sqrt{2}$ (c) $2(\sqrt{3} - \sqrt{2})$ (d) $3(\sqrt{3} - \sqrt{2})$
 (S.S.C. 1999)
50. $\frac{\sqrt{24} + \sqrt{216}}{\sqrt{96}} = ?$
 (a) $2\sqrt{6}$ (b) 2 (c) $6\sqrt{2}$ (d) $\frac{2}{\sqrt{6}}$
51. The value of $\frac{\sqrt{80} - \sqrt{112}}{\sqrt{45} - \sqrt{63}}$ is :
 (a) $\frac{3}{4}$ (b) $1\frac{1}{3}$ (c) $1\frac{7}{9}$ (d) $1\frac{3}{4}$
 (S.S.C. 2000)
52. If $3\sqrt{5} + \sqrt{125} = 17.88$, then what will be the value of $\sqrt{80} + 6\sqrt{5}$?
 (a) 13.41 (b) 20.46 (c) 21.66 (d) 22.35
 (Bank P.O. 2000)
53. $\sqrt{50} \times \sqrt{98}$ is equal to :
 (a) 63.75 (b) 65.95 (c) 70 (d) 70.25
54. Given $\sqrt{2} = 1.414$. The value of $\sqrt{8} + 2\sqrt{32} - 3\sqrt{128} + 4\sqrt{50}$ is :
 (a) 8.426 (b) 8.484 (c) 8.526 (d) 8.876
 (S.S.C. 2003)
55. The approximate value of $\frac{3\sqrt{12}}{2\sqrt{28}} + \frac{2\sqrt{21}}{\sqrt{98}}$ is :
 (a) 1.0605 (b) 1.0727 (c) 1.6007 (d) 1.6026
 (Section Officers', 2003)

56. $\sqrt{\frac{.081 \times .484}{.0064 \times 6.25}}$ is equal to : (N.I.E.T. 1997)
- (a) 0.9 (b) 0.99 (c) 9 (d) 99
57. $\sqrt{\frac{0.204 \times 42}{0.07 \times 3.4}}$ is equal to :
- (a) $\frac{1}{6}$ (b) 0.06 (c) 0.6 (d) 6
58. $\sqrt{\frac{0.081 \times 0.324 \times 4.624}{1.5625 \times 0.0289 \times 72.9 \times 64}}$ is equal to : (S.S.C. 2002)
- (a) 0.024 (b) 0.24 (c) 2.4 (d) 24
59. $\sqrt{\frac{9.5 \times .085}{.0017 \times .19}}$ equals : (S.S.C. 2004)
- (a) .05 (b) 5 (c) 50 (d) 500
60. The value of $\sqrt{\frac{(0.03)^2 + (0.21)^2 + (0.065)^2}{(0.003)^2 + (0.021)^2 + (0.0065)^2}}$ is : (S.S.C. 2002)
- (a) 0.1 (b) 10 (c) 10^2 (d) 10^3
61. The square root of $(7 + 3\sqrt{5})(7 - 3\sqrt{5})$ is : (S.S.C. 2004)
- (a) $\sqrt{5}$ (b) 2 (c) 4 (d) $3\sqrt{5}$
62. $\left(\sqrt{3} - \frac{1}{\sqrt{3}}\right)^2$ simplifies to : (R.R.B. 2000)
- (a) $\frac{3}{4}$ (b) $\frac{4}{\sqrt{3}}$ (c) $\frac{4}{3}$ (d) None of these
63. $\left(\sqrt{2} + \frac{1}{\sqrt{2}}\right)^2$ is equal to : (C.B.I. 2003)
- (a) $2\frac{1}{2}$ (b) $3\frac{1}{2}$ (c) $4\frac{1}{2}$ (d) $5\frac{1}{2}$
64. If $a = 0.1039$, then the value of $\sqrt{4a^2 - 4a + 1} + 3a$ is : (S.S.C. 1999)
- (a) 0.1039 (b) 0.2078 (c) 1.1039 (d) 2.1039
65. The square root of $\frac{(0.75)^3}{1 - 0.75} + [0.75 + (0.75)^2 + 1]$ is : (S.S.C. 1999)
- (a) 1 (b) 2 (c) 3 (d) 4
66. If $3a = 4b = 6c$ and $a + b + c = 27\sqrt{29}$, then $\sqrt{a^2 + b^2 + c^2}$ is : (Hotel Management, 1999)
- (a) $3\sqrt{29}$ (b) 81 (c) 87 (d) None of these
67. The square root of $0.\overline{4}$ is : (S.S.C. 2004)
- (a) $0.\overline{6}$ (b) $0.\overline{7}$ (c) $0.\overline{8}$ (d) $0.\overline{9}$
68. Which one of the following numbers has rational square root ? (S.S.C. 2004)
- (a) 0.4 (b) 0.09 (c) 0.9 (d) 0.025
69. The value of $\sqrt{0.4}$ is : (S.S.C. 2004)
- (a) 0.02 (b) 0.2 (c) 0.51 (d) 0.63

