Linear Inequalities

1. Solve the following inequalities and show the graph of solution on number line:

(i)
$$5x + 3 > 6x - 7$$

(ii)
$$\frac{7-3x}{5} \le \frac{x}{2} - 8$$

(iii)
$$\frac{x}{5} < \frac{3x-2}{4} - \frac{5x-3}{3}$$

(iv)
$$\frac{2x-3}{4} + 8 \ge \frac{4x}{3} + 2$$

2. Solve the following inequalities:

(i)
$$\frac{x-3}{x+5} > 0$$

(ii)
$$\frac{x-2}{x-4} \le 0$$

(iii)
$$\frac{x-3}{x-5} <$$

$$\frac{x-3}{x+5} > 0$$
 (ii) $\frac{x-2}{x-4} \le 0$ (iii) $\frac{x-3}{x-5} < 3$ (iv) $\frac{x+3}{x+7} \ge 2$

3. Solve the following inequations:

(i)
$$-8 \le 5x - 3 < 7$$

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 (ii) $7 \le \frac{3x+11}{2} \le 11$

(iii)
$$4x + 3 \ge 2x + 17$$
, $3x - 5 < -2$ (iv) $\frac{x-4}{7} < 3$, $\frac{2x+5}{-3} > 4$

(iv)
$$\frac{x-4}{7} < 3$$
, $\frac{2x+5}{-3} > 4$

4. In drilling world's deepest hole, it was found that the temperature T in degree celsius, x km below the surface of earth was given by:

$$T = 30 + 25(x - 3), \quad 3 < x < 15.$$

At what depth will the temperature be between $200^{\circ}C$ and $300^{\circ}C$.

5. A manufacturer has 600 litres of a 12% solution of acid. How many litres of a 30% acid solution must be added to it so that acid content in the resulting mixture will be more than 15% but less than 8% .

6. Solve the following linear inequalities graphically:

(i)
$$2x-7y+9 \ge 0$$
.

(ii)
$$x \ge 3$$
, $y \ge 2$.

(iii)
$$2x + y \ge 6$$
, $3x + 4y \le 12$

(iv)
$$3x + 2y \ge 24$$
, $3x + y \le 15$, $x \ge 4$

(v)
$$x + y \le 10, x + y \ge 4, x \le 8, y \le 8, x \ge 0, y \ge 0$$

(vi)
$$x + y \le 12$$
, $x + y \ge 4$, $x \le 9$, $y \le 9$, $x \ge 0$, $y \ge 0$

(vii)
$$3x + 5y \le 15$$
, $5x + 3y \le 15$, $x \ge 0$, $y \ge 0$

(viii)
$$x + 2y \le 10$$
, $3x + 4y \le 24$, $x \ge 0$, $y \ge 0$

(ix)
$$x + y \ge 5$$
, $5x + 7y \le 35$, $x - y \ge 0$, $x \ge 0$, $y \ge 0$

(x)
$$x + y \ge 6$$
, $3x + 2y \le 18$, $x - 2y \le 0$, $x \ge 0$, $y \ge 0$

Prepared By: Vaibhav(Lecturer, Maths), Govt. Multipurpose Sec. School, Patiala