70. The value of $\sqrt{0.121}$ is :
 (a) 0.011 (b) 0.11 (c) 0.347 (d) 1.1
71. The value of $\sqrt{0.064}$ is :
 (a) 0.008 (b) 0.08 (c) 0.252 (d) 0.8
72. The value of $\sqrt{\frac{0.16}{0.4}}$ is :
 (a) 0.02 (b) 0.2 (c) 0.63 (d) None of these
 (IGNOU, 2003)
73. The value of $\frac{1 + \sqrt{0.01}}{1 - \sqrt{0.1}}$ is close to :
 (a) 0.6 (b) 1.1 (c) 1.6 (d) 1.7
 (C.B.I. 1997)
74. If $\sqrt{5} = 2.236$, then the value of $\frac{1}{\sqrt{5}}$ is :
 (a) .367 (b) .447 (c) .745 (d) None of these
 (shops 2000 x 2001 / 2000 x 2001 = 1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
75. If $\sqrt{24} = 4.899$, the value of $\sqrt{\frac{8}{3}}$ is :
 (a) 0.544 (b) 1.333 (c) 1.633 (d) 2.666
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
76. If $\sqrt{6} = 2.449$, then the value of $\frac{3\sqrt{2}}{2\sqrt{3}}$ is :
 (a) 0.6122 (b) 0.8163 (c) 1.223 (d) 1.2245
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
77. If $\sqrt{5} = 2.236$, then the value of $\frac{\sqrt{5}}{2} - \frac{10}{\sqrt{5}} + \sqrt{125}$ is equal to :
 (a) 5.59 (b) 7.826 (c) 8.944 (d) 10.062
 (M.B.A. 1998)
78. If $2*3 = \sqrt{13}$ and $3*4 = 5$, then the value of $5*12$ is :
 (a) $\sqrt{17}$ (b) $\sqrt{29}$ (c) 12 (d) 13
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
79. The least perfect square number divisible by 3, 4, 5, 6 and 8 is :
 (a) 900 (b) 1200 (c) 2500 (d) 3600
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
80. The least perfect square, which is divisible by each of 21, 36 and 66, is :
 (a) 213444 (b) 214344 (c) 214434 (d) 231444
 (C.B.I. 2003)
81. The least number by which 294 must be multiplied to make it a perfect square, is :
 (a) 2 (b) 3 (c) 6 (d) 24
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
82. Find the smallest number by which 5808 should be multiplied so that the product becomes a perfect square.
 (S.S.C. 1999)
 (a) 2 (b) 3 (c) 7 (d) 11
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
83. The least number by which 1470 must be divided to get a number which is a perfect square, is :
 (a) 5 (b) 6 (c) 15 (d) 30
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
84. What is the smallest number to be subtracted from 549162 in order to make it a perfect square ?
 (a) 28 (b) 36 (c) 62 (d) 81
 (1000 x 2001 / 2000 x 2001 = 1000/2000 = 1/2)
85. What is the least number which should be subtracted from 0.000326 to make it a perfect square ?
 (S.S.C. 2003)
 (a) 0.000002 (b) 0.000004 (c) 0.02 (d) 0.04

99. If $x = (7 - 4\sqrt{3})$, then the value of $\left(x + \frac{1}{x}\right)$ is : (S.S.C. 2000)

- (a) $3\sqrt{3}$ (b) $8\sqrt{3}$ (c) 14 (d) $14 + 8\sqrt{3}$

100. If $x = \frac{\sqrt{3}+1}{\sqrt{3}-1}$ and $y = \frac{\sqrt{3}-1}{\sqrt{3}+1}$, then the value of $(x^2 + y^2)$ is : (S.S.C. 2003)

- (a) 10 (b) 13 (c) 14 (d) 15

101. If $a = \frac{\sqrt{5}+1}{\sqrt{5}-1}$ and $b = \frac{\sqrt{5}-1}{\sqrt{5}+1}$, the value of $\left(\frac{a^2 + ab + b^2}{a^2 - ab + b^2}\right)$ is :

- (a) $\frac{3}{4}$ (b) $\frac{4}{3}$ (c) $\frac{3}{5}$ (d) $\frac{5}{3}$

102. A man plants 15376 apple trees in his garden and arranges them so that there are as many rows as there are apples trees in each row. The number of rows is :

- (a) 124 (b) 126 (c) 134 (d) 144

103. A General wishes to draw up his 36581 soldiers in the form of a solid square. After arranging them, he found that some of them are left over. How many are left ?

- (a) 65 (b) 81 (c) 100 (d) None of these

104. A group of students decided to collect as many paise from each member of the group as is the number of members. If the total collection amounts to Rs. 59.29, the number of members in the group is :

- (a) 57 (b) 67 (c) 77 (d) 87

105. The cube root of .000216 is :

- (a) .6 (b) .06 (c) .006 (d) None of these

106. $\sqrt[3]{4\frac{12}{125}} = ?$

- (a) $1\frac{2}{5}$ (b) $1\frac{3}{5}$ (c) $1\frac{4}{5}$ (d) $2\frac{2}{5}$

107. $\sqrt[3]{.000064} = ?$

- (a) .02 (b) .2 (c) 2 (d) None of these

108. The largest four-digit number which is a perfect cube, is :

- (a) 8000 (b) 9261 (c) 9999 (d) None of these

109. By what least number 675 be multiplied to obtain a number which is a perfect cube ?

- (a) 5 (b) 6 (c) 7 (d) 8

110. What is the smallest number by which 3500 be divided to make it a perfect cube ?

- (a) 9 (b) 50 (c) 300 (d) 450.

ANSWERS

- | | | | | | | | | |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1. (b) | 2. (a) | 3. (a) | 4. (c) | 5. (b) | 6. (a) | 7. (c) | 8. (c) | 9. (b) |
| 10. (d) | 11. (b) | 12. (b) | 13. (c) | 14. (d) | 15. (c) | 16. (c) | 17. (b) | 18. (b) |
| 19. (b) | 20. (d) | 21. (d) | 22. (b) | 23. (d) | 24. (b) | 25. (d) | 26. (d) | 27. (d) |
| 28. (d) | 29. (a) | 30. (b) | 31. (a) | 32. (d) | 33. (c) | 34. (b) | 35. (b) | 36. (a) |

37. (a) 38. (b) 39. (c) 40. (a) 41. (c) 42. (a) 43. (d) 44. (c) 45. (c)
 46. (a) 47. (d) 48. (c) 49. (b) 50. (b) 51. (b) 52. (d) 53. (c) 54. (b)
 55. (a) 56. (b) 57. (d) 58. (a) 59. (c) 60. (b) 61. (b) 62. (c) 63. (c)
 64. (c) 65. (b) 66. (c) 67. (a) 68. (b) 69. (d) 70. (c) 71. (c) 72. (c)
 73. (c) 74. (b) 75. (c) 76. (d) 77. (b) 78. (d) 79. (d) 80. (a) 81. (c)
 82. (b) 83. (d) 84. (d) 85. (a) 86. (a) 87. (b) 88. (c) 89. (c) 90. (d)
 91. (b) 92. (a) 93. (c) 94. (d) 95. (c) 96. (b) 97. (d) 98. (a) 99. (c)
 100. (c) 101. (b) 102. (a) 103. (c) 104. (c) 105. (b) 106. (b) 107. (b) 108. (b)
 109. (a) 110. (d)
-

SOLUTIONS

1. $\sqrt{53824} \text{ (232)}$

$$\begin{array}{r} 53824 \\ \hline 4 \\ 43 \\ \hline 138 \\ 129 \\ \hline 924 \\ 924 \\ \hline \times \end{array}$$

$$\therefore \sqrt{53824} = 232.$$

2. $\sqrt{64009} \text{ (253)}$

$$\begin{array}{r} 64009 \\ \hline 4 \\ 45 \\ \hline 240 \\ 225 \\ \hline 1509 \\ 1509 \\ \hline \times \end{array}$$

$$\therefore \sqrt{64009} = 253.$$

$$\begin{aligned} 3. \text{ Given exp.} &= \sqrt{10 + \sqrt{25 + \sqrt{108 + \sqrt{154 + 15}}}} = \sqrt{10 + \sqrt{25 + \sqrt{108 + \sqrt{169}}}} \\ &= \sqrt{10 + \sqrt{25 + \sqrt{108 + 13}}} = \sqrt{10 + \sqrt{25 + \sqrt{121}}} \\ &= \sqrt{10 + \sqrt{25 + 11}} = \sqrt{10 + \sqrt{36}} = \sqrt{10 + 6} = \sqrt{16} = 4. \end{aligned}$$

$$\begin{aligned} 4. \text{ Given exp.} &= \sqrt{41 - \sqrt{21 + \sqrt{19 - 3}}} = \sqrt{41 - \sqrt{21 + \sqrt{16}}} = \sqrt{41 - \sqrt{21 + 4}} \\ &= \sqrt{41 - \sqrt{25}} = \sqrt{41 - 5} = \sqrt{36} = 6. \end{aligned}$$

5. Given exp. = $\sqrt{176 + 49} = \sqrt{225} = 15.$

4. $\sqrt{2401} \text{ (49)}$

$$\begin{array}{r} 2401 \\ \hline 16 \\ 89 \\ 801 \\ 801 \\ \hline \times \end{array}$$

6. Given exp. = $\frac{25}{11} \times \frac{14}{5} \times \frac{11}{14} = 5.$

7. Given exp. = $\left(\frac{\sqrt{225}}{\sqrt{729}} - \frac{\sqrt{25}}{\sqrt{144}} \right) + \frac{\sqrt{16}}{\sqrt{81}} = \left(\frac{15}{27} - \frac{5}{12} \right) + \frac{4}{9} = \left(\frac{15}{108} \times \frac{9}{4} \right) - \frac{5}{16}.$

8. $\sqrt{(272)^2 - (128)^2} = \sqrt{(272 + 128)(272 - 128)} = \sqrt{400 \times 144} = \sqrt{57600} = 240.$

9. $6*24 = 6 + 24 + \sqrt{6 \times 24} = 30 + \sqrt{144} = 30 + 12 = 42.$

10. $10y\sqrt{y^3 - y^2} = 10 \times 5\sqrt{5^3 - 5^2} = 50 \times \sqrt{125 - 25} = 50 \times \sqrt{100} = 50 \times 10 = 500.$

11. $\sqrt{110\frac{1}{4}} = \sqrt{\frac{441}{4}} = \frac{\sqrt{441}}{\sqrt{4}} = \frac{21}{2} = 10.5.$

12. $\sqrt{\frac{25}{81} - \frac{1}{9}} = \sqrt{\frac{25-9}{81}} = \sqrt{\frac{16}{81}} = \frac{\sqrt{16}}{\sqrt{81}} = \frac{4}{9}.$

13. (a) 1 | 15876 (126

$$\begin{array}{r} 1 \\ \hline 22 \\ 58 \\ 44 \end{array}$$

$$\begin{array}{r} 246 \\ 1476 \\ 1476 \\ \hline \times \end{array}$$

SOLUTIONS

$\therefore \sqrt{15876} = 126.$

14. A number ending in 8 can never be a perfect square.

15. $\sqrt{0.16} = \sqrt{\frac{16}{100}} = \frac{\sqrt{16}}{\sqrt{100}} = \frac{4}{10} = 0.4.$

16. $\sqrt{0.000441} = \sqrt{\frac{441}{10^6}} = \frac{\sqrt{441}}{\sqrt{10^6}} = \frac{21}{10^3} = \frac{21}{1000} = 0.021.$

17. $\sqrt{0.00004761} = \sqrt{\frac{4761}{10^8}} = \frac{\sqrt{4761}}{\sqrt{10^8}} = \frac{69}{10^4} = \frac{69}{10000} = 0.0069.$

18. $1.5^2 \times \sqrt{0.0225} = 1.5^2 \times \sqrt{\frac{225}{10000}} = 2.25 \times \frac{15}{100} = 2.25 \times 0.15 = 0.3375.$

19. $\sqrt{0.01 + \sqrt{0.0064}} = \sqrt{0.01 + \sqrt{\frac{64}{10000}}} = \sqrt{0.01 + \frac{8}{100}} = \sqrt{0.01 + 0.08} = \sqrt{0.09} = 0.3.$

20. Given exp. = $\sqrt{\frac{1}{100}} + \sqrt{\frac{81}{100}} + \sqrt{\frac{121}{100}} + \sqrt{\frac{9}{10000}} = \frac{1}{10} + \frac{9}{10} + \frac{11}{10} + \frac{3}{100}$
 $= 0.1 + 0.9 + 1.1 + 0.03 = 2.13.$

21. Given exp. = $\sqrt{\frac{25}{10000}} \times \sqrt{\frac{225}{100}} \times \sqrt{\frac{1}{10000}} = \frac{5}{100} \times \frac{15}{10} \times \frac{1}{100} = \frac{75}{100000} = 0.00075.$

22. (a) 1 | 1.5625 (1.25

$$\begin{array}{r} 1 \\ \hline 22 \\ 56 \\ 44 \end{array}$$

$$\begin{array}{r} 245 \\ 1225 \\ 1225 \\ \hline \times \end{array}$$

$\therefore \sqrt{1.5625} = 1.25.$

23. $\sqrt{6760000} = \sqrt{0.00000676 \times 10^{12}} = \sqrt{0.00000676} \times \sqrt{10^{12}} = .0026 \times 10^6 = 2600.$

24. Given exp. = $\sqrt{\frac{18225}{10^2}} + \sqrt{\frac{18225}{10^4}} + \sqrt{\frac{18225}{10^6}} + \sqrt{\frac{18225}{10^8}}$
 $= \frac{\sqrt{18225}}{10} + \frac{\sqrt{18225}}{10^2} + \frac{\sqrt{18225}}{10^3} + \frac{\sqrt{18225}}{10^4} = \frac{135}{10} + \frac{135}{100} + \frac{135}{1000} + \frac{135}{10000}$
 $= 13.5 + 1.35 + 0.135 + 0.0135 = 14.9985.$

25. Given exp. = $\sqrt{1.30} + \sqrt{1300} + \sqrt{0.0130} = \sqrt{\frac{130}{100}} + \sqrt{13 \times 100} + \sqrt{\frac{130}{10000}}$
 $= \frac{\sqrt{130}}{10} + \sqrt{13} \times 10 + \frac{\sqrt{130}}{100} = \frac{11.40}{10} + 3.605 \times 10 + \frac{11.40}{100}$
 $= 1.14 + 36.05 + 0.114 = 37.304.$

26. $\frac{52}{x} = \sqrt{\frac{169}{289}} \Leftrightarrow \frac{52}{x} = \frac{13}{17} \Leftrightarrow x = \left(\frac{52 \times 17}{13}\right) = 68.$

27. Let the missing number be x .

Then, $x^2 = 15 \times 135 \Leftrightarrow x = \sqrt{15 \times 135} = \sqrt{15^2 \times 3^2} = 15 \times 3 = 45.$

28. Let $\frac{4\frac{1}{2}}{x} = \frac{x}{32}$. Then, $x^2 = 32 \times \frac{9}{2} = 144 \Leftrightarrow x = \sqrt{144} = 12.$

29. Let $\frac{x}{\sqrt{128}} = \frac{\sqrt{162}}{x}$.

Then, $x^2 = \sqrt{128 \times 162} = \sqrt{64 \times 2 \times 18 \times 9} = \sqrt{8^2 \times 6^2 \times 3^2} = 8 \times 6 \times 3 = 144.$

$\therefore x = \sqrt{144} = 12.$

30. $\frac{0.13}{p^2} = 13 \Leftrightarrow p^2 = \frac{0.13}{13} = \frac{1}{100} \Leftrightarrow p = \sqrt{\frac{1}{100}} = \frac{1}{100} = \frac{1}{10} = 0.1$

31. Let the required number be x . Then, $\frac{x}{\sqrt{0.25}} = 25 \Leftrightarrow \frac{x}{0.5} = 25 \Leftrightarrow x = 25 \times 0.5 = 12.5.$

32. $\sqrt{3^n} = 729 = 3^6 \Leftrightarrow (\sqrt{3^n})^2 = (3^6)^2 \Leftrightarrow 3^n = 3^{12} \Leftrightarrow n = 12.$

33. $\sqrt{18 \times 14 \times x} = 84 \Leftrightarrow 18 \times 14 \times x = 84 \times 84 \Leftrightarrow x = \frac{84 \times 84}{18 \times 14} = 28.$

34. Let $28\sqrt{x} + 1426 = 3 \times 718$.

Then, $28\sqrt{x} = 2154 - 1426 \Leftrightarrow 28\sqrt{x} = 728 \Leftrightarrow \sqrt{x} = 26 \Leftrightarrow x = (26)^2 = 676.$

35. Let $\sqrt{\frac{x}{169}} = \frac{54}{39}$. Then, $\frac{\sqrt{x}}{13} = \frac{54}{39} \Leftrightarrow \sqrt{x} = \left(\frac{54}{39} \times 13\right) = 18 \Leftrightarrow x = (18)^2 = 324.$

36. $\frac{\sqrt{x}}{\sqrt{441}} = 0.02 \Leftrightarrow \frac{\sqrt{x}}{21} = 0.02 \Leftrightarrow \sqrt{x} = 0.02 \times 21 = 0.42 \Leftrightarrow x = (0.42)^2 = 0.1764.$

37. Let $\sqrt{\frac{0.0196}{x}} = 0.2$. Then, $\frac{0.0196}{x} = 0.04 \Leftrightarrow x = \frac{0.0196}{0.04} = \frac{196}{4} = 49.$

38. Let $\sqrt{0.0169 \times x} = 1.3$. Then, $0.0169x = (1.3)^2 = 1.69 \Leftrightarrow x = \frac{1.69}{0.0169} = 100.$

39. $37 + \sqrt{0.0615 + x} = 37.25 \Leftrightarrow \sqrt{0.0615 + x} = 0.25$

$\Leftrightarrow 0.0615 + x = (0.25)^2 = 0.0625 \Leftrightarrow x = .001 = \frac{1}{10^3} = 10^{-3}.$

40. $\sqrt{(x-1)(y+2)} = 7 \Rightarrow (x-1)(y+2) = 7^2 \Rightarrow (x-1) = 7 \text{ and } (y+2) = 7$
 $\Rightarrow x = 8 \text{ and } y = 5.$

41. $\frac{\sqrt{a}}{\sqrt{b}} = \frac{.004 \times .4}{\sqrt{.04 \times .4}} \Rightarrow \frac{a}{b} = \frac{.004 \times .4 \times .004 \times .4}{.04 \times .4} = \frac{.0000064}{.04}$
 $\therefore \frac{a}{b} = \frac{.00064}{4} = .00016 = \frac{16}{10^5} = 16 \times 10^{-5}.$

42. Let the number be x . Then,

$$\frac{3}{5}x^2 = 126.15 \Leftrightarrow x^2 = \left(126.15 \times \frac{5}{3}\right) = 210.25 \Leftrightarrow x = \sqrt{210.25} = 14.5.$$

43. $\sqrt{\frac{0.361}{0.00169}} = \sqrt{\frac{0.36100}{0.00169}} = \sqrt{\frac{36100}{169}} = \frac{190}{13}.$

44. $\sqrt{\frac{48.4}{0.289}} = \sqrt{\frac{48.400}{0.289}} = \sqrt{\frac{48400}{289}} = \frac{220}{17} = 12\frac{16}{17}.$

45. $\sqrt{1 + \frac{x}{169}} = \frac{14}{13} \Rightarrow 1 + \frac{x}{169} = \frac{196}{169} \Rightarrow \frac{x}{169} = \left(\frac{196}{169} - 1\right) = \frac{27}{169} \Rightarrow x = 27.$

46. $\sqrt{1 + \frac{55}{729}} = 1 + \frac{x}{27} \Rightarrow \sqrt{\frac{784}{729}} = \frac{27+x}{27} \Rightarrow \frac{28}{27} = \frac{27+x}{27} \Rightarrow 27+x = 28 \Rightarrow x = 1.$

47.
$$\begin{array}{r} 1 \\ \hline 2 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 24 & 100 \\ & 96 \\ \hline 281 & 400 \\ & 281 \\ \hline 2824 & 11900 \\ & 11296 \end{array}$$

$\therefore \sqrt{2} = 1.414.$

48. $2\sqrt{27} - \sqrt{75} + \sqrt{12} = 2\sqrt{9 \times 3} - \sqrt{25 \times 3} + \sqrt{4 \times 3} = 6\sqrt{3} - 5\sqrt{3} + 2\sqrt{3} = 3\sqrt{3}.$

49. $(\sqrt{12} + \sqrt{18}) - (\sqrt{3} + \sqrt{2}) = (\sqrt{4 \times 3} + \sqrt{9 \times 2}) - (\sqrt{3} + \sqrt{2}) = (2\sqrt{3} + 3\sqrt{2}) - (\sqrt{3} + \sqrt{2})$
 $= (2\sqrt{3} - \sqrt{3}) + (3\sqrt{2} - \sqrt{2}) = \sqrt{3} + 2\sqrt{2}.$

50. $\frac{\sqrt{24} + \sqrt{216}}{\sqrt{96}} = \frac{\sqrt{4 \times 6} + \sqrt{36 \times 6}}{\sqrt{16 \times 6}} = \frac{2\sqrt{6} + 6\sqrt{6}}{4\sqrt{6}} = \frac{8\sqrt{6}}{4\sqrt{6}} = 2.$

51. $\frac{\sqrt{80} - \sqrt{112}}{\sqrt{45} - \sqrt{63}} = \frac{\sqrt{16 \times 5} - \sqrt{16 \times 7}}{\sqrt{9 \times 5} - \sqrt{9 \times 7}} = \frac{4\sqrt{5} - 4\sqrt{7}}{3\sqrt{5} - 3\sqrt{7}} = \frac{4(\sqrt{5} - \sqrt{7})}{3(\sqrt{5} - \sqrt{7})} = \frac{4}{3} = 1\frac{1}{3}.$

52. $3\sqrt{5} + \sqrt{125} = 17.88 \Rightarrow 3\sqrt{5} + \sqrt{25 \times 5} = 17.88$

$$\Rightarrow 3\sqrt{5} + 5\sqrt{5} = 17.88 \Rightarrow 8\sqrt{5} = 17.88 \Rightarrow \sqrt{5} = 2.235.$$

$\therefore \sqrt{80} + 6\sqrt{5} = \sqrt{16 \times 5} + 6\sqrt{5} = 4\sqrt{5} + 6\sqrt{5} = 10\sqrt{5} = (10 \times 2.235) = 22.35.$

53. $\sqrt{50} \times \sqrt{98} = \sqrt{50 \times 98} = \sqrt{4900} = 70.$

54. Given exp. = $\sqrt{4 \times 2} + 2\sqrt{16 \times 2} - 3\sqrt{64 \times 2} + 4\sqrt{25 \times 2}$
 $= 2\sqrt{2} + 8\sqrt{2} - 24\sqrt{2} + 20\sqrt{2} = 6\sqrt{2} = 6 \times 1.414 = 8.484.$

55. Given exp. = $\frac{3\sqrt{12}}{2\sqrt{28}} \times \frac{\sqrt{98}}{2\sqrt{21}} = \frac{3\sqrt{4 \times 3}}{2\sqrt{4 \times 7}} \times \frac{\sqrt{49 \times 2}}{2\sqrt{21}} = \frac{6\sqrt{3}}{4\sqrt{7}} \times \frac{7\sqrt{2}}{2\sqrt{21}} = \frac{21\sqrt{6}}{4\sqrt{7 \times 21}} = \frac{21\sqrt{6}}{28\sqrt{3}}$
 $= \frac{3}{4}\sqrt{2} = \frac{3}{4} \times 1.414 = 3 \times 0.3535 = 1.0605.$

56. Sum of decimal places in the numerator and denominator under the radical sign being the same, we remove the decimal.

∴ Given exp. = $\sqrt{\frac{81 \times 484}{64 \times 625}} = \frac{9 \times 22}{8 \times 25} = 0.99.$

57. Given exp. = $\sqrt{\frac{204 \times 42}{7 \times 34}} = \sqrt{36} = 6.$

58. Given exp. = $\sqrt{\frac{81 \times 324 \times 4624}{15625 \times 289 \times 729 \times 64}} = \frac{9 \times 18 \times 68}{125 \times 17 \times 27 \times 8} = \frac{3}{125} = 0.024.$

59. Given exp. = $\sqrt{\frac{9.5 \times .08500}{.19 \times .0017}} = \sqrt{\frac{95 \times 8500}{19 \times 17}} = \sqrt{5 \times 500} = \sqrt{2500} = 50.$

60. Given exp. = $\sqrt{\frac{(0.03)^2 + (0.21)^2 + (0.065)^2}{\left(\frac{0.03}{10}\right)^2 + \left(\frac{0.21}{10}\right)^2 + \left(\frac{0.065}{10}\right)^2}}$
 $= \sqrt{\frac{100[(0.03)^2 + (0.21)^2 + (0.065)^2]}{(0.03)^2 + (0.21)^2 + (0.065)^2}} = \sqrt{100} = 10.$

61. $\sqrt{(7 + 3\sqrt{5})(7 - 3\sqrt{5})} = \sqrt{(7)^2 - (3\sqrt{5})^2} = \sqrt{49 - 45} = \sqrt{4} = 2.$

62. $\left(\sqrt{3} - \frac{1}{\sqrt{3}}\right)^2 = (\sqrt{3})^2 + \left(\frac{1}{\sqrt{3}}\right)^2 - 2 \times \sqrt{3} \times \frac{1}{\sqrt{3}} = 3 + \frac{1}{3} - 2 = 1 + \frac{1}{3} = \frac{4}{3}.$

63. $\left(\sqrt{2} + \frac{1}{\sqrt{2}}\right)^2 = (\sqrt{2})^2 + \left(\frac{1}{\sqrt{2}}\right)^2 + 2 \times \sqrt{2} \times \frac{1}{\sqrt{2}} = 2 + \frac{1}{2} + 2 = 4 + \frac{1}{2} = 4\frac{1}{2}.$

64. $\sqrt{4a^2 - 4a + 1 + 3a} = \sqrt{(1)^2 + (2a)^2 - 2 \times 1 \times 2a + 3a}$
 $= \sqrt{(1 - 2a)^2} + 3a = (1 - 2a) + 3a = (1 + a) = (1 + 0.1039) = 1.1039.$

65. $\sqrt{\frac{(0.75)^3}{(1 - 0.75)} + [0.75 + (0.75)^2 + 1]} = \sqrt{\frac{(0.75)^3 + (1 - 0.75)[(1)^2 + (0.75)^2 + 1 \times 0.75]}{1 - 0.75}}$
 $= \sqrt{\frac{(0.75)^3 + [(1)^3 - (0.75)^3]}{1 - 0.75}} = \sqrt{\frac{1}{0.25}} = \sqrt{\frac{100}{25}} = \sqrt{4} = 2.$

66. $4b = 6c \Rightarrow b = \frac{3}{2}c$ and $3a = 4b \Rightarrow a = \frac{4}{3}b = \frac{4}{3}\left(\frac{3}{2}c\right) = 2c.$

$a + b + c = 27\sqrt{29} \Rightarrow 2c + \frac{3}{2}c + c = 27\sqrt{29} \Rightarrow \frac{9}{2}c = 27\sqrt{29} \Rightarrow c = 6\sqrt{29}.$

$$\begin{aligned}
 \therefore \sqrt{a^2 + b^2 + c^2} &= \sqrt{(a+b+c)^2 - 2(ab+bc+ca)} \\
 &= \sqrt{(27\sqrt{29})^2 - 2\left(2c \times \frac{3}{2}c + \frac{3}{2}c \times c + c \times 2c\right)} \\
 &= \sqrt{(729 \times 29) - 2\left(3c^2 + \frac{3}{2}c^2 + 2c^2\right)} = \sqrt{(729 \times 29) - 2 \times \frac{13}{2}c^2} \\
 &= \sqrt{(729 \times 29) - 13 \times (6\sqrt{29})^2} = \sqrt{29(729 - 468)} \\
 &= \sqrt{29 \times 261} = \sqrt{29 \times 29 \times 9} = 29 \times 3 = 87.
 \end{aligned}$$

67. $\sqrt{0.4} = \sqrt{\frac{4}{9}} = \frac{2}{3} = 0.666\dots = 0.\overline{6}$.

68. $\sqrt{0.09} = \sqrt{\frac{9}{100}} = \frac{3}{10} = 0.3$, which is rational.

$\therefore 0.09$ has rational square root.

69. $6 \left| \begin{array}{r} 0.400000 (.63) \\ 36 \\ \hline 400 \\ 369 \\ \hline \end{array} \right.$

70. $3 \left| \begin{array}{r} 0.121000 (.347) \\ 9 \\ \hline 310 \\ 256 \\ \hline 687 \\ 5400 \\ 4809 \\ \hline \end{array} \right.$

71. $2 \left| \begin{array}{r} 0.064000 (.252) \\ 4 \\ \hline 240 \\ 225 \\ \hline 1500 \\ 1006 \\ \hline \end{array} \right.$

72. $\sqrt{\frac{0.16}{0.4}} = \sqrt{\frac{0.16}{0.40}} = \sqrt{\frac{16}{40}} = \sqrt{\frac{4}{10}} = \sqrt{0.4} = 0.63$.

73.
$$\begin{aligned}
 \frac{1 + \sqrt{0.01}}{1 - \sqrt{0.1}} &= \frac{1 + 0.1}{1 - 0.316} = \frac{1.1}{0.684} \\
 &= \frac{1100}{684} = 1.6.
 \end{aligned}$$

3 $\left| \begin{array}{r} 0.100000 (.316) \\ 9 \\ \hline 100 \\ 61 \\ \hline 3900 \\ 3756 \\ \hline \end{array} \right.$

74. $\frac{1}{\sqrt{5}} = \frac{1}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{5}}{5} = \frac{2.236}{5} = 0.447$.

75. $\sqrt{\frac{8}{3}} = \sqrt{\frac{8 \times 3}{3 \times 3}} = \sqrt{\frac{24}{9}} = \frac{4.899}{3} = 1.633$.

76. $\frac{3\sqrt{2}}{2\sqrt{3}} = \frac{3\sqrt{2}}{2\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{3\sqrt{6}}{2 \times 3} = \frac{\sqrt{6}}{2} = \frac{2.449}{2} = 1.2245$.

Square Roots and Cube Roots

To reduce Root 38

$$77. \frac{\sqrt{5}}{2} - \frac{10}{\sqrt{5}} + \sqrt{125} = \frac{(\sqrt{5})^2 - 20 + 2\sqrt{5} \times 5\sqrt{5}}{2\sqrt{5}} = \frac{5 - 20 + 50}{2\sqrt{5}}$$

$$= \frac{35}{2\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{35\sqrt{5}}{10} = \frac{7}{2} \times 2.236 = 7 \times 1.118 = 7.826.$$

78. Clearly, $a * b = \sqrt{a^2 + b^2}$.

$$\therefore 5 * 12 = \sqrt{5^2 + 12^2} = \sqrt{25 + 144} = \sqrt{169} = 13.$$

79. L.C.M. of 3, 4, 5, 6, 8 is 120. Now, $120 = 2 \times 2 \times 2 \times 3 \times 5$.

To make it a perfect square, it must be multiplied by $2 \times 3 \times 5$.

So, required number = $2^2 \times 2^2 \times 3^2 \times 5^2 = 3600$.

80. L.C.M. of 21, 36, 66 = 2772. Now, $2772 = 2 \times 2 \times 3 \times 3 \times 7 \times 11$.

To make it a perfect square, it must be multiplied by 7×11 .

So, required number = $2^2 \times 3^2 \times 7^2 \times 11^2 = 213444$.

81. $294 = 7 \times 7 \times 2 \times 3$.

To make it a perfect square, it must be multiplied by 2×3 i.e., 6.

\therefore Required number = 6.

82. $5808 = 2 \times 2 \times 2 \times 2 \times 3 \times 11 \times 11 = 2^2 \times 2^2 \times 3 \times 11^2$.

To make it a perfect square, it must be multiplied by 3.

83. $1470 = 7 \times 7 \times 5 \times 6$. To make it a perfect square, it must be divided by 5×6 , i.e., 30.

84. $7 \overline{)549162} (741$

49

144

591

576

1481

1562

1481

81

\therefore Required number to be subtracted = 81.

85. $0.000326 = \frac{326}{10^6}$.

\therefore Required number to be subtracted = $\frac{2}{10^6} = 0.000002$.

1 $\overline{)326} (18$

1

226

224

2

86. $8 \overline{)680621} (824$

64

162

406

324

1644

8221

6576

1645

\therefore Number to be added = $(825)^2 - 680621 = 680625 - 680621 = 4$.

87. Greatest number of four digits is 9999.

\therefore Required number = $(9999 - 198) = 9801$.

9 $\overline{)9999} (99$

81

1899

1701

198

88. Least number of 4 digits is 1000.

$$\begin{array}{r} 3 \quad | \quad \overline{1000} \text{ (31)} \\ \quad \quad | \quad 9 \\ 61 \quad | \quad \overline{100} \\ \quad \quad | \quad 61 \\ \quad \quad | \quad 39 \end{array}$$

$\therefore (31)^2 < 1000 < (32)^2$. Hence, required number = $(32)^2 = 1024$.

89. $\frac{1}{(\sqrt{5} - \sqrt{3})} = \frac{1}{(\sqrt{5} - \sqrt{3})} \times \frac{(\sqrt{5} + \sqrt{3})}{(\sqrt{5} + \sqrt{3})} = \frac{(\sqrt{5} + \sqrt{3})}{(5 - 3)} = \frac{(2.2361 + 1.7321)}{2} = \frac{3.9682}{2} = 1.9841$.

90. Given exp. = $\frac{1}{(\sqrt{9} - \sqrt{8})} \times \frac{(\sqrt{9} + \sqrt{8})}{(\sqrt{9} + \sqrt{8})} - \frac{1}{(\sqrt{8} - \sqrt{7})} \times \frac{(\sqrt{8} + \sqrt{7})}{(\sqrt{8} + \sqrt{7})} + \frac{1}{(\sqrt{7} - \sqrt{6})} \times \frac{(\sqrt{7} + \sqrt{6})}{(\sqrt{7} + \sqrt{6})}$
 $\quad \quad \quad - \frac{1}{(\sqrt{6} - \sqrt{5})} \times \frac{(\sqrt{6} + \sqrt{5})}{(\sqrt{6} + \sqrt{5})} + \frac{1}{(\sqrt{5} - \sqrt{4})} \times \frac{(\sqrt{5} + \sqrt{4})}{(\sqrt{5} + \sqrt{4})}$
 $= \frac{(\sqrt{9} + \sqrt{8})}{(9 - 8)} - \frac{(\sqrt{8} + \sqrt{7})}{(8 - 7)} + \frac{(\sqrt{7} + \sqrt{6})}{(7 - 6)} - \frac{(\sqrt{6} + \sqrt{5})}{(6 - 5)} + \frac{(\sqrt{5} + \sqrt{4})}{(5 - 4)}$
 $= (\sqrt{9} + \sqrt{8}) - (\sqrt{8} + \sqrt{7}) + (\sqrt{7} + \sqrt{6}) - (\sqrt{6} + \sqrt{5}) + (\sqrt{5} + \sqrt{4}) = (\sqrt{9} + \sqrt{4}) = 3 + 2 = 5$.

91. Given exp. = $(2 + \sqrt{2}) + \frac{1}{(2 + \sqrt{2})} \times \frac{(2 - \sqrt{2})}{(2 - \sqrt{2})} - \frac{1}{(2 - \sqrt{2})} \times \frac{(2 + \sqrt{2})}{(2 + \sqrt{2})}$
 $= (2 + \sqrt{2}) + \frac{(2 - \sqrt{2})}{(4 - 2)} - \frac{(2 + \sqrt{2})}{(4 - 2)} = (2 + \sqrt{2}) + \frac{1}{2}(2 - \sqrt{2}) - \frac{1}{2}(2 + \sqrt{2}) = 2$.

92. $\frac{7}{(3 + \sqrt{2})} = \frac{7}{(3 + \sqrt{2})} \times \frac{(3 - \sqrt{2})}{(3 - \sqrt{2})} = \frac{7(3 - \sqrt{2})}{(9 - 2)} = (3 - \sqrt{2}) = (3 - 1.4142) = 1.5858$.

93. Given exp. = $\frac{3\sqrt{2}}{(\sqrt{6} - \sqrt{3})} \times \frac{(\sqrt{6} + \sqrt{3})}{(\sqrt{6} + \sqrt{3})} - \frac{4\sqrt{3}}{(\sqrt{6} - \sqrt{2})} \times \frac{(\sqrt{6} + \sqrt{2})}{(\sqrt{6} + \sqrt{2})} - \frac{6}{2(\sqrt{2} - \sqrt{3})}$
 $= \frac{3\sqrt{2}(\sqrt{6} + \sqrt{3})}{(6 - 3)} - \frac{4\sqrt{3}(\sqrt{6} + \sqrt{2})}{(6 - 2)} + \frac{3}{(\sqrt{3} - \sqrt{2})} \times \frac{(\sqrt{3} + \sqrt{2})}{(\sqrt{3} + \sqrt{2})}$
 $= \sqrt{2}(\sqrt{6} + \sqrt{3}) - \sqrt{3}(\sqrt{6} + \sqrt{2}) + 3(\sqrt{3} + \sqrt{2})$
 $= \sqrt{12} + \sqrt{6} - \sqrt{18} - \sqrt{6} + 3\sqrt{3} + 3\sqrt{2}$
 $= 2\sqrt{3} - 3\sqrt{2} + 3\sqrt{3} + 3\sqrt{2} = 5\sqrt{3}$.

94. $\frac{\sqrt{7} + \sqrt{5}}{\sqrt{7} - \sqrt{5}} = \frac{(\sqrt{7} + \sqrt{5})}{(\sqrt{7} - \sqrt{5})} \times \frac{(\sqrt{7} + \sqrt{5})}{(\sqrt{7} + \sqrt{5})} = \frac{(\sqrt{7} + \sqrt{5})^2}{(7 - 5)} = \frac{7 + 5 + 2\sqrt{35}}{2} = \frac{12 + 2\sqrt{35}}{2} = 6 + \sqrt{35}$.

95. $a + b\sqrt{3} = \frac{(5 + 2\sqrt{3})}{(7 + 4\sqrt{3})} \times \frac{(7 - 4\sqrt{3})}{(7 - 4\sqrt{3})} = \frac{35 - 20\sqrt{3} + 14\sqrt{3} - 24}{(7)^2 - (4\sqrt{3})^2} = \frac{11 - 6\sqrt{3}}{49 - 48} = 11 - 6\sqrt{3}$,
 $\therefore a = 11, b = -6$.

96. $\frac{\sqrt{2} - 1}{\sqrt{2} + 1} = \frac{(\sqrt{2} - 1)}{(\sqrt{2} + 1)} \times \frac{(\sqrt{2} - 1)}{(\sqrt{2} - 1)} = (\sqrt{2} - 1)^2$.

$\therefore \sqrt{\frac{\sqrt{2} - 1}{\sqrt{2} + 1}} = (\sqrt{2} - 1) = (1.414 - 1) = 0.414$.

97. Given exp. = $\frac{3 + \sqrt{6}}{5\sqrt{3} - 4\sqrt{3} - 4\sqrt{2} + 5\sqrt{2}} = \frac{(3 + \sqrt{6})}{(\sqrt{3} + \sqrt{2})}$

$$= \frac{(3 + \sqrt{6})}{(\sqrt{3} + \sqrt{2})} \times \frac{(\sqrt{3} - \sqrt{2})}{(\sqrt{3} - \sqrt{2})} = \frac{3\sqrt{3} - 3\sqrt{2} + 3\sqrt{2} - 2\sqrt{3}}{(3 - 2)} = \sqrt{3}.$$

98. Given exp. = $\frac{(2 + \sqrt{3})}{(2 - \sqrt{3})} \times \frac{(2 + \sqrt{3})}{(2 + \sqrt{3})} + \frac{(2 - \sqrt{3})}{(2 + \sqrt{3})} \times \frac{(2 - \sqrt{3})}{(2 - \sqrt{3})} + \frac{(\sqrt{3} - 1)}{(\sqrt{3} + 1)} \times \frac{(\sqrt{3} - 1)}{(\sqrt{3} - 1)}$

$$= \frac{(2 + \sqrt{3})^2}{(4 - 3)} + \frac{(2 - \sqrt{3})^2}{(4 - 3)} + \frac{(\sqrt{3} - 1)^2}{(3 - 1)} = [(2 + \sqrt{3})^2 + (2 - \sqrt{3})^2] + \frac{4 - 2\sqrt{3}}{2}$$

$$= 2(4 + 3) + 2 - \sqrt{3} = 16 - \sqrt{3}.$$

99. $x + \frac{1}{x} = (7 - 4\sqrt{3}) + \frac{1}{(7 - 4\sqrt{3})} \times \frac{(7 + 4\sqrt{3})}{(7 + 4\sqrt{3})} = (7 - 4\sqrt{3}) + \frac{(7 + 4\sqrt{3})}{(49 - 48)}$
 $= (7 - 4\sqrt{3}) + (7 + 4\sqrt{3}) = 14.$

100. $x = \frac{(\sqrt{3} + 1)}{(\sqrt{3} - 1)} \times \frac{(\sqrt{3} + 1)}{(\sqrt{3} + 1)} = \frac{(\sqrt{3} + 1)^2}{(3 - 1)} = \frac{3 + 1 + 2\sqrt{3}}{2} = 2 + \sqrt{3}.$

$$y = \frac{(\sqrt{3} - 1)}{(\sqrt{3} + 1)} \times \frac{(\sqrt{3} - 1)}{(\sqrt{3} - 1)} = \frac{(\sqrt{3} - 1)^2}{(3 - 1)} = \frac{3 + 1 - 2\sqrt{3}}{2} = 2 - \sqrt{3}.$$

$$\therefore x^2 + y^2 = (2 + \sqrt{3})^2 + (2 - \sqrt{3})^2 = 2(4 + 3) = 2 \times 7 = 14.$$

101. $a = \frac{(\sqrt{5} + 1)}{(\sqrt{5} - 1)} \times \frac{(\sqrt{5} + 1)}{(\sqrt{5} + 1)} = \frac{(\sqrt{5} + 1)^2}{(5 - 1)} = \frac{5 + 1 + 2\sqrt{5}}{4} = \left(\frac{3 + \sqrt{5}}{2}\right).$

$$b = \frac{(\sqrt{5} - 1)}{(\sqrt{5} + 1)} \times \frac{(\sqrt{5} - 1)}{(\sqrt{5} - 1)} = \frac{(\sqrt{5} - 1)^2}{(5 - 1)} = \frac{5 + 1 - 2\sqrt{5}}{4} = \left(\frac{3 - \sqrt{5}}{2}\right).$$

$$\therefore a^2 + b^2 = \frac{(3 + \sqrt{5})^2}{4} + \frac{(3 - \sqrt{5})^2}{4} = \frac{(3 + \sqrt{5})^2 + (3 - \sqrt{5})^2}{4} = \frac{2(9 + 5)}{4} = 7.$$

Also, $ab = \frac{(3 + \sqrt{5})}{2} \cdot \frac{(3 - \sqrt{5})}{2} = \frac{(9 - 5)}{4} = 1.$

$$\therefore \frac{a^2 + ab + b^2}{a^2 - ab + b^2} = \frac{(a^2 + b^2) + ab}{(a^2 + b^2) - ab} = \frac{7 + 1}{7 - 1} = \frac{8}{6} = \frac{4}{3}.$$

102.	1 <u>15376</u> (124)	103. 1 <u>36581</u> (191)
	1 <u>15376</u>	1 <u>36581</u>
22	53	29
	44	265
244	976	261
	976	381
	x	481
		381
		100

∴ Number of rows = 124. ∴ Number of men left = 100.

104. Money collected = (59.29×100) paise = 5929 paise.

∴ Number of members = $\sqrt{5929} = 77$.

105. $(.000216)^{1/3} = \left(\frac{216}{10^6}\right)^{1/3} = \left(\frac{6 \times 6 \times 6}{10^2 \times 10^2 \times 10^2}\right)^{1/3} = \frac{6}{10^2} = \frac{6}{100} = .06$

106. $\sqrt[3]{4 \frac{12}{125}} = \sqrt[3]{\frac{512}{125}} = \left(\frac{8 \times 8 \times 8}{5 \times 5 \times 5} \right)^{1/3} = \frac{8}{5} = 1 \frac{3}{5}$

107. $\sqrt{.000064} = \sqrt{\frac{64}{10^5}} = \frac{8}{10^3} = \frac{8}{1000} = .008$

$$\therefore \sqrt[3]{\sqrt{.000064}} = \sqrt[3]{.008} = \sqrt[3]{\frac{8}{1000}} = \frac{2}{10} = 0.2$$

108. Clearly, 9261 is a perfect cube satisfying the given property.

109. $675 = 5 \times 5 \times 3 \times 3 \times 3$.

To make it a perfect cube, it must be multiplied by 5.

110. $3600 = 2^3 \times 5^2 \times 3^2 \times 2$.

To make it a perfect cube, it must be divided by $5^2 \times 3^2 \times 2$ i.e., 450.

OBJECTIVE GENERAL KNOWLEDGE

FOR COMPETITIONS

— R.S. Aggarwal

- * Over 10,000 questions on General Science, Indian Polity, History, Geography, Economics and General Awareness.
- * Questions classified under various headings to ensure better classification under various headings to ensure better understanding of the subject.
- * Separate Model Sets for rarely available Assertion-Reason and Matching-Type Questions and Questions based on Maps and Diagrams.
- * Previous years' questions included and fully solved